

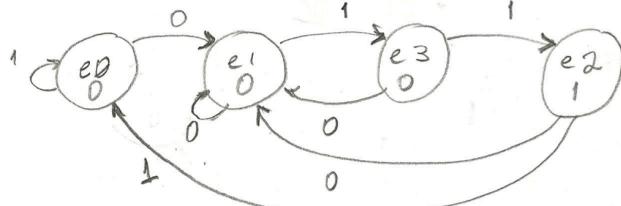
Resolução da Lista 1 de SD2 - 1/2015

1.

$$D_1 = A \cdot D_0$$

$$D_0 = \bar{A} + \bar{D}_1 \cdot D_0$$

$$Z = D_1 \cdot D_0$$



$D_1 \cdot D_0$	$D_1^* \cdot D_0^*$		Saída
	$A=0$	$A=1$	
e0 0	e1 0 1	e0 0 0	0
e1 0	e1 0 1	e3 1 1	0
e2 1	e1 0 1	e0 0 0	1
e3 1	e1 0 1	e2 1 0	0

$$e0 \rightarrow 00$$

$$e1 \rightarrow 01$$

$$e2 \rightarrow 10$$

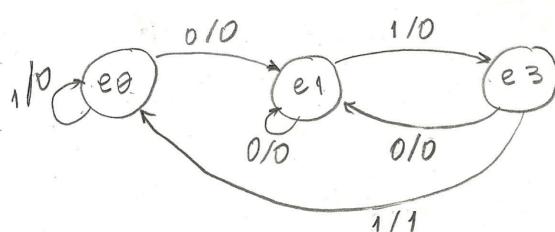
$$e3 \rightarrow 11$$

$$0, 1, 1$$

Projeto usando máquina de Mealy:

$D_1 \cdot D_0$	$D_1^* \cdot D_0^*/Z$	
	$A=0$	$A=1$
0 0	01/0	00/0
0 1	01/0	11/0
1 0	01/0	00/0
1 1	01/0	10/1

$D_1 \cdot D_0$	$D_1^* \cdot D_0^*/Z$	
	$A=0$	$A=1$
0 0	01/0	00/0
0 1	01/0	11/0
1 1	01/0	00/1



	00	01	11	10
0	0	0	0	X
1	1	0	1	X

$$D_1^* = \bar{D}_1 \cdot D_0 \cdot A$$

	00	01	11	10
0	1	1	1	X
1	0	1	0	X

$$D_0^* = \bar{A} + \bar{D}_1 \cdot D_0$$

$$Z = D_1 \cdot D_0 \cdot A$$

2.

7.12) Equações de excitação e saída:

$$D_1 = \bar{Q}_1 + Q_2$$

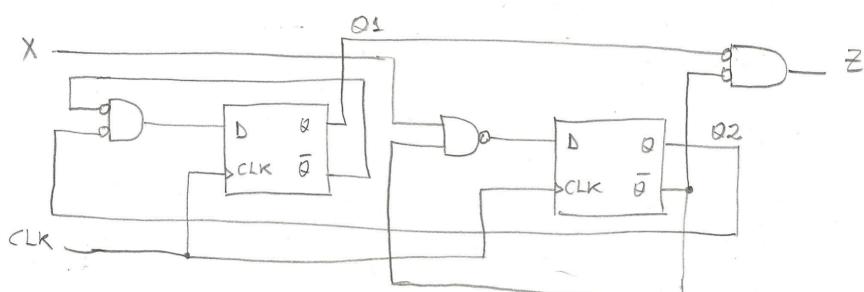
$$D_2 = \bar{Q}_2 \cdot X$$

$$Z = Q_1 + \bar{Q}_2$$

Tabela:

Estado Atual		Prox. Estado		Saída
Q_1	Q_2	$X=0$	$X=1$	Z
(A) 0 0		(C) 1 0	(D) 1 1	1
(B) 0 1		(C) 1 0	(C) 1 0	0
(C) 1 0		(A) 0 0	(B) 0 1	1
(D) 1 1		(C) 1 0	(C) 1 0	1

7.13) NOR $\rightarrow \overline{A+B} = \bar{A} \cdot \bar{B}$



Equações:

$$D_1 = \bar{Q}_1 \cdot \bar{Q}_2 = Q_1 \cdot \bar{Q}_2$$

$$D_2 = \bar{Q}_2 \cdot X$$

$$Z = \bar{Q}_1 \cdot \bar{Q}_2 = \bar{Q}_1 \cdot Q_2$$

Prox. estado e saída são invertidos.

Estado atual		Prox. Estado		Saída
Q_1	Q_2	$X=0$	$X=1$	Z
0 0		0 1	0 0	0
0 1		0 1	0 1	1
1 0		1 1	1 0	0
1 1		0 1	0 1	0

7.18) Equações:

$$D_2 = (Q_1 \oplus Q_0) \oplus (\bar{Q}_1 \cdot \bar{Q}_2)$$

$$D_1 = Q_2$$

$$D_0 = Q_1$$

Estado Atual			Próximo Estado				
	Q_2	Q_1	Q_0		Q_2^*	Q_1^*	Q_0^*
A	0	0	0	E	1	0	0
B	0	0	1	A	0	0	0
C	0	1	0	F	1	0	1
D	0	1	1	B	0	0	1
E	1	0	0	C	0	1	0
F	1	0	1	G	1	1	0
G	1	1	0	H	1	1	1
H	1	1	1	D	0	1	1

7.19) Equações:

$$D_3 = \bar{Q}_1 + (\overline{Y \cdot \bar{Q}_2}) = \bar{Q}_1 + Y \cdot \bar{Q}_2$$

$$D_2 = \bar{Q}_3 \cdot (\overline{Y + \bar{Q}_1}) = \bar{Q}_3 \cdot (Y + Q_1)$$

$$D_1 = X$$

Estado Atual			Próximo Estado				
	Q_1	Q_2	Q_3	$XY=00$	$XY=01$	$XY=11$	$XY=10$
000				001	011	111	101
001				001	001	101	101
010				001	011	111	101
011				001	001	101	101
100				010	011	111	110
101				000	001	101	100
110				010	010	110	110
111				000	000	100	100

$$1) \quad S_0 \rightarrow 00$$

$$S_1 \rightarrow 01$$

$$S_2 \rightarrow 10$$

Estado Atual	Proximo Estado ($S_1^* S_0^*$)				Saída Q
	AB=00	AB=01	AB=11	AB=10	
00	00	00	01	01	0
01	00	10	10	00	0
10	00	00	00	00	1

(Q1 Q0)

$$Q_1^* = \bar{Q}_0 \cdot B$$

$$Q_0^* = \bar{Q}_1 \cdot \bar{Q}_0 \cdot A$$

$$Q = Q_1 \cdot \bar{Q}_0$$

$$S_0 \rightarrow 00$$

$$S_1 \rightarrow 01$$

$$S_2 \rightarrow 10$$

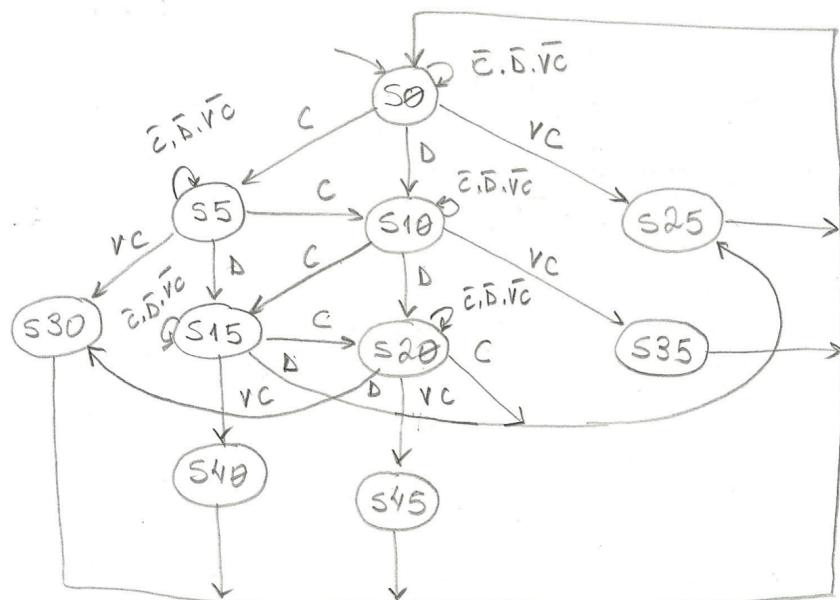
Estado Atual	Proximo Estado ($S_1^* S_0^*$) / Saída Q			
	AB=00	AB=01	AB=11	AB=10
00	00/0	00/0	01/0	01/0
01	00/0	10/0	10/0	00/0
10	00/0	00/0	10/1	00/0

