

Final Year Project Report
Development and implementation dynamic balance algorithms
for bipedal robot locomotion.

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May 8, 2015

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Chapter 1

Introduction

Nowadays humanity has invented almost all devices that are needed for modern humans and society in general. Science is now engaged in the improvement and optimization of existing solutions. These solutions can be traced with trends that are repeated and replicated. For example, the car has 4 wheels while bike - two, and wheels are round, at room there are four walls, etc. This approach is quite good: gain experience, accumulate knowledge and apply them to the latest developments.

According to [1] it is very important to consider the level of uncertainty of the environment where a robot works, because its body will interact with this environment. It was a common belief before the advent of industrial robots that robots should look like humans. The first use of the word "robot" refers to a humanoid machine that was supposed to serve a human. However, from the very beginning almost every automatic device intended for production and other operations normally performed by the human was called robot. Intensive development of robots started after the Second World War, which was associated with the emergence of the nuclear industry.

Robots in today's definition (autonomous devices that work in automatic mode) can be attributed to the machine "Lunokhod-1", created in 1966. It was the first machine in the history that worked on the surface of the Moon (1970). Lately robots began to replace humans not only in manufacturing but also in the military sphere. Constantly emerging information about the achievements of the leading countries in the development of military land, underwater robots and unmanned aerial vehicles is evidenced for this thesis. Bipedal humanoid walking robots comprise the area of robotics that is developing most rapidly nowadays.

The trend towards automation is a core part of progress. Automation reduces the cost of technical processes and the risk to humans. Therefore, the research and development for this task are on the cutting edge of science and technology and require special attention and investment into its development. There are more and more situations requiring people to perform a wide variety of work in heavy, dangerous, and sometimes incompatible with the life conditions. In response, there are new tools of extreme robotics. However, for the most part they are very similar to each other. Usually, autonomous wheeled or tracked vehicles with manipulators are used to perform tasks on the ground. Mostly these robots are teleoperated. These robots are being produced for more than a dozen years. Engineers have so far accumulated a lot of experience in their development and applications, which are in some cases very efficient. However, it is obvious that this technique has (like any other) a limited scope of application. People still have to work in dangerous conditions such as in chemical, biological, or radioactive hazards, work in extremely hot or cold conditions, fight against criminals and terrorist. Human workspace is very specific due to people's two arms and two legs. Universal robot should operate in the same environment and workspace. For this reason other areas of extreme robotics are developing now. One of these is a robotic system including an anthropomorphic bipedal walking robot. Such robot's kinematics, size and weight are similar to human's, it is equipped with an energy source,

communication channel with the control station, and a powerful autonomous control system, allowing it to perform actions in supervisory or automatic mode. For instance, autonomous actions include independent movement from place to place in absence of communication). Such robots have significant advantages in workspaces initially adapted for humans.

Chapter 2

Literature review

Bipedal locomotion is a very complex task and according to [2] it is described by nontrivial dynamics. It still doesn't have complete general solution however the research of this has a long history. The development of the models starts from the inverted pendulum model of human walking and goes to the complex approach of actuated passive walking with ZMP control. According to [3], there are 5 groups of approaches to the problem of locomotion control. There are:

1. Analytical
2. Central Pattern Generator (CPG)
3. Neural Networks
4. Hidden Markov Model (HMM)
5. Rule based

2.1 Analytical approach

The oldest one and also the most studied group is analytical one. It requires the knowledge of general form that locomotion should take.

For bipedal locomotion it requires the following steps:

1. Apply stability constraints
2. Design gait algorithm (including double support, single support and no-support phases [3]).
3. Solve remaining degrees of freedom (DoF) with Inverse Kinematics (IK).

According to [4], the most natural method that represents the human body is inverted pendulum. Inverted pendulum model of human balance problem is one of the most primitive and old example of analytical approach [5]. It stated that control of the balance can be achieved with two components: ankle mechanism (invertors/evertors) and hip load/unloading mechanism. In different positions each of the mechanism plays a different role. Thus in tandem or intermediate position balance is achieved by invertors/evertors mechanism while direction is controlled by hip load/unloading mechanism. It doubts on commonly used condition: reaction force of the floor has to go through center of gravity of the robot. It was stated, that modern bio-mechanical studies show that there are angular moments around center of gravity. Thus this approach is too approximate and it is not very accurate. Moreover, according to [6] six

determinants theory[7] well described by inverted pendulum model needs more energy to control the mechanism and this problem can be solved by passive dynamic walking machines, that need external energy only for transition from one pendular stance leg to another. In [8] such architecture was considered. There robot was able to move forward at constant not very high speed and author mentioned that the gait of the robot was human like. Human gait is desirable because of its energy effectiveness [9].

