

# Combined Hall-Sensor Calibration and MTPA Control for BLDC Motors with Large Stator Inductance

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**Abstract**—Brushless DC (BLDC) motors are extensively utilized in industrial applications, yet they frequently encounter performance limitations due to Hall-sensor misalignment and significant stator inductance. These non-idealities manifest as torque ripple, acoustic noise, and a reduction in torque-per-ampere capability. This paper presents a unified control strategy that synergizes a lookup-table (LUT) based Hall-sensor calibration with a Maximum Torque Per Ampere (MTPA) Proportional-Integral (PI) controller. The proposed calibration routine employs an extrapolated averaging technique to rectify commutation intervals without introducing filter delays. Concurrently, the MTPA controller dynamically compensates for the current phase lag by adjusting the advance firing angle, thereby driving the average d-axis current to zero. Verification through detailed machine simulations confirms that the combined approach effectively restores balanced commutation and enhances torque generation efficiency compared to uncompensated baselines.

**Index Terms**—BLDC motor, Hall-sensor misalignment, MTPA, Lookup Table (LUT), Advance Angle Control.

## I. INTRODUCTION

### A. Background

Brushless DC (BLDC) motors are widely used in modern industries such as electric mobility, robotics, manufacturing, and industrial automation due to their high power density, good reliability and efficiency, superior torque-speed characteristics, simplicity, and low cost [3], [4]. Among various motor drive methods, Hall-sensor-controlled BLDC machines are commonly chosen for their ability to operate at a wide range of speeds and in applications where sensorless control may not be preferred [3], [4].

A BLDC motor consists of a permanent magnet synchronous machine (PMSM), which is electronically commutated by a voltage source inverter (VSI). A schematic diagram of a typical BLDC motor drive is shown in Fig. 1-1, where the VSI is controlled using three Hall sensors that detect the rotor position [6]. Each Hall sensor outputs a square wave signal with a value of 1 or 0, depending on the rotor position. To provide six evenly spaced readings, the three Hall sensors must be spaced apart by  $120^\circ$  [6]. In the  $120^\circ$  commutation scheme used in this work, each phase conducts for two-thirds of the electrical cycle [8]. In common operating mode

(COM), the VSI shifts its switching by  $30^\circ$  ahead of the Hall state transitions [9]. When stator inductance is negligible, the  $30^\circ$  shift aligns the fundamental component of the phase current with the phase back electromotive force (EMF), thus enabling maximum torque-per-ampere (MTPA) operation [9]. However, motors with significant stator inductance require dynamic adjustment of the advance firing angle to maintain MTPA operation.

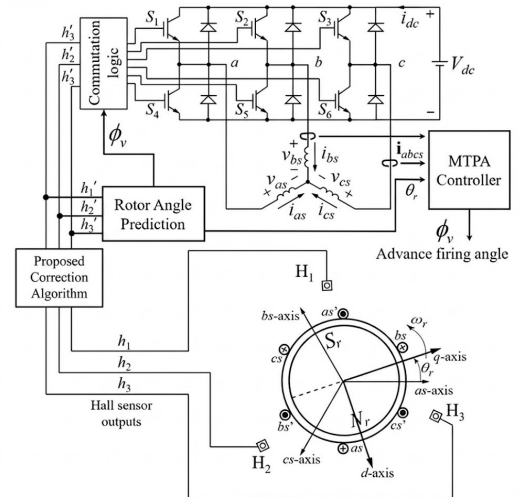


Fig. 1: Diagram for a Hall-sensor controlled BLDC motor driven by a VSI. The misaligned Hall sensors are passed through the proposed algorithm.

Furthermore, manufacturing imperfections cause the Hall sensors to deviate from their intended  $120^\circ$  spacing, resulting in asymmetric commutation timing as shown in Figure 3. This leads to imbalanced currents across phases, elevated torque oscillations, and overall degradation of motor performance [7]–[10]. Signal conditioning techniques, including moving average filters, have been applied to Hall sensor outputs [10], [11], yet these introduce timing delays that further compromise MTPA alignment. In motors with large winding inductance,

proportional-integral controllers have been developed to dynamically adjust the commutation advance angle [8], [12], [13]. However, these compensation strategies rely on accurate rotor position estimation, which becomes unreliable when the Hall sensors themselves are misaligned.

Thus to combat these problems, this paper builds upon previous work and presents a practical dual-strategy approach combining lookup table (LUT) calibration [2] with dynamic MTPA advance angle control [1] to simultaneously correct for Hall sensor positioning errors and compensate for inductance-related phase lag in 120° commutation mode. The proposed method is validated through simulation using MATLAB/Simulink on an industrial BLDC motor model exhibiting significant Hall misalignment and high winding time constant.

