Java Parser for XCSP3 Version 1.2.1

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The version 1.2.1 of the XCSP3 Java Parser recognizes almost all concepts of XCSP3. Its current limitations are the following:

- the attribute **as** can only be used for variables and arrays of variables (but for the moment, no instance among the 23,000 that have been generated, exploits this attribute differently).
- compressed tuples are not handled, but short tuples such as e.g., (1,*,2,3), are.

Note that this is a Java parser that uses DOM (Document Object Model) to parse XCSP3 instances. However, feel free to adapt it.

As mentioned above, the Java parser (class XParser) is rather complete. It allows us to scan any XCSP3 file and to build a pre-digested representation of the various objects of the instance. However to simplify things, we propose an interface that is composed of callback functions. This interface corresponds to classes XCallbacks and XCallbacks2. Currently, this interface has been developed for XCSP3-core, i.e., for integer variables, the 20 most popular constraints over integer variables, and mono-optimization. This interface will be progressively extended.

To start, once you have imported the classes required to parse, with DOM, XCSP3 instances, you should start writing (in Java 8) something like:

```
class XCSP3 implements XCallbacks2 {
  public XCSP3(String fileName) throws Exception {
    Document doc = XUtility.loadDocument(fileName);
  }
}
```

If when running this code on a given XCSP3 filename, i.e., on the name of an XCSP3 instance file such as those that can be found at xcsp.org/series, an exception is not raised, that's fine. Maybe, as a first attempt, use an uncompressed file as for example, queens8.xml

instead of queens8.xml.lzma. Otherwise, you may need to redefine the way you can convert an XCSP3 file (whose name is given) into an object Document, as follows:

```
class XCSP3 implements XCallbacks2 {
   public Document loadDocument(String fileName) throws Exception {
      // Put your code here to convert the file, whose name is given, into an org.w3c.dom.Document
      // See the code in XUtility.loadDocument(fileName) for a hint
   }
   public XCSP3(String fileName) throws Exception {
      Document doc = XUtility.loadDocument(fileName);
   }
}
```

Now, let us assume that everything is fine with the loading of the document. To parse the document, we then build an object XParser so as to be able to interact with all entries that were initially in <variables>, <constraints> and <objectives>. These entries are respectively stored in parser.vEntries, parser.cEntries and parser.oEntries. Here, we just display the description of all these entries.

```
class XCSP3 implements XCallbacks2 {
  public XCSP3(String fileName) throws Exception {
    Document doc = XUtility.loadDocument(fileName);
    XParser parser = new XParser(doc);
    parser.vEntries.stream().forEach(e -> System.out.println(e.toString()));
    parser.cEntries.stream().forEach(e -> System.out.println(e.toString()));
    parser.oEntries.stream().forEach(e -> System.out.println(e.toString()));
  }
}
```

1 Parsing Variables

Now, consider the following XCSP3¹ instance testExtension1.xml:

 $^{^{1}}$ This instance, as well as all other instances mentioned in this document, can be downloaded from this directory.

```
<instance format="XCSP3" type="CSP">
  <variables>
    <var id="x0"> 0 1 </var>
    <var id="x1"> 0 1 </var>
    <var id="x2"> 0 1 </var>
    <var id="x3"> 0 1 </var>
    <var id="x4"> 0 1 </var>
    <var id="x5"> 0 1 </var>
    <var id="x6"> 0 1 </var>
  </re>
  <constraints>
    <extension>
      <list> x4 x5 x0 </list>
      \langle \text{supports} \rangle (0,0,1)(0,1,0)(1,0,0)(1,1,1) \langle /\text{supports} \rangle
    </extension>
    <extension>
      <list> x0 x6 x1 </list>
      <supports> (0,0,1)(0,1,0)(1,0,0)(1,1,1) </supports>
    </extension>
    <extension>
      <list> x3 x6 x2 </list>
      <supports> (0,0,1)(0,1,0)(1,0,0)(1,1,1) </supports>
    </extension>
    <extension>
      t> x4 x5 x3 </list>
      <supports> (0,0,0)(0,1,1)(1,0,1)(1,1,0) </supports>
    </extension>
  </constraints>
</instance>
```

and simplify your code so as to just have:

```
class XCSP3 implements XCallbacks2 {
  public XCSP3(String fileName) throws Exception {
    loadInstance(fileName);
  }
}
```

Remark 1 You can provide the name of the classes that you want to discard when calling the XParser constructor. For example, parser = new XParser(fileName, "symmetryBreaking"); But this is an advanced use.