$$Q_1^* = \bar{Q}_1 \cdot \bar{Q}_0 \cdot B + Q_1 \cdot A \cdot B$$

$$Q_0^* = \bar{Q}_1 \cdot \bar{Q}_0 \cdot A$$

$$Q = Q_1 \cdot \bar{Q}_0 \cdot A \cdot B$$

2)



Codificação One-Hot:

$S_0 \rightarrow 000\ 000\ 000\ 1$
 $S_5 \rightarrow 000\ 000\ 001\ 0$
 $S_{10} \rightarrow 000\ 000\ 010\ 0$
 $S_{25} \rightarrow 000\ 000\ 100\ 0$
 $S_{30} \rightarrow 000\ 0010\ 000\ 0$
 $S_{15} \rightarrow 000\ 0100\ 000\ 0$
 $S_{20} \rightarrow 000\ 1000\ 000\ 0$
 $S_{35} \rightarrow 001\ 0000\ 000\ 0$
 $S_{40} \rightarrow 0100\ 0000\ 000\ 0$
 $S_{45} \rightarrow 1000\ 0000\ 000\ 0$

Estado	Saida
S_{25}	REFRI
S_{35}	REFRI TROCO\$D
S_{45}	REFRI TROCO\$D
S_{40}	REFRI TROCO\$D TROCO\$C
S_{30}	REFRI TROCO\$C

Estado Atual
($Q_9 \dots Q_0$)

Estado Atual ($Q_9 \dots Q_0$)	C	D	VC	Próx. Estado ($Q_9^* \dots Q_0^*$)
$S_0 - 0000000001$	0	0	0	$S_0 - 0000000001$
$S_0 - 0000000001$	X	X	1	$S_{25} - 0000001000$
$S_0 - 0000000001$	X	1	X	$S_{10} - 0000000100$
$S_0 - 0000000001$	1	X	X	$S_5 - 0000000010$
$S_5 - 0000000010$	0	0	0	$S_5 - 0000000010$
$S_5 - 0000000010$	X	X	1	$S_{30} - 0000010000$
$S_5 - 0000000010$	X	1	X	$S_{15} - 0000100000$
$S_5 - 0000000010$	1	X	X	$S_{10} - 0000000100$
$S_{10} - 0000000100$	0	0	0	$S_{10} - 0000000100$
$S_{10} - 0000000100$	X	X	1	$S_{35} - 0010000000$
$S_{10} - 0000000100$	X	1	X	$S_{20} - 0001000000$
$S_{10} - 0000000100$	1	X	X	$S_{15} - 0000100000$
$S_{25} - 0000001000$	X	X	X	$S_0 - 0000000001$
$S_{30} - 0000010000$	X	X	X	$S_0 - 0000000001$
$S_{15} - 0000100000$	0	0	0	$S_{15} - 0000100000$
$S_{15} - 0000100000$	X	X	1	$S_{40} - 0100000000$
$S_{15} - 0000100000$	X	1	X	$S_{35} - 0010000000$
$S_{15} - 0000100000$	1	X	X	$S_{20} - 0001000000$
$S_{20} - 0001000000$	0	0	0	$S_{20} - 0001000000$
$S_{20} - 0001000000$	X	X	1	$S_{45} - 1000000000$
$S_{20} - 0001000000$	X	1	X	$S_{30} - 0000001000$
$S_{20} - 0001000000$	1	X	X	$S_{25} - 0000001000$
$S_{35} - 0010000000$	X	X	X	$S_0 - 0000000001$
$S_{40} - 0100000000$	X	X	X	$S_0 - 0000000001$
$S_{45} - 1000000000$	X	X	X	$S_0 - 0000000001$

Equações:

$$\theta_9^* = \theta_6 \cdot VC$$

$$\theta_8^* = \theta_5 \cdot VC$$

$$\theta_7^* = \theta_2 \cdot VC$$

$$\theta_6^* = \theta_2 \cdot D + \theta_5 \cdot C + \theta_6 \cdot \bar{C}, \bar{D}, \bar{VC}$$

$$\theta_5^* = \theta_1 \cdot D + \theta_2 \cdot C + \theta_5 \cdot \bar{C}, \bar{D}, \bar{VC}$$

$$\theta_4^* = \theta_1 \cdot VC + \theta_6 \cdot D$$

$$\theta_3^* = \theta_0 \cdot VC + \theta_5 \cdot D + \theta_6 \cdot C$$

$$\theta_2^* = \theta_0 \cdot D + \theta_1 \cdot C + \theta_2 \cdot \bar{C}, \bar{D}, \bar{VC}$$

$$\theta_1^* = \theta_0 \cdot C + \theta_1 \cdot \bar{C}, \bar{D}, \bar{VC}$$

$$\theta_0^* = \theta_0 \cdot \bar{C}, \bar{D}, \bar{VC} + \theta_3 + \theta_4 + \theta_7 + \theta_8 + \theta_9$$

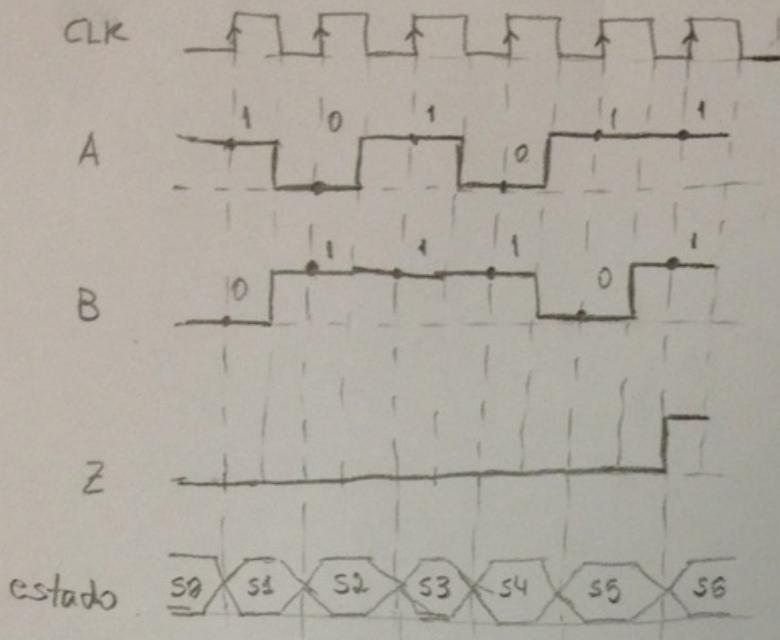
$$REFRI = \theta_3 + \theta_7 + \theta_9 + \theta_8 + \theta_4$$