### B. Modeling of the BLDC System

The BLDC motor will be modeled as a surface-mounted Permanent Magnet Synchronous Machine (PMSM). For this machine topology, the direct and quadrature axis inductances are equal, that is,  $L_d = L_q = L_s$  [3], where  $L_s$  denotes the synchronous inductance,  $L_d$  the direct axis inductance and  $L_q$  the quadrature axis inductance. We will show later that this equality simplifies the analysis and is a defining characteristic of surface-mounted PMSMs.

The stator voltage equation in the stationary  $abc$  reference frame can be expressed as:

$$\mathbf{v}_{abc} = R_s \mathbf{i}_{abc} + L_s \frac{d}{dt} \mathbf{i}_{abc} + \mathbf{e}_{abc} \quad (1)$$

where  $\mathbf{v}_{abc}$ ,  $\mathbf{i}_{abc}$ , and  $\mathbf{e}_{abc}$  are the phase voltage, current, and back-EMF vectors respectively, and  $R_s$  is the stator resistance.

While the  $abc$  frame provides a direct physical representation of the machine quantities, Maximum Torque Per Ampere (MTPA) control design is significantly simplified by converting to the synchronous rotating reference frame. To facilitate MTPA, we transform the system variables into the  $dq$  reference frame using the Park transformation matrix  $\mathbf{K}_s^r(\theta_r)$ :

$$\mathbf{K}_s^r(\theta_r) = \frac{2}{3} \begin{bmatrix} \cos(\theta_r) & \cos(\theta_r - \frac{2\pi}{3}) & \cos(\theta_r + \frac{2\pi}{3}) \\ \sin(\theta_r) & \sin(\theta_r - \frac{2\pi}{3}) & \sin(\theta_r + \frac{2\pi}{3}) \\ 1/2 & 1/2 & 1/2 \end{bmatrix} \quad (2)$$

where  $\theta_r$  is the electrical rotor position. This transformation aligns the reference frame with the rotor flux, converting the time-varying  $abc$  quantities into constant or slowly varying  $dq$  quantities under steady-state operation.

Applying the Park transformation to (1), we obtain the dynamic equations in the  $dq$  frame:

$$v_q = R_s i_q + L_q \frac{di_q}{dt} + \omega_r L_d i_d + \omega_r \psi_m \quad (3)$$

$$v_d = R_s i_d + L_d \frac{di_d}{dt} - \omega_r L_q i_q \quad (4)$$

where  $\omega_r$  is the electrical rotor speed,  $\psi_m$  is the permanent magnet flux linkage, and the coupling terms  $\omega_r L_d i_d$  and  $\omega_r L_q i_q$  represent the rotational back-EMF components in each axis.

The mechanical dynamics are governed by:

$$J \frac{d\omega_m}{dt} = T_e - T_L - B\omega_m \quad (5)$$

where  $J$  is the rotor inertia,  $\omega_m$  is the mechanical rotor speed,  $T_L$  is the load torque,  $B$  is the viscous friction coefficient, and  $T_e$  is the electromagnetic torque. The electrical and mechanical speeds are related by  $\omega_r = P\omega_m$ , where  $P$  is the number of pole pairs.

By the principle of electromechanical energy conversion [3], the electromagnetic torque for a machine with  $P$  pole pairs is given by:

$$T_e = \frac{3P}{2} [\psi_m i_q + (L_d - L_q) i_d i_q] \quad (6)$$

By recognizing that for the surface-mounted PMSM, where  $L_d = L_q = L_s$ , the reluctance torque term  $(L_d - L_q) i_d i_q$  vanishes, and the voltage equations also simplifies with  $L_d = L_q = L_s$ . Hence the torque equation reduces to:

$$T_e = \frac{3P}{2} \psi_m i_q \quad (7)$$

In the  $dq$  frame, we can clearly see how we can achieve Maximum Torque Per Ampere control. Notice from (7) that the  $d$ -axis current  $i_d$  does not contribute to the electromagnetic torque production. Instead,  $i_d$  only increases the stator current magnitude and consequently the copper losses, which scale with  $I^2 R_s$  where  $I = \sqrt{i_d^2 + i_q^2}$ . To maximize torque efficiency and minimize losses per ampere, the optimal control strategy should maintain  $i_d = 0$ , thereby aligning all stator current with the torque-producing  $q$ -axis.