Furthermore, [10] summaries principles that allows to combine passive dynamic control with powered bipeds. The results show that the gait become energy efficient however it implies further work on robustness and flexibility of walking

In 1970 Miomir Vukobratovic proposed Zero Moment Point (ZMP), a theoretical model to explain biped locomotion. Also ZMP is a basic dynamical stability constraint. According to [11] we can divide all the existing humanoid bipedal walking robots into two big groups: ZMP-controlled ones and passive - dynamic walkers.

Zero moment point is a concept related with dynamics and control of legged locomotion for humanoid robots. It specifies the point with respect to which dynamic reaction force at the contact of the foot with the ground does not produce any moment in the horizontal direction, i.e. the point where the total of horizontal inertia and gravity forces equals to zero. Miomir Vukobratovic in [12] defines ZMP (Zero Moment Point) as a point in which we can reduce all the forces and moments with one single force F_a and moment M_a respectively fig. 2.1.

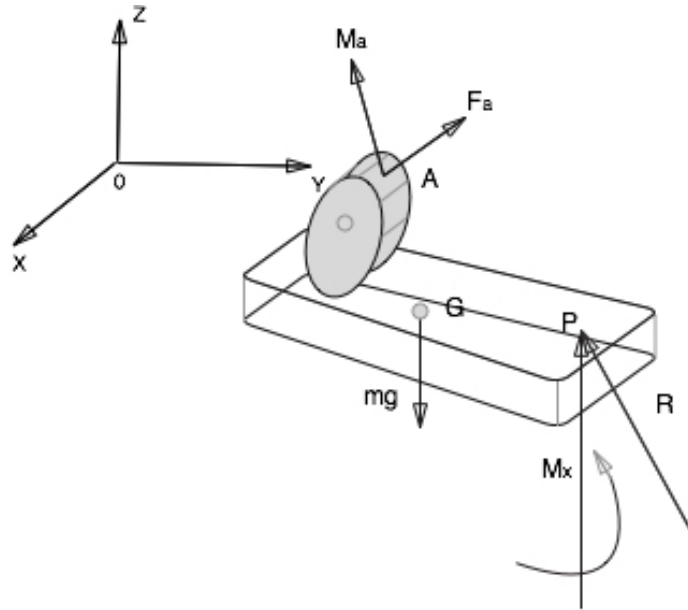


Figure 2.1: The sole with acting forces on it

On the figure above we consider only the sole separately from other parts of the leg. It has its own center of gravity G. At point P there is resulting ground reaction that maintains the construction in the equilibrium. The force of ground reaction R and moment M consists of its three components (R_x, R_y, R_z) and (M_x, M_y, M_z) respectively. Horizontal components of R should compensate friction force in the point of contact. Thus, the horizontal reaction of force (R_x, R_y) represents friction force that compensate horizontal component of F_a . In the same time the moment M_z represents friction reaction forces fig. 2.2 that compensates vertical component of M_a and the moment induced by F_a . [12]

According to [13], this ZMP should be on the foot. The problem is that we cannot manipulate the foot directly [14]. According to [12] we can do it by ensuring the appropriate dynamics of the mechanism above the foot. If the resulting force in ZMP lies not in vertical direction (conditions from the paragraph above doesn't hold and R and M_z doesn't compensate corre-