$$TROCO1C = \theta_8 + \theta_4$$

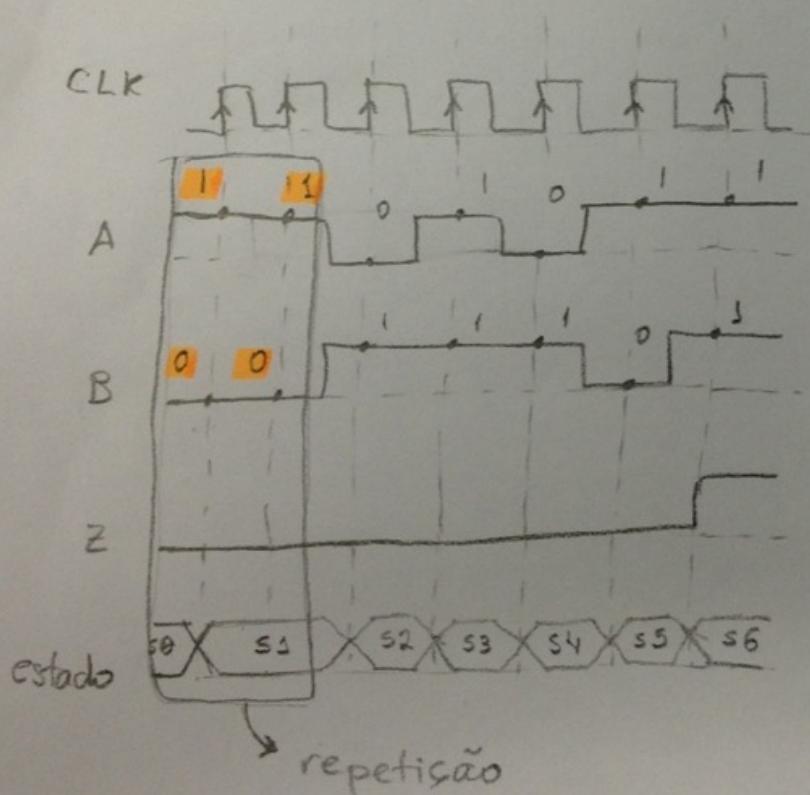
$$TROCO1D = \theta_7 + \theta_8$$

$$TROCO2D = \theta_9$$

* OBS: A tabela e as equações foram encontradas supondo-se que não há possibilidade de se colocar 2 moedas ao mesmo tempo.



Sem repetição
de uma mesma
entrada.



Repetição da
primeira entrada.

Como no enunciado considera-se válida a repetição
de uma mesma entrada, o circuito deve continuar
no mesmo estado.

ESTADO ATUAL	PRÓXIMO ESTADO				SAÍDA Z
	AB=00	AB=01	AB=11	AB=10	
S0	S0	ERRO	ERRO	S1	0
S1	S0	S2	ERRO	S1	0
S2	S0	S2	S3	ERRO	0
S3	S0	S4	S3	ERRO	0
S4	S0	S4	ERRO	S5	0
S5	S0	ERRO	S6	S5	0
S6	S0	ERRO	S6	S1	1
ERRO	S0	ERRO	ERRO	S1	0

Estados equivalentes

$Q_2\ Q_1\ Q_0$	$Q_2^*\ Q_1\ Q_0$				Z
	AB=00	AB=01	AB=11	AB=10	
000	000	111	111	001	0
001	000	010	111	001	0
010	000	010	011	111	0
011	000	100	011	111	0
100	000	100	111	101	0
101	000	111	110	101	0
110	000	111	110	001	1
111	000	111	111	001	0

Estados equivalentes

Tabelas de transição e saída.

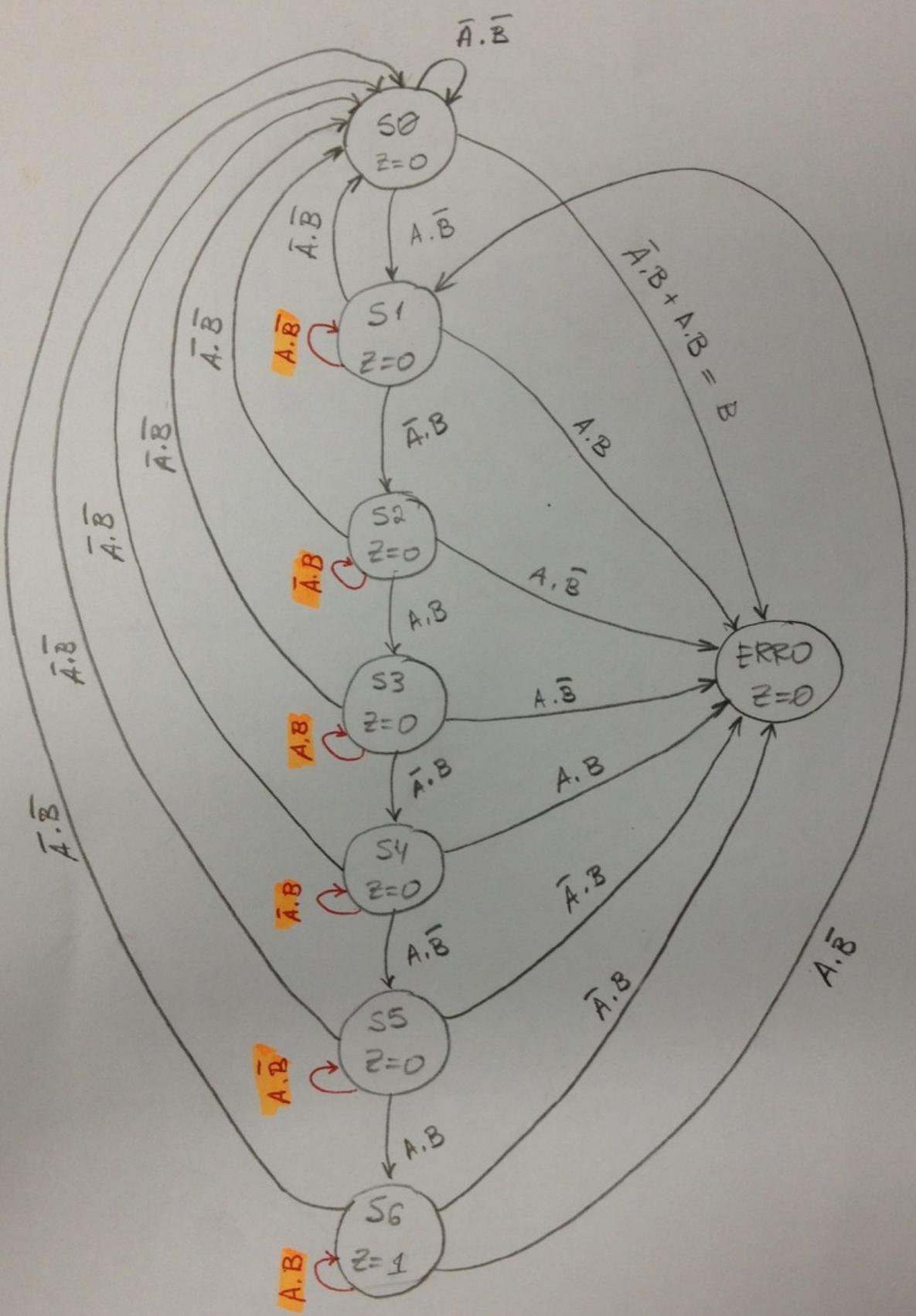
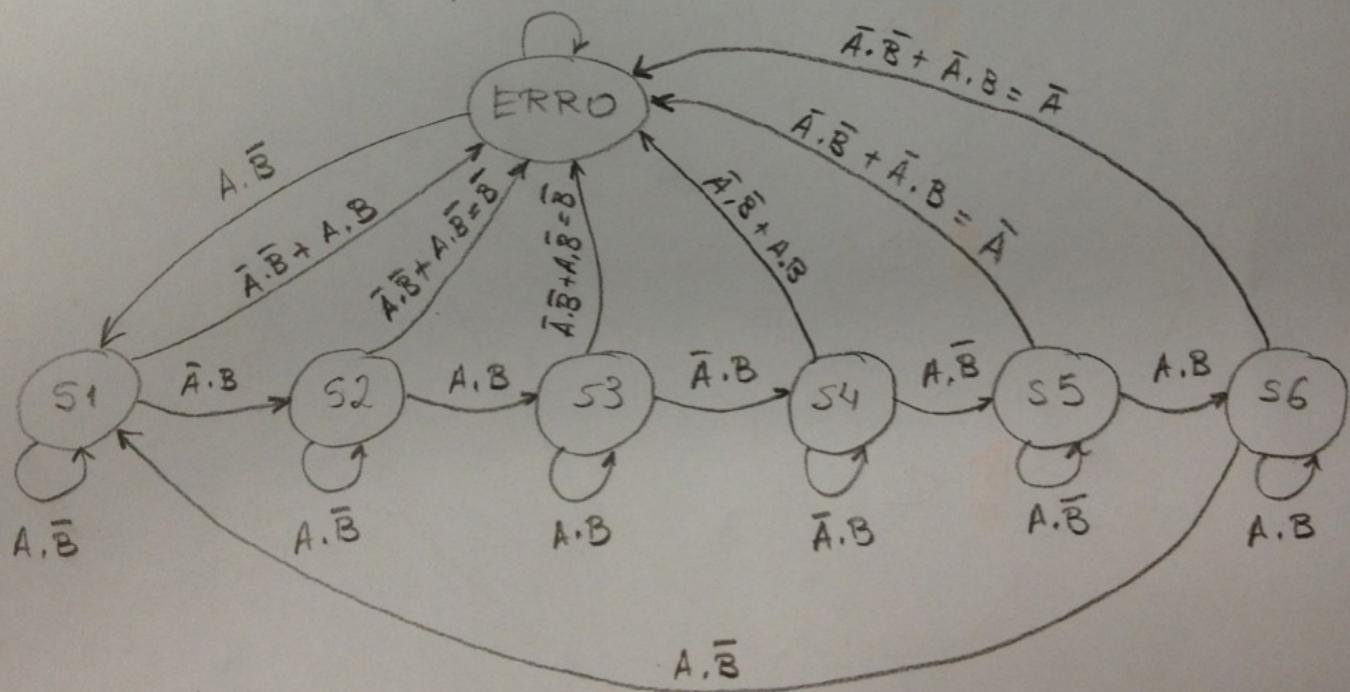