In the context of six-step commutation, the controller must regulate the commutation instants to maintain the time-averaged  $d$ -axis current magnitude close to zero while maximizing the  $q$ -axis current component [1], [8]. This ensures efficient operation and maximum torque output for a given current magnitude.

### C. Inductive Phase Lag and Angle Compensation

In the ideal case where stator inductance is negligible, the voltage equations (3) and (4) simplify to their resistive forms:

$$v_q \approx R_s i_q + \omega_r \psi_m, \quad v_d \approx R_s i_d \quad (8)$$

In this case, the back-EMF components are

$$e_{qs} = \omega_r \psi_m, \quad e_{ds} = 0 \quad (9)$$

Note that this means when the current phase is aligned with the back-EMF, the current is purely  $q$ -axis and  $i_d \approx 0$ . Previous analysis has shown that advancing the commutation by 30° from the Hall sensor transition, results in fundamental current aligning with the  $q$ -axis [8], [9]. This results in  $i_d \approx 0$  and achieves the MTPA condition.

However, for motors with non-negligible stator inductance, the inductive terms in (3) and (4) become significant. [3]. There will be commutation delay caused by the dynamic terms  $L_s \frac{di_q}{dt}$  and  $L_s \frac{di_d}{dt}$ , which describes how the phase current

must transition from zero to its conducting value for each commutation.

Additionally, the rotational coupling terms  $\omega_r L_s i_d$  in (3) and  $\omega_r L_s i_q$  in (4) scale proportionally with rotor speed. At higher speeds, these terms become significant relative to the resistive drops, creating cross-axis voltage coupling that further delays the current response. The combined effect of both the transient and rotational inductive terms causes the fundamental component of the phase current to lag behind the back-EMF  $e_{qs} = \omega_r \psi_m$  by an angle  $\phi_v$ , as illustrated in ??.

The consequence of this misalignment is a non-zero average  $d$ -axis current  $\bar{i}_d$ . Recall from (7) that only  $i_q$  contributes to electromagnetic torque. When the phase current lags the back-EMF, a portion of the stator current magnitude is directed along the  $d$ -axis, which does not produce torque but increases copper losses proportional to  $i_d^2 R_s$ . Therefore, for a given torque requirement, the motor must draw higher stator current, reducing the torque-per-ampere ratio defined as

$$\text{TPA} = \frac{T_e}{I_{rms}} = \frac{T_e}{\sqrt{i_d^2 + i_q^2}} \quad (10)$$

To recover MTPA operation and maximize (10), the commutation timing must be advanced by a compensation angle  $\phi_v$  such that the effective firing angle becomes  $\phi'_v = 30 + \phi_v$ . This compensation realigns the current with the back-EMF, forcing  $\bar{i}_d \rightarrow 0$  and ensuring all stator current contributes to torque production. The required compensation angle  $\phi_v$  is operating-point dependent, as it varies with speed  $\omega_r$ , torque  $T_e$ , and DC bus voltage  $v_{dc}$ , necessitating a dynamic controller rather than a fixed offset [1], [8].

#### D. Hall Sensor Misalignment and Its Impact on MTPA Control Accuracy

Ideally, the three Hall sensors  $H_1$ ,  $H_2$ , and  $H_3$  should be positioned exactly  $120^\circ$  electrical apart to provide six equally-spaced rotor position estimates per electrical cycle. However, as illustrated in Figure 2, practical sensors deviate from ideal positions due to manufacturing tolerances.

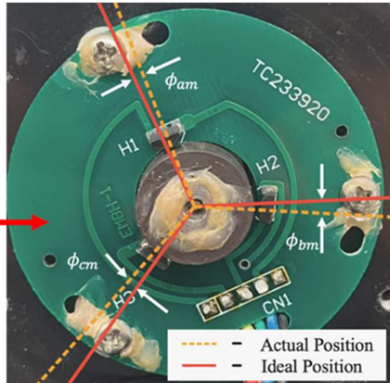


Fig. 2: Manufacturing tolerances in Hall sensor placement lead to misalignment from ideal  $120^\circ$  spacing.

These angular offsets creates distortion as visualized in Figure 3. Let  $\Delta t_n$  denote the time duration of the  $n$ -th switching interval. Ideally, all six intervals within one electrical cycle should be equal:  $\Delta t_n = T_e/6$ , where  $T_e = 2\pi/\omega_r$  is the electrical period. However, with Hall misalignment, the intervals become [2]

$$\Delta t_n = \frac{\pi/3 + \Delta\epsilon_n}{\omega_r} \quad (11)$$

creating uneven conduction intervals and distort phase currents.