When you execute the code for the instance testExtension1.xml above, you must obtain something like:

```
Missing Implementation
Method buildVarInteger
Class org.xcsp.parser.XCallbacks2
Line 105
```

Here, is is indicated that a method whose name is buildVarInteger needs to be implemented. Indeed, to manage integer variables, we have to implement the two following methods:

```
void buildVarInteger(XVarInteger x, int minValue, int maxValue)
void buildVarInteger(XVarInteger x, int[] values)
```

For managing variables, it seems relevant to introduce a map for making the correspondence between the variables in the parser (XVarInteger objects) and the variables in your solver (here, assumed to correspond to VarInteger objects). Note that:

- minValue may be equal to XConstants.VAL_MINUS_INFINITY_INT, for denoting $-\infty$, and
- maxValue may be equal to XConstants.VAL_PLUS_INFINITY_INT, for denoting $+\infty$.

but we have no such a case for the first 80 problems (and 23,000 generated instances) we have modeled.

```
class XCSP3 implements XCallbacks2 {
   private Map<XVarInteger, VarInteger > mapVar = new LinkedHashMap<>();

   public void buildVarInteger(XVarInteger xx, int minValue, int maxValue) {
      VarInteger x = ... // Build your solver variable x here using xx.id, minValue and maxValue mapVar.put(xx,x);
   }

   public void buildVarInteger(XVarInteger xx, int[] values) {
      VarInteger x = ... // Build your solver variable x here using xx.id and values mapVar.put(xx,x);
   }

   public XCSP3(String fileName) throws Exception {
      loadInstance(fileName);
   }
}
```

Remark 2 The parser automatically flattens all variables from arrays. Also, all variables with degree 0 (i.e., all useless variables that occur in no constraint and no objective) are automatically discarded. If you want to execute specific code, you can override the following methods of XCallbacks:

```
void loadVariables(XParser parser)
void loadVar(XVar v, Map<XDom, Object> cache4DomObject)
void loadArray(XArray va, Map<XDom, Object> cache4DomObject)
```

2 Parsing Constraints extension and intension

Now, when you execute the code for the instance testExtension1.xml introduced earlier, you must obtain something like:

```
Missing Implementation
Method buildCtrExtension
Class org.xcsp.parser.XCallbacks2
Line 129
```

The implementation of a required method is missing here. Because, most of the time, we shall have to translate parser variables into solver variables, we propose first to add the following auxiliary functions:

The signature of the following missing method is:

```
void buildCtrExtension(String id, XVarInteger[] list, int[][] tuples, boolean positive
, Set<TypeFlag> flags)
```

And now, assuming that you can call in your solver a method extension to build an extensional constraint, you can add:

The specified Boolean argument indicates is the table is positive (set of tuples seen as supports) or negative (set of tuples seen as conflicts). Note that we have a set of flags as last argument for the method. It allows us to know if * is present in some tuple(s), forming then a short tuple such as for example (2,*,4,1), and if all tuples are valid (cleaned) meaning that all tuples belong to the Cartesian product of the variable domains. Note that the integer value used for denoting * is XConstants.STAR_INT whose value is Integer.MAX_VALUE - 1. If everything is ok, you should get 8 solutions for the instance testExtension1.xml. Check that you obtain the same result with the equivalent instance testExtension2.xml that uses an array instead of stand-alone variables.

```
<instance format="XCSP3" type="CSP">
 <variables>
    <array id="x" size="[7]"> 0 1 </array>
  <constraints>
    <extension>
     \langle list \rangle \times [4..5] \times [0] \langle / list \rangle
     <supports> (0,0,1)(0,1,0)(1,0,0)(1,1,1) </supports>
    </extension>
    <extension>
     t> x[0] x[6] x[1] 
     <supports> (0,0,1)(0,1,0)(1,0,0)(1,1,1) </supports>
    </extension>
    <extension>
     t> x[3] x[6] x[2] </list>
     <supports> (0,0,1)(0,1,0)(1,0,0)(1,1,1) </supports>
    </extension>
    <extension>
     t> x[4] x[5] x[3] 
      <supports> (0,0,0)(0,1,1)(1,0,1)(1,1,0) </supports>
    </extension>
  </constraints>
</instance>
```