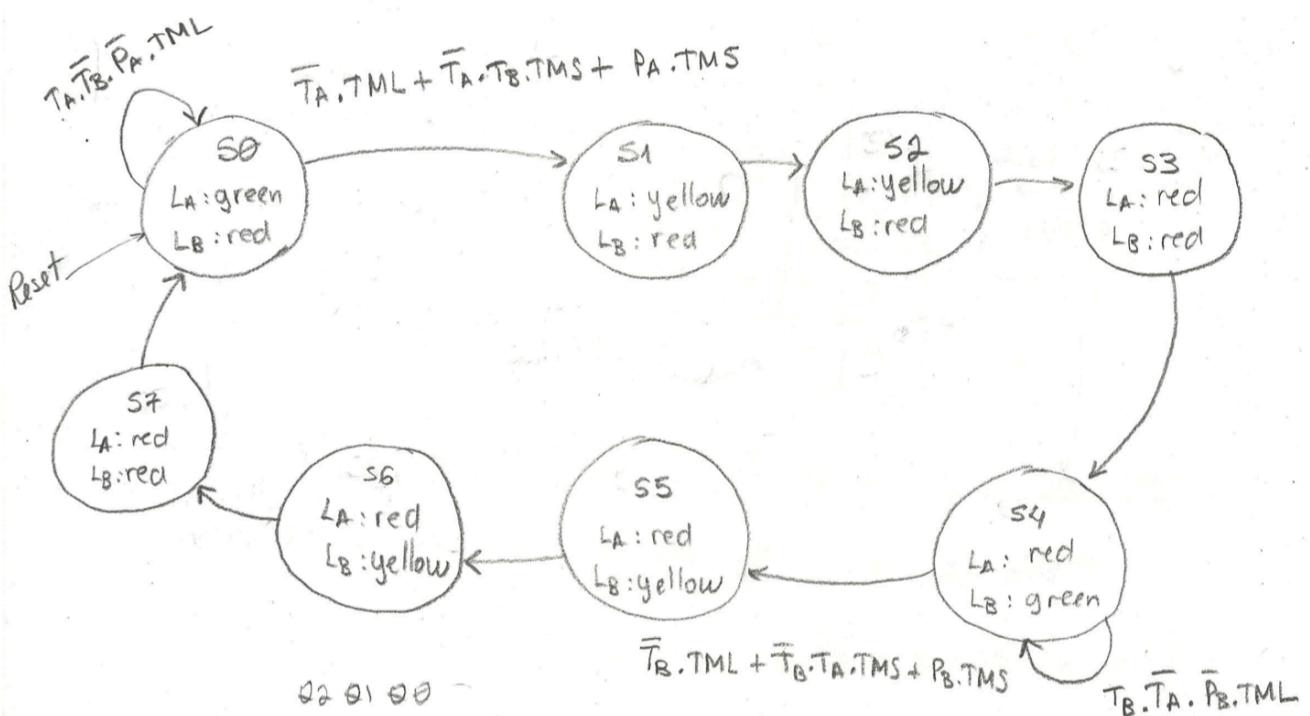
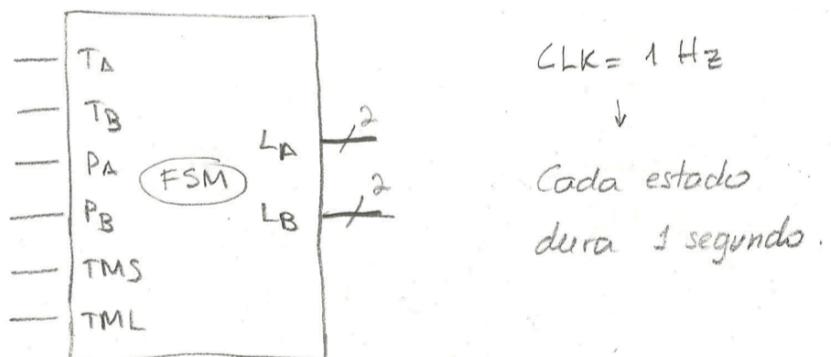
Diagrama de estados.