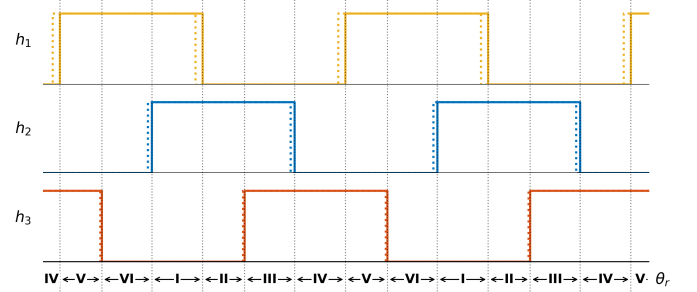


Fig. 3: Hall sensor misalignment causes uneven switching intervals, resulting in distorted phase currents and increased low-frequency torque ripple.

The uneven switching intervals have two detrimental effects on MTPA control. First, the rotor position estimation  $\hat{\theta}_r$  used in the Park transformation (2) becomes inaccurate. Since the transformation matrix  $\mathbf{K}_s^r(\theta_r)$  depends directly on the rotor angle, errors in  $\hat{\theta}_r$  propagate through to the calculated  $dq$  currents in (3) and (4), introducing oscillations in the measured  $i_d$  and  $i_q$ .

Second, and more critically for MTPA operation, the time-averaged  $d$ -axis current calculation becomes corrupted. The averaging window should ideally span one switching interval of constant duration. However, with misaligned Hall sensors, the intervals  $\Delta t_n$  fluctuate according to (11). This causes  $\bar{i}_d$  to oscillate even when the motor is in true MTPA condition, making the PI controller respond to measurement artifacts rather than actual  $d$ -axis current errors. The result is incorrect firing angle compensation  $\phi_v$  and potential instability in the MTPA loop.

## II. HALL SENSOR SIGNAL CORRECTION VIA LOOKUP TABLE CALIBRATION

Hall sensor misalignment corrupts the switching interval timing, which degrades both steady-state performance and the accuracy of the MTPA controller. This section first reviews conventional averaging filter approaches and their limitations, then presents the proposed Lookup Table (LUT) based calibration strategy that eliminates filter-induced delays while preserving correction accuracy.

### A. Limitations of Averaging Filter Approaches

Previous research has proposed moving average filters to smooth the irregular Hall intervals caused by sensor misalignment [1]. These filters operate on the sequence of measured time intervals  $\{\Delta t_n\}$  between consecutive Hall transitions and output smoothed values  $\{\Delta t'_n\}$  that approximate ideal equal spacing. A typical  $M$ -step averaging filter has the form

$$\Delta t'_n = \sum_{m=0}^{M-1} b_m \Delta t_{n-m} \quad (12)$$

where the coefficients  $b_m$  sum to unity. For example, the 3-step and 6-step extrapolating filters from [1] use correction terms of the form

$$\tau_{a3}^{corr}(n) = \frac{1}{3}(\tau(n-2) + 2\tau(n-3)) \quad (13)$$

$$\tau_{a6}^{corr}(n) = \frac{1}{3} \left( -\tau(n-1) + \sum_{k=3}^6 \tau(n-k) \right) \quad (14)$$

where  $\tau(n)$  denotes the measured time interval for the  $n$ -th switching sector.

These filters successfully balance the conduction intervals in steady state by attenuating the harmonics in the interval sequence  $\{\Delta t_n\}$ . However, the critical drawback is that any averaging filter with memory introduces a group delay of approximately  $M/2$  intervals [1]. During transients such as rapid accelerations or load changes, this delay causes the estimated rotor speed  $\hat{\omega}_r$  to lag the actual speed  $\omega_r$ . The result is a mismatch in the calculated rotor position  $\hat{\theta}_r$ , which propagates through the Park transformation (2) and corrupts the computed  $d$ -axis and  $q$ -axis currents.

For the MTPA controller, this lag is particularly problematic. The controller relies on an accurate calculation of the average  $d$ -axis current  $\bar{i}_{ds}$  to determine the required firing angle compensation. When  $\hat{\theta}_r$  lags the true position due to filter delay, the measured  $\bar{i}_{ds}$  oscillates even when the motor is operating at the true MTPA condition, causing the PI controller to make incorrect adjustments. This can lead to instability in the MTPA loop and degraded transient response, which is unacceptable for applications requiring rapid dynamic performance such as robotics and electric vehicles.

