$$h_{\mu_{\varphi}}(f) + \int_{X} \varphi d\mu_{\varphi} = \sup_{\mathcal{M}(f,X)} \{h_{\mu}(f) + \int_{X} \varphi d\mu\},$$