For dealing with unary extensional constraints, you have to implement:

```
void buildCtrExtension(String id, XVarInteger x, int[] values, boolean positive, Set <
    TypeFlag > flags)
```

Remark 3 When a constraint is recognized as totally entailed (no conflicts) or totally disentailed (no supports), as it is the case for extensional constraints when the number of tuples is 0, the parser respectively calls the methods below. You may wish to override the default behavior of these methods.

```
void buildCtrTrue(String id, XVar[] list)
void buildCtrFalse(String id, XVar[] list)
```

Let us consider now the following instance, called **testPrimitive.xml**, involving three variables x, y and z of domain $\{1, 2, 3, 4, 5\}$, and five constraints $x \le 4$, x > y, y > z, $x \ne z$ and x = y + z. Observe that one (small) group of constraints is present in this instance.

```
<instance format="XCSP3" type="CSP">
  <variables>
   <var id="x"> 0..5 </var>
   <var id="y"> 0..5 </var>
   <var id="z"> 0..5 </var>
  </ra></ra>
  <constraints>
    <intension> le(x,4) </intension>
    <group>
      <intension> gt(%0,%1) </intension>
     <args> x y </args>
     <args> y z </args>
    <intension> ne(x,z) </intension>
    <intension> eq(x,add(y,z)) </intension>
  </constraints>
</instance>
```

It is important to understand that the parser automatically individualizes all constraints from groups (and blocks), meaning that callback functions for all constraints are systematically

called in turn. However, if you want to execute specific code, you can always override the following methods of XCallbacks:

```
void loadConstraints(XParser parser)
void loadBlock(XBlock b)
void loadGroup(XGroup g)
void loadSlide(XSlide s)
```

When you execute the code for the instance testPrimitive.xml, you must obtain something like:

```
Missing Implementation
Method buildCtrPrimitive
Class org.xcsp.parser.XCallbacks2
Line 113
```

The code for the following method is missing:

```
void buildCtrPrimitive(String id, XVarInteger x, TypeConditionOperatorRel op, int k)
```

Primitive unary intensional constraints are special cases of intensional constraints. The parser intercepts them (we shall see later how to deactivate this, if needed). Primitive unary constraints that can be intercepted have the form:

```
x \odot k
```

with x being a variable, $\odot \in \{<, \leq, \geq, >, \neq, =\}$ and $k \in \mathbb{Z}$. For example, we can have x > 10 or $y \neq 5$. If you implement the code for dealing with unary primitive constraints in this method, and run again the code for this instance, you must obtain something like:

```
Missing Implementation
Method buildCtrPrimitive
Class org.xcsp.parser.XCallbacks2
Line 117
```

This time, the code for the following method is missing:

Primitive binary intensional constraints are special cases of intensional constraints. The parser intercepts them (we shall discuss to which extent, later). Primitive binary constraints that can be intercepted have the form:

```
(x \oplus y) \odot k
```

with x and y being two variables, $\emptyset \in \{+, -, *, /, \%, ||\}$, $\emptyset \in \{<, \leq, \geq, >, \neq, =\}$ and $k \in \mathbb{Z}$. For example, we can have x - y > 0 or |x - y| = 5 (note that || stands here for the distance between two objects). If you implement the code for dealing with binary primitive constraints (or a relevant subset of them) in this method, and run again the code for this instance, you must obtain something like:

```
Missing Implementation
Method buildCtrPrimitive
Class org.xcsp.parser.XCallbacks2
Line 121
```

This time, the code for the following method is missing:

```
void buildCtrPrimitive(String id, XVarInteger x, TypeArithmeticOperator opa, XVarInteger y, TypeConditionOperatorRel op, XVarInteger z)
```

Primitive ternary intensional constraints are special cases of intensional constraints. The parser intercepts them. Primitive ternary constraints that can be intercepted have the form:

```
(x \oplus y) \odot z
```

with x, y and z being three variables, $\emptyset \in \{+, -, *, /, \%, ||\}$, and $\emptyset \in \{<, \leq, \geq, >, \neq, =\}$. For example, we can have x + y = z or x * y > z. If you implement the code for dealing with ternary primitive constraints (or a relevant subset of them) in this method, and run again the code for this instance, you should be fine. Do you get 2 solutions for this instance?