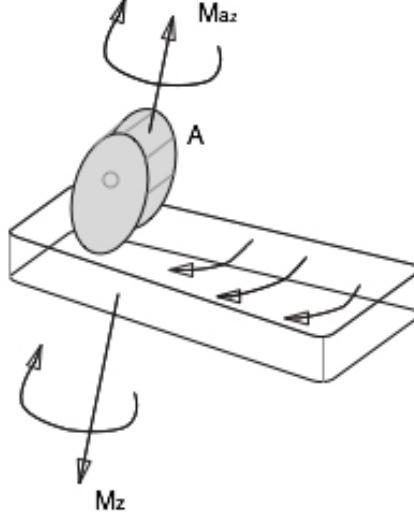


Figure 2.2: Rotational moment in the sole

spondent components of F_a and M_a) than foot will slide. It means that dynamical stability was not achieved due to the fact, that there is a rotational moment that will affect the robot. On the other hand, in [15] it was proven: if ZMP was achieved in the polygon of foot and moreover it coincides with the contact point, than robot is stable, due to the fact, that all the resulting forces lies in vertical direction. During the walk the position of ZMP should be computed simultaneously and the main problem of control is to keep ZMP and contact point to be coincided inside the support polygon of contact foot with the ground. The name zero moment point relates to the fact, that dynamical stability is maintained if horizontal components M_x and M_y are both equal to zero.

$$M_x = M_y = 0 \quad (2.1)$$

In the point P there should exist such equivalent force R and vertical moment M_z that compensate the force reaction of the ground and maintains the stability of the construction. If we want to achieve the dynamical stability, that the following equations holds:

$$R + F_a + mg = 0 \quad (2.2)$$

Where m is a foot mass. In [12] there is defined point O - the origin coordinates frame from which we can define radius vectors \vec{OP} , \vec{OG} and \vec{OA} where A is a point of ankle joint.

$$\vec{OP} \times \vec{R} + \vec{OG} \times mg + M_A + M_z + \vec{OA} \times F_a = 0 \quad (2.3)$$

Placing the origin frame into the point P and making a projection on the horizontal plane gives us the following equations:

$$(\vec{OP} \times \vec{R})^H + \vec{OG} \times mg + M_A^H + (\vec{OA} \times F_a)^H = 0 \quad (2.4)$$

According to [12] equation 2.4 represents the foot equilibrium. However ot doesn't solve the problem, that it is still unknown whether for the given motion of mechanism it is in the equilibrium. It is only of ZMP lies inside the support polygon.

In [16] it was stated, that we have to make the following assumptions in order to compute the position of ZMP:

1. The bipedal robot consists of n rigid links.

2. All kinematic information, such as position of CoM, link orientation, velocities, etc. are known and calculated by forward kinematics.
3. The floor is rigid and motionless.
4. The feet cannot slide over the floor surface.
5. All joints are actively actuated.

With this constraints we can define the mass of the robot as:

$$m_{robot} = \sum_{i=1}^n m_i \quad (2.5)$$

In [16] it was considered schematic bipedal robot to derive the coordinates of ZMP [Fig. 3]

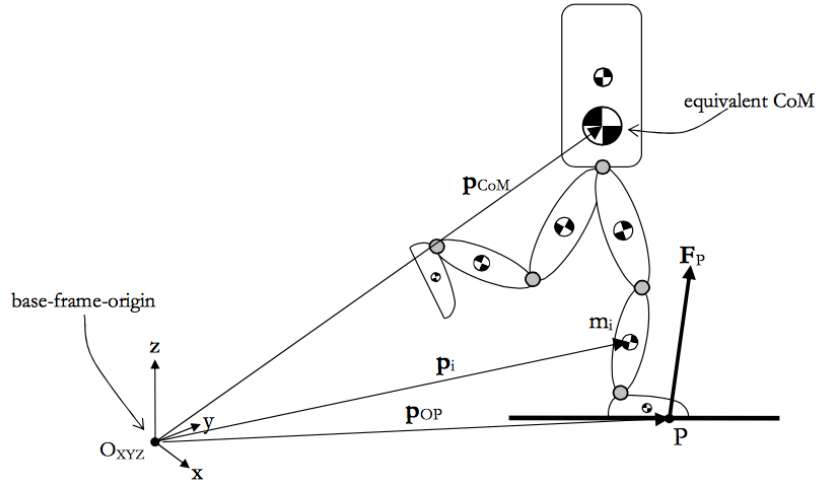


Figure 2.3: Rotational moment in the sole [16]

Here p_i are the distances between base frame and equivalent center of mass of i -link. From this total linear momentum P is:

$$P = \sum_{i=1}^n m_i \dot{p}_i \quad (2.6)$$

And total angular momentum H is:

$$H = \sum_{i=1}^n \dot{p}_i \times m_i \dot{p}_i + I_i \omega_i \quad (2.7)$$

Where ω_i is a angular velocity and I_i is inertia tensor that is computed as:

$$I_i = R_i I_i R_i^T \quad (2.8)$$

Here R_i is a rotation matrix from i -link w.r.t. the origin base frame and I_i is a inertia matrix of i -link w.r.t. the link frame origin attached to their links.

