

# Materiais Elétricos e Magnéticos para Engenharia

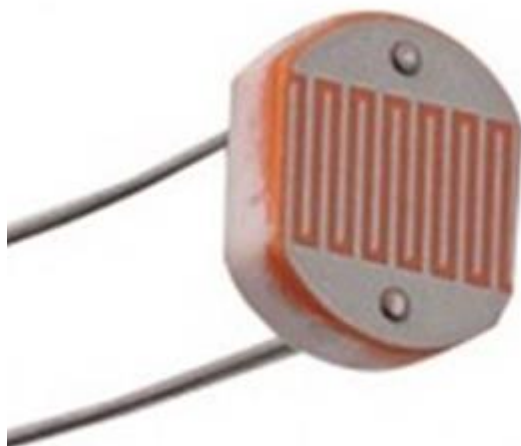
**Professor: Marcus V. Batistuta**

Laboratório #4  
**LDR**

1º Semestre de 2018

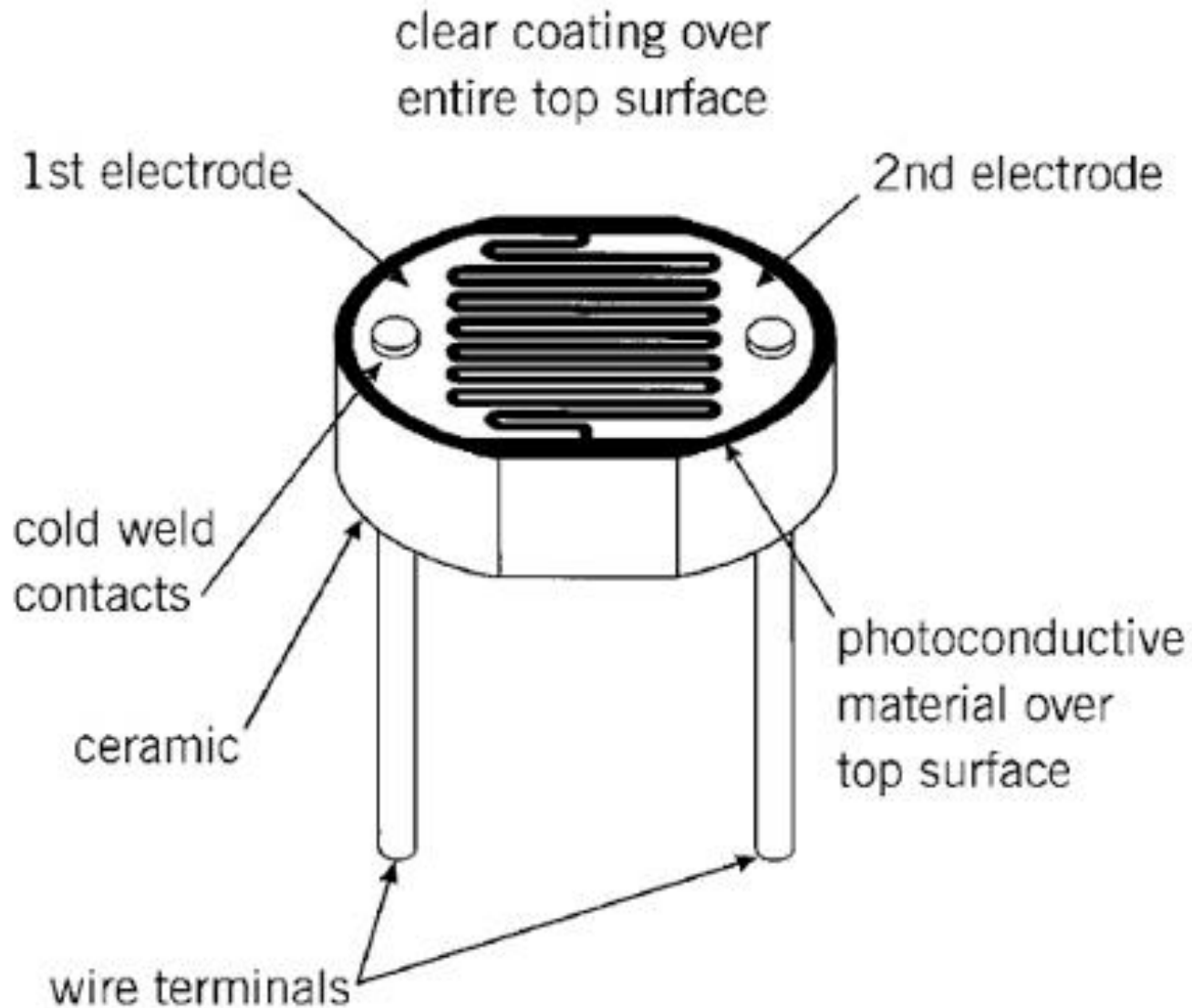
**FGA - Universidade de Brasília**

# LDR: *Light Dependent Resistor*

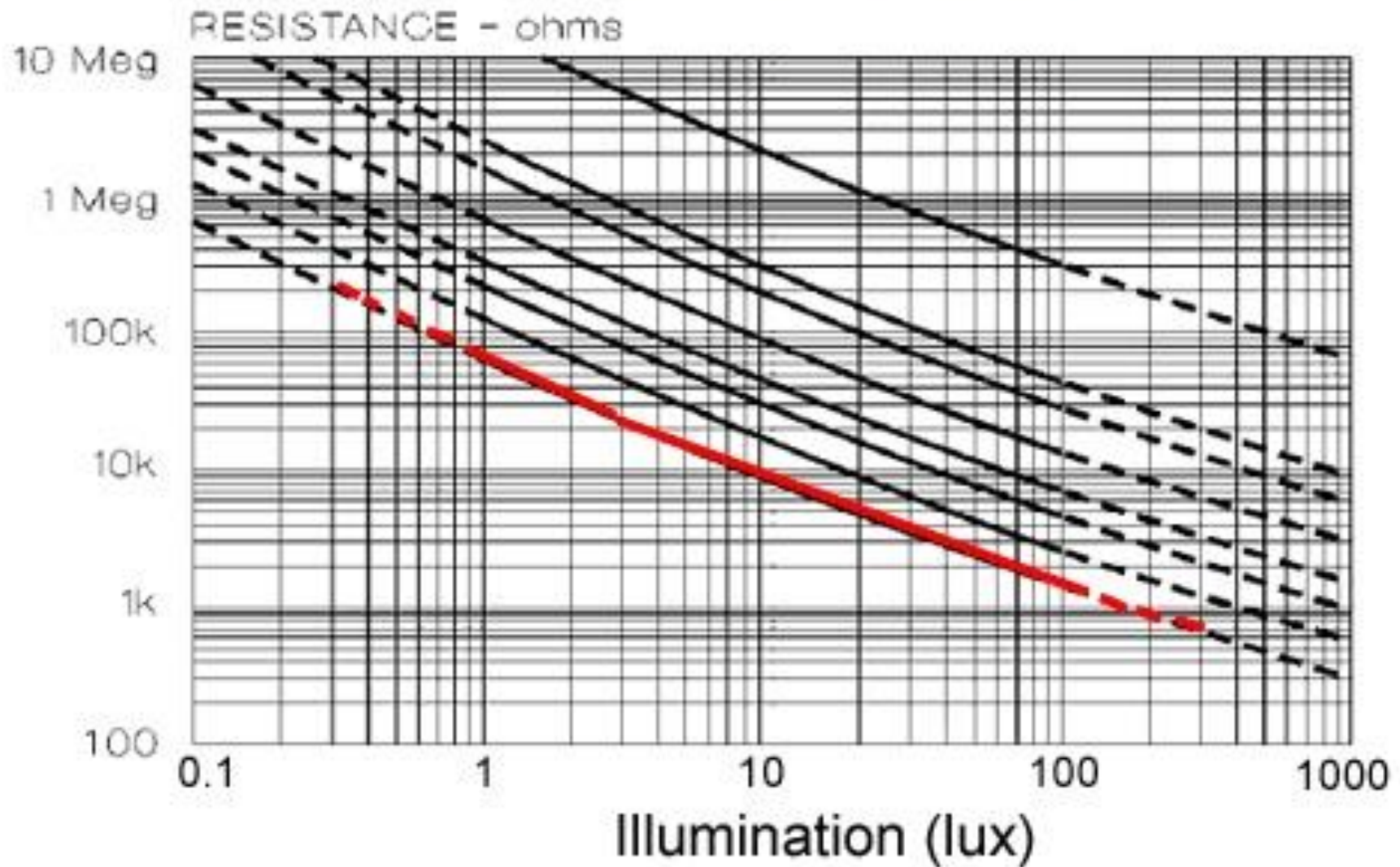


Semiconductor	Tipo	$E_g$ eV	
		0 K	300 K
CdS	<i>d</i>	2,582	2,42
CdSe	<i>d</i>	1,840	1,74

## ***LDR: Light Dependent Resistor***



# Resistance vs. Illumination



$$1 \text{ lux} = 1 \text{ lumen/m}^2$$

# Fotometria

Quantity		Unit		Dimension	Notes
Name	Symbol <sup>[nb 1]</sup>	Name	Symbol	Symbol	
Luminous energy	$Q_V$ <sup>[nb 2]</sup>	lumen second	lm·s	$\mathbf{T \cdot J}$ <sup>[nb 3]</sup>	Units are sometimes called <i>talbots</i> .
<b>Luminous flux</b> / luminous power	$\Phi_V$ <sup>[nb 2]</sup>	lumen (= cd·sr)	lm	$\mathbf{J}$ <sup>[nb 3]</sup>	Luminous energy per unit time.