### B. Proposed LUT-Based Calibration Strategy

To eliminate the delay caused by memories while preserving correction accuracy, this work employs a two-stage Lookup Table (LUT) based approach [2]. The key idea is that Hall sensor misalignment is a fixed geometric error that does not change during operation. Therefore, the correction values can be identified once during a calibration phase and then applied instantaneously during runtime without any filtering.

Fig. 4: Control flow diagram showing the transition from calibration mode (using averaging filter to identify errors) to runtime mode (using LUT correction for zero-delay operation).

During the calibration phase, first the motor is driven to a stable steady-state speed. Then a filter can be chosen, for this study I used a high-order averaging filter such as the 6-step filter from (14). This filter has significant delay thus it does not have a good transient response, as such it is a good candidate to be compared against the proposed LUT method. The chosen filter is applied to balance the measured Hall intervals and remove the effects of misalignment. The filtered interval  $\tau'(n)$  represents what the commutation interval duration would be if the Hall sensors were ideally positioned.

For each of the six Hall states  $S \in \{1, 2, 3, 4, 5, 6\}$ , the filter would learn the specific time duration for each sector at that specific reference speed,  $\bar{\tau}[S]|_{\omega=\omega_{ref}}$ . Furthermore, we can get a speed estimate  $\hat{\omega}_r$  at that operating point using the filtered intervals. Where the speed estimate is computed as

$$\hat{\omega}_r[n] = \frac{\pi/3}{t[n] - t[n-1]} \quad (15)$$

Where  $t[n]$  is the timestamp of the current Hall transition and  $t[n-1]$  is the timestamp of the previous Hall transition.

The misalignment angle in each state can then be calculated with.

$$\Delta\phi_{LUT}[S] = \hat{\omega}_r[n] \cdot \bar{\tau}[S]|_{\omega=\omega_{ref}} \quad (16)$$

The angular corrections for all six Hall states are recorded and stored in a Lookup Table. Note that these corrections represent geometric errors in sensor placement, and thus they remain valid across all operating conditions and speeds. The calibration only needs to be performed once after motor assembly or can be repeated if the Hall sensor PCB is replaced. For subsequent operation, the controller can apply these pre-computed corrections during startup and directly without any filtering, eliminating runtime delay as shown in Figure 4.

### C. Runtime Phase: Feed-Forward Correction

During normal runtime operation, the averaging filters are completely bypassed. When a Hall transition occurs for state  $S$ , the controller retrieves the pre-stored correction angle  $\Delta\phi_{LUT}[S]$  from the Lookup Table. Then the speed estimate  $\hat{\omega}_r[n]$  is computed using (15) with the current measured interval. The corrected time interval for the next switching sector is then calculated as

$$\tau_{corr}(n) = \frac{\Delta\phi_{LUT}[S]}{\hat{\omega}_r[n]} \quad (17)$$

The next commutation instant  $t_{out}(n)$  is then scheduled as

$$t_{out}(n) = t_{in}(n) + \tau_{corr}(n) \quad (18)$$

where  $t_{in}(n)$  is the time of the current Hall transition.

This feed-forward correction approach eliminates the phase lag from filter approach while correcting the Hall sensor misalignment error. The rotor speed estimation  $\hat{\omega}_r[n]$  remains accurate during transients because it is based on corrected intervals rather than filtered intervals with memory. Consequently, the rotor position estimate  $\hat{\theta}_r$  tracks the true position closely, providing the MTPA controller with accurate feedback for calculating  $\bar{i}_{ds}$  and adjusting the firing angle compensation.

The LUT-based method thus preserves the system's dynamic response capability while achieving the same steady-state correction accuracy as high-order averaging filters.

#### D. Implementation Considerations

The LUT requires minimal memory, storing only six angular correction values (one per Hall state). On a typical microcontroller, this consumes less than 24 bytes. The runtime computation in (17) involves one table lookup, one subtraction, and one division, which can be executed within microseconds on modern DSPs.

The calibration phase can be automated as part of the motor commissioning process. The motor is accelerated to a moderate speed (typically 20-30% of rated speed to avoid excessive vibration from uncorrected Hall signals), and correction values are identified over several electrical cycles to ensure statistical reliability. Once calibrated, the LUT values are stored in non-volatile memory and loaded at startup for all subsequent operations.

Another advantage of LUT is that it can be used for more accurate speed estimation. Since we know the angles between each commutation sector, we can use this to get a more accurate speed for each sector.