Taking the derivative from 2.6 and 2.7 we have got:

$$\dot{P} = \sum_{i=1}^n m_i \ddot{p}_i \quad (2.9)$$

$$\dot{H} = \sum_{i=1}^n \ddot{p}_i \times m_i \dot{p}_i + \dot{p}_i \times m_i \ddot{p}_i + I_i \dot{\omega}_i + \omega_i \times I_i \omega_i \quad (2.10)$$

In [11] it was mentioned that ZMP approach give us the solution that is based on the principle of dynamical stability, however it is not energy efficient. It requires simultaneous control over all the joints of the robot. The method that was described in [17] is called passive-walker dynamics and it uses gravity forces to reduce the amount of necessary energy to control the robot.

It was mentioned earlier that active control of the robot should be performed with applying dynamical stability principle, elsewhere the robot will loose the balance and fall. So, it makes sense to apply passive-walker dynamics with ZMP based control. According to [12] ZMP method is the most well known and so it is necessary to start with it.

According to [12] the most important task in the bipedal locomotion is to maintain dynamical stability. It can be accomplished if the foot have a full contact with the ground, it means, that the contact is not only in the edge or in the point. Moreover it shows that ZMP position depends on the robot dynamics: the resulting force in the contact polygon and total moment there. So, during the motion the position of ZMP changes and there are situations when ZMP reaches the edge of support polygon. In these situations if additional moments appear, robot will rotate around foot edge and collapse. [12] suggests the way to measure the load on the sole via force sensors on it. The algorithm of ZMP control is quite obvious. Compute wanted ZMP coordinates, measure the error and apply correcting signal. Very important notion is about Center of Pressure (CoP). According to [12] the pressure between foot and the ground can be replaced with the force applied in CoP. With this we can define stability condition as ZMP and CoP coincident. Usually ZMP is required to be under the center of the foot during the single support phase, transitioning to the other foot in the double support phase.

ASIMO - bipedal robot of Honda company was build on top of this theory and the history of its evolution is described in [18]. Nowadays ASIMO is one of the most developed robot, it can interact with human and perform different task starting with playing football and finishing stair climbing.

In [19] it was mentioned the new approach to solve ZMP control problem. Using neural network trained with back propagation method was used to control the position of the robot given the errors between ZMP position and CoP. In [20] the problem of foot rotation was formulated. The author introduced the Foot-Rotation Indicator (FRI) the point, that can leave the support polygon and describe the impending rotation. When FRI lies outside the support polygon it means that there is rotational moment and acting on the foot that helps control instability of the gait.

2.2 Central Pattern Generator

Experiment in [21] shown that reflexes are significant for locomotion. During reverse engineering neural network that controls locomotion was found. It was situated in spinal regions that was the reason to name this network Central Pattern Generator (CPG). Another definition of CPG can be found in [22]: CPG is rhythm generating network in the nervous system which create and control the rhythmic motor patterns of animal motions. This approach for gait generation was considered in [23]. Neural oscillator was used for generation biped motions. And it can be described as neural network, produces rhythmic pattern outputs without the need for patterned input [3]. CPG is a group of oscillating neurons with some phase between them which results rhythmic body motion. The pattern is generated not only by internal neural system but also by external sensor information [23]. The key element in CPG is adaptive neural element, that can be described by pair of first order differential equations. Each pair of the following equations

from adaptive neuron.

$$\tau_1 \dot{x}_1 = -x_1 - \beta f(\nu_1) - \gamma f(x_2) + u_0 + u_{f_1} \quad (2.11)$$

$$\tau_2 \dot{\nu}_1 = -\nu_1 + f(x_1) \quad (2.12)$$

$$\tau_1 \dot{x}_2 = -x_2 - \beta f(\nu_2) - \gamma f(x_1) + u_0 + u_{f_2} \quad (2.13)$$

$$\tau_2 \dot{\nu}_2 = -\nu_2 + f(x_2) \quad (2.14)$$

Here x_1 is initial state of neuron, excited by the constant input u_0 . When excitation reaches some threshold neuron goes to state ν_1 through equation 2.12. When it exceeds some threshold it starts to suppress to the state x_1 through the 2.11 equation by the factor β . Thus x_1 , x_2 , ν_1 and ν_2 are state variables. β represents the rate of adaptations, u_{f_1} and u_{f_2} are the feedback inputs mainly from sensors, γ is the coefficient between state variables and $f(x)$ is a threshold function. Such element works the following way: when it takes constant input it reacts, then adapts and stop reacting, generating oscillations.