Luminous intensity	$I_V$	candela (= lm/sr)	cd	$\mathbf{J}$ <sup>[nb 3]</sup>	Luminous power per unit <i>solid angle</i> .
Luminance	$L_V$	candela per square metre	cd/m <sup>2</sup>	$\mathbf{L^{-2} \cdot J}$	Luminous power per unit solid angle per unit <i>projected</i> source area. Units are sometimes called <i>nits</i> .
Illuminance	$E_V$	lux (= lm/m <sup>2</sup> )	lx	$\mathbf{L^{-2} \cdot J}$	Luminous power <i>incident</i> on a surface.
Luminous exitance / luminous emittance	$M_V$	lux	lx	$\mathbf{L^{-2} \cdot J}$	Luminous power <i>emitted</i> from a surface.
Luminous exposure	$H_V$	lux second	lx·s	$\mathbf{L^{-2} \cdot T \cdot J}$	
Luminous energy density	$\omega_V$	lumen second per cubic metre	lm·s·m <sup>-3</sup>	$\mathbf{L^{-3} \cdot T \cdot J}$	
Luminous efficacy	$\eta$ <sup>[nb 2]</sup>	lumen per watt	lm/W	$\mathbf{M^{-1} \cdot L^{-2} \cdot T^3 \cdot J}$	Ratio of luminous flux to <i>radiant flux</i> or power consumption, depending on context.
Luminous efficiency / luminous coefficient	$V$			1	
See also: <a href="#">SI</a> · <a href="#">Photometry</a> · <a href="#">Radiometry</a>					

# Fotômetro Analógico



$$P_{(W)} = \Phi_{v(lm)} / \eta_{(lm/W)}$$

## Luminous efficacy table

Light type	Typical luminous efficacy (lumens/watt)
Tungsten incandescent light bulb	12.5-17.5 lm/W
Halogen lamp	16-24 lm/W
Fluorescent lamp	45-75 lm/W
LED lamp	30-90 lm/W
Metal halide lamp	75-100 lm/W
High pressure sodium vapor lamp	85-150 lm/W
Low pressure sodium vapor lamp	100-200 lm/W
Mercury vapor lamp	35-65 lm/W

## Lumens to watts table

Lumens	Incandescent light bulb watts	Fluorecent / LED watts
375 lm	25 W	6.23 W
600 lm	40 W	10 W
900 lm	60 W	15 W
1125 lm	75 W	18.75 W
1500 lm	100 W	25 W
2250 lm	150 W	37.5 W
3000 lm	200 W	50 W