Maybe, you don't get all these primitive propagators in your solver. Or you just want to manage yourself the Boolean expressions (predicates) of intension constraints. Here is how you can proceed. First, have a look at the following enumeration, XCallbacksParameters, put in class XCallbacks, together with two default methods called defaultParameters() and currentParameters().

```
enum XCallbacksParameters {
  RECOGNIZE_SPECIAL_UNARY_INTENSION_CASES
  RECOGNIZE_SPECIAL_BINARY_INTENSION_CASES
  RECOGNIZE_SPECIAL_TERNARY_INTENSION_CASES
  RECOGNIZE_SPECIAL_COUNT_CASES,
RECOGNIZE_SPECIAL_NVALUES_CASES
  INTENSION_TO_EXTENSION_ARITY_LIMIT, // set it to 0 for deactivating "intension to extension"
      conversion
  INTENSION_TO_EXTENSION_SPACE_LIMIT,
  INTENSION_TO_EXTENSION_PRIORITY;
/** Returns a map with the default parameters that can be used for parsing (
    recognizing primitives, converting in extensionnal form, \dots) */
default Map<XCallbacksParameters, Object> defaultParameters() {
  Object dummy = new Object();
 Map<XCallbacksParameters, Object> map = new HashMap<>();
 map.put(XCallbacksParameters.RECOGNIZE_SPECIAL_UNARY_INTENSION_CASES, dummy);
 \verb|map.put(XCallbacksParameters.RECOGNIZE\_SPECIAL\_BINARY\_INTENSION\_CASES\,, | dummy); \\
 \verb|map.put(XCallbacksParameters.RECOGNIZE\_SPECIAL\_TERNARY\_INTENSION\_CASES, dummy);|
  map.put(XCallbacksParameters.RECOGNIZE_SPECIAL_COUNT_CASES, dummy);
  map.put(XCallbacksParameters.RECOGNIZE_SPECIAL_NVALUES_CASES, dummy);
  map.put(XCallbacksParameters.INTENSION_TO_EXTENSION_ARITY_LIMIT, 0);
  map.put(XCallbacksParameters.INTENSION_TO_EXTENSION_SPACE_LIMIT, 1000000);
  map.put(XCallbacksParameters.INTENSION_TO_EXTENSION_PRIORITY, Boolean.TRUE);
/stst Returns the map with the current parameters that are used when parsing (
    recognizing primitives, converting in extensionnal form, ...). If this default
 is not overridden, the default parameters are used. */
default Map < XCallbacksParameters , Object > currentParameters() {
 return defaultParameters();
```

If you want to take control of the parameters that are used when parsing, you need to override the default method currentParameters() as follows. Here, you simply introduce a private field for representing the map that you will use, initialize it with the default parameters, and returns that private map when currentParameters() is called.

```
class XCSP3 implements XCallbacks2 {
   private Map<XCallbacksParameters, Object> currentParameters = defaultParameters();
   public Map<XCallbacksParameters, Object> currentParameters() {
     return currentParameters;
   }
   ...
}
```

If you want to deactivate the recognition of unary and binary primitives constraints, you just have to modify the code of your constructor as follows:

But you have to implement right now the following method:

```
void buildCtrIntension(String id, XVarInteger[] scope, XNodeParent<XVarInteger> tree)
```

For intension, we know that tree is an object XNodeParent that represents the root node of a syntactic tree denoting the Boolean expression (and containing XVarInteger objects). Let us go further. Suppose that you don't have any propagators for primitive constraints, and you don't have a generic filtering algorithm for dealing with arbitrary form of intensional constraints (after possible decomposition), then your last hope is to convert them into extensional form. The parser can do it for you as follows:

```
public XCSP3(String fileName) throws Exception {
    currentParameters().remove(XCallbacksParameters.
        RECOGNIZE_SPECIAL_UNARY_INTENSION_CASES);
    currentParameters().remove(XCallbacksParameters.
        RECOGNIZE_SPECIAL_BINARY_INTENSION_CASES);
    currentParameters().remove(XCallbacksParameters.
        RECOGNIZE_SPECIAL_TERNARY_INTENSION_CASES);
    currentParameters().put(XCallbacksParameters.INTENSION_TO_EXTENSION_ARITY_LIMIT, 3);
    currentParameters().put(XCallbacksParameters.INTENSION_TO_EXTENSION_SPACE_LIMIT, 10000000);
    currentParameters().put(XCallbacksParameters.INTENSION_TO_EXTENSION_PRIORITY, Boolean.TRUE);
    loadInstance(fileName);
}
```

However, note that we can control the translation, by fixing the maximal arity (here, 3) of intensional constraints to be converted, and the maximal size (here, 1,000,000) of the Cartesian product of their variable domains. In any case, it is very likely that you will need to

implement buildCtrIntension() because there are situations where intensional constraints do not correspond to primitives and cannot be translated into extensionnal forms.

