

Universidade do Minho
Escola de Engenharia

A NOVEL OPENFOAM SOLVER FOR ALUMINIUM ALLOY PROFILE EXTRUSION


A. OLIVEIRA^{1,2}, H. PUGA³, J. MIGUEL NÓBREGA²

¹ PORTALUM - PORTUGUESA DE ALUMÍNIO, LDA, R. de Casares 670, 4820 Fafe, Portugal, antoniopedro.adf@hotmail.com

² Institute for Polymers and Composites, University of Minho, Campus de Azurém, 4800-058 Guimarães, Portugal, mnobrega@dep.uminho.pt

³CMEMS – UMinho, University of Minho, Campus of Azurém, 4800-058, Guimarães, Portugal, helderpuga@gmail.com

Contents

- 
- 1 Introduction
 - 2 Motivation and goals
 - 3 State of the art
 - 4 alExtFoam implementation and verification
 - 5 alExtFoam verification and validation
 - 6 Conclusions and Future work

1 Introduction

Industry

- Architecture/construction;
- Automobile and transportation industry.

Properties

- Low density;
- Good electrical and thermal conductivity;
- Reflectivity;
- Low toxicity.

Application of aluminum extrusion profiles



Heat sinks



Door handles



Window structures

1 Introduction

Direct extrusion

Extrusion Types:

- Direct extrusion;
- Indirect extrusion;
- Hydrostatic;
- Side extrusion;
- Impact extrusion;
- Etc.

Direct extrusion press :



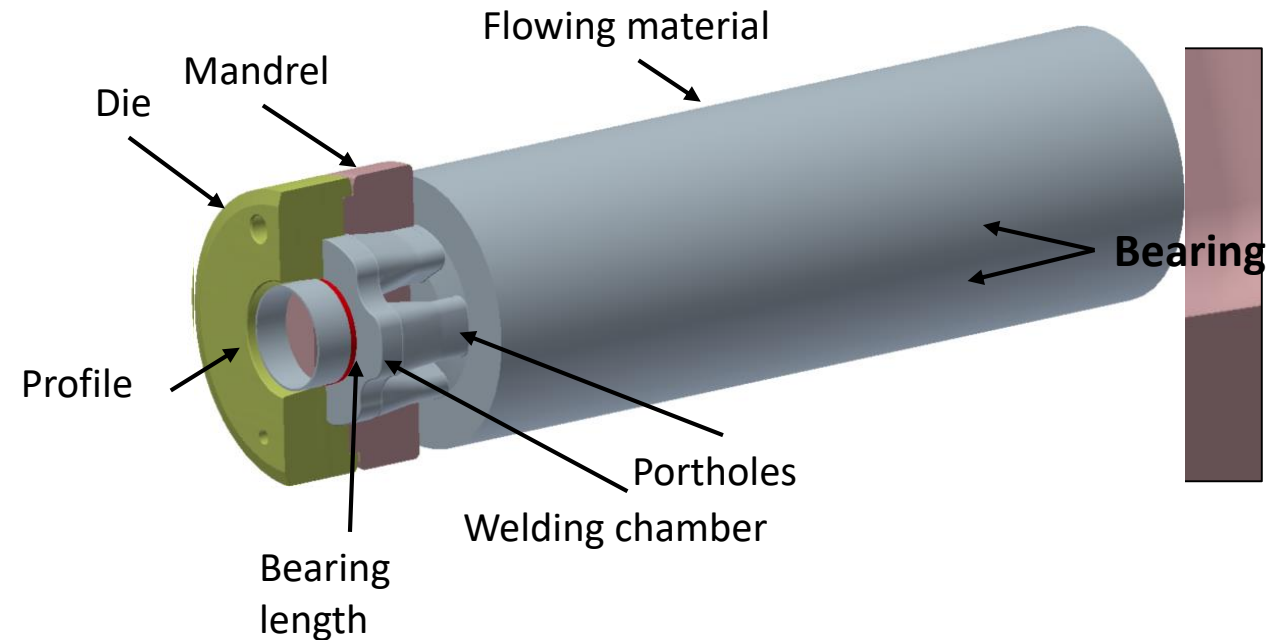
1 Introduction

Extrusion dies

Challenge: Assure that the material flows through the die outlet with the same average velocity

Bearing:

1. Is the parallel zone located at the die exit;
2. Will settle the shape of the extruded profile;
3. Longer bearing length higher resistance to the flow;
4. Aims promoting a balanced flow distribution.



1 Introduction

Extrusion dies: Flow balancing checks

Physical tests

- Experimental trial-and-error iterations with bearing length corrections;
- Time consuming;
- Expensive method (400€/test).



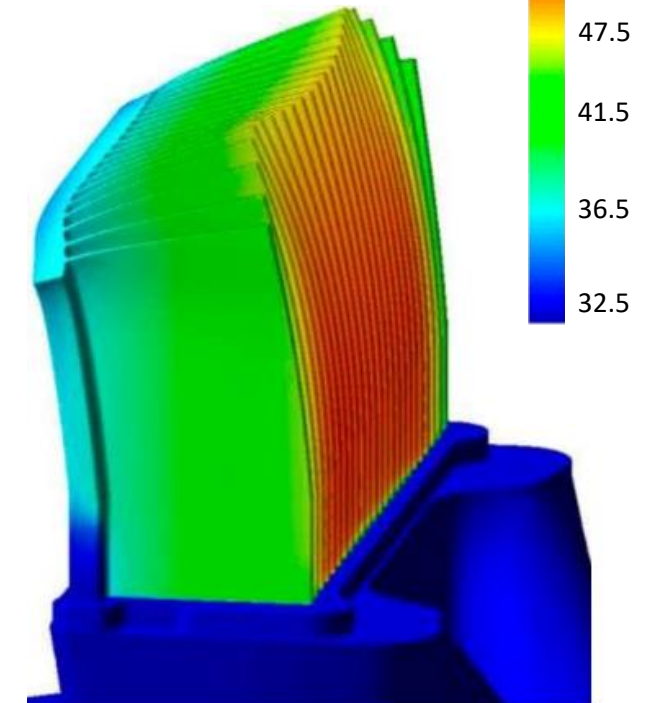
Computational modelling

- Optimize the bearing length with process simulation;
- Reduce the resources spent in physical tests.

non-uniform flow



Experimental



Simulation

1 Introduction



- Aluminum alloy casting and extrusion company;
- Located in Fafe, Portugal;
- Casting division - capacity of 40 tons per day;
- Extrusion division - capacity of 15 tons per day;

2 Motivation and goals

Motivation

- Increase the knowledge about aluminum extrusion;
- Improve design methodology;
- Reduce production costs, without affecting the product performance.

Goals

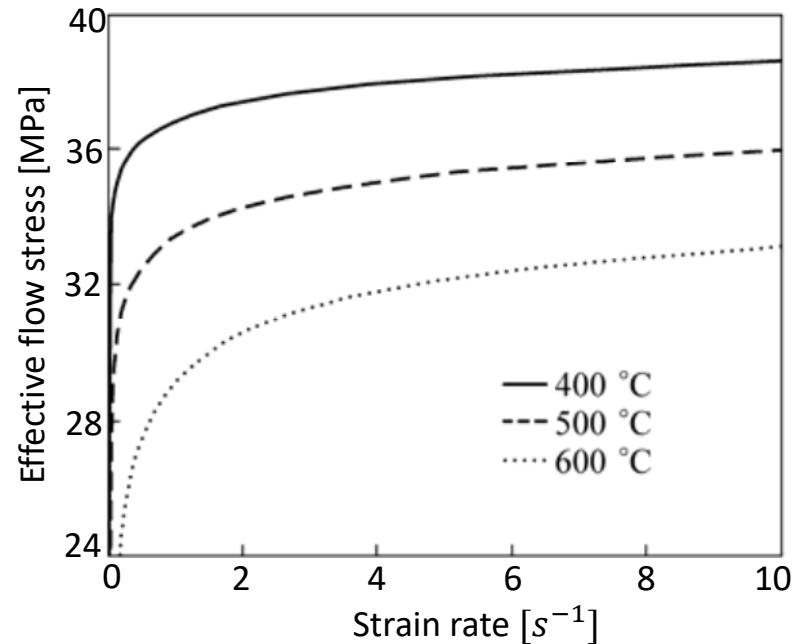
- Create a computational code capable of simulating the extrusion process of aluminum alloys (alExtFoam);
- Verify and validate the developed code;
- Test the application of the code in an industrial relevant problem.

3 State of art

Constitutive equations for the aluminum alloys

The effective flow stress for hot aluminum alloys:

$$\bar{\tau} = f(\dot{\varepsilon}, T)$$



Constitutive models to predict effective flow stress:

- Norton-Hoff

$$\bar{\tau}_{ij,NH} = 2K_{NH}(\sqrt{3}\dot{\varepsilon})^{e-1}\dot{\varepsilon}_{ij}$$

- Hansel-Spittel

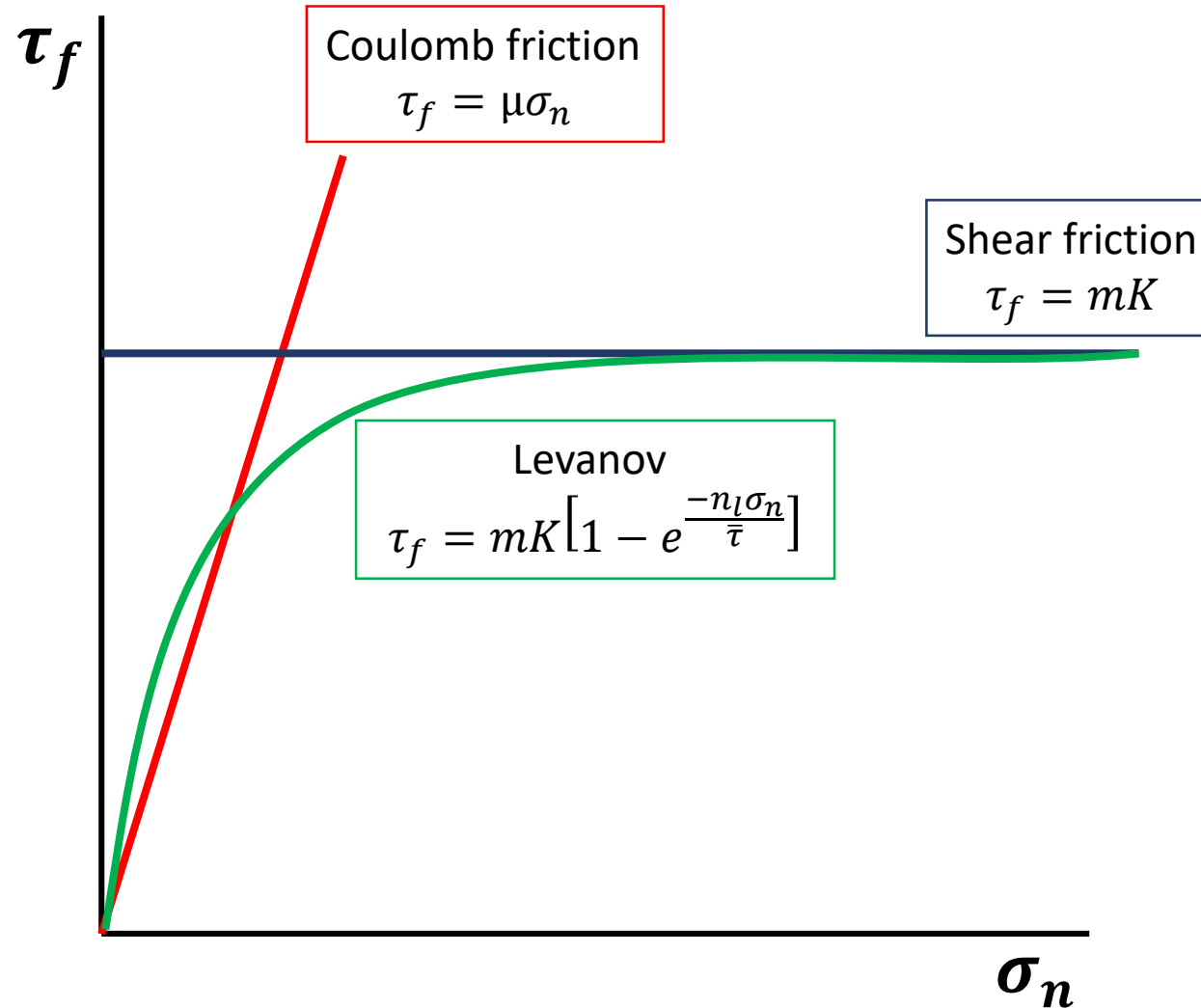
$$\bar{\tau}_{HS} = Ae^{m_1 T} T^{m_9} \varepsilon^{m_2} e^{\frac{m_4}{\varepsilon}} (1 + \varepsilon)^{m_5} T e^{m_7 \varepsilon} \dot{\varepsilon}^{m_3} \dot{\varepsilon}^{m_8} T$$

- Zener-Hollomon

$$\bar{\tau}_{ZH} = \frac{1}{\alpha} \sinh^{-1} \left(\left(\frac{Z}{A} \right)^{1/n} \right), \quad Z = \dot{\varepsilon} e^{\frac{Q}{RT}}$$

