

$C \cup V$ all symbols $(\Sigma \cup N^+)^*$

$$CFG = L = \{a^n b^n; n \geq 0\} \quad G = (V, \Sigma, R, S)$$

A derivation of G of w_n from w_0 may be any string in V^*

$$V = \{S, a, b\} \quad \Sigma = \{a, b\}$$
$$R = \{S \rightarrow aSb; S \rightarrow \epsilon\}$$

$$S \rightarrow aSb \rightarrow aaSbb \rightarrow \dots \rightarrow a^n S b^n \rightarrow a^n b^n$$

CFG and PL



- ❑ Computer programs written in any language must satisfy some rigid criteria in order to be syntactically correct, and therefore amenable for mechanical interpretation.
- ❑ The syntax of most of the languages can be captured by CFG
- ❑ If a programming language is described by CFG, it will be easy for parsing.
- ❑ Parsing is the process of analyzing a program to find the syntax.

$$G = (V, \Sigma, R, S)$$

$$V = \{+, *, (,), id, T, F, E\}$$

$$\Sigma = \{+, *, (,), id\}$$

$$S = E$$

$$R \Rightarrow E \rightarrow E + T$$

$$E \rightarrow T$$

$$T \rightarrow T * F$$

$$T \rightarrow F$$

$$F \rightarrow (E)$$

$$F \rightarrow id$$

$$w_n \rightarrow (id * id) + (id + id)$$

Starting NT $\rightarrow E_{w_0}$

$$E_{w_0} \rightarrow E + T$$

$$w_1 \rightarrow T + T$$

$$\rightarrow F + T$$

$$\rightarrow (E) + T$$

$$\rightarrow (T) + T$$

$$\rightarrow (T * F) + T$$

$$\rightarrow (F * F) + T$$

$$\rightarrow (id * F) + T$$

$$\rightarrow (id * id) + T$$

$$\rightarrow (id * id) + F$$

$$\rightarrow (id * id) + (E)$$

$$\rightarrow (id * id) + (E + T)$$

$$\rightarrow (id * id) + (T + T)$$

$$\rightarrow (id * id) + (F + T)$$

$$\rightarrow (id * id) + (F + F)$$

$$\rightarrow (id * id) + (id + F)$$

$$\rightarrow (id * id) + (id + id)$$

Why
Context
Free

$$E \rightarrow E + E$$

replace
with RHS
of rule

RL and CFL

All RLs are CFL.

$M = (K, \Sigma, \delta, s, F)$ and corresponds to a Regular language L

$$G(M) = (V, \Sigma, R, S)$$

$$V = K \cup \Sigma$$

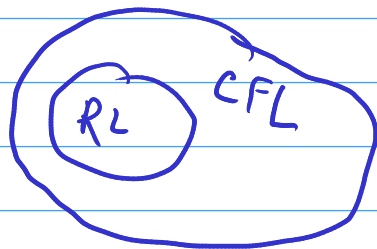
$$S = s$$

$$R = \{ Q \rightarrow aP \mid \delta(Q, a) = P \} \cup \{ Q \rightarrow \epsilon \mid Q \in F \}$$

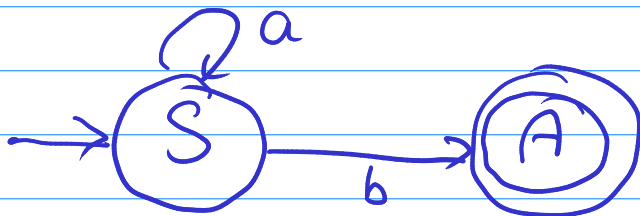
\rightarrow The surroundings of this 'E' have no part to play with rules for JUST replacement

Difference bet. BNF & CFL?
(They are fundamentally same)

$a^n b^n$ where $n \geq 0$ is a CFL
 If there exists a CFG for L $S \rightarrow Bb$



but $a^n b^n$ is not
 an RL
 because a CFL & RL though

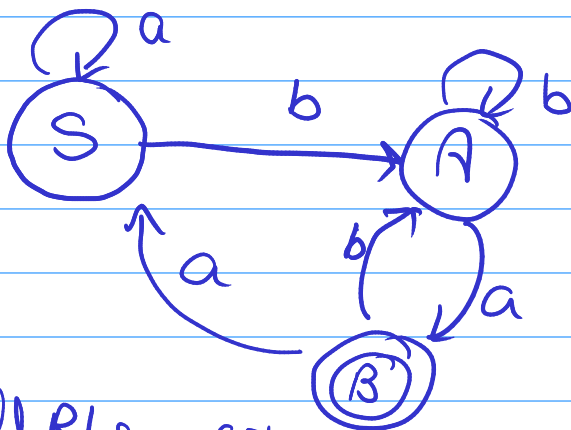


a^*b

$$\delta(Q, a) = P$$

$$Q \rightarrow aP$$

$$\begin{aligned} S &\rightarrow aS \\ S &\rightarrow bA \\ A &\rightarrow \epsilon \end{aligned}$$



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$G(M) = (V, \Sigma, R, S)$

$V = K \cup \Sigma$

$S = s$

$R = \{ Q \rightarrow aP \mid \delta(Q, a) = P \} \cup \{ Q \rightarrow \epsilon \mid Q \in F \}$

all RLs are CFLs

but all CFLs
 are not
 RLs

$$\begin{aligned} S &\rightarrow aS & A &\rightarrow bA & B &\rightarrow bA \\ S &\rightarrow bA & A &\rightarrow aB & B &\rightarrow aS & B &\rightarrow \epsilon \end{aligned}$$

They are regular grammars $\left\{ \begin{array}{l} \text{RHS has max 2 symbols (or 1 or null)} \\ \text{for this grammar} \end{array} \right.$

all Regular grammars are Context free grammars