Human like gait was achieved by robot with small Degree of Freedom (DoF) in [23]. The idea of this oscillator was to build robust system that perform simple control with minimum structure of neural architecture that can be interesting for high DoF robot.

A detailed examination of a biological CPG from an engineering perspective was conducted in [24] but, for most applications, the neuron pair is approximated with a pair of differential equations [3].

Oscillators can be divided into two types [3]

2.2.1 Simple Sinusoidal Oscillator

For sinusoidal signal it is very easy to maintain phase relationships. Human sized biped was considered in [25]. However it is too simple model and according to [3], is not very appropriate for bipeds, while it is good for systems that are statically stable.

2.2.2 Systems of Differential Equations

Analysis of biological CPGs has identified oscillators made from pairs of mutually inhibiting neurons [26]. These oscillators are able to generate different gaits and produces various solutions from sinusoidal to more complex forms. It can control biped even on the rough ground.

Matsuoka oscillator

Matsuoka oscillator is capable for different gait and is widely used [3]. They are popular because of their dynamics and in particular limit cycle behavior [27].

The model of neuron with adaptation can be represented the following way:

$$\begin{aligned} \tau \dot{x} + x &= \sum_{j=1}^n c_j s_j - bx' \\ T \dot{x}' + x' &= y \\ y &= g(x - \theta) \end{aligned} \quad (2.15)$$

Here τ is a time constant, x is membrane potential of the neuron, s_j is impulse rate of input stimuli, θ is threshold value below which neuron doesn't fire, c_j weights of synaptic conjunctions ($c_j > 0$ for excitatory synapses and $c_j < 0$ for inhibitory synapses), y is firing rate of the neuron, x'

is the variable that represents the degree of the adaptation, T (>0) and b (≥ 0) are parameters that specify the time course of the adaptation [27].

Matsuoka in [27] discuss oscillations generated by mutual inhibition between n neurons with adaptation:

$$\begin{aligned} \dot{x}_i + x_i &= - \sum_{j=1}^n a_{ij} y_j - b x_i' + s_i \\ T \dot{x}_i' + x_i' &= y_i \\ y &= g(x_i) \quad (i = 1, \dots, n) \end{aligned} \tag{2.16}$$

Here a_{ij} represents the strength of inhibitory connection between the neurons. $a_{ij} < 0$ for $i \neq j$ and $= 0$ for $i=j$. $\sum_{j=1}^n a_{ij} y_j$ is the total input from the neurons inside a neural network and s_i is the total input from the outside the network.

Matsuoka oscillator schematically is represented in 2.4.

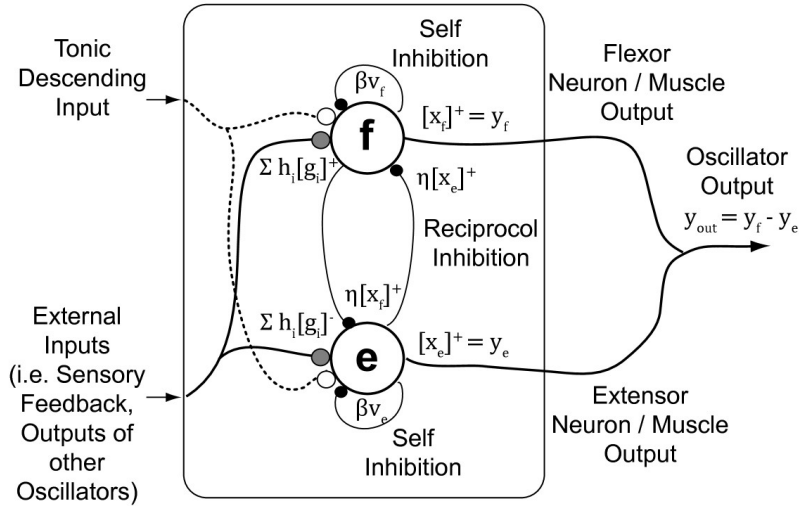


Figure 2.4: Matsuoka oscillator

Two neurons, a flexor (f) and an extensor (e), reciprocally inhibit each other. External inputs (g_i) such as sensory feedback or inputs for other neurons can be either inhibitory or excitatory, depending on the gain (h_i). Black circles indicate inhibitory inputs. White circles indicate excitatory inputs. Gray circles can be either inhibitory or excitatory.