3 State of art

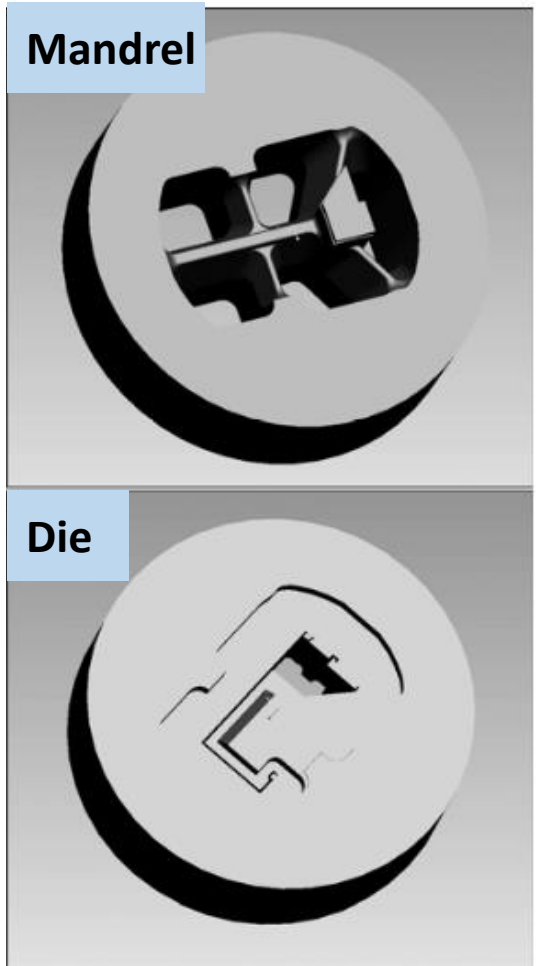
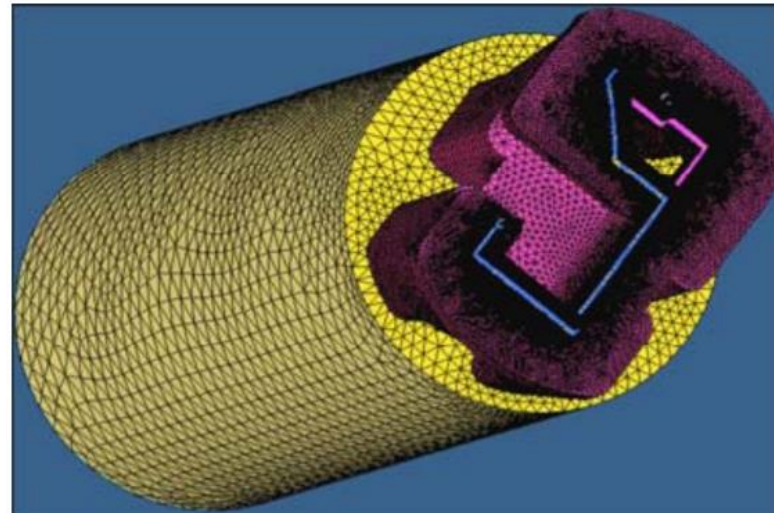
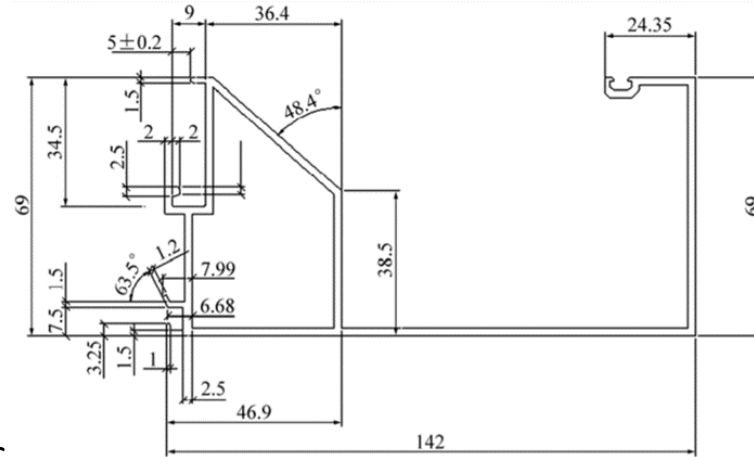
Wall boundary conditions



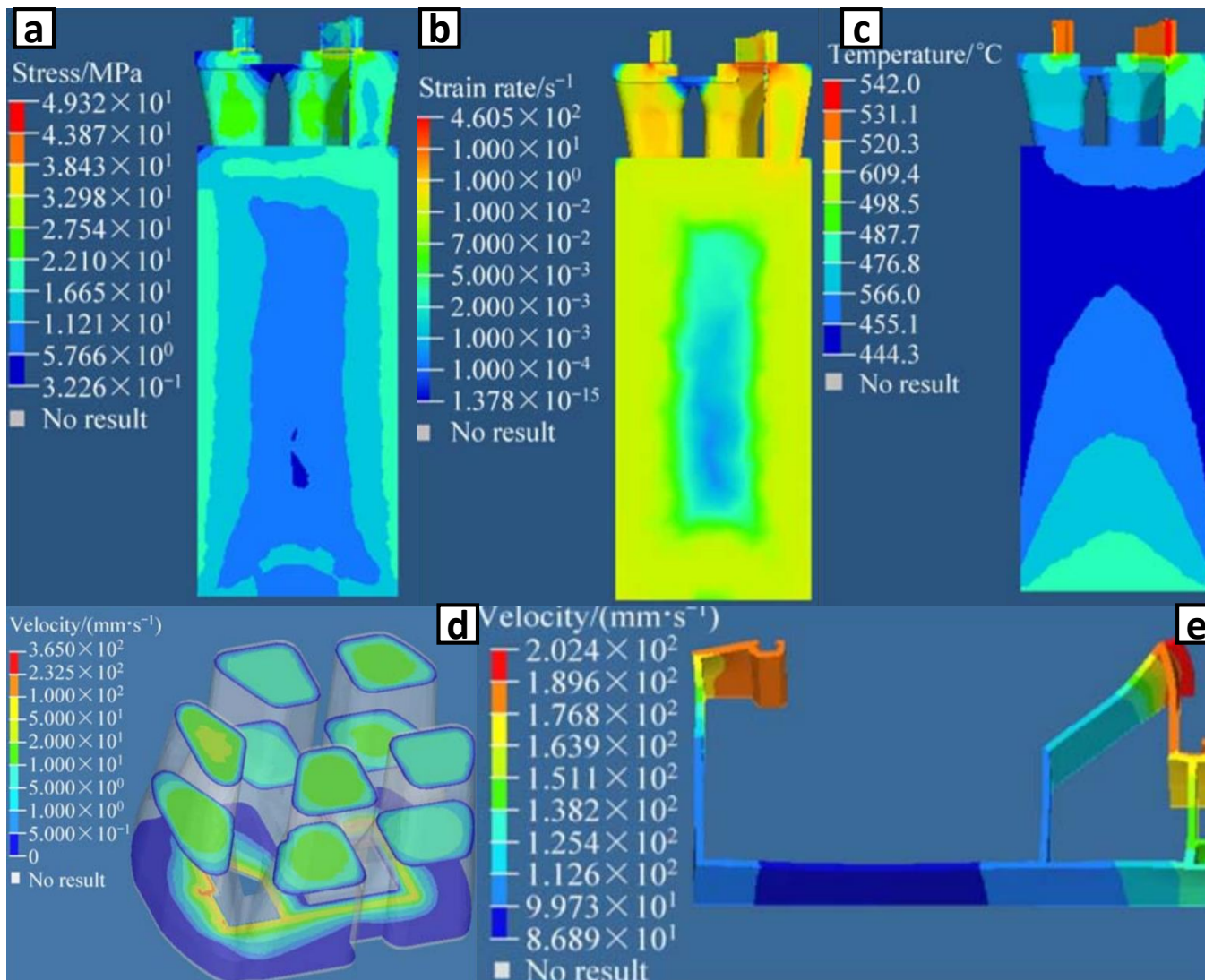
3 State of art

Illustrative study*

- AA6063
- Zener-Hollomon constitutive model
- Shear friction and Coulomb friction models



3 State of art

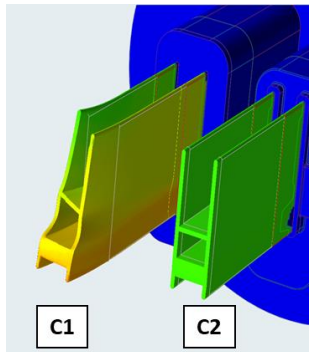


Z. HE, H. Wang, M. Wang, and G. LI, "Simulation of extrusion process of complicated aluminium profile and die trial," Trans. Nonferrous Met. Soc. China, vol. 22, no. 7, pp. 1732–1737, 2012

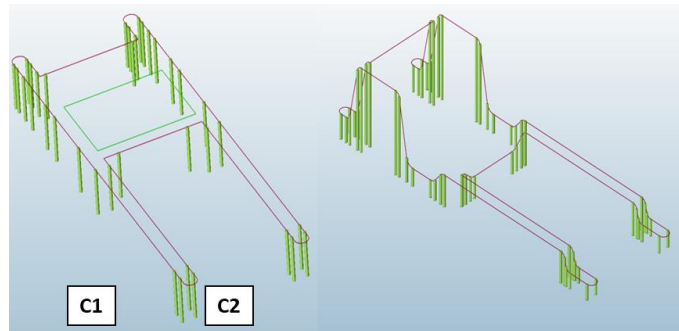
3 State of art

QFORM

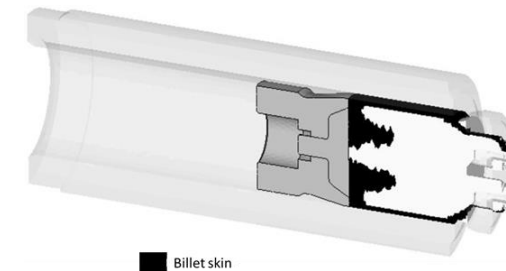
Altair Inspire™ Extrude Metal



Nose cone prediction

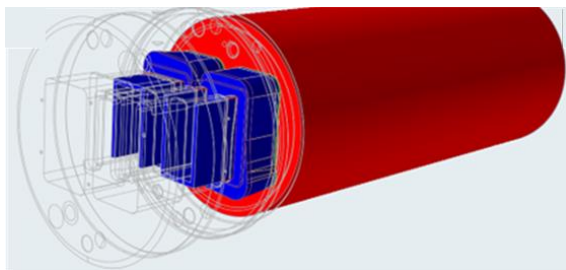


Bearing optimization

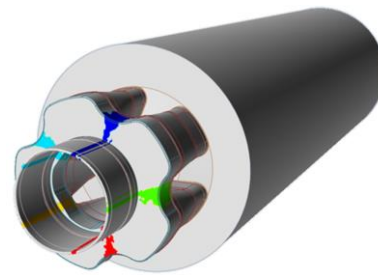


Skin tracking

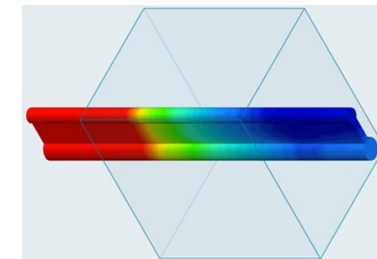
Profile quality



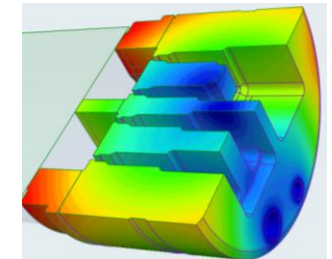
Transverse weld length



Weld quality and location



Quenching



Tool deflection

4 alExtFoam implementation and verification

Solver implementation

Base code: *SimpleFOAM*

1. Linear momentum conservation law

$$u_j \frac{\partial u_i}{\partial x_j} = -\frac{1}{\rho} \frac{\partial p}{\partial x_i} + \nu \frac{\partial^2 u_i}{\partial x_j \partial x_j}$$

2. Continuity equation

$$\frac{\partial u_i}{\partial x_i} = 0$$

SimpleFOAM

Extrusion process:

```
Info << "\nStarting time loop\n" << endl;
while (simple.loop())
{
    Incompressible;
    Non-Newtonian;
    Non-isothermal;
    Steady-state.
    laminarTransport.correct();
    turbulence->correct();

    runTime.write();

    runTime.printExecutionTime(Info);
}

Info << "End\n" << endl;
return 0;
```


4 alExtFoam implementation and verification

Solver implementation

Base code: *SimpleFOAM*

1. Linear momentum conservation law

$$u_j \frac{\partial u_i}{\partial x_j} = -\frac{1}{\rho} \frac{\partial p}{\partial x_i} + \nu \frac{\partial^2 u_i}{\partial x_j \partial x_j}$$