Examples	
Illuminance	Surfaces illuminated by:
0.0001 lux	Moonless, overcast night sky ( <a href="#">starlight</a> ) <sup>[3]</sup>
0.002 lux	Moonless clear night sky with <a href="#">airglow</a> <sup>[3]</sup>
0.27–1.0 lux	Full moon on a clear night <sup>[3][4]</sup>
3.4 lux	Dark limit of civil <a href="#">twilight</a> under a clear sky <sup>[5]</sup>
50 lux	Family living room lights (Australia, 1998) <sup>[6]</sup>
80 lux	Office building hallway/ <a href="#">toilet</a> lighting <sup>[7][8]</sup>
100 lux	Very dark overcast day <sup>[3]</sup>
320–500 lux	Office lighting <sup>[9][10][11]</sup>
400 lux	<a href="#">Sunrise</a> or <a href="#">sunset</a> on a clear day.
1000 lux	Overcast day; <sup>[3]</sup> typical <a href="#">TV studio</a> lighting
10 000–25 000 lux	Full <a href="#">daylight</a> (not direct sun) <sup>[3]</sup>
32 000–100 000 lux	Direct <a href="#">sunlight</a>

## Criação e Recombinação de Pares Elétron-Buraco

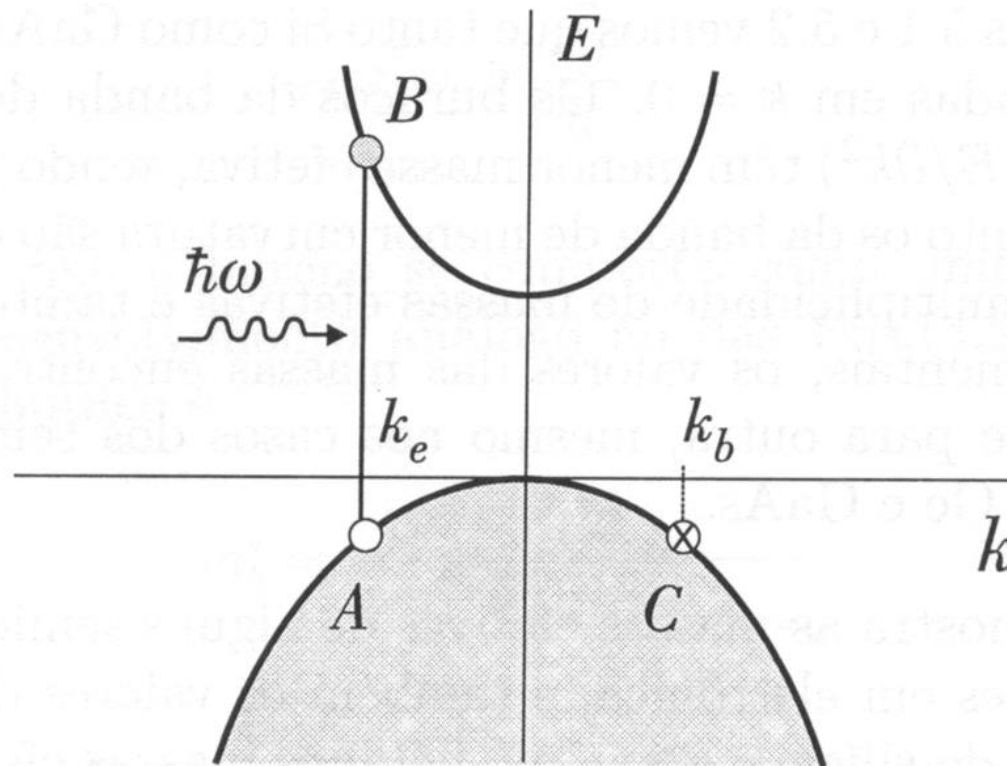


Figura 5.5: Absorção de um fóton de energia  $\hbar\omega$  e vetor de onda desprezível acompanhada da criação de um par elétron-buraco em semicondutor de gap direto.

