

$$h_{\mu_\varphi}(f) + \int_X \varphi d\mu_\varphi = \sup_{\mathcal{M}(f, X)} \left\{ h_\mu(f) + \int_X \varphi d\mu \right\},$$