2. Continuity equation

$$\frac{\partial u_i}{\partial x_i} = 0$$

3. Energy conservation equation

$$\frac{\partial (Tu_i)}{\partial x_i} - \frac{\partial}{\partial x_i} \left(\alpha_{td} \frac{\partial T}{\partial x_i} \right) = \frac{1}{\rho c_p} \tau'_{ij} \frac{\partial u_i}{\partial x_j}$$

alExtFoam

```
Info << "\nStarting time loop\n" << endl;

while (simple.loop())
{
    Info<< "Time = " << runTime.timeName() << nl << endl;

    {
        #include "UEqn.H"
        #include "pEqn.H"
    }

    #include "TEqn.H"

    laminarTransport.correct();
    turbulence->correct();

    runTime.write();

    runTime.printExecutionTime(Info);
}

Info << "End\n" << endl;
return 0;
```

4 alExtFoam implementation and verification

Solver implementation

alExtFoam

Energy conservation equation

Energy conservation equation

$$\underbrace{\frac{\partial(Tu_i)}{\partial x_i}}_{\text{advection}} \underbrace{- \frac{\partial}{\partial x_i} \left(\alpha_{td} \frac{\partial T}{\partial x_i} \right)}_{\text{diffusion}} = \underbrace{\frac{1}{\rho c_p} \tau'_{ij} \frac{\partial u_i}{\partial x_j}}_{\text{source}}$$

1

2

3

```
while (simple.correctNonOrthogonal())
{
    volTensorField gradU = fvc::grad(U);
    tmp <volScalarField> nu = laminarTransport.nu();
    tmp <volSymmTensorField> taurho = scalar(2)*nu*symm(gradU);
    //taurho = tau divided by rho

    fvScalarMatrix TEqn
    (
        fvm::div(phi, T) ← 1
        - fvm::laplacian(DT, T) ← 2
        - (1/c)*(taurho && gradU) ← 3
    ==
        fvOptions(T)
    );
    TEqn.relax();
    fvOptions.constrain(TEqn);
    TEqn.solve();
    fvOptions.correct(T);
}
```


4 alExtFoam implementation and verification

Constitutive equation - Zener-Hollomon model Implementation

```

① [ volScalarField& T=U_.mesh().lookupObject<volScalarField>("T");
    Tw_ = (min(max(T, Tmin_)), Tmax_);

② [ volTensorField gradU = fvc::grad(U_);
    strainRate_ = symm(gradU);

③ → effectiveStrainRate_ = ( max(sqrt(scalar(2.0/3.0)*magSqr(strainRate_))(),(eSRMin_)));

④ → ZenerHollomon_ = effectiveStrainRate_*exp(Q_/(Tw_*R_));
⑤ → effectiveFlowStress_ = (asinh(pow( ZenerHollomon_/A_,(scalar(1)/n_))))/alpha_;
    dynamicViscosity_ = (effectiveFlowStress_/(scalar(3)*effectiveStrainRate_));

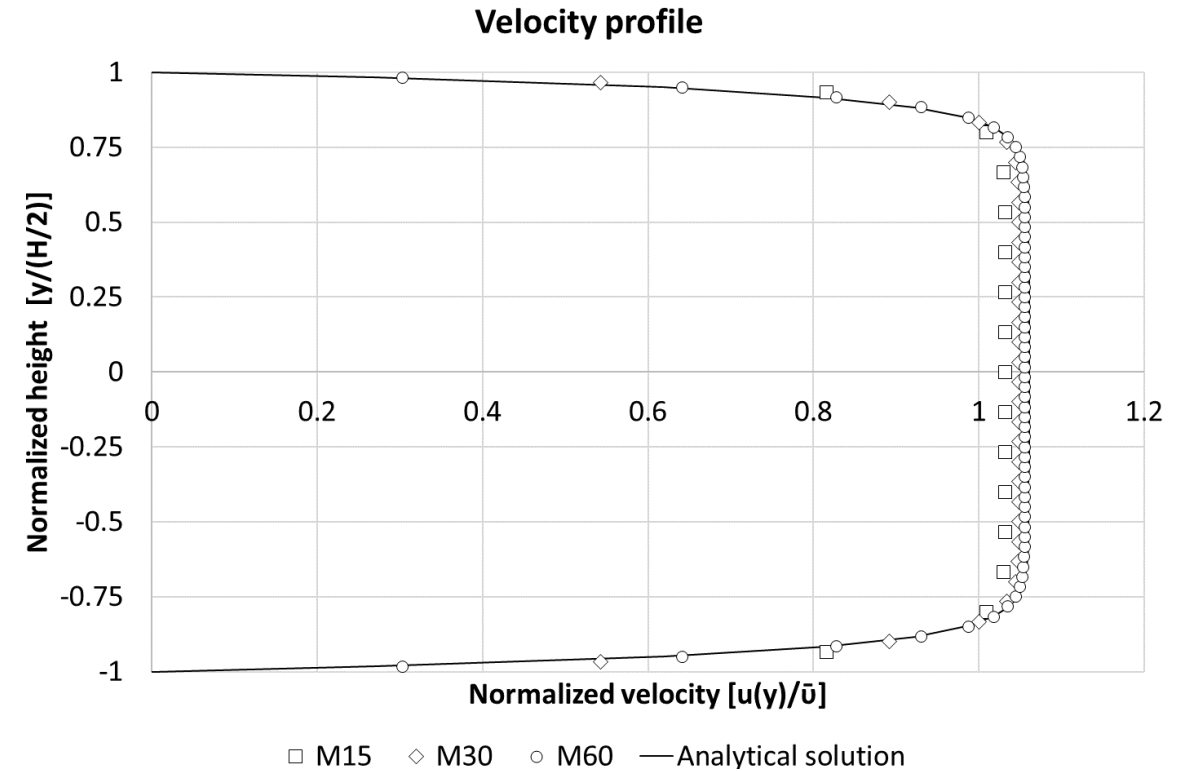
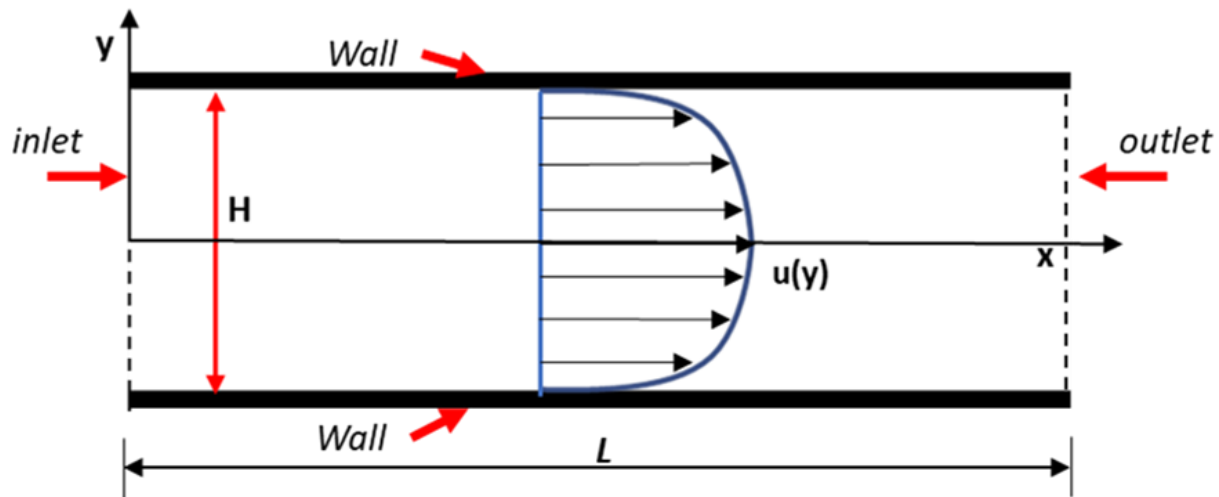
⑥ [ return
    (
        dynamicViscosity_/rho_
    );

```

$$\left. \begin{aligned}
 T &= \begin{cases} T > T_{min} \\ T < T_{max} \end{cases} \\
 \dot{\epsilon}_{ij} &= \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)
 \end{aligned} \right\} \xrightarrow{\text{①}} \dot{\epsilon} = \sqrt{\frac{2}{3} \dot{\epsilon}_{ij} \dot{\epsilon}_{ij}} \xrightarrow{\text{②}} \dot{\epsilon} > eSRMin \xrightarrow{\text{③}} Z = \dot{\epsilon} e^{\frac{Q}{RT}} \xrightarrow{\text{④}} \bar{\tau} = \frac{1}{\alpha} \sinh^{-1} \left(\left(\frac{Z}{A} \right)^{1/n} \right) \xrightarrow{\text{⑤}} v = \frac{1}{3\rho} \frac{\bar{\tau}}{\dot{\epsilon}} \xrightarrow{\text{⑥}}$$

4 alExtFoam implementation and verification

Constitutive equation - Flow between parallel plates



	M15	M30	M60
RMSE %	2	0.6	0.3

4 alExtFoam implementation and verification

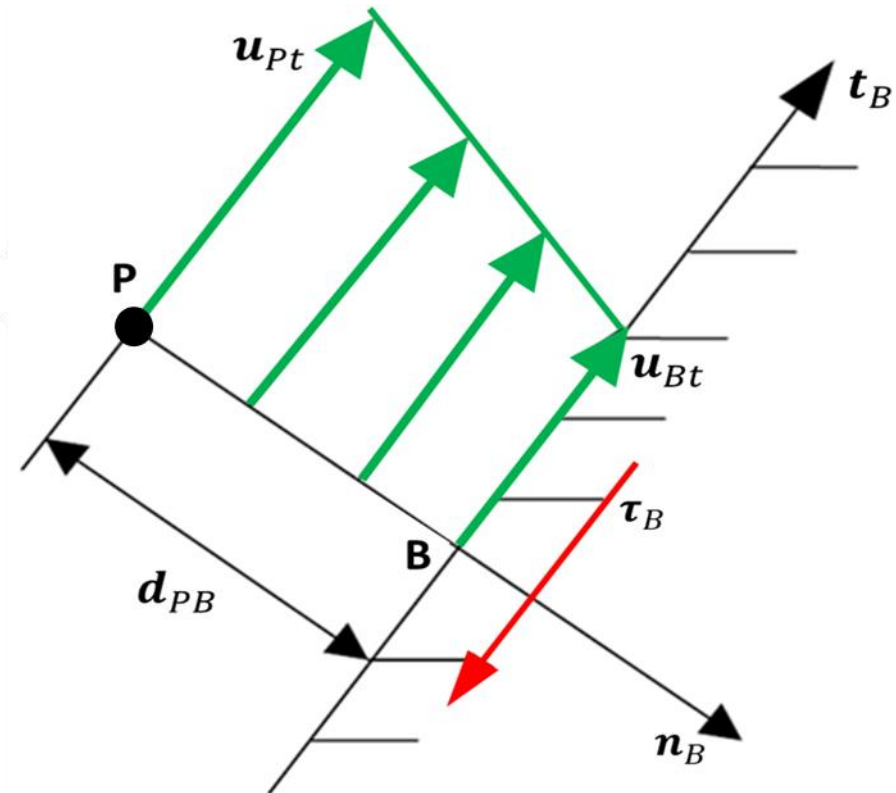
Slip boundary condition - Implementation

Shear friction law

$$\tau_B = mK$$

Velocity in the boundary:

$$u_{Bt} = \begin{cases} u_{Pt} (1 - f(\dot{\epsilon}_{ij})), & f(\dot{\epsilon}_{ij}) < 1 \\ 0, & f(\dot{\epsilon}_{ij}) \geq 1 \end{cases}$$



4 alExtFoam implementation and verification

Slip boundary condition - Implementation

Shear friction law

$$\tau_B = mK$$

Velocity in the boundary:

$$u_{Bt} = \begin{cases} u_{Pt} (1 - f(\dot{\epsilon}_{ij})), & f(\dot{\epsilon}_{ij}) < 1 \\ 0, & f(\dot{\epsilon}_{ij}) \geq 1 \end{cases}$$

Diagram illustrating the implementation of the shear friction law and velocity calculation:

- ①: $f(\dot{\epsilon}_{ij})$ is calculated using dynamic viscosity and effective flow stress.
- ②: $f(\dot{\epsilon}_{ij})$ is calculated using the effective flow stress and the shear rate.
- ③: $f(\dot{\epsilon}_{ij})$ is calculated using the slip factor, shear rate, and dynamic viscosity.
- ④: $f(\dot{\epsilon}_{ij})$ is calculated using the slip factor, shear rate, and dynamic viscosity.
- ⑤: $f(\dot{\epsilon}_{ij})$ is calculated using the slip factor, shear rate, and dynamic viscosity.
- ⑥: u_{Bt} is calculated using the slip factor, shear rate, and dynamic viscosity.

