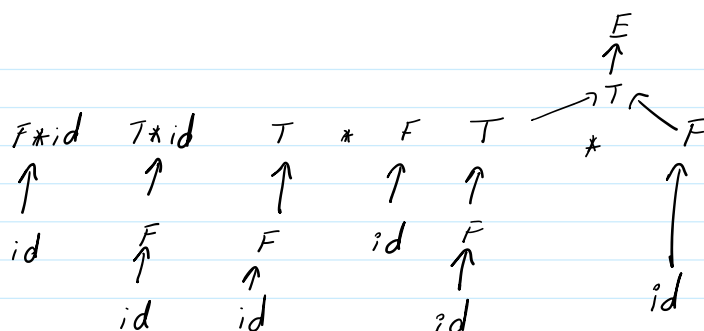


Bottom Up Parsing (LR Parsing)

$$\begin{aligned}
 E &\rightarrow E + T \mid T \\
 T &\rightarrow T * F \mid F \\
 F &\rightarrow E \mid id
 \end{aligned}$$



$$id * id \quad E \rightarrow T \rightarrow T * F \rightarrow T * id \rightarrow F * id \rightarrow id * id$$

Handle Parsing

'handle' is a substring matching the body of a production st its reduction represents one step along the reverse rightmost derivation

(right sentential form)

RSF	Handle	Reducing P
$id_1 id_2$	id_1	$F \rightarrow id$
$F * id_2$	F	$T \rightarrow F$
$T + id_2$	id_2	$F \rightarrow id_2$
$T * F$	$T * F$	$F \rightarrow T * F$
T	T	$E \rightarrow T$

$$S \xrightarrow{*}_{rm} aAw \xrightarrow{*}_{rm} a\beta w$$

β after a is an input string we say β is a handle of $a\beta w$

leftmost substring in a production is not necessarily a handle.

Shift Reduce Parsing - LR(1)

we have a stack, a current stack symbol / input symbol we can either

shift: push current symbol on top of stack

reduce: reduce stack to a parent production

Stack	Input	Action
\$	$id_1 id_2 \$$	shift
$\$ id_1$	$* id_2 \$$	reduce
$\$ F$	$* id_2 \$$	reduce
$\$ T$	$* id_2 \$$	shift
$\$ T *$	$id_2 \$$	shift
$\$ T * id_2$	$\$$	reduce
$\$ T * F$	$\$$	reduce
$\$ T$	$\$$	reduce

$\$$ - stack bottom and end of input

Shift reduce conflicts:

At some step in parsing, you can't

decide whether to shift or reduce

grammars with such conflicts fall out of LR(k)

Lemma - an ambiguous grammar is never LR

\$ I * id ₂	\$	reduce
\$ T * F	\$	reduce
\$ T	\$	reduce
\$ E		accept

Lemma- an ambiguous grammar is never LR

$stmt \rightarrow$ if expr. then stmt
 | if expr then stmt else stmt
 | other
 if expr. then stmt, else stmt₂

$E \rightarrow I + E$
 | $E * E$
 | id
 id + id + id