

Comparison of mine to Saldamlis extension

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According to 4th chapter in theses of Levon Saldamli.

4.2.1 Field Variables – used

4.2.2 Field Constructor – used, slightly modified – `field(expr in domainName.regionName);`
in `expr` appears only coordinate variables defined in `domainName`

4.2.3 Field Type in Expressions

- **4.2.3.1 Binary operators** – used

- **4.2.3.2 Special operators** – for time derivative of field should be used
`pder` operator instead of `der`

4.2.4 Accessing Field Values – Accessing field values in function-like style
should not be allowed, if possible, for two reasons:

- it is not allowed in current Modelica for regular variables (unknown functions of time)
- If more then one coordinate system are defined in a domain, it is not clear which coordinates are used in the function-like expression

Regions consisting of one point and the `in` operator will be used instead. e.g.

```
model heatPID
  record Room extends DomainBlock3D;
    Region0D sensorPosition(shape = shapeFunc, range = {{1, 1},
{0.5, 0.5}, {0.5, 0.5}});
  end Room
  Room room(...)
  field Real T(domain = room);
  Real Ts;
  ...
equation
  Ts = T in room.sensorPosition;
  ...
end heatPid;
```

4.3.1. Domains Geometry Definition

Main difference: Saldamli describes boundary by curves in 2D resp. surfaces in 3D and thus specifies the domain shape.

This approach doesn't work very well in 3D. If boundary is made of several surfaces in 3D, parameters (arguments) of shape-functions of these surfaces

would have to be bounded not just in cartesian product of intervals but in some more complex sets to compose continuous boundary. And there is no way to write this in Levens extension.

I prefer the way used in Peters book – write a function (or equation) that maps an cartesian product of intervals onto the interior and other regions of the domain. I don't think this approach can describe more complicated geometries in 3D, but is closer to the way how such a region (subsets of R^n) is usually described in mathematics. I think it will be also easier to generate the computational grid if we have a function or equation that maps cartesian product on the domain.

There are two ways for the second approach:

- using shape-function (used in the book)
- using equations holding coordinate transformations and define always some general coordinates that are bounded in cartesian product of intervals

For illustration see `domain_comparison.lyx/pdf` file.

This way of domain definition should be supplemented with Constructive Solid Geometry – it is building more complex domains using union, intersection and difference of previously defined domains. This is not designed already. It should be also possible to define domain in external file from some CAD app.

4.3.1.1 Domain Type similar (built-in) - In both cases all domains extend the general built-in `Domain` type. Saldamli's built-in `Domain` has different members. We have only replaceable `Region interior`;

3.2.1.2 Boundary type (built-in) – we don't need it. Here is `Region0D`, `Region1D`, `Region2D` and `Region3D` built-in type to describe boundaries, interior and other regions in the domain instead.

4.3.1.3 Coordinate Systems Saldamli's domain always has cartesian coordinates defined. I would not insist on this.

I'm not sure if we should have a special data type `Coordinate`, or it should be of type `Real` and the compiler itself would infer that a variable is a coordinate that must be treated in a special way. Other option is to consider the variable type as something different from a data type because coordinate variable indeed doesn't hold any data and has a symbolic meaning (something like `time`). Then coordinates could be perhaps defined using keyword with lower case:

```
coordinate x;
```

4.3.2 Differential Operators

4.3.2.1 Partial derivative Saldamli uses `der(u,x,y...)`, here `pder(u,x,y...)`. Time derivatives should not be written as `(p)der(u)` but also `pder(u,time)`.

4.3.2.2 Normal derivative (or rather normal vector) - similar, unfinished design. It perhaps should be member of the region, e.g.:

```
pder(u,omega.boundary.n) = 0 in omega.boundary;
```

or an operator applied on a region, something like:

```
pder(u,normal(omega.boundary)) = 0;
```

Writing boundary conditions using normal vector but outside differentiation should be also allowed e.g.:

```
field Real[3] flux;
```

```
flux*region.n = 0 in omega.boundary; /*scalar product
```

4.3.2.3 **Vector notation** – coordinate-free differential operators as **gradient**, **divergence**, **rotation** ... I didn't work up how to define this. Could be accepted.

4.3.3 Domain Specifier in Equations

keyword **in** accepted. Should be used not only for boundary conditions but also for PDE to specify region and to access field values in particular points (example above).

4.3.4 **Field Reduction** – integral operator. I didn't consider yet, could be perhaps undertaken.

Other notes:

Equations may be written within or outside domain class. Outside domain coordinates must be accessed of course `domainName.coordName`. To make a shortcut we introduced **region** and **domain** (or **dom**) keywords as a alias for domain and region specified after **in** op.

To access region we can write

```
pder(u,region.n) = 0 in omega.boundary;
```

similarly for domain

```
pder(u,dm.x) in omega.interior;
```

It should be possible to write equations that relate fields defined in different domains. This is not designed yet.