shearFrictionModelFoam

```

① { const volScalarField& dynamicViscosity =this-
    >db().objectRegistry::lookupObject<volScalarField> ("dynamicViscosity");
    scalarField Dvw= dynamicViscosity.boundaryField()[patchI];

② { const volScalarField& effectiveFlowStress =this-
    >db().objectRegistry::lookupObject<volScalarField> ("effectiveFlowStress");
    volScalarField k = effectiveFlowStress/sqrt(scalar(3));
    scalarField kw = k.boundaryField()[patchI];

③ → scalarField dist = scalar(1)/(this->patch().deltaCoeffs());

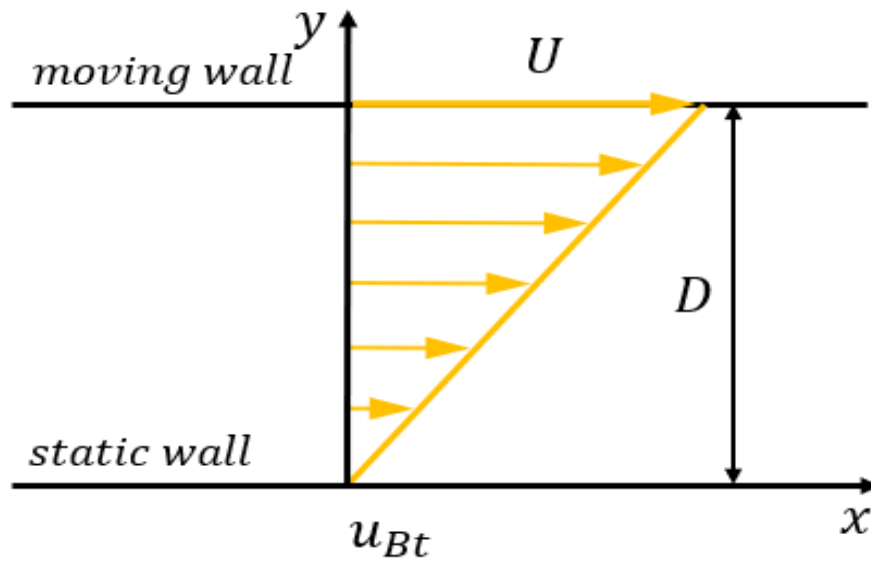
④ { vectorField velInt = this->patchInternalField();
    vectorField velIntTg = transform(I - sqr(nHat), velInt);
    scalarField magVelIntTg = mag(velIntTg);

⑤ → scalarField strainFunction = (slipFactor_*kw*dist)/(Dvw*(magVelIntTg + SMALL));
    forAll(this->patch(), faceI)
    {
        if (strainFunction[faceI] < scalar(1.0))
        {
            u_wallslip[faceI] = velIntTg[faceI]*(1.0 - strainFunction[faceI]);
        }
        else
        {
            u_wallslip[faceI] = vector::zero;
        }
    }
  }

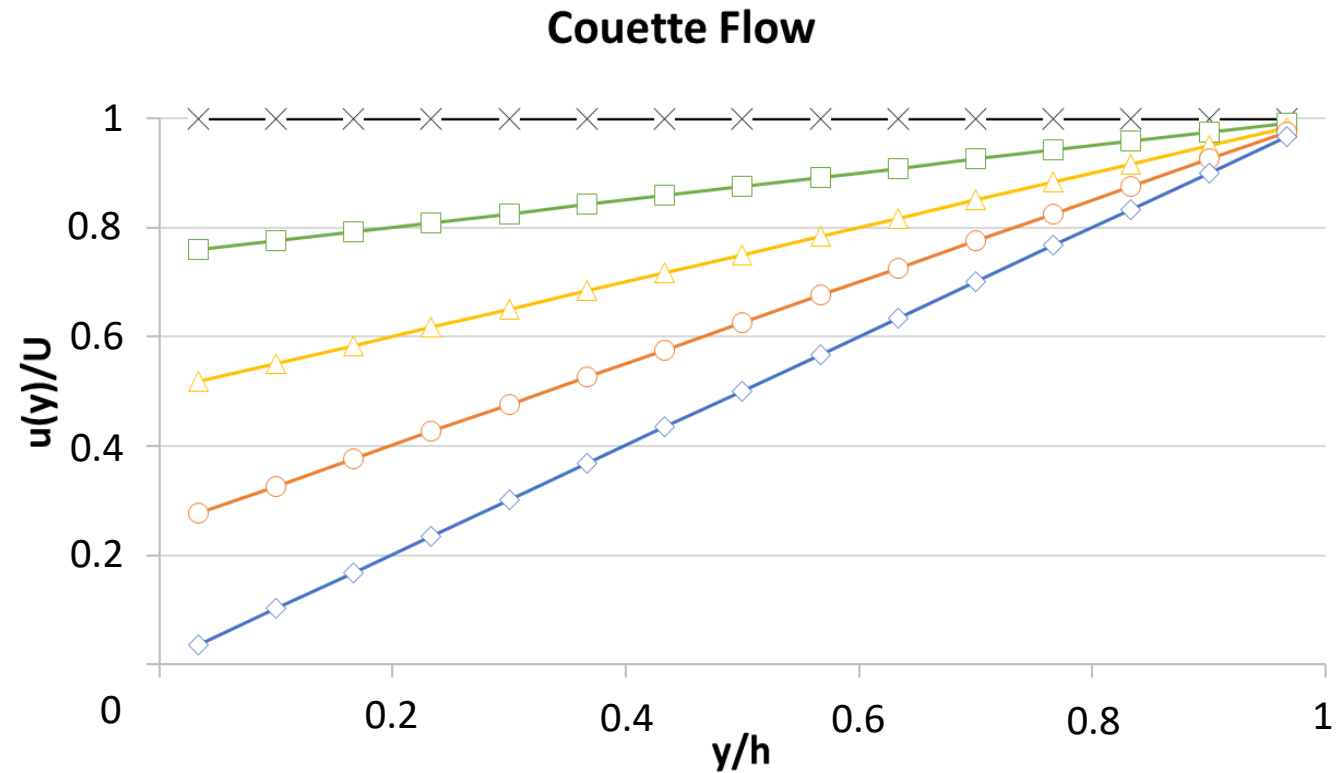
```

4 alExtFoam implementation and verification

Slip boundary condition – Couette Flow



$$u(y) = U - m\sqrt{3}\dot{\epsilon}(y - D)$$



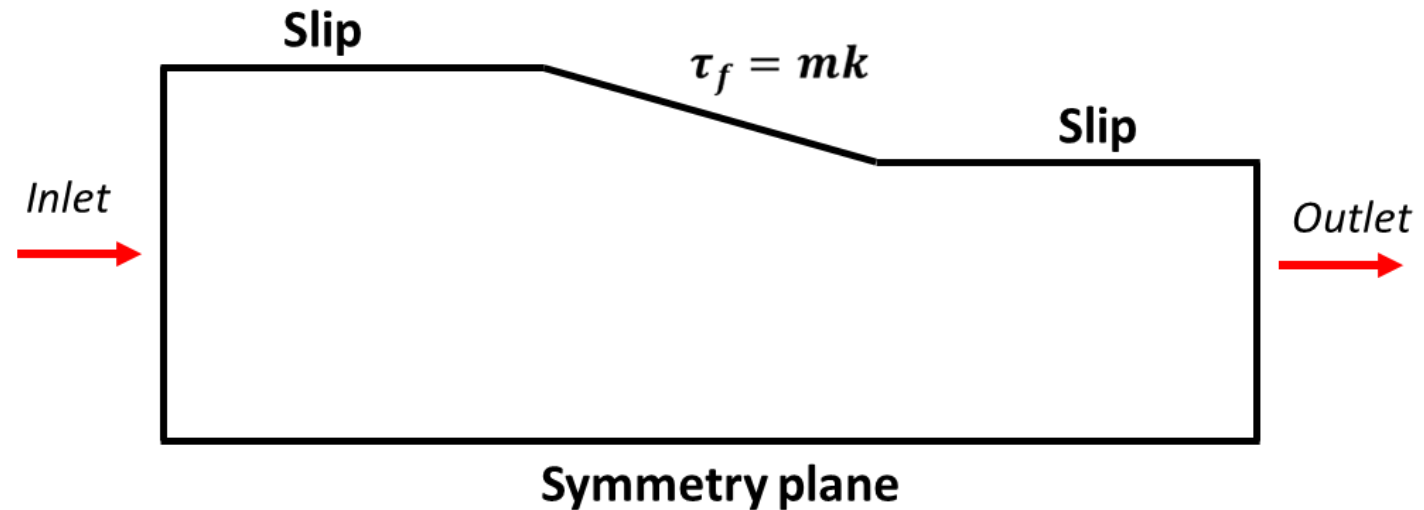
m	0	0.25	0.5	0.75	1
Numerical solution	×	□	△	○	◇
Analytical solution	—	—	—	—	—

4 alExtFoam implementation and verification

Slip boundary condition - Convergent die

Considerations:

- Plane strain forward extrusion through a convergent die;
- Verify *shearFrictionModelFoam*:
 - Segal experimental case;
 - Bašić numerical simulation.
- Constant yield stress;
- **shearFrictionModelFoam** ($m = 1$)