Após a equivalência de estados:

ESTADO ATUAL	PRÓXIMO ESTADO				SAÍDA Z
	AB=00	AB = 01	AB = 11	AB = 10	
ERRO	ERRO	ERRO	ERRO	S1	0
S1	ERRO	S2	ERRO	S1	0
S2	ERRO	S2	S3	ERRO	0
S3	ERRO	S4	S3	ERRO	0
S4	ERRO	S4	ERRO	S5	0
S5	ERRO	ERRO	S6	S5	0
S6	ERRO	ERRO	S6	S1	1

$$\bar{A}.\bar{B} + \bar{A}.B + A.B = \bar{A}.\bar{B} + B$$





$S_0 \rightarrow 000$
 $S_1 \rightarrow 001$
 $S_2 \rightarrow 010$
 $S_3 \rightarrow 011$
 $S_4 \rightarrow 100$
 $S_5 \rightarrow 101$
 $S_6 \rightarrow 110$
 $S_7 \rightarrow 111$

saldos:

$00 \rightarrow \text{green}$
 $01 \rightarrow \text{yellow}$
 $10 \rightarrow \text{red}$

Estado Atual $Q_2\ Q_1\ Q_0$	Entradas						Próximo Estado $Q_2^*\ Q_1^*\ Q_0^*$
	T_A	T_B	P_A	P_B	TMS	TML	
000	1	0	0	X	X	1	000
000	0	X	X	X	X	1	001
000	0	1	X	X	1	X	001
000	X	X	1	X	1	X	001
001	X	X	X	X	X	X	010
010	X	X	X	X	X	X	011
011	X	X	X	X	X	X	100
100	0	1	X	0	X	1	100
100	X	0	X	X	X	1	101
100	1	0	X	X	1	X	101
100	X	X	X	1	1	X	101
101	X	X	X	X	X	X	110
110	X	X	X	X	X	X	111
111	X	X	X	X	X	X	000

$$Q_2^* = \bar{Q}_2 \cdot Q_1 \cdot Q_0 + Q_2 \cdot \bar{Q}_1 \cdot \bar{Q}_0 (\bar{T}_A \cdot T_B \cdot \bar{P}_B \cdot TML + \bar{T}_B \cdot TML + \\ + T_A \cdot \bar{T}_B \cdot TMS + P_B \cdot TMS) + Q_2 \cdot \bar{Q}_1 \cdot Q_0 + Q_2 \cdot Q_1 \cdot \bar{Q}_0$$

$$Q_1^* = \bar{Q}_2 \cdot \bar{Q}_1 \cdot Q_0 + \bar{Q}_2 \cdot Q_1 \cdot \bar{Q}_0 + Q_2 \cdot \bar{Q}_1 \cdot \bar{Q}_0 + Q_2 \cdot Q_1 \cdot \bar{Q}_0$$

$$Q_0^* = \bar{Q}_2 \cdot \bar{Q}_1 \cdot \bar{Q}_0 (-P_A \cdot TML) + \bar{T}_A \cdot TML + \bar{T}_A \cdot T_B \cdot TMS + \\ + \bar{Q}_2 \cdot Q_1 \cdot \bar{Q}_0 + Q_2 \cdot \bar{Q}_1 \cdot \bar{Q}_0 (\bar{T}_B \cdot TML + T_A \cdot \bar{T}_B \cdot TMS + \\ + P_B \cdot TML) + Q_2 \cdot Q_1 \cdot \bar{Q}_0$$

Sardas:

Estado atual $Q_2 Q_1 Q_0$	Sardas			
	L_{A1}	L_{A0}	L_{B1}	L_{B0}
0 0 0	0	0	1	0
0 0 1	0	1	1	0
0 1 0	0	1	1	0
0 1 1	1	0	1	0
1 0 0	1	0	0	0
1 0 1	1	0	0	1
1 1 0	1	0	0	1
1 1 1	1	0	1	0

$\overline{Q_2} \overline{Q_1}$	00	01	11	10
$\overline{Q_0}$	0	0 0	1 1	
1	0	1	1 1	1

$$L_{A1} = Q_2 + Q_1 \cdot \overline{Q_0}$$

$\overline{Q_2} \overline{Q_1}$	00	01	11	10
$\overline{Q_0}$	0	0	1	0 0
1	1	1	0	0 0

$$L_{A0} = \overline{Q}_2 \cdot Q_1 \cdot \overline{Q}_0 + \overline{Q}_2 \cdot \overline{Q}_1 \cdot Q_0$$

$\overline{Q_2} \overline{Q_1}$	00	01	11	10
$\overline{Q_0}$	0	1 1	0	0
1	1	1 1	1	0

$\overline{Q_2} \overline{Q_1}$	00	01	11	10
$\overline{Q_0}$	0	0	0	1 0
1	0	0	0	0 1

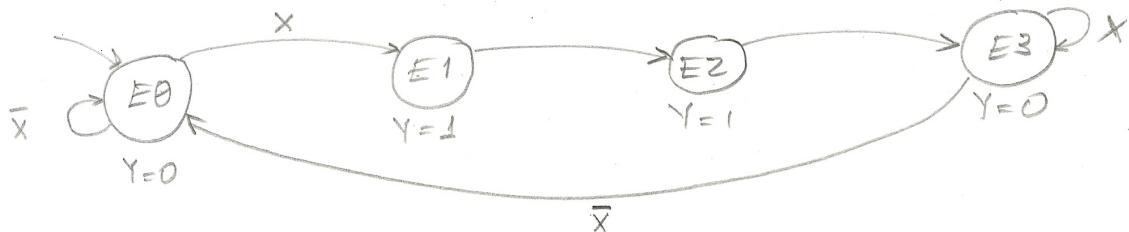
$$L_{B1} = \overline{Q}_2 + Q_1 \cdot Q_0$$

$$L_{B0} = Q_2 \cdot Q_1 \cdot \overline{Q}_0 + Q_2 \cdot \overline{Q}_1 \cdot Q_0$$

3.23. Entrada X

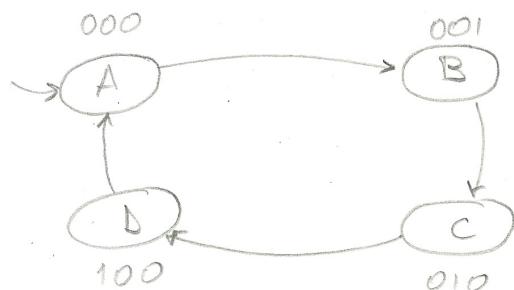
Saída Y

$X: 0 \rightarrow 1 \rightarrow Y=1$ por 2 ciclos de clock e depois $Y=0$.

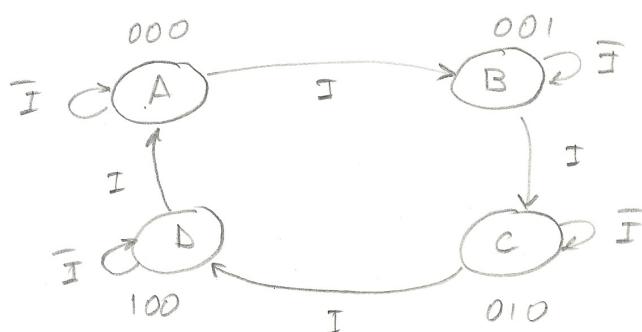


3.24. Saídas: X, y e z

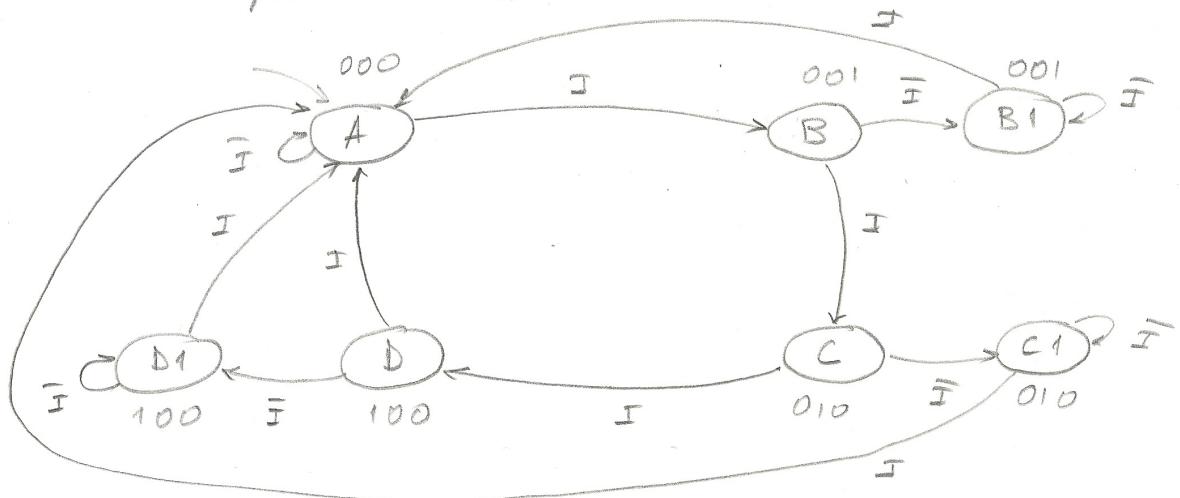
Sequência: 000, 001, 010, 100, 000, ...
A. B. C. D. A



