#### Assignment 1; due Friday November 7

#### Part 1

### Exercise 1 Solution

The system is the closed kinematic chain.

- (a) False
- (b) False
- (c) False
- (d) True.

### Exercise 2 Solution

- (a) FALSE. SCARA robots can consist only of 4 rotational axes
- (b) TRUE. 3 rotational axes can give us 3 DoF. The forth one cannot add one more.
- (c) FALSE. The Chebyshev linkage has 4 rotational joints and only one DoF.
- (d) FALSE. The explanation is like in previous example.

### Exercise 3 Solution

- (a) TRUE. By definition.
- (b) FALSE. By definition.
- (c) FALSE. Because of b)
- (d) FALSE. Because of a)

# Exercise 4 Solution

- (a) FALSE. We can choose coordinates frames in the end effector.
- (b) TRUE. We can choose coordinates frames in the end effector, so it could be many matrices. If there is only one base frame there is only one DH matrix.
- (c) FALSE. Because we can change direction of X and Z axes. However, multiplication of all DH matrices will give us translation from base frame to the frame in the end effector and it will be unique.
- (d) FALSE. The same explanation as in c)

#### Part 2

# Exercise 1 Solution

$$\begin{aligned} & a_{i-1} \quad \alpha_{i-1} \quad d_i \quad \theta_i \\ & 1 \quad 0 \quad 0 \quad 0 \quad \theta_1 \\ & 2 \quad 0 \quad -\frac{\pi}{2} \quad 0 \quad \theta_2 \\ & 3 \quad 20 \quad 0 \quad 0 \quad 0 \\ & 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 0 \quad 1 \quad 0 \\ & -\sin(\theta_1) \quad \cos(\theta_1) \quad 0 \quad 0 \\ & 0 \quad 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 0 \quad 1 \quad 0 \\ & -\sin(\theta_2) \quad -\cos(\theta_2) \quad 0 \quad 0 \\ & 0 \quad 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 1 \quad 0 \\ & 0 \quad 0 \quad 0 \quad 1 \end{aligned}$$

# Exercise 2 Solution

0

 ${}_{6}^{0}T_{4} = \left( \begin{array}{cccc} 0.7857 & -0.2540 & -0.5641 & -1.6624 \\ 0.6163 & 0.2430 & 0.7491 & 0.2349 \\ 0.0532 & 0.9362 & -0.3475 & 0.2124 \\ 0 & 0 & 0 & 1 \end{array} \right)$ 

 ${}_{6}^{0}T_{5} = \begin{pmatrix} 0.4057 & 0.3911 & -0.8261 & -0.1587 \\ -0.5013 & -0.6606 & -0.5589 & 1.8721 \\ 0.7643 & -0.6408 & 0.0719 & 0.9183 \end{pmatrix}$ 

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$$\frac{3}{4}T = \begin{pmatrix} \cos(\theta_4) & -\sin(\theta_4) & 0 & 0.2 \\ 0 & 0 & 1 & 0 \\ -\sin(\theta_4) & -\cos(\theta_4) & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\frac{4}{5}T = \begin{pmatrix} \cos(\theta_5) & -\sin(\theta_5) & 0 & 1.5 \\ \sin(\theta_5) & \cos(\theta_5) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\frac{5}{6}T = \begin{pmatrix} \cos(\theta_6) & -\sin(\theta_6) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\frac{6}{6}T = \frac{0}{172}\frac{1}{173}\frac{2}{17}\frac{3}{17}\frac{4}{15}\frac{5}{6}T = \begin{pmatrix} \cos(\theta_6) & -\sin(\theta_6) & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\frac{6}{6}T = \frac{0}{172}\frac{1}{173}\frac{2}{17}\frac{3}{17}\frac{4}{15}\frac{5}{6}T = \begin{pmatrix} -\frac{\cos(\theta_6) -\cos(\theta_6) -\cos(\theta_6) & -\cos(\theta_6) &$$

Exercise 3
Solution

#### Exercise 4

#### Solution

#### Exercise 5

### Solution