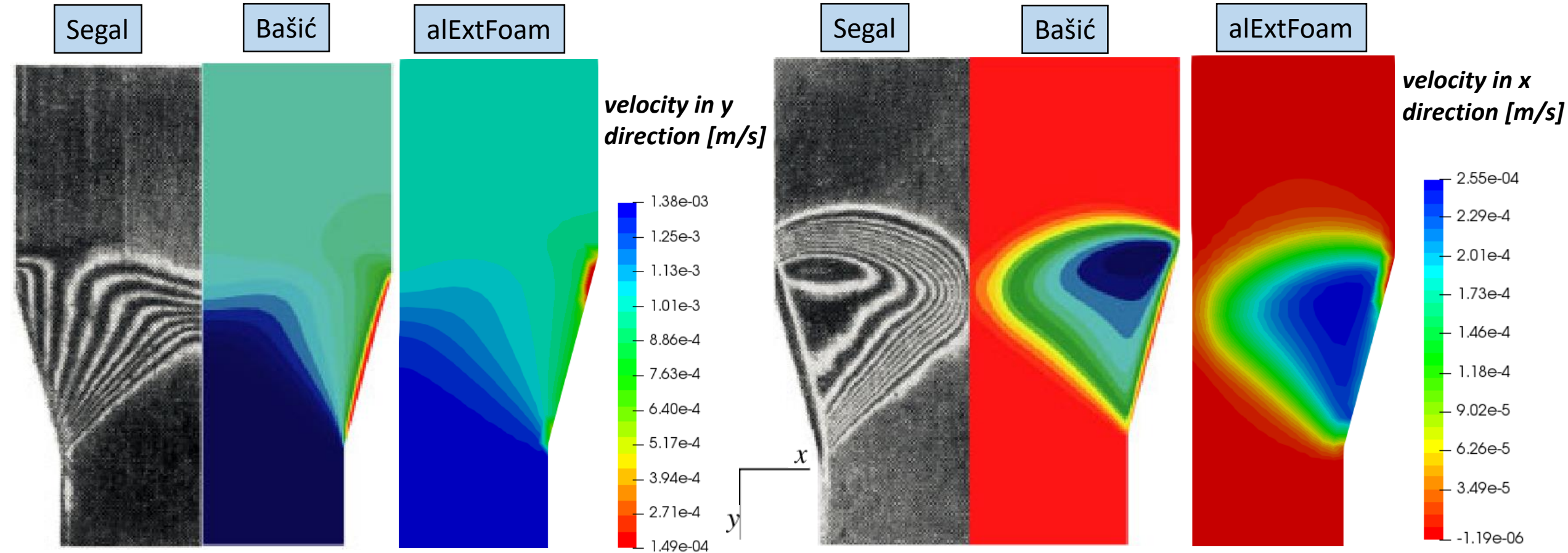


V. Segal and E. Makušok, "Analysis of Plastic Metal Deformation by Moire Method.," *Metallurgical*, vol. VI, 1974.

H. Bašić, I. Demirdžić, and S. Muzaferija, "Finite volume method for simulation of extrusion processes," 2005.

4 alExtFoam implementation and verification

Slip boundary condition - Convergent die



V. Segal and E. Makušok, "Analysis of Plastic Metal Deformation by Moire Method.," *Metallurgical*, vol. VI, 1974.

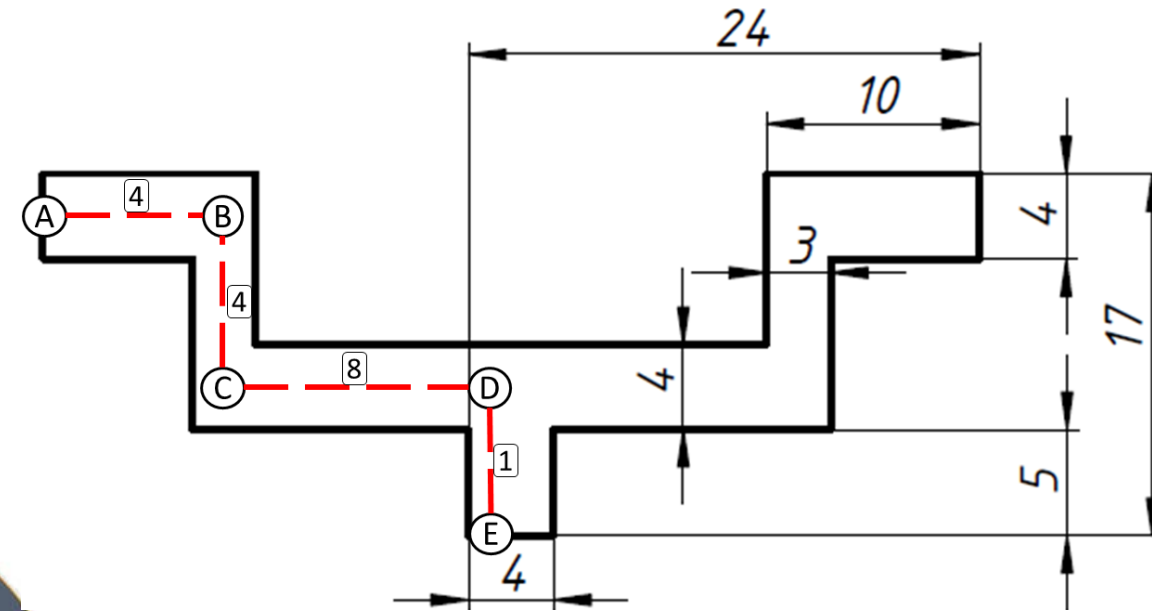
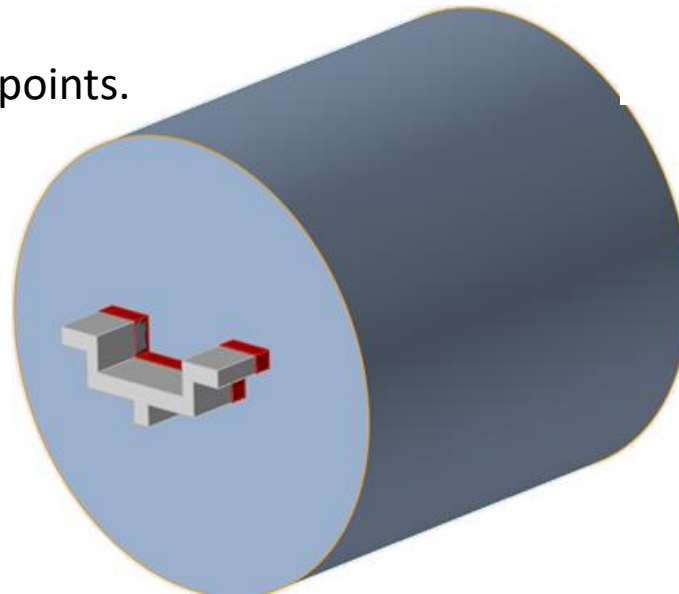
H. Bašić, I. Demirdžić, and S. Muzaferija, "Finite volume method for simulation of extrusion processes," 2005.

5 alExtFoam verification and validation

U-shaped profile

Considerations:

- Comparison of *alExtFoam* with *IEM*;
- Zener-Holomon Constitutive model;
- *ShearFrictionModelFoam* with different friction coefficient;
- Velocity checked in 22 central points.



Dimensions in [mm]

Figure 10 is a line graph showing the velocity profile of the flow at the inlet for two different models: IEM (red line with circles) and alExtFoam (black line with squares). The x-axis is labeled "Points" and ranges from 1 to 20. The y-axis is labeled "Velocity [m/s]" and ranges from 0.55 to 0.8. The graph shows two curves that start at approximately 0.61 m/s at point 1 and increase to a peak of about 0.77 m/s at point 20. The IEM curve is slightly higher than the alExtFoam curve for most of the range. Vertical dashed lines mark points A, B, C, D, and E on the x-axis.

Points	IEM [m/s]	alExtFoam [m/s]
1	0.61	0.61
2	0.62	0.61
3	0.63	0.63
4	0.64	0.64
5	0.65	0.65
6	0.66	0.66
7	0.67	0.67
8	0.68	0.68
9	0.69	0.69
10	0.70	0.70
11	0.71	0.71
12	0.72	0.72
13	0.73	0.73
14	0.74	0.74
15	0.75	0.75
16	0.76	0.76
17	0.76	0.76
18	0.76	0.76
19	0.76	0.76
20	0.76	0.76



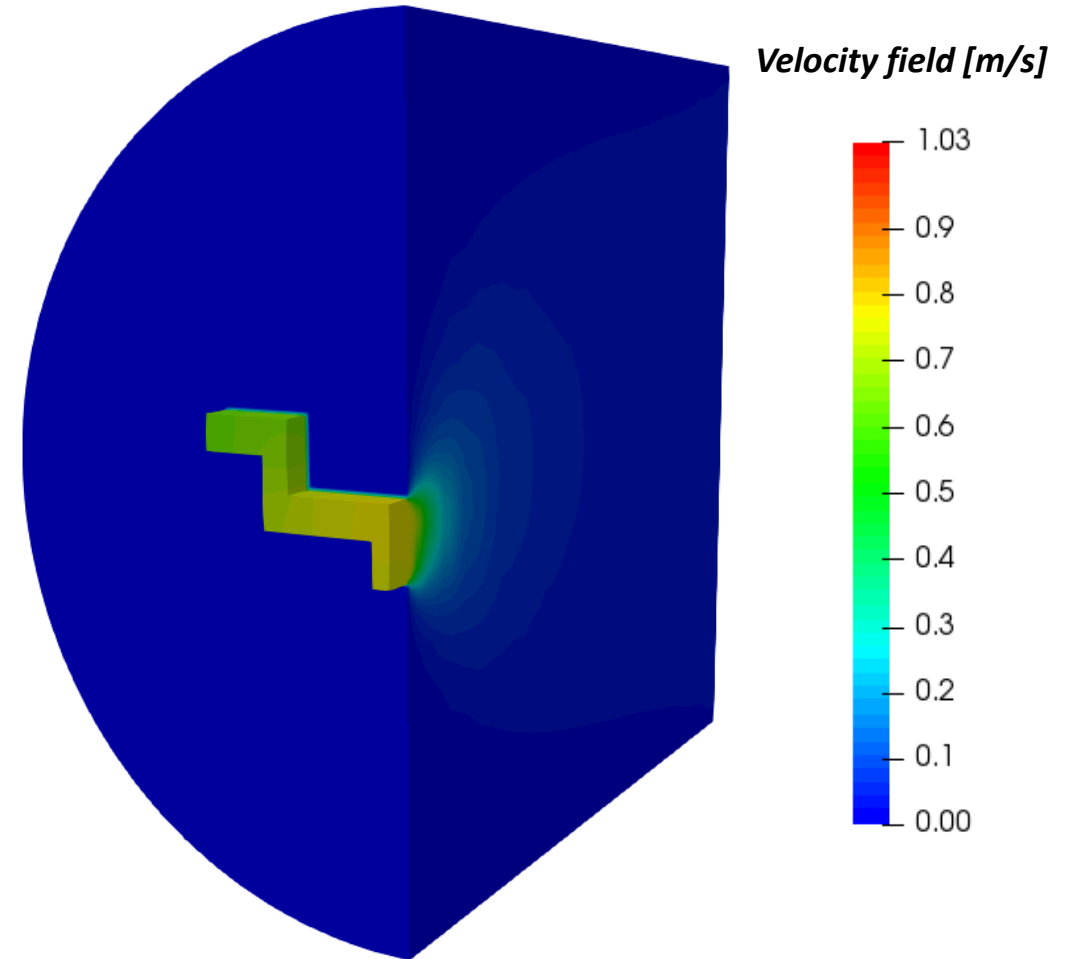
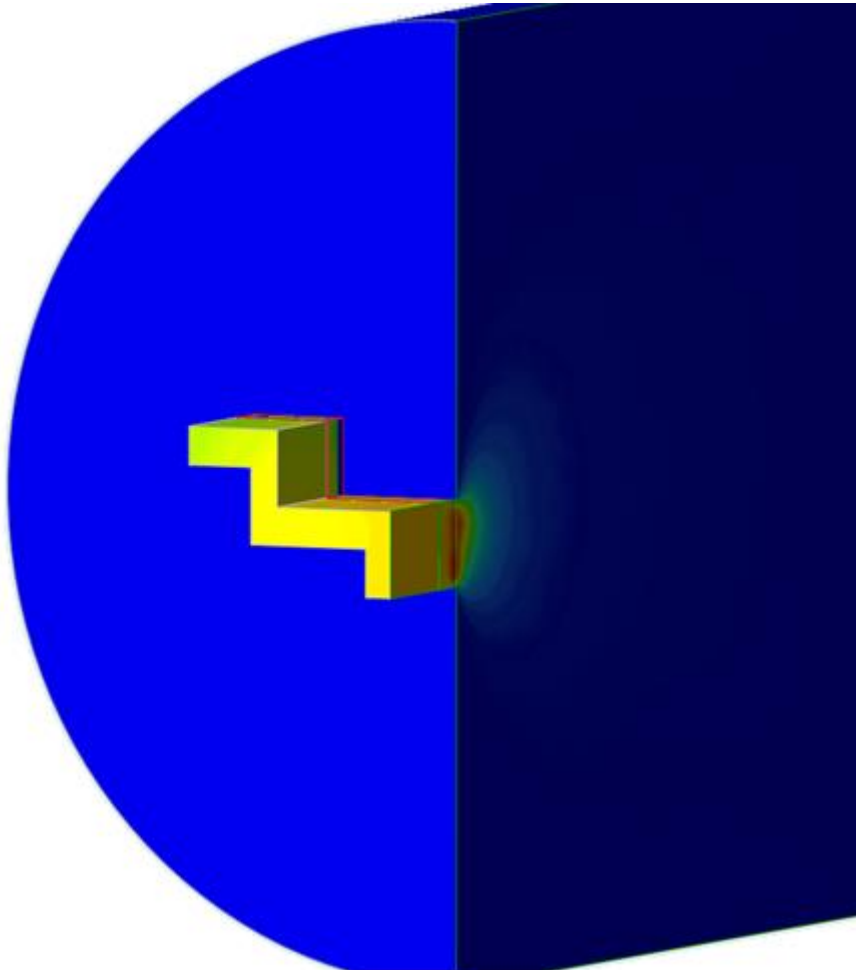
5 alExtFoam verification and validation

U-shaped profile: Results

IEM

alExtFoam

Velocity
field



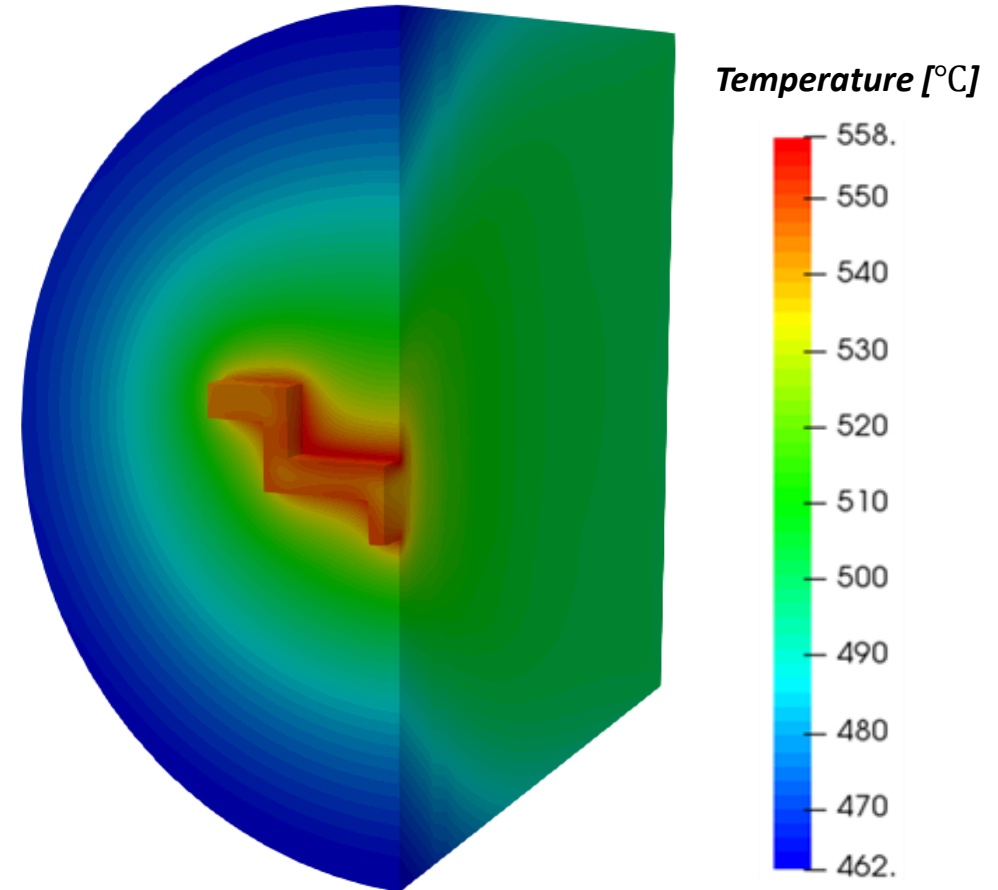
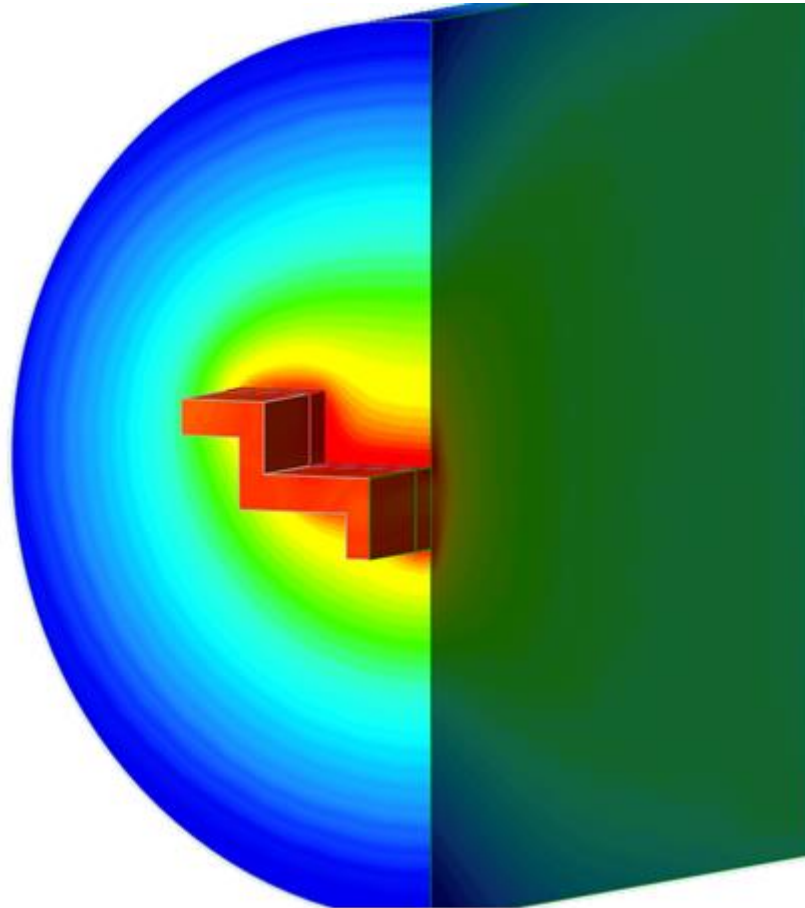
5 alExtFoam verification and validation