3.25. Entrada I: para a sequência quando $I=0$.

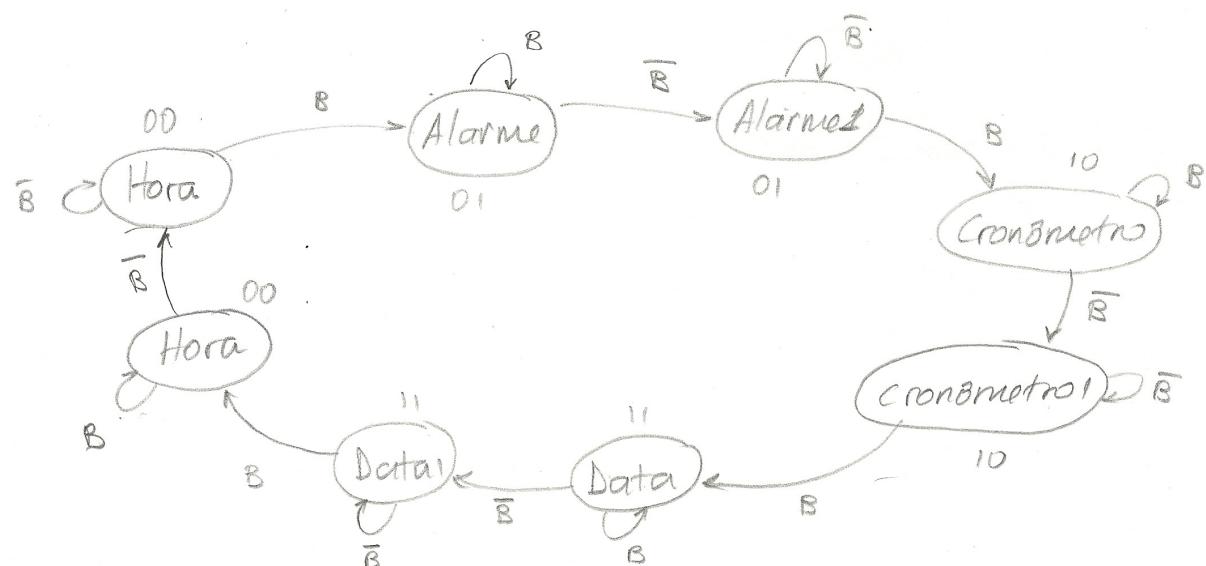


3.26. Se $I=0$, sequência é interrompida e, quando $I=1$, sequência começará em 000.



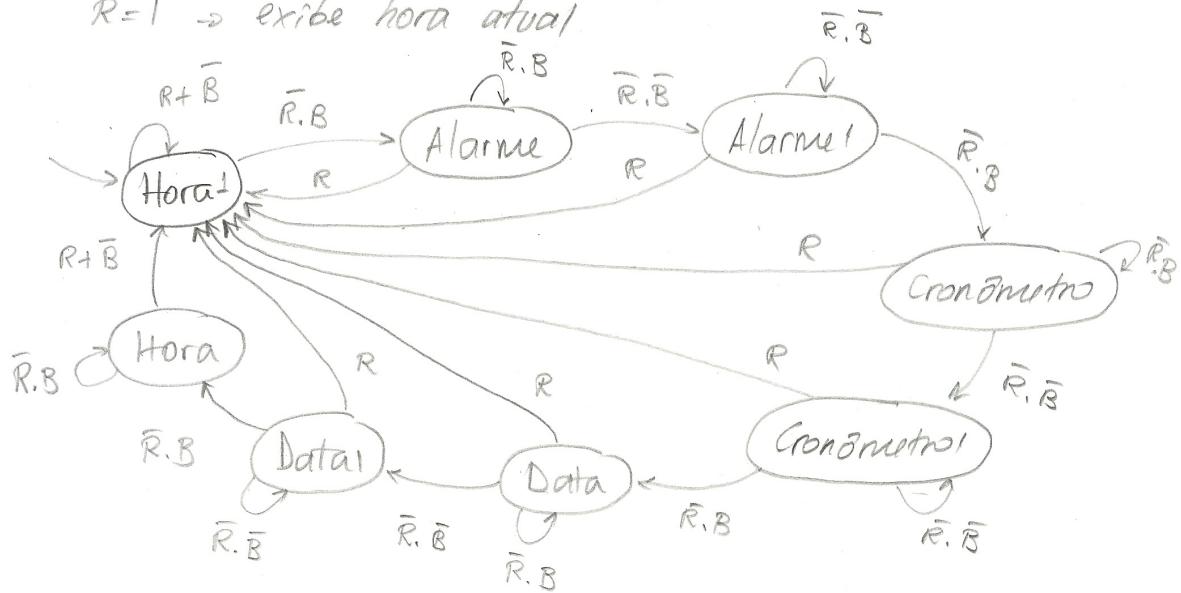
<u>3.27.</u>	<u>s1</u>	<u>s0</u>	<u>Operação</u>
	0	0	Hora atual
	0	1	Alarme
	1	0	Cronômetro
	1	1	Data

$B=1$: próximo item
Entrada B
Saídas s1, s0



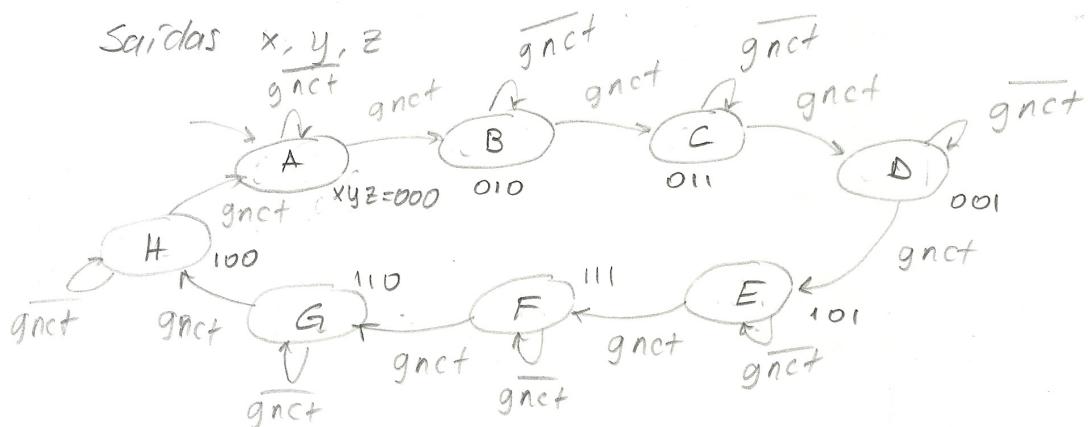
3.28. Entrada R.