### III. MTPA CONTROL VIA DYNAMIC ADVANCE ANGLE COMPENSATION

With the Hall sensor timing corrected by the LUT-based strategy from Section II, the control system can now implement Maximum Torque per Ampere (MTPA) operation reliably. As discussed in Section ??, motors with large stator inductance experience phase lag between the phase current and back-EMF. The standard 30° advance angle in COM is insufficient to compensate for this lag, which varies with operating conditions. This section presents a PI-based controller that dynamically adjusts the firing angle to maintain the MTPA condition across varying speed and load.

#### A. d-Axis Current as the MTPA Metric

Recall from (??) that for a surface-mounted PMSM, maximum torque per ampere is achieved when  $i_d = 0$ , meaning all stator current is aligned with the q-axis back-EMF. Therefore, the control objective is to maintain the time-averaged d-axis current at zero:  $\bar{i}_d = 0$ .

Using the corrected rotor position estimate  $\hat{\theta}_r$  from the LUT-based Hall correction, the instantaneous d-axis current is calculated via the Park transformation (2):

$$i_{ds}(t) = \frac{2}{3} \left[ i_{as} \sin(\hat{\theta}_r) + i_{bs} \sin\left(\hat{\theta}_r - \frac{2\pi}{3}\right) + i_{cs} \sin\left(\hat{\theta}_r + \frac{2\pi}{3}\right) \right] \quad (19)$$

The six-step commutation produces discontinuous phase currents, causing  $i_{ds}(t)$  to contain high-frequency harmonics. To obtain a stable control signal,  $i_{ds}(t)$  is averaged over each switching interval [1]:

$$\bar{i}_{ds}[n] = \frac{1}{\Delta t_n} \int_{t_n}^{t_n + \Delta t_n} i_{ds}(t) dt \quad (20)$$

where  $\Delta t_n$  is the duration of the  $n$ -th conduction interval. In practice, this averaging can be implemented by accumulating samples of  $i_{ds}(t)$  over each interval.

When  $\bar{i}_{ds} = 0$ , the fundamental component of the phase current is aligned with the back-EMF, achieving MTPA operation [1], [8].

#### B. PI Controller for Advance Angle Compensation

A Proportional-Integral (PI) controller drives  $\bar{i}_{ds}$  to zero by compensating the advance firing angle. The control error is simply the negative of the averaged d-axis current:

$$e[n] = -\bar{i}_{ds}[n] \quad (21)$$

The PI controller outputs a compensation angle  $\Delta\phi_v[n]$ :

$$\Delta\phi_v[n] = K_p e[n] + K_i \sum_{j=0}^n e[j] \quad (22)$$

where  $K_p$  and  $K_i$  are the proportional and integral gains. The proportional term provides fast response, while the integral term eliminates steady-state error.

Fig. 5: Flowchart of the MTPA PI controller. The corrected Hall signals provide accurate  $\hat{\theta}_r$  for computing  $i_{ds}$  from phase currents. The average  $\bar{i}_{ds}$  is fed to the PI controller, which outputs compensation angle  $\Delta\phi_v$  to maintain MTPA.

The total firing angle combines the COM advance with the dynamic compensation:

$$\phi'_v[n] = 30 + \Delta\phi_v[n] \quad (23)$$

This corrected angle  $\phi'_v$  adjusts when the VSI commutates relative to Hall transitions. At higher speeds, the inductive lag increases due to the rotational coupling term  $\omega_r L_s i_q$  in (4), requiring larger  $\Delta\phi_v$ . Similarly, at higher torque (larger  $i_q$ ), the current rise time during commutation is longer, also requiring more advance. The PI controller automatically finds the optimal  $\Delta\phi_v$  for each operating point, maximizing the torque-per-ampere ratio.

Together with the LUT-based Hall correction from Section II, this combined control architecture [1] enables BLDC motors with Hall sensor misalignment and large stator inductance to achieve near-optimal MTPA operation. The commutation timing is influenced by both corrections:

$$t_{out}(n) = t_{in}(n) + \tau_{corr}(n) + \frac{\Delta\phi_v[n]}{\hat{\omega}_r[n]} \quad (24)$$

where the first correction term  $\tau_{corr}(n)$  from (17) balances the Hall intervals, and the second term applies the MTPA advance compensation. The system dynamically adjusts both corrections in real time to maintain optimal performance under transients.

### IV. DETAILED MACHINE SIMULATIONS

The proposed combined control strategy was validated using a high-fidelity BLDC motor model.