U-shaped profile: Results

IEM

alExtFoam

Temperature
field



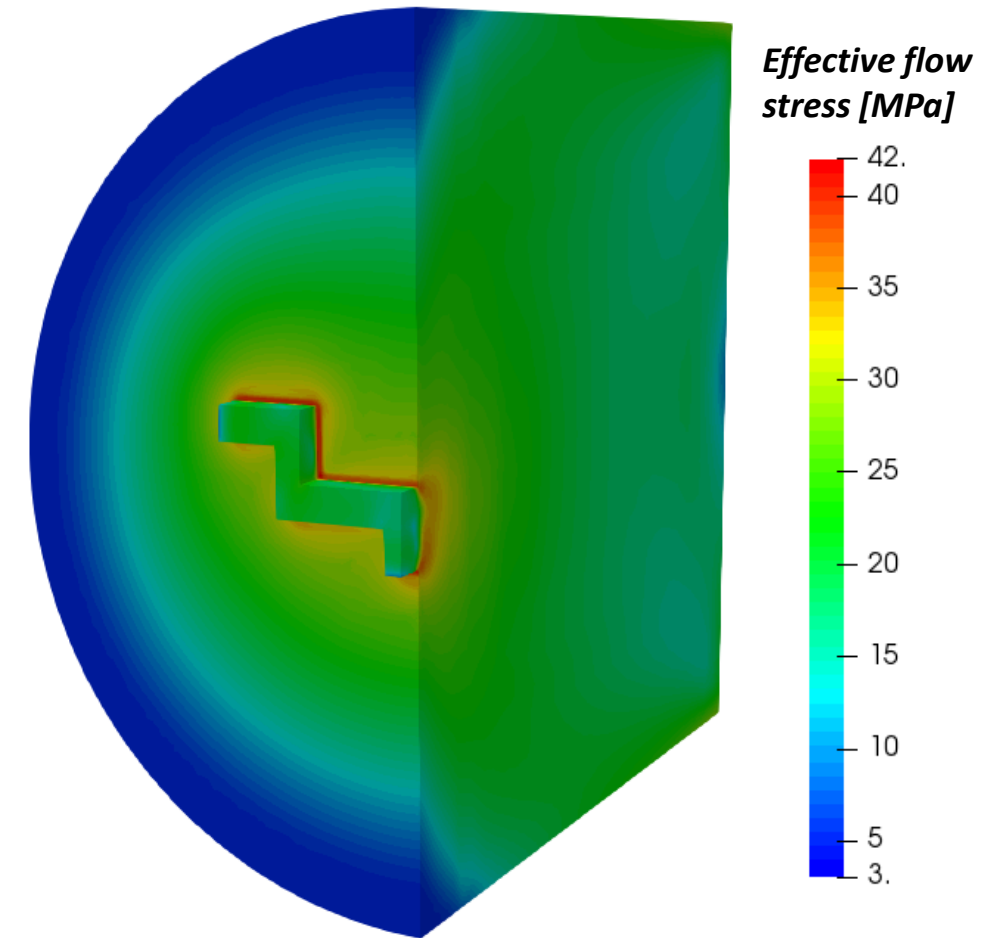
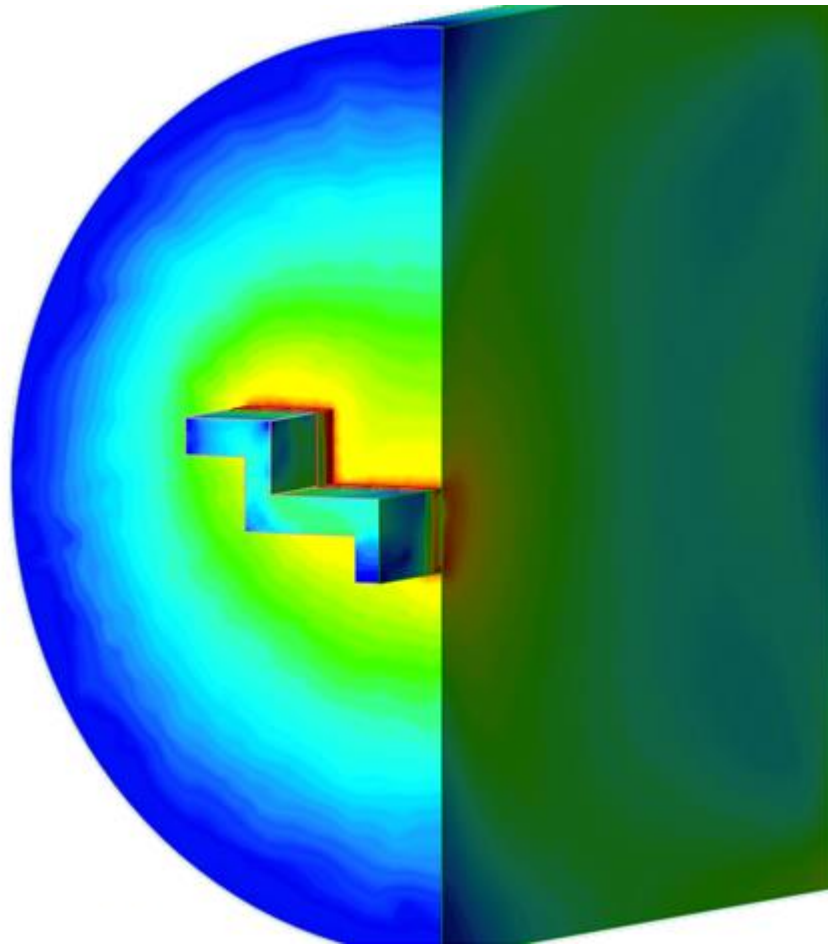
5 alExtFoam verification and validation

U-shaped profile: Results

IEM

alExtFoam

Effective flow
stress field



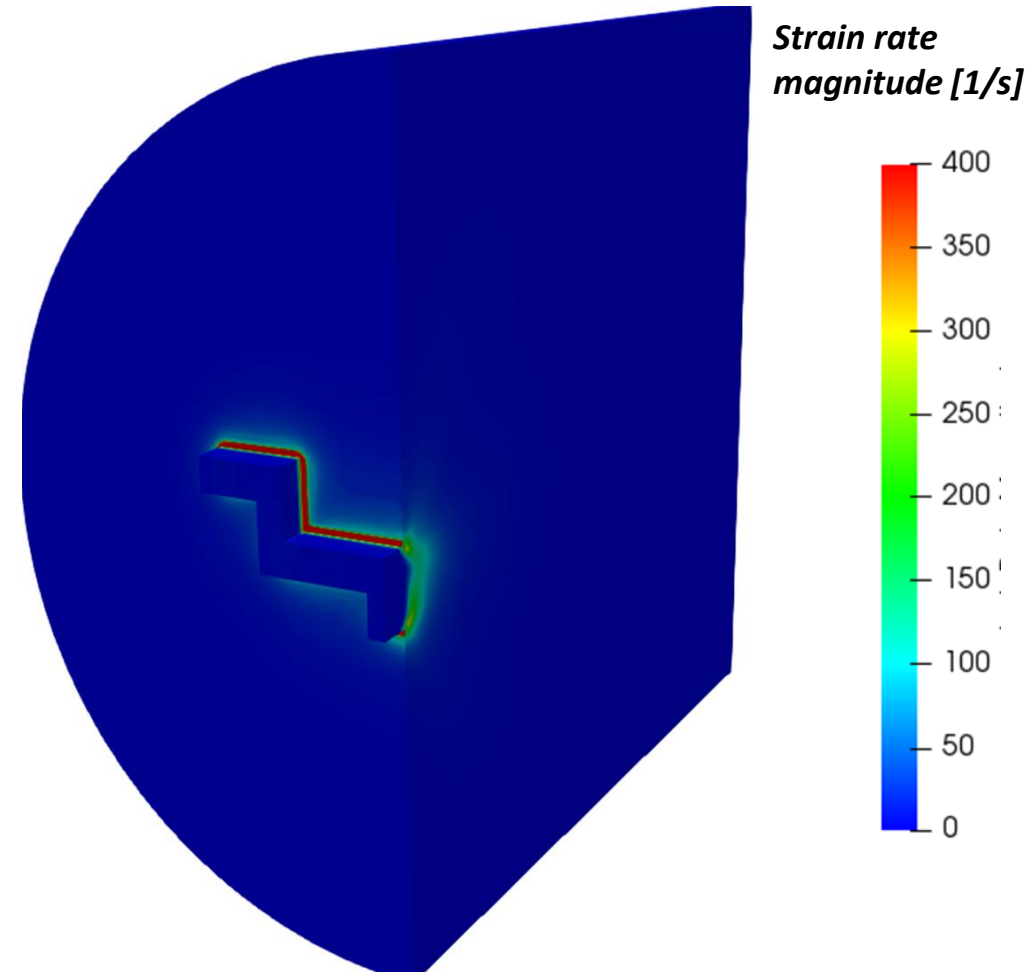
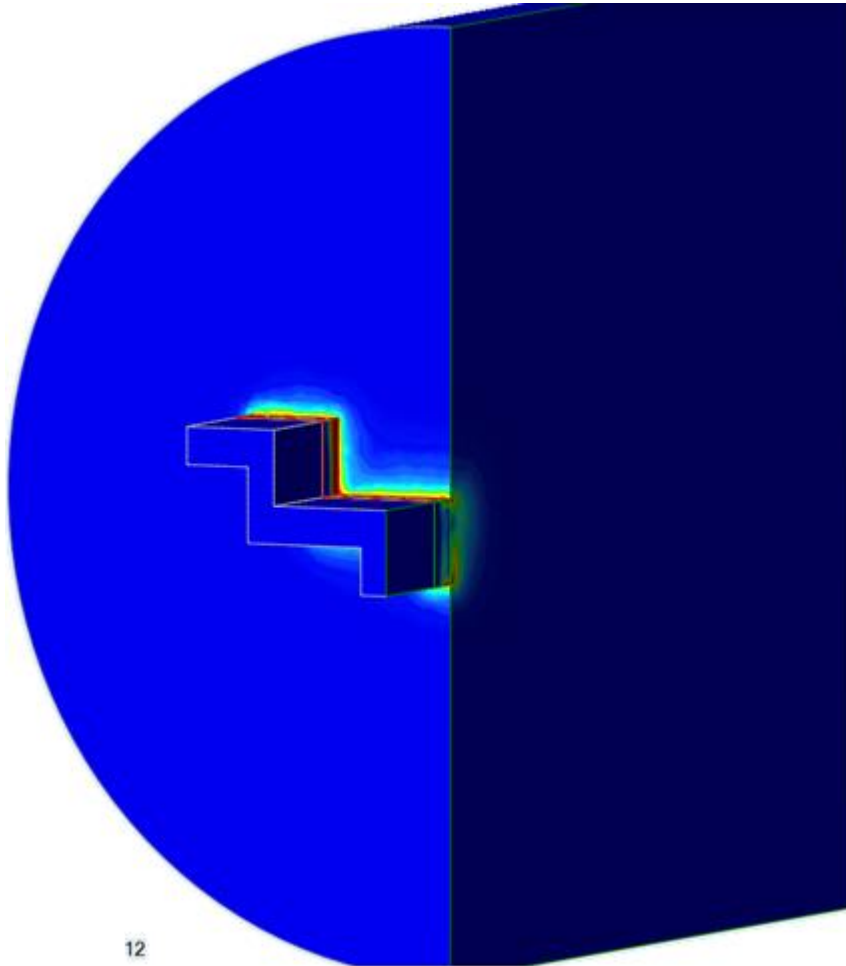
5 alExtFoam verification and validation