Van der Pol oscillator

Van der Pol oscillator benefits are stable limit cycles and relatively interpretable coefficients. Frequency, amplitude and shape coefficients can be identified, although they are not completely independent. Transition between gaits is reached with simple change of oscillator parameters.

The equation of van der Pol oscillator is:

$$\ddot{x} - \epsilon(1 - x^2)\dot{x} + x = 0 \tag{2.17}$$

Where x is the dynamical variable and $\epsilon > 0$ a parameter. The van der Pol oscillator has exactly one limit cycle and all other trajectories spiral into it that is proved in [28].

Rayleigh oscillator

Rayleigh oscillator is similar to Van der Pol oscillator but it has reduced sensory requirements, that is an advantage over conventional prosthetic systems.

The equation of Rayleigh oscillator is:

$$\ddot{x} + \epsilon(3x^2 - 1)\dot{x} + (\omega^2 - \epsilon)x = 0 \quad (2.18)$$

Amari-Hopfield oscillator

Amari-Hopfield oscillator is similar to Matsuoka oscillator, it generates locomotions resilient to perturbations as a result of limit cycle properties.

Spiking Integrate and Fire with Adaption neurons

Spiking Integrate and Fire with Adaption neurons were used in [29] for biped locomotion. The CPG was a hierarchical structure of hip timing, knee timing and output patterning. This structure allowed to tune parameters of every of three hierarchical part, and so to configure walking frequency, gait and joint angles independently.

2.3 Neural Networks

Despite of the fact that oscillators can be described as a neural network they do not require any input for their work. Canonical Neural Networks (NN) have input data and output. There are several groups of NN.

2.3.1 Feed-Forward Networks

In this networks each neuron has its own connection and transfer function. They are ready for state motion generation. Input data is current kinematics and sensory data. They can generate not state based trajectories only with time input.

Multi-layer perceptron

Multi-layer perceptron (MLP) is one of such models. They have from three (input, output, hidden) layers and can have more hidden ones. According to [30], two MLPs were used to specify parameters of a bipedal ditch crossing gait trained with Genetic Algorithm (GA) produced the best solution in terms of stability. It was more stable and efficient than one from a fully analytical approach, and slightly better than the result obtained with a fuzzy logic based method. Activation function of perceptron is sigmoid function.

Radial Basis Function Network

Radial Basis Function Network is another example of Feed-Forward Networks (FFN). Activation function is usually Gaussian or Euclidean. Neurons in hidden layers connected only with small part of input neurons. For this reason two types of vectors are necessary: weights vector and centre vector which is the same dimension as input. Each vector responds if it is close to its weight vector. Output neurones are the functions of linear combinations of outputs of network and their weighted connections. It was used for hexapod locomotion [31].

Cerebellar Model Articulation Controller

A Cerebellar Model Articulation Controller (CMAC) is a type of associative memory network based on cerebellum [32]. Input space is continuous and divided into hyper-rectangles. So input should be located at one rectangle in the moment. Numerous hidden layers are slightly moved rectangles. Hence rectangles will overlap on different layers. The output for each layer is wighted sum of activated rectangles. The CMACs successfully learned the movement patterns and showed resilience to perturbation (including on uneven or slippery floors), thereby translating a rigid analytical solution into an adaptable one [33].

2.3.2 Recurrent Networks

The structure of such networks is more complicated than FFN. Thus we can produce more complex patterns and handle different type input.

For recurrent networks there are different types of input and the difference between FFN is that pattern is not required to be provided as an input but it is generated , tuned or chosen internally by the inputs.

Jordan and Elman Recurrent NN

Jordan recurrent NN is similar to FFN, the difference is that output of the network is recurrently fed to the input.