Remark 4 The way primitive constraints are recognized is not complete. There are some cases where the recognition process may fail. In the future, we might propose a canonical representation of the syntactic tree to improve things.

3 Parsing Other Constraints

Now, consider the following instance:

```
<instance format="XCSP3" type="CSP">
  <variables>
    <array id="x" note="x[i] is the ith value of the series" size="[5]"> 0..4 </array>
    <array id="y" note="y[i] is the distance between x[i] and x[i+1]" size="[4]"> 1..4
          </array>
  </re>
  <constraints>
    <allDifferent> x[] </allDifferent>
    <allDifferent> y[] </allDifferent> <group class="channeling">
      <intension> eq(%0,dist(%1,%2)) </intension>
      <args> y[0] x[0] x[1] </args>
      <args> y[1] x[1] x[2] </args>
<args> y[2] x[2] x[3] </args>
      <args> y[3] x[3] x[4] </args>
    </group>
  </constraints>
</instance>
```

If you run your code for this instance, you must obtain something like:

```
Missing Implementation
Method buildCtrAllDifferent
Class org.xcsp.parser.XCallbacks2
Line 141
```

Assuming that you can call a method allDifferent in your solver, you need to implement a method just as follows:

```
public void buildCtrAllDifferent(String id, XVarInteger[] list) {
   allDifferent(trVars(list));
}
```

After implementing this method, you should get 8 solutions. Note that there exist several variants of allDifferent, corresponding to what is precisely described in the XCSP3 specifications. They are:

```
void buildCtrAllDifferent(String id, XVarInteger[] list)
void buildCtrAllDifferentExcept(String id, XVarInteger[] list, int[] except)
void buildCtrAllDifferentList(String id, XVarInteger[][] lists)
void buildCtrAllDifferentMatrix(String id, XVarInteger[][] matrix)
```

Now, you can keep proceeding that way for all constraints in XCSP3-core:

- extension and intension
- regular and mdd

- allDifferent, allEqual and ordered
- sum, count, nValues and cardinality
- maximum, minimum, element and channel
- stretch, noOverlap and cumulative

Note that the meta-constaint slide, which is present in XCSP3-core, is automatically decomposed by the parser.

By default, the parser will try to recognize special cases of count: atLeast, atMost, exactly, among and will consequently call, when possible, one of the following callback functions:

```
void buildCtrAtLeast(String id, XVarInteger[] list, int value, int k)
void buildCtrAtMost(String id, XVarInteger[] list, int value, int k)
void buildCtrExactly(String id, XVarInteger[] list, int value, int k)
void buildCtrExactly(String id, XVarInteger[] list, int value, XVarInteger k)
void buildCtrAmong(String id, XVarInteger[] list, int[] values, int k)
void buildCtrAmong(String id, XVarInteger[] list, int[] values, XVarInteger k)
```

If you prefer always dealing yourself with count, whatever the case is, you have to remove the parameter XCallbacksParameters.RECOGNIZE_SPECIAL_COUNT_CASES and implement²:

```
void buildCtrCount(String id, XVarInteger[] list, int[] values, Condition cond)
void buildCtrCount(String id, XVarInteger[] list, XVarInteger[] values, Condition c)
```

Note that an object Condition is instance of one of the four classes:

- ConditionVar, when the condition represents a pair composed of an operator (TypeConditionOperator) and a variable (XVarInteger)
- \bullet Condition Val, when the condition represents a pair composed of an operator (Type ConditionOperator) and an integer k
- ConditionIntvl, when the condition represents a pair composed of an operator (Type-ConditionOperator) and an interval (represented by two integers min and max)
- ConditionIntset, when the condition represents a pair composed of an operator (Type-ConditionOperator) and a set of integers (represented by an array t)