U-shaped profile: Results

IEM

alExtFoam

Strain rate
field



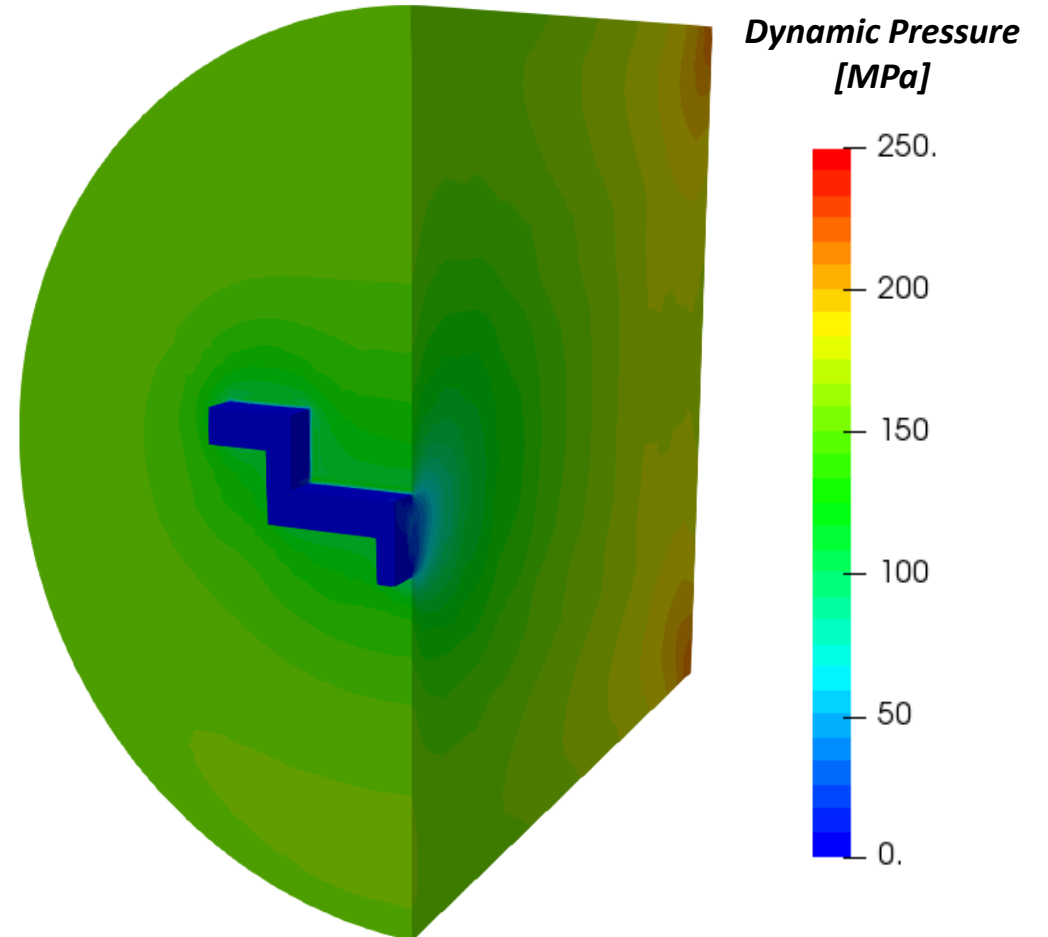
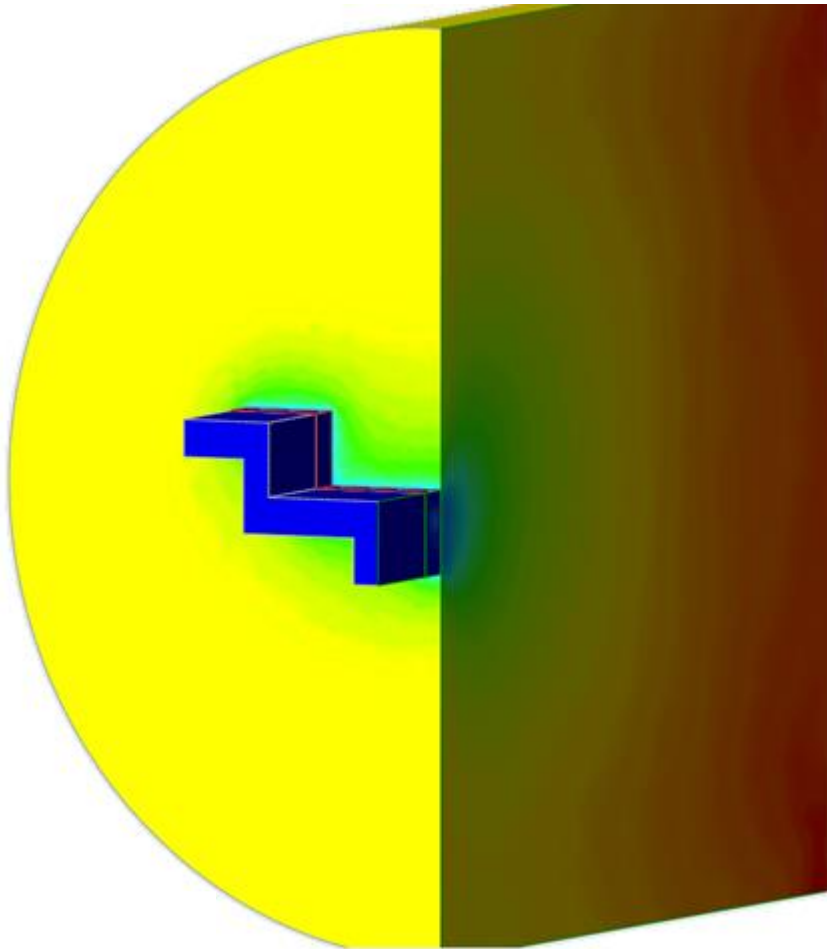
5 alExtFoam verification and validation

U-shaped profile: Results

IEM

alExtFoam

Pressure
field

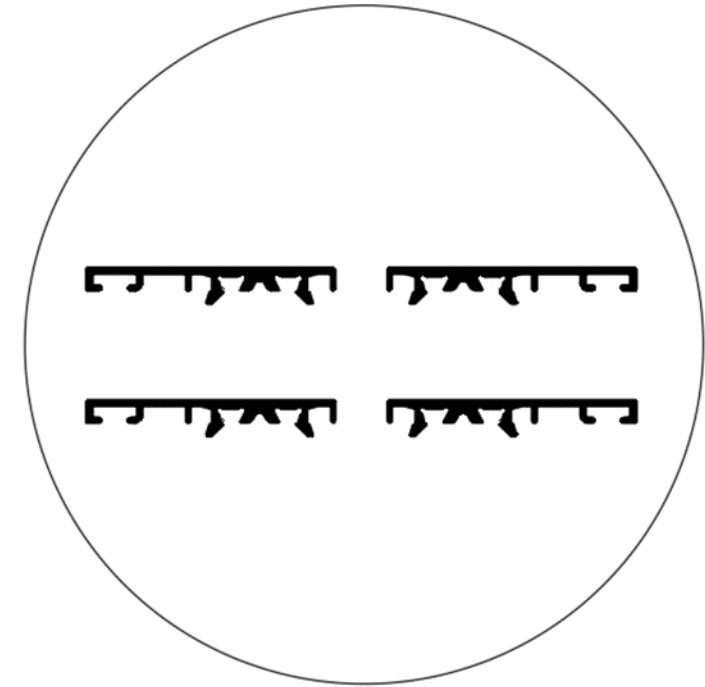


5 alExtFoam verification and validation

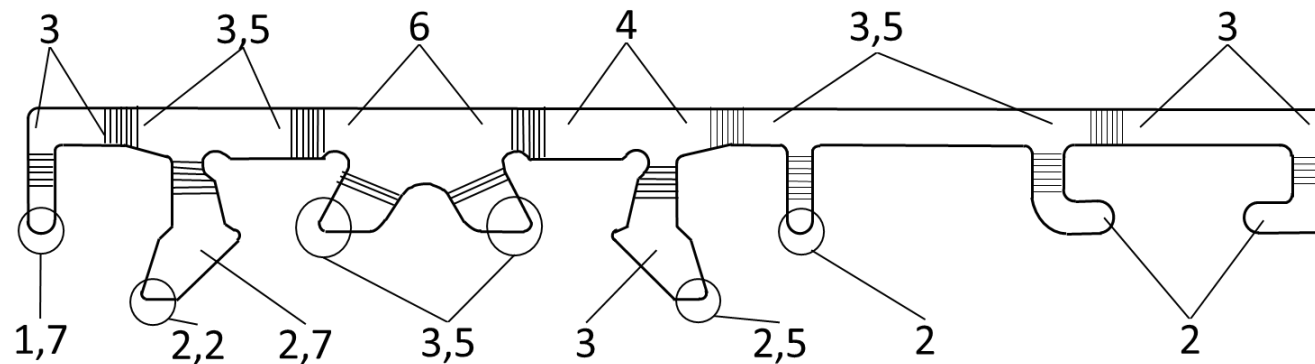
Multi-hole extrusion profile

Goal

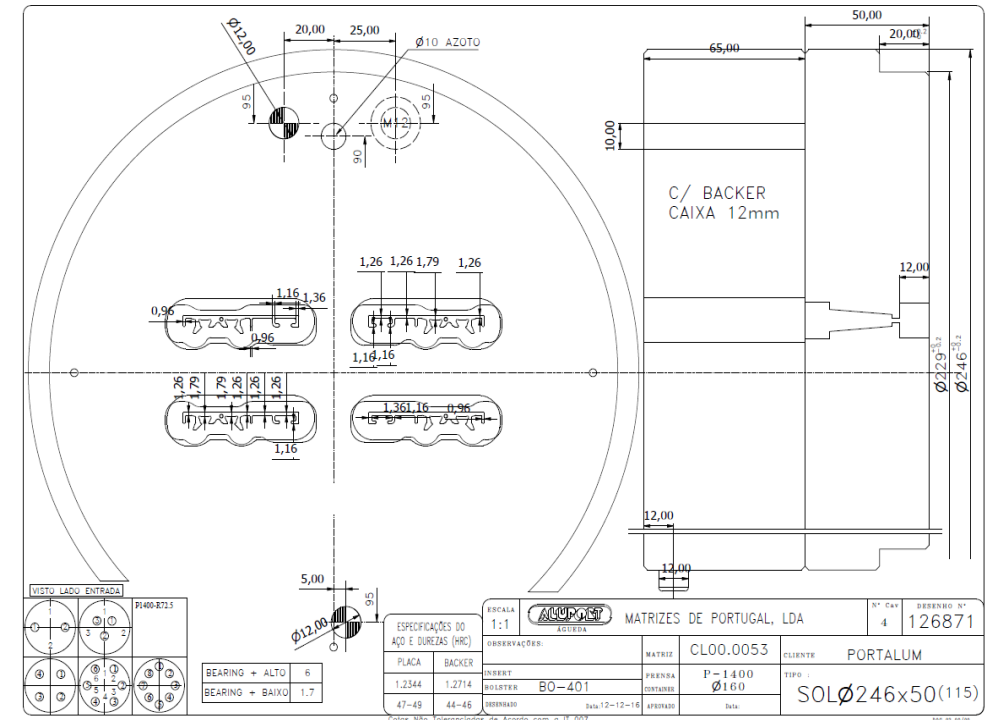
- Validate the *alExtFoam* with a industrial relevant extrusion geometry;
- Verify if the velocity distribution is consistent with the dimensions assigned by the designer in the bearing zone.



