Evaluation of Variables with Hypothesis Tests

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Before you start; "Zorunlu Paket Yükleniyor" means Installing required package

Motor Cars (mtcars) Dataset Analysis

```
data(mtcars)
summary(mtcars$mpg)
##
      Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
##
     10.40
           15.43
                    19.20
                            20.09
                                    22.80
                                            33.90
t.test(mtcars$mpg, mu = 25, altenative = "two.sided")
##
   One Sample t-test
##
## data: mtcars$mpg
## t = -4.6079, df = 31, p-value = 6.587e-05
## alternative hypothesis: true mean is not equal to 25
## 95 percent confidence interval:
## 17.91768 22.26357
## sample estimates:
## mean of x
## 20.09062
```

Attention should be paid to the assumption of whether the variances are equal (var.equal)

Diamond Prices Example

```
require(knitr)
## Zorunlu paket yükleniyor: knitr
```

```
require(dplyr)
## Zorunlu paket yükleniyor: dplyr
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
      filter, lag
## The following objects are masked from 'package:base':
##
##
      intersect, setdiff, setequal, union
require(ggplot2)
## Zorunlu paket yükleniyor: ggplot2
data(diamonds)
force(diamonds)
## # A tibble: 53,940 x 10
##
      carat cut
                color clarity depth table price
                                                        X
##
     <dbl> <ord>
                     <ord> <ord>
                                   <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1 0.23 Ideal
                     Ε
                           SI2
                                    61.5
                                           55
                                                326 3.95 3.98 2.43
## 2 0.21 Premium
                     Ε
                           SI1
                                    59.8
                                           61
                                                326 3.89
                                                           3.84 2.31
## 3 0.23 Good
                     Ε
                           VS1
                                    56.9
                                                327
                                                     4.05 4.07 2.31
                                           65
                           VS2
## 4 0.29 Premium
                     Ι
                                    62.4
                                           58
                                                334
                                                    4.2
                                                           4.23 2.63
## 5 0.31 Good
                                    63.3
                                                335 4.34 4.35 2.75
                     J
                           SI2
                                         58
## 6 0.24 Very Good J
                           VVS2
                                    62.8
                                           57
                                                336 3.94
                                                           3.96
                                                                 2.48
## 7 0.24 Very Good I
                           VVS1
                                    62.3
                                           57
                                                336 3.95
                                                           3.98 2.47
## 8 0.26 Very Good H
                           SI1
                                    61.9
                                           55
                                                337 4.07
                                                           4.11 2.53
                           VS2
                                    65.1
## 9 0.22 Fair
                                                337 3.87
                                                           3.78 2.49
                     Ε
                                           61
## 10 0.23 Very Good H
                           VS1
                                    59.4
                                           61
                                                338 4
                                                           4.05 2.39
## # i 53,930 more rows
head(diamonds,3)
## # A tibble: 3 x 10
    carat cut
                  color clarity depth table price
                                                     Х
                                                           у
                  <ord> <ord>
                                <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
    <dbl> <ord>
## 1 0.23 Ideal
                  Ε
                        SI2
                                 61.5
                                             326 3.95 3.98 2.43
                                         55
## 2 0.21 Premium E
                        SI1
                                 59.8
                                             326 3.89 3.84 2.31
                                         61
## 3 0.23 Good
                        VS1
                                 56.9
                                             327 4.05 4.07 2.31
fair <- diamonds %>%
filter(cut == "Fair") %>%
select(price)
premium <- diamonds %>%
filter(cut == "Premium") %>%
select(price)
t.test(fair$price, premium$price, var.equal = FALSE)
```

```
##
## Welch Two Sample t-test
##
## data: fair$price and premium$price
## t = -2.3453, df = 2210.6, p-value = 0.0191
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -414.05655 -36.94333
## sample estimates:
## mean of x mean of y
## 4358.758 4584.258
```

As seen in the results, the p-value is 0.019 and "Fair" and "premium" at a 5% significance level. The null hypothesis that the average prices of diamonds with different cuts are equal is rejected.

