$$h_{\mu_{\varphi}}(f) + \int_{X} \varphi d\mu_{\varphi} = \sup_{M(f,X)} \{ h_{\mu}(f) + \int_{X} \varphi d\mu \},$$