

given x $y = \omega_0 + \omega_1 x$ this distribution is our assumption

$t \sim N(t/y(x, \omega), \sigma)$

$(x_1, t_1) \quad (x_2, t_2) \quad \dots \quad (x_N, t_N)$

$$p((x_1, t_1), (x_2, t_2), \dots, (x_N, t_N) | y(x, \omega))$$

$$y(x, \omega) = \omega_0 + \omega_1 x$$

maximise p for ω_0, ω_1

ALSO

Let's assume mean is target, variance is same otherwise, the problem is very hard!

$$\prod_{n=1}^N p(t_n | x_n, \omega_0, \omega_1)$$

$$= \prod_{n=1}^N \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2}\left(\frac{y(x_n, \omega) - t_n}{\sigma}\right)^2}$$

$$= \max_{\omega_0, \omega_1} \left(\frac{1}{(2\pi)^{N/2} \sigma^N} e^{-\frac{1}{2\sigma^2} \left(\sum_{n=1}^N ((\omega_0 + \omega_1 x_n) - t_n)^2 \right)} \right)$$

$$\max_{\omega_0, \omega_1} \left(-\frac{N}{2} \log 2\pi - N \log \sigma - \frac{1}{2\sigma^2} \sum_{n=1}^N ((\omega_0 + \omega_1 x_n) - t_n)^2 \right)$$

$$\max_{\omega_0, \omega_1} \left[-\frac{1}{2\sigma^2} \sum_{n=1}^N ((\omega_0 + \omega_1 x_n) - t_n)^2 \right]$$

$$\left\{ \min_{\omega_0, \omega_1} \left[\frac{1}{2} \sum_{n=1}^N ((\omega_0 + \omega_1 x_n) - t_n)^2 \right] \right\} = SSE$$

(σ^2 is constant)

How to minimize? You already know, bish.