Individual 4

Yu Fan Mei Introduction to Proof and Problem Solving

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Problem 12. (1) Consider the statement

$$p \equiv \{ \forall M \in \mathbb{R}, \exists K \in \mathbb{R} \text{ s.t. } \forall x > K, f(x) > M \}.$$

- (a) Write $\neg p$.
- (b) Consider the function f from \mathbb{R} into \mathbb{R} defined by

$$f(x) = \begin{cases} \frac{1}{x} & x \neq 0 \\ 0 & x = 0 \end{cases}.$$

Does f satisfy p or $\neg p$? Prove your answer.

Solution. (a) The negation of p is

$$\neg p \equiv \{\exists M \in \mathbb{R} \text{ such that } \forall K \in \mathbb{R}, \exists x < K \text{ such that } f(x) \leq M\}$$

Proof. We will do something...

While working on this proof, I received no external assistance aside from advice from Professor Mehmetaj.