$R=1 \rightarrow$ exibe hora atual



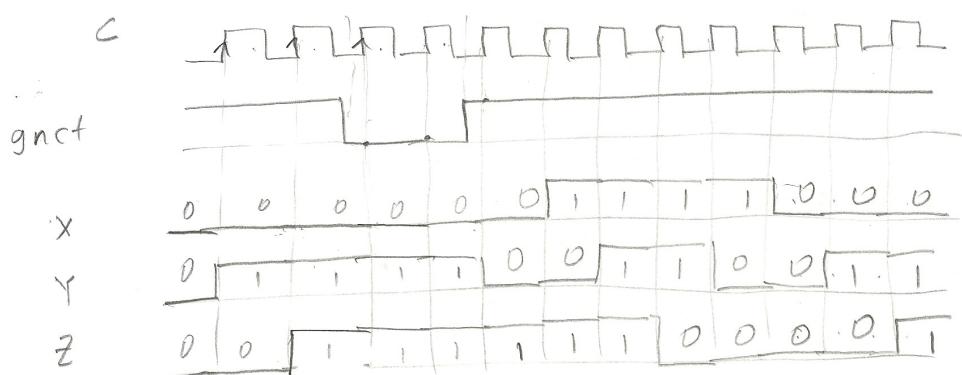
3.29. Entrada gnt

Saiidas x, y, z



3.30.

C



1)

ESTADO ATUAL (Q ₂ Q ₁ Q ₀)	PRÓXIMO ESTADO	
	A = 0	A = 1
0 0 0	1 0 0	0 0 1
0 0 1	0 0 0	0 1 1
0 1 1	0 0 1	0 1 0
0 1 0	0 1 1	1 1 0
1 1 0	0 1 0	1 1 1
1 1 1	1 1 0	1 0 1
1 0 1	1 1 1	1 0 0
1 0 0	1 0 1	0 0 0

→ Contador Gray crescente/decrescente.

Q ₂ Q ₁		00	01	11	10
Q ₀ A		00	01	11	10
00	1	0	0	1	
01	0	1	1	0	
11	0	0	1	1	
10	0	0	1	1	

$$\begin{aligned} Q_2^* &= \bar{Q}_2 \cdot \bar{Q}_0 \cdot \bar{A} + Q_1 \cdot \bar{Q}_0 \cdot A \\ &\quad + Q_2 \cdot Q_0 \end{aligned}$$

Q ₂ Q ₁		00	01	11	10
Q ₀ A		00	01	11	10
00	0	1	1	0	
01	0	1	1	0	
11	1	1	0	0	
10	0	0	1	1	

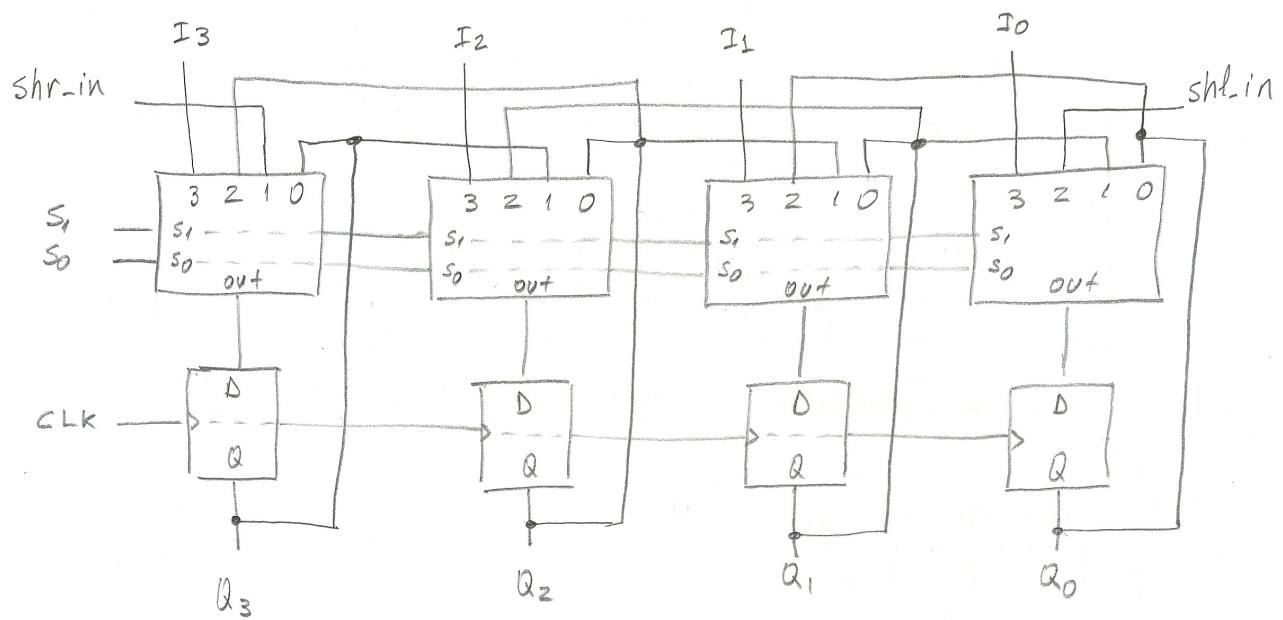
$$\begin{aligned} Q_1^* &= Q_1 \cdot \bar{Q}_0 + \bar{Q}_2 \cdot Q_0 \cdot A \\ &\quad + Q_2 \cdot Q_0 \cdot \bar{A} \end{aligned}$$

Q ₂ Q ₁		00	01	11	10
Q ₀ A		00	01	11	10
00	0	1	0	1	
01	1	0	1	0	
11	0	0	1	0	
10	0	1	0	1	

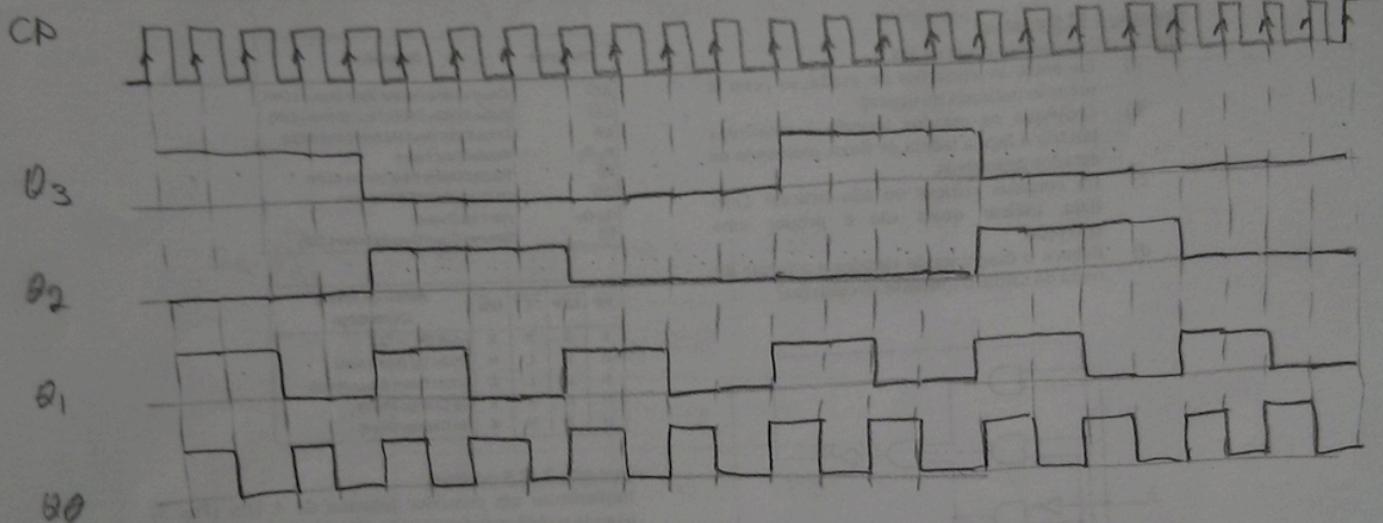
$$\begin{aligned} Q_0^* &= \bar{Q}_2 \cdot Q_1 \cdot \bar{A} + Q_2 \cdot \bar{Q}_1 \cdot \bar{A} \\ &\quad + \bar{Q}_2 \cdot \bar{Q}_1 \cdot A + Q_2 \cdot Q_1 \cdot A \end{aligned}$$

2)

S_1	S_0	Operação
0	0	Hold
0	1	Shift Right
1	0	Shift Left
1	1	Load



O contador conta de 11 até 0. Logo, o módulo é 12.