So, in your implementation of count, you may write some code that looks like:

```
void buildCtrCount(String id, XVarInteger[] list, int[] values, Condition cond) {
   TypeConditionOperator op = cond.operator;
   if (cond instanceof ConditionVar) {
        XVarInteger x = ((ConditionVar)cond).x;
        ...
   } else if (cond instanceof ConditionVal) {
        int k = ((ConditionVal)cond).k;
        ...
   } else if (cond instanceof ConditionIntvl) {
        int min = ((ConditionIntvl)cond).min;
        int max = ((ConditionIntvl)cond).max;
        ...
   } else {
        int[] t = ((ConditionIntset)cond).t;
        ...
   }
}
```

²In any case, you will have to deal with the cases of **count** that do not correspond to those that can be identified.

Also, by default, the parser will try to recognize special cases of nValues: allDifferent, allEqual, notAllEqual and will consequently call, when possible, one of the following callback functions:

```
void buildCtrAllDifferent(String id, XVarInteger[] list)
void buildCtrAllEqual(String id, XVarInteger[] list)
void buildCtrNotAllEqual(String id, XVarInteger[] list)
```

If you prefer always dealing yourself with nValues, whatever the case is, you have to remove the parameter XCallbacksParameters.RECOGNIZE_SPECIAL_NVALUES_CASES and implement:

```
void buildCtrNValues(String id, XVarInteger[] list, Condition cond)
void buildCtrNValuesExcept(String id, XVarInteger[] list, int[] except, Condition c)
```

4 Parsing Objectives

If we consider now an optimization problem, with simply a variable to minimize.

```
<instance format="XCSP3" type="COP">
  <variables>
    <array id="x" size="[5]"> 0..500 </array>
    <array id="y" size="[5][5]"> 1..500 </array>
  </ra></ra>
  <constraints>
    <group class="channeling">
      <intension> eq(%0,add(%1,%2)) </intension>
      <args> x[1] x[0] y[0][1] </args>
      <args> x[2] x[0] y[0][2] </args>
<args> x[3] x[0] y[0][3] </args>
      <args> x[4] x[0] y[0][4] </args>
      <args> x[2] x[1] y[1][2] </args>
      <args> x[3] x[1] y[1][3] </args>
      <args> x[4] x[1] y[1][4] </args>
      <args> x[3] x[2] y[2][3] </args>
      <args> x[4] x[2] y[2][6] </args>
<args> x[4] x[2] y[2][4] </args>
<args> x[4] x[3] y[3][4] </args>
    </group>
    <allDifferent> y[0][1..4] y[1][2..4] y[2][3..4] y[3][4] </allDifferent>
  </constraints>
  <objectives>
    <minimize > x[4] </minimize >
  </objectives>
</instance>
```

You have to implement the following method:

```
void buildObjToMinimize(String id, XVarInteger x)
```

Once it is done, do you get 11 as optimal value?

As a last example, let us consider the following quadratic assignment instance.

```
<instance format="XCSP3" type="COP">
  <variables>
    <array id="x" size="[12]"> 0..11 </array>
<array id="d" size="[12][12]"> 0 5 9..12 15..18 21 26 29 30 33..40 44 46 48 54..56
          58 59 61 63 64 66 68..70 72 73 76 78..80 83 85 86 90 93 95..97 </array>
  </re>
  <constraints>
    <allDifferent> x[] </allDifferent>
    <group>
      <extension>
        t> %0 %1 %2 </list>
         (0,1,36)(0,2,54) ... (ellipsis here) ... (11,9,86)(11,10,18) </
             supports>
      </extension>
      <args> x[0..1] d[0][1] </args>
<args> x[0] x[2] d[0][2] </args>
      <args> x[0] x[3] d[0][3] </args> <args> x[0] x[4] d[0][4] </args>
      <args> x[1] x[5] d[1][5] </args> <args> x[2] x[6] d[2][6] </args>
      <args> x[2] x[7] d[2][7] </args>
<args> x[5] x[8] d[5][8] </args>
      <args> x[7] x[9] d[7][9] </args> <args> x[8] x[10] d[8][10] </args>
      <args> x[9] x[11] d[9][11] </args>
    </group>
  </constraints>
  <objectives>
    <minimize type="sum">
      <coeffs> 90 10 23 43 88 26 16 1 96 29 37 </coeffs>
    </minimize>
  </objectives>
</instance>
```

You have to implement the following method:

Once it is done, do you get 4,776 as optimal value?