Wilcoxon Test

```
require(UsingR)
```

```
## Zorunlu paket yükleniyor: UsingR
## Zorunlu paket yükleniyor: MASS
## Warning: package 'MASS' was built under R version 4.4.1
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
       select
## Zorunlu paket yükleniyor: HistData
## Zorunlu paket yükleniyor: Hmisc
##
## Attaching package: 'Hmisc'
## The following objects are masked from 'package:dplyr':
##
##
       src, summarize
## The following objects are masked from 'package:base':
##
##
       format.pval, units
```

```
data(exec.pay)
summary(exec.pay)
##
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                              Max.
      0.00
                     27.00
                                     41.50 2510.00
##
           14.00
                             59.89
wilcox.test(exec.pay, conf.int = TRUE)
##
   Wilcoxon signed rank test with continuity correction
##
## data: exec.pay
## V = 19306, p-value < 2.2e-16
## alternative hypothesis: true location is not equal to 0
## 95 percent confidence interval:
## 25.99998 32.99994
## sample estimates:
## (pseudo)median
##
         29.00002
```

As seen from the test results, the 95% confidence interval is between 25-32 thousand dollars.

Prop Test

```
prop.test(x = c(40,320), n = c(220,775), alternative = "two.sided")

##

## 2-sample test for equality of proportions with continuity correction

## data: c(40, 320) out of c(220, 775)

## X-squared = 38.635, df = 1, p-value = 5.11e-10

## alternative hypothesis: two.sided

## 95 percent confidence interval:

## -0.2956399 -0.1665302

## sample estimates:

## prop 1 prop 2

## 0.1818182 0.4129032
```

It tests whether the rates between two groups are equal. x is the number of successes, n is the total sample size.

Participation in Education (Quine) Example

```
library(MASS)
data(quine)
head(quine)
```

```
Eth Sex Age Lrn Days
##
## 1
     Α
          M FO SL
                      2
## 2
      A M FO SL
                     11
     A M FO SL
## 3
                    14
## 4
      Α
         M FO AL
                      5
## 5
    A M FO AL
                      5
## 6
    A M FO AL 13
attach(quine)
tab <- table(Eth,Sex)</pre>
prop.test(tab, alternative = "two.sided", conf.level = 0.95,
correct = FALSE)
##
   2-sample test for equality of proportions without continuity correction
##
## data: tab
## X-squared = 0.0040803, df = 1, p-value = 0.9491
## alternative hypothesis: two.sided
## 95 percent confidence interval:
## -0.1564218 0.1669620
## sample estimates:
     prop 1
              prop 2
## 0.5507246 0.5454545
```

When we look at the results in question, the null hypothesis is rejected because the p-value is very high, such as 0.94.

Seat Belt Example

```
crash <- matrix(c(178,144,135,47), ncol=2)</pre>
colnames(crash) <- c('Alive','Death')</pre>
rownames(crash) <- c('Without_Belt', 'Belted')</pre>
prop.table(crash)
##
                    Alive
                                Death
## Without Belt 0.3531746 0.26785714
## Belted
               0.2857143 0.09325397
prop.test(crash)
   2-sample test for equality of proportions with continuity correction
##
##
## data: crash
## X-squared = 16.848, df = 1, p-value = 4.05e-05
## alternative hypothesis: two.sided
## 95 percent confidence interval:
## -0.27155920 -0.09891401
```

```
## sample estimates:
## prop 1 prop 2
## 0.5686901 0.7539267
```

With these results, the null hypothesis that the death rates of seat belt users and non-users are not different is rejected.

Chi-Square Test (Relationship between Hepatitis and Tattoos)

Let's say the results obtained in a study on the relationship between hepatitis disease and the place where tattoos are made (licensed, unlicensed and not tattooed) are as follows:

```
hep \leftarrow matrix(c(17,35,8,53,22,491), ncol = 2)
colnames(hep) <- c('Positive', 'Negative')</pre>
rownames(hep) <- c('Licensed', 'Unlicensed', 'Not_Tattooed')</pre>
prop.table(hep)
##
                  Positive
                              Negative
## Licensed
                0.02715655 0.08466454
## Unlicensed 0.05591054 0.03514377
## Not_Tattooed 0.01277955 0.78434505
chisq.test(hep)
##
## Pearson's Chi-squared test
##
## data: hep
## X-squared = 230.76, df = 2, p-value < 2.2e-16
```

According to the test results obtained, the null hypothesis that there is no relationship between tattooing and hepatitis disease is rejected at the 5% significance level.