Proposed bearing length [mm]

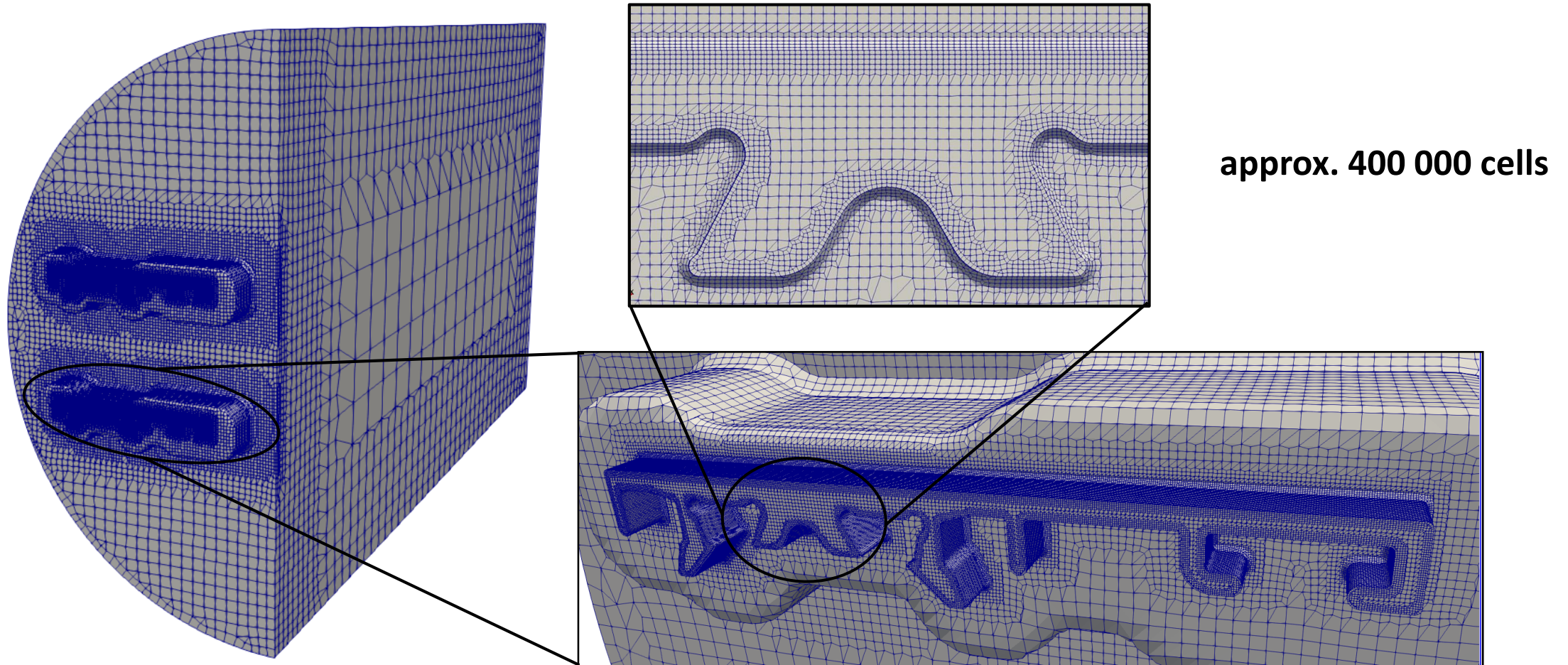


This diagram shows an exploded view of a three-part mechanical assembly. The parts are arranged horizontally. The leftmost part is a circular flange with four internal slots and a central hole. The middle part is a circular plate with four rectangular cutouts and a central hole. The rightmost part is a long cylindrical shaft. Two red arrows point towards the assembly from the bottom left and bottom center, indicating the direction of assembly.



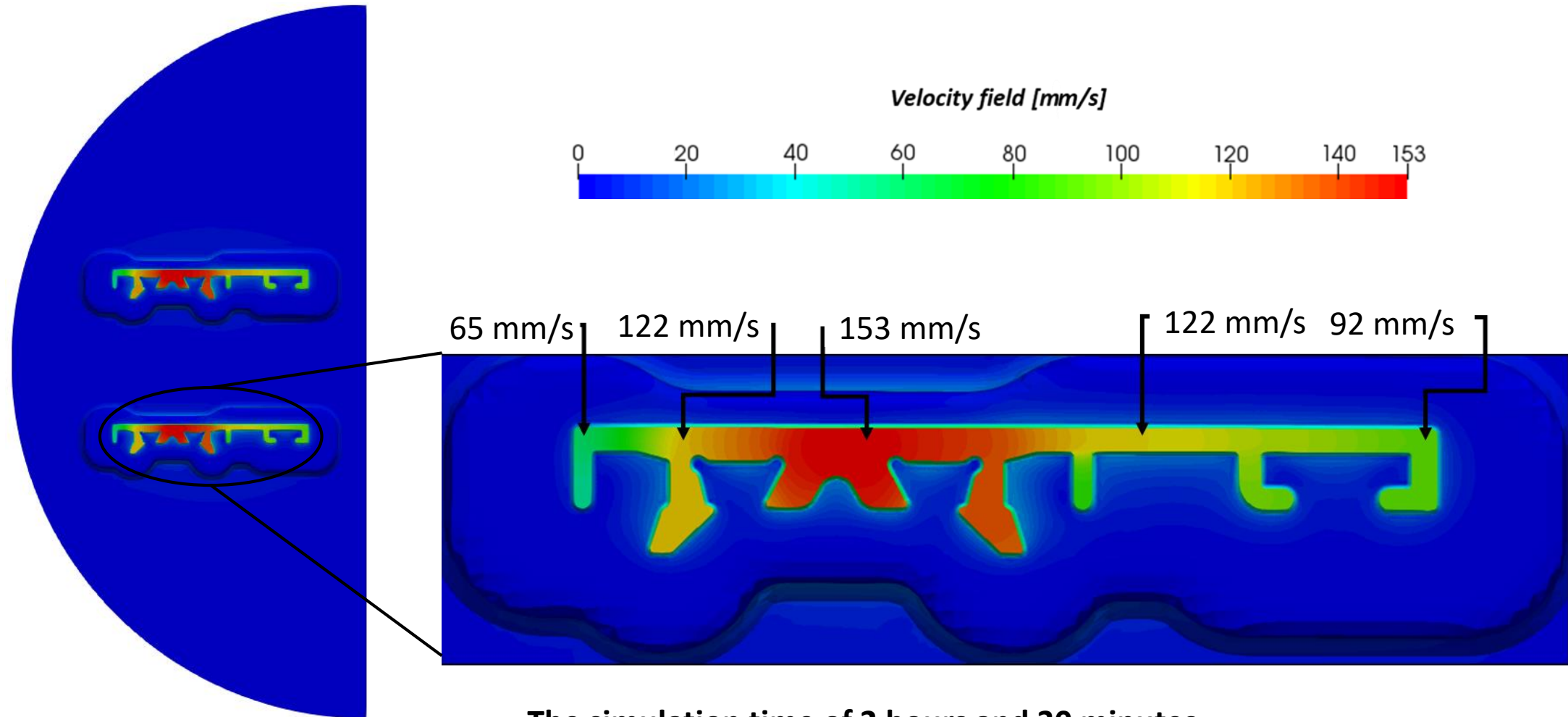
5 alExtFoam verification and validation

Multi-hole extrusion profile: Mesh generation (cfmesh)



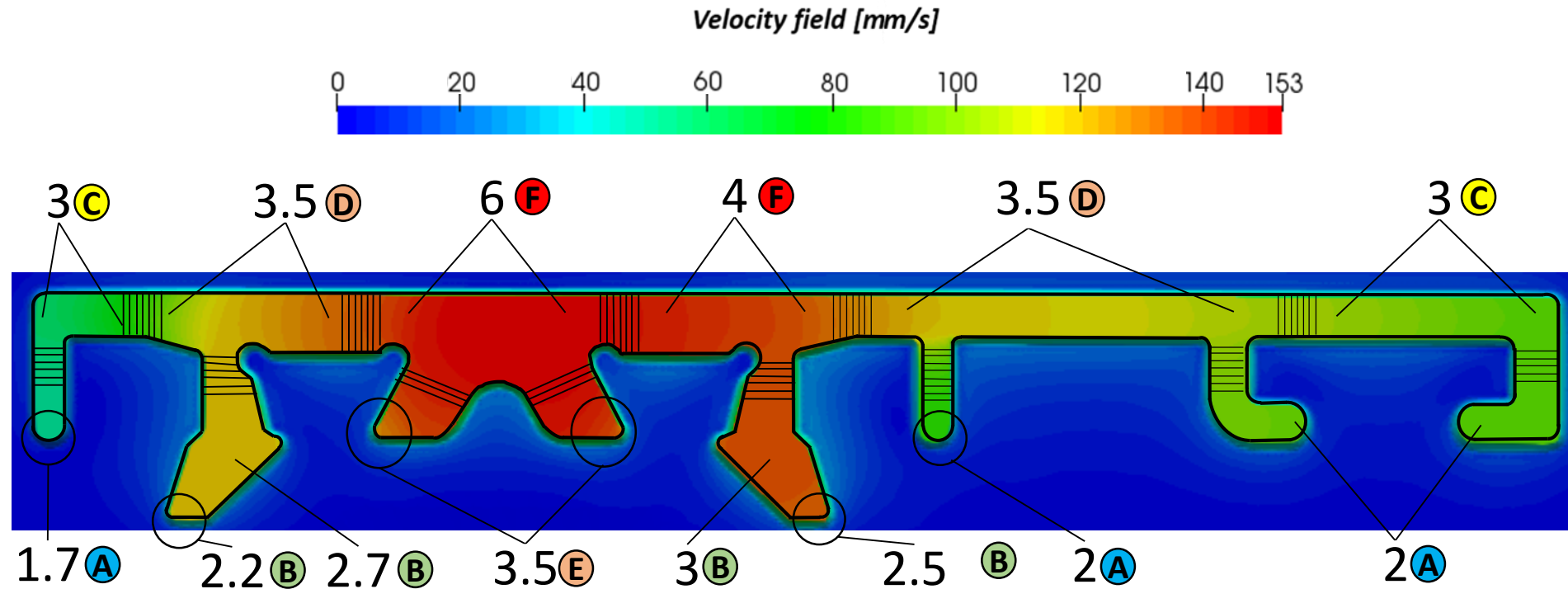
5 alExtFoam verification and validation

Multi-hole extrusion profile: Velocity field



5 alExtFoam verification and validation

Multi-hole extrusion profile: Velocity field



Bearing length rules:

- Bearing is longer for thicker sections and towards the center of the die;
- Bearing is shorter for high restriction areas;

6 Conclusions and Future work

- alExtFoam is a tool capable of simulating the extrusion of aluminum alloys;
- The Parallel plates, Couette and Convergent die flow cases allowed to verify the implementation of the constitutive and wall boundary condition;
- Calculation errors are very low when compared with analytical, experimental and numerical solutions;
- alExtFoam provides solutions similar to Inspire Extrude Metal;
- alExtFoam has proven to be able to evaluate the extrusion die design typical of the industry;
- 2h 30 min is an efficient simulation time that can be easily introduced into the production process;

6 Conclusions and Future work

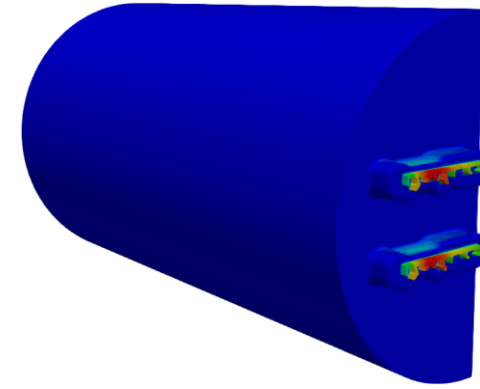
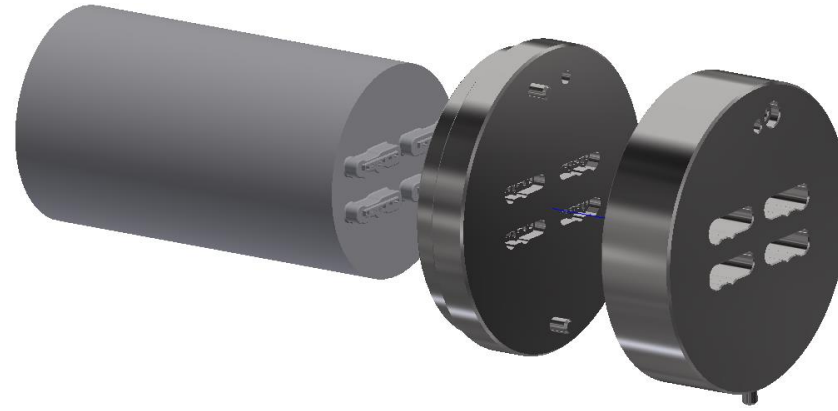
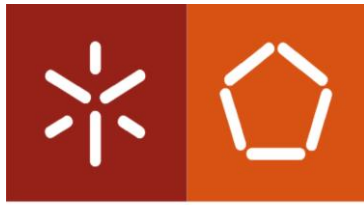


alExtFoam can now help the company:

- To improve the understanding about the influence of the process parameters (temperature and velocity) on the extrusion process;
- To reduce the costs related to the die design and the extrusion parameters.

6 Conclusions and Future work

- Bearing length automatic optimization;
- Levanov friction model implementation;
- Automatic mesh generation algorithm for different mesh refinement levels;
- Code optimization;
- Improve solver to be able to cope unsteady problems.



Universidade do Minho
Escola de Engenharia

A NOVEL OPENFOAM SOLVER FOR ALUMINIUM ALLOY PROFILE EXTRUSION

A. OLIVEIRA^{1,2}, H. PUGA³, J. MIGUEL NÓBREGA²

¹ PORTALUM - PORTUGUESA DE ALUMÍNIO, LDA, R. de Casares 670, 4820 Fafe, Portugal, antoniopedro.adf@hotmail.com

² Institute for Polymers and Composites, University of Minho, Campus de Azurém, 4800-058 Guimarães, Portugal, mnobrega@dep.uminho.pt

³CMEMS – UMinho, University of Minho, Campus of Azurém, 4800-058, Guimarães, Portugal, helderpuga@gmail.com