Elman recurrent NN the difference from Jordan recurrent NN is that delayed output of hidden layer is connected with input of hidden layer. The Elman network was used in [34], the resilient back-propagation training algorithm was used and the system showed an ability to learn supervised trajectories and interpolate between them. The example of Elman recurrent NN is shown on 2.5

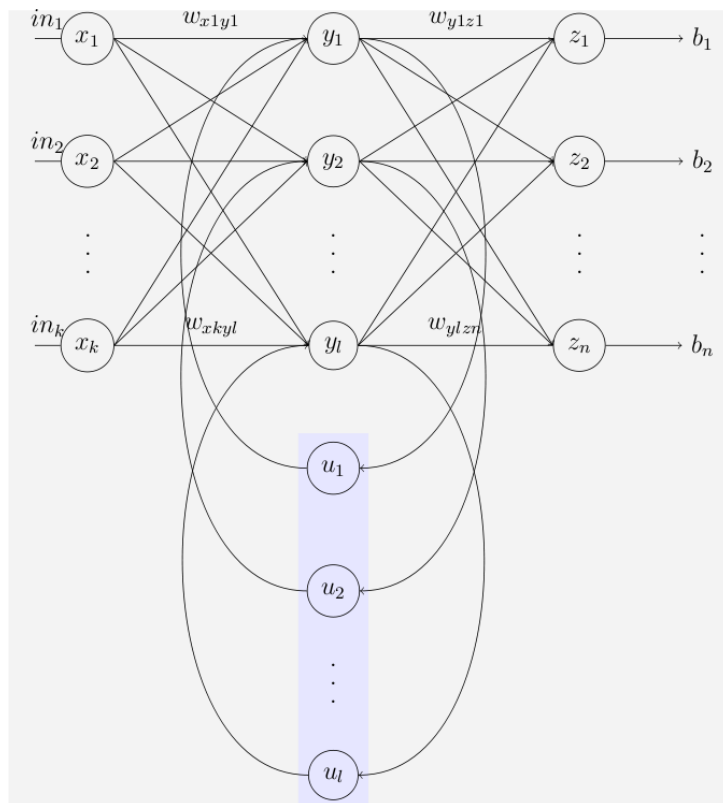


Figure 2.5: Elman recurrent NN

Fully Connected Recurrent NN

In several works [35], [36] a network of several fully connected leaky-integrator neurons were used as a pattern generator.

The network was able to learn multiple sinusoidal patterns, selectable by an input level, but evolution took more generations as the number of patterns required increased. Learned patterns were resilient to noise at the inputs, and even if the input was disrupted by a large amount, the output would quickly return to normal when the input was corrected. It was found that a six neuron model was sufficient to store eight different sinusoidal patterns, as long as the form of those patterns was different [3].

The problem of GA parameters optimization is that for complex systems a huge amount of generations will necessary.

Reservoir

Usually recurrent NN should be as small as possible order to simplify parameters tuning. Reservoir network follows different principle. It uses big network with potentially much redundancy. The idea is that during training only output layer is trained and reservoir is unchanged. It works with the following assumption: system dynamics is already present when the network is constructed randomly and the only necessary thing is to adjust weights for it. Thus the training process is very simple, e.g. linear regression.

There is practice [37] of generating trajectories with reservoir taken the human capture data.

2.4 Hidden Markov Model

Learning by imitation is one of commonly used approach for bipedal locomotion researches. Obviously, direct copying of movements operator is impossible due to different kinematic and dynamic characteristics. So, from the operator we can take only the pattern and than imitate it on the robot. Here observing is estimating the underlying state variables of the source system where only output data is available. For this task Hidden Markov Models can be used [38].

Recognition algorithm is used for identification of movement. If movement was not identified it is added to database as new. Hidden Markov model provides abstraction of the pattern which is used for motion synthesis.

Although typically used for imitation tasks, HMM have also been employed to detect problematic states.

The problem of Hidden Markov Model is that it doesn't provide emergent behavior.

2.5 Rule based approach

After the identification of the current state we can find the next one using rule-based method. For bipeds fuzzy-logic systems were used in some researches [39]. Fuzzy logic controller helps to deal with a bit of uncertainty in the environment. And it can be used to vary ZMP position in the support polygon [39]. For proper work it requires optimization of rules, that was basically chosen [30].

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