### A. Steady-State Performance

The effectiveness of the method is demonstrated by observing the alignment of phase currents and back-EMF. Figure 6 compares the uncompensated case (a), the filter-only case (b), and the combined Method (c). The uncompensated waveforms show significant distortion and phase lag. The filter balances the switching intervals, but the phase lag persists. The combined method (c) achieves both balanced intervals and optimal phase alignment.

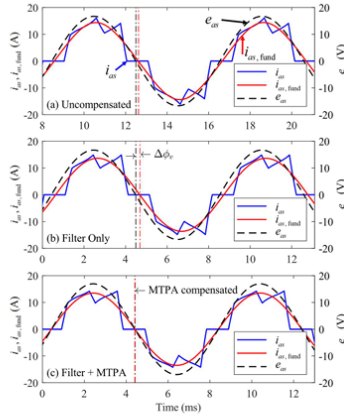


Figure 2-9 Alignment of the fundamental phase current and back emf: (a) at the initial state with Hall-sensor misalignment; (b) after the filter is applied; and (c) after both the filter and MTPA controller are applied.

Fig. 6: Alignment of the fundamental phase current and back-EMF: (a) uncompensated; (b) filter only; (c) combined filter + MTPA controller.

Figure 7 presents the steady-state performance comparison in terms of torque generation efficiency, defined as the ratio of average torque to RMS phase current ( $K_t = \bar{T}_e / I_{rms}$ ). The uncompensated case exhibits the lowest efficiency due to significant phase misalignment. The filter-only approach improves commutation symmetry but introduces delays that prevent optimal torque production. The proposed combined method (LUT + MTPA) demonstrates the highest torque-per-ampere ratio, confirming that the algorithm successfully compensates for both Hall sensor placement errors and inductive phase lag, thereby recovering the optimal operating point.

### B. Transient Performance

To verify the robustness of the proposed control, transient response tests were conducted.

Figure 8 shows a comparison of the current response during startup. The uncompensated case shows large current spikes, while the proposed method smooths the current envelope. Figure 9 provides a detailed view of the phase currents with and without compensation.

Figure 10 illustrates the speed response of the motor to a step command. The yellow trace representing the proposed LUT correction demonstrates a response time comparable to the ideal sensor placement (blue trace), significantly outper-

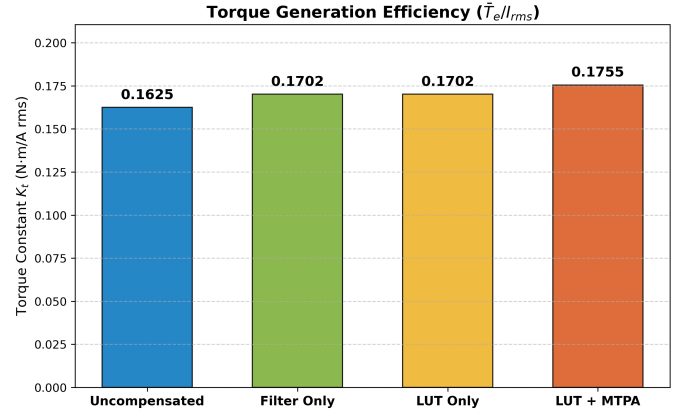


Fig. 7: Comparison of Torque Generation Efficiency (Torque Constant  $K_t$ ) across four operating cases. The proposed LUT + MTPA method achieves the highest torque-per-ampere, indicating optimal alignment.

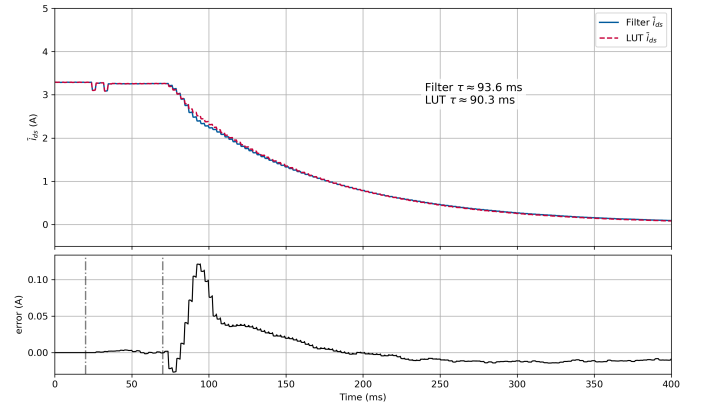


Fig. 8: Comparison of phase current transients during startup. The proposed method (Red) reduces peak overshoot compared to uncompensated (Blue).