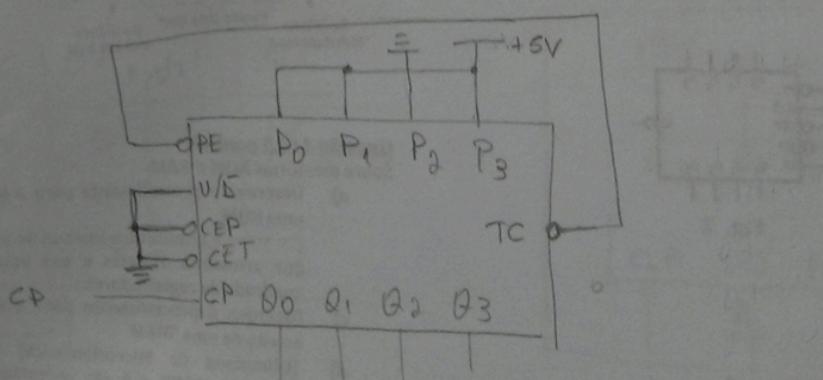


$$f_{Q_3} = f_{CP}/12 = 120/12 = 10$$

$$f_{Q_2} = f_{CP}/12 = 120/12 = 10$$

$$f_{Q_1} = f_{CP}/4 = 120/4 = 30$$

$$f_{Q_0} = f_{CP}/2 = 120/2 = 60$$



4) 74×194

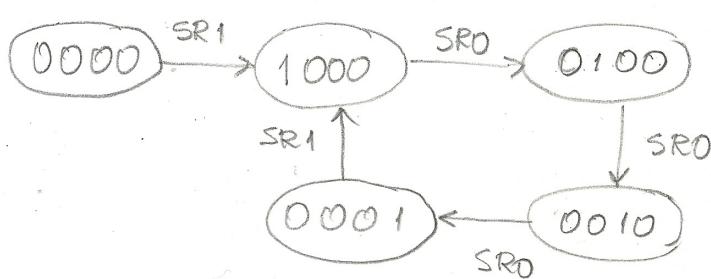
$\bar{Q}_A \bar{Q}_B \bar{Q}_C Q_D$

$$1000 \rightarrow ROR1 = 0100$$

$$ROR2 = 0010$$

$$ROR3 = 0001$$

$$ROR4 = 1000$$



Shift Right:

$$S_1 S_0 = 01$$

$\bar{Q}_A Q_B$ $\bar{Q}_C Q_D$	00	01	11	10
00	SR1	SRO	X	SRO
01	SR1	X	X	X
11	X	X	X	X
10	SRO	X	X	X

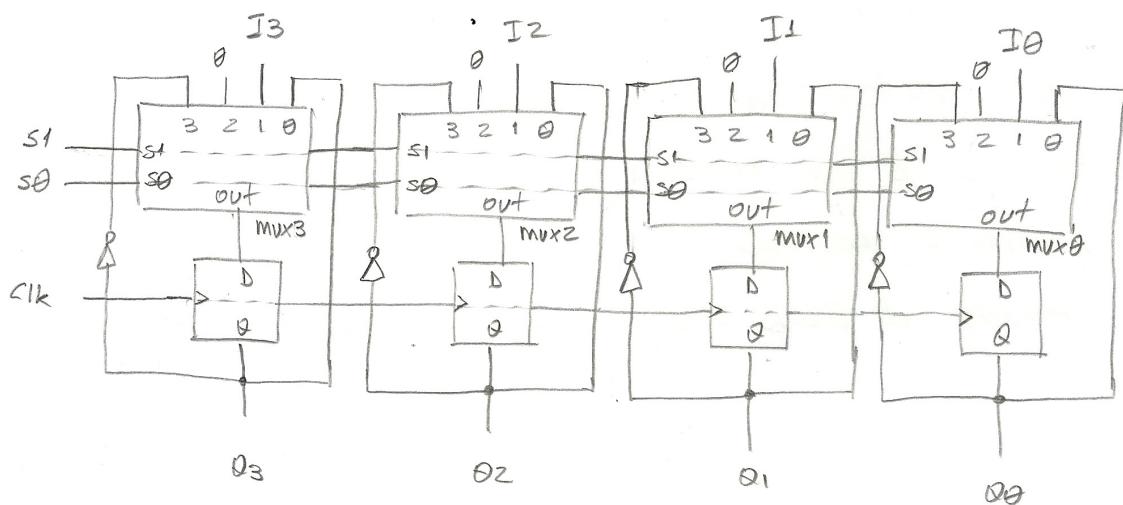
$$SL1 = X$$

$$P_A, P_B, P_C, P_D = X$$

$$SRI = \bar{Q}_A \cdot \bar{Q}_B \cdot \bar{Q}_C$$

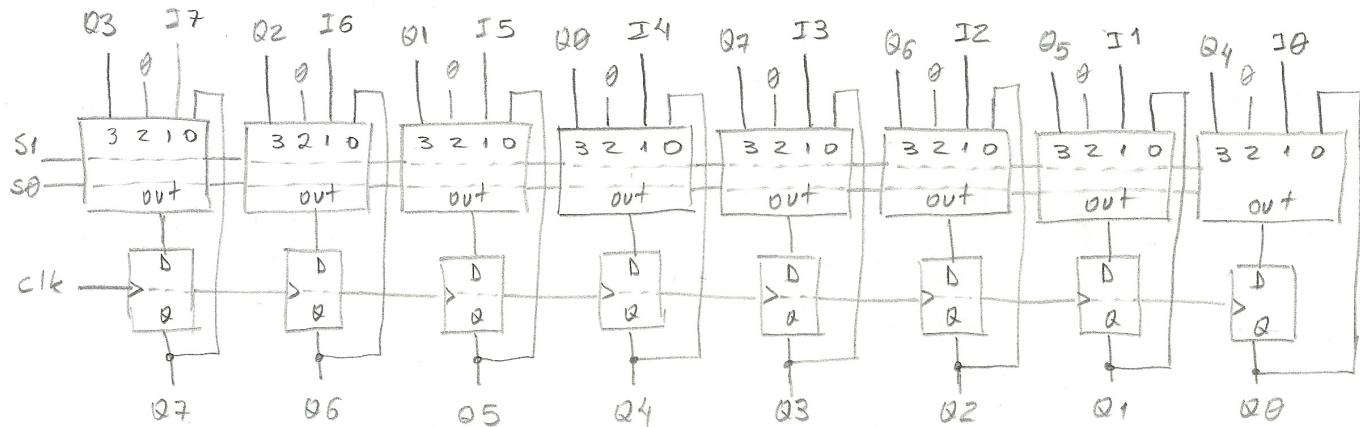
	00	01	11	10
00	1	0	X	0
01	1	X	X	X
11	X	X	X	X
10	0	X	X	X

$\frac{S1}{S2}$	$S0$	OP
0	0	Hold
0	1	Load $I_3 \dots I_0$
1	0	Clear
1	1	Complement



4.4. Basta ligar Q_0 na entrada 3 do mux_3 , Q_1 na entrada 3 do mux_2 , Q_2 na entrada 3 do mux_1 , Q_3 na entrada 3 do mux_0 .

<u>4.5.</u>	<u>S1</u>	<u>S0</u>	<u>Op.</u>
	00		Hold
	01		Load
	10		Clear
	11		Swap nibble



4.6. Basta utilizar um registrador de 8 bits e ligar a entrada B na entrada "load" do registrador. Assim, quando a entrada B for acionada, os dados de entrada de 8 bits serão carregados no registrador.