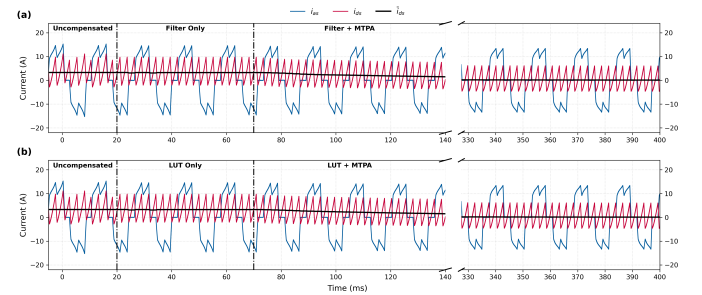


Fig. 9: Stacked view of phase currents, highlighting the zoomed-in improvement in waveform quality.

forming the 3-step and 6-step averaging filters which introduce noticeable delays and overshoot.

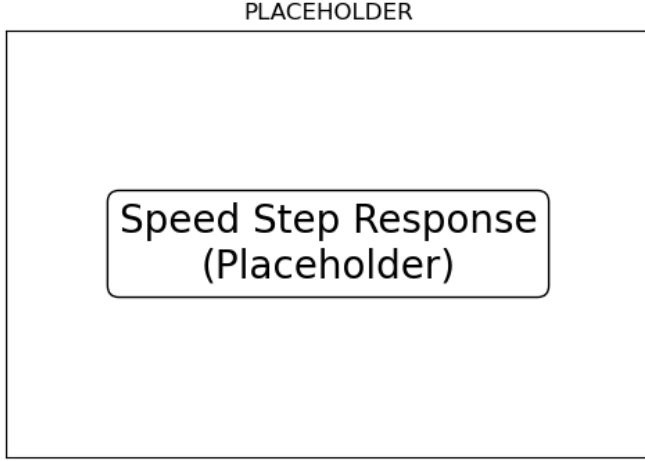


Fig. 10: Simulated speed response step increase. (a) with ideal Hall sensor placement; (b) Comparison of averaging filters vs. proposed LUT correction. The LUT method achieves faster convergence.

Figure 11 depicts the system response to a sudden load torque step. The LUT-based controller maintains stability and exhibits superior torque dynamic performance. The speed dip is minimized, and the electromagnetic torque recovers smoothly without the oscillatory behavior observed in the conventional averaging methods.

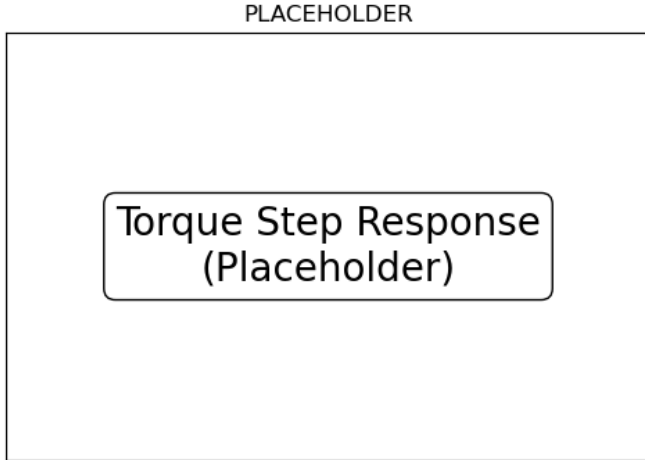


Fig. 11: Simulated response to a load step increase: (a) speed response; (b) electromagnetic torque response. The proposed LUT correction (yellow trace) shows superior dynamic tracking.

## V. CONCLUSION

This paper presented a unified control framework addressing two critical performance bottlenecks in BLDC drives: sensor misalignment and inductive lag. By integrating a

LUT-based calibration with a dynamic MTPA controller, the system achieves smooth and efficient operation. Simulation results confirm the method's ability to minimize torque ripple and maximize torque-per-ampere, while maintaining excellent transient response characteristics suitable for dynamic industrial applications.

## APPENDIX MOTOR PARAMETERS

The main parameters of the BLDC motor used in this study are listed in Table I.

TABLE I: Motor Parameters

Parameter	Symbol	Value
Stator Resistance	$R_s$	$0.5 \Omega$
Stator Inductance	$L_s$	1.2 mH
Flux Linkage	$\psi_m$	0.05 Wb
Pole Pairs	$P$	4
Rated Speed	$\omega_{rated}$	3000 rpm

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