$$J = (\sigma_n + \sigma_p)\mathcal{E} = \sigma\mathcal{E}$$

$$\sigma = e(n_0 \mu_n + p_0 \mu_p)$$

Errado

## LDR: Resposta Espectral

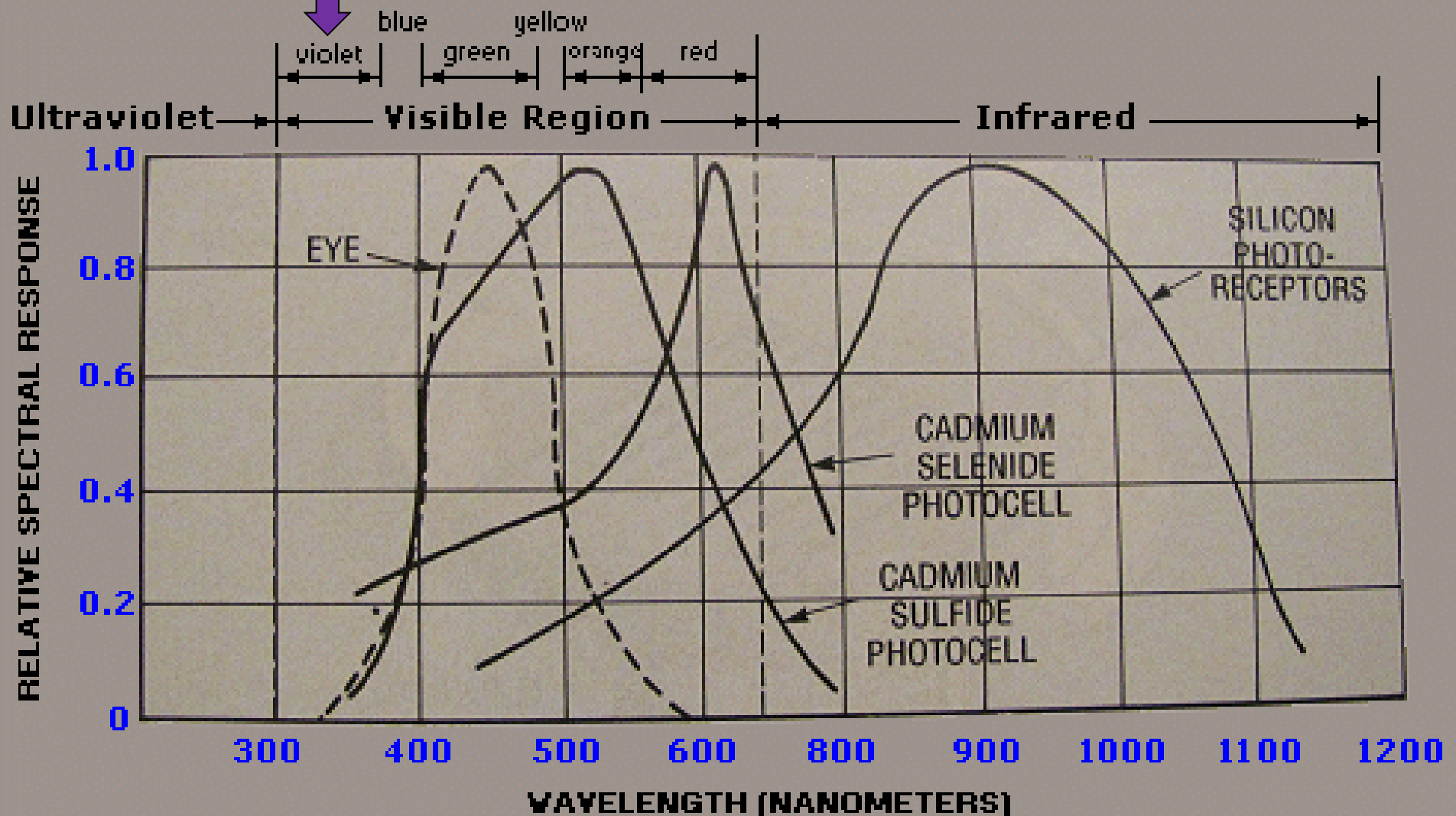
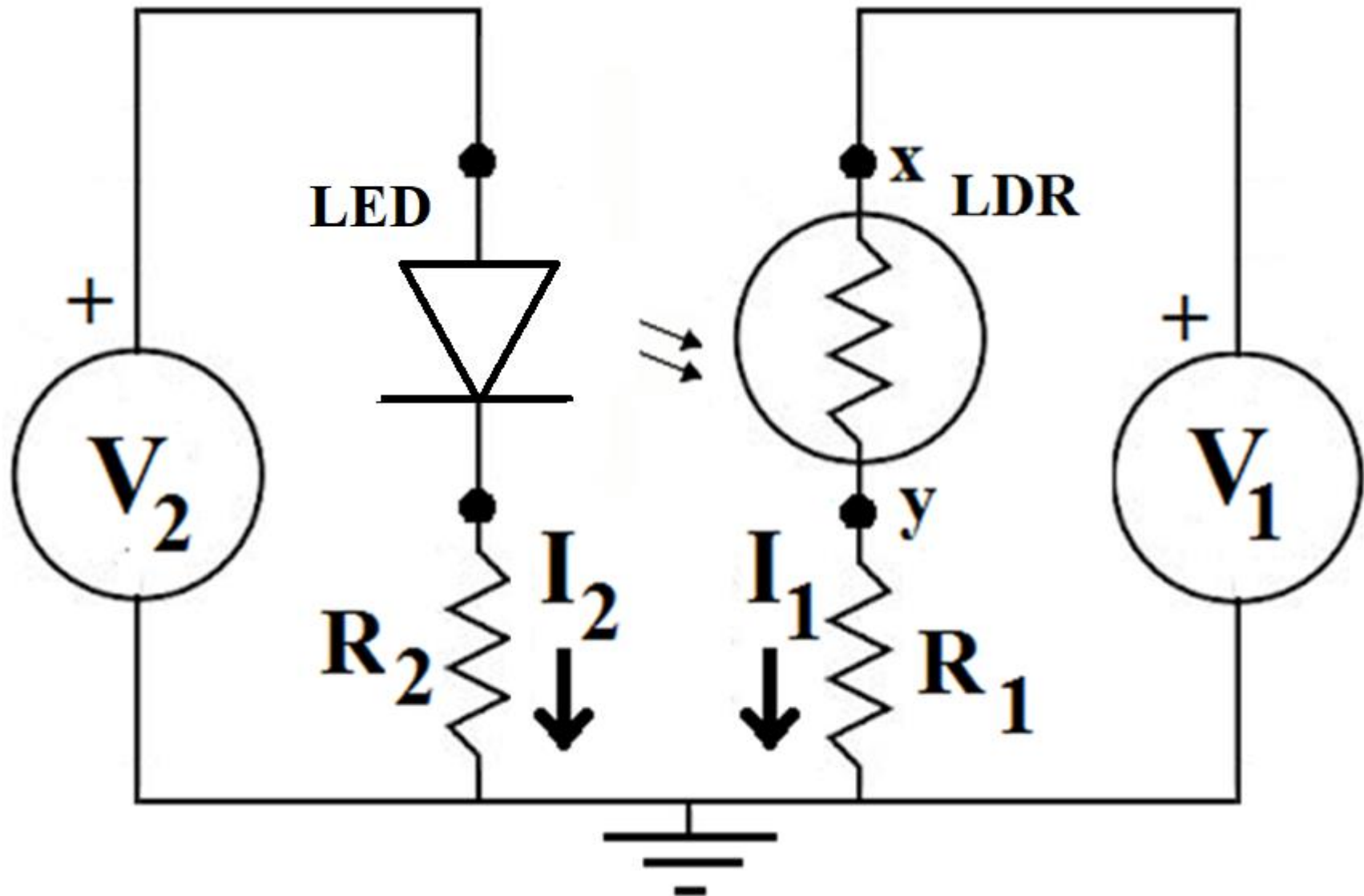
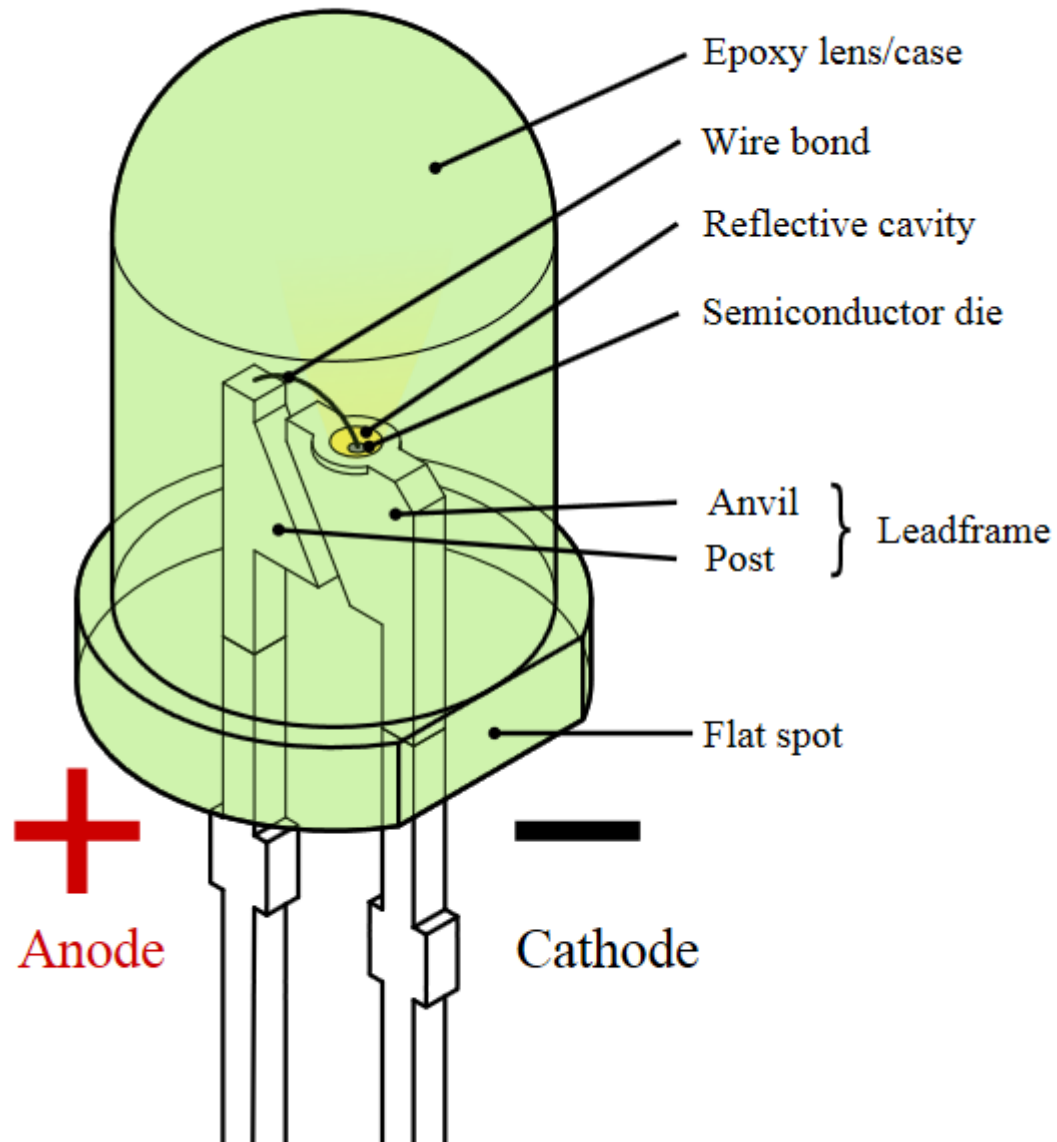


Fig. 3--Characteristic curves of photosensitive devices compared with the response curve of the human eye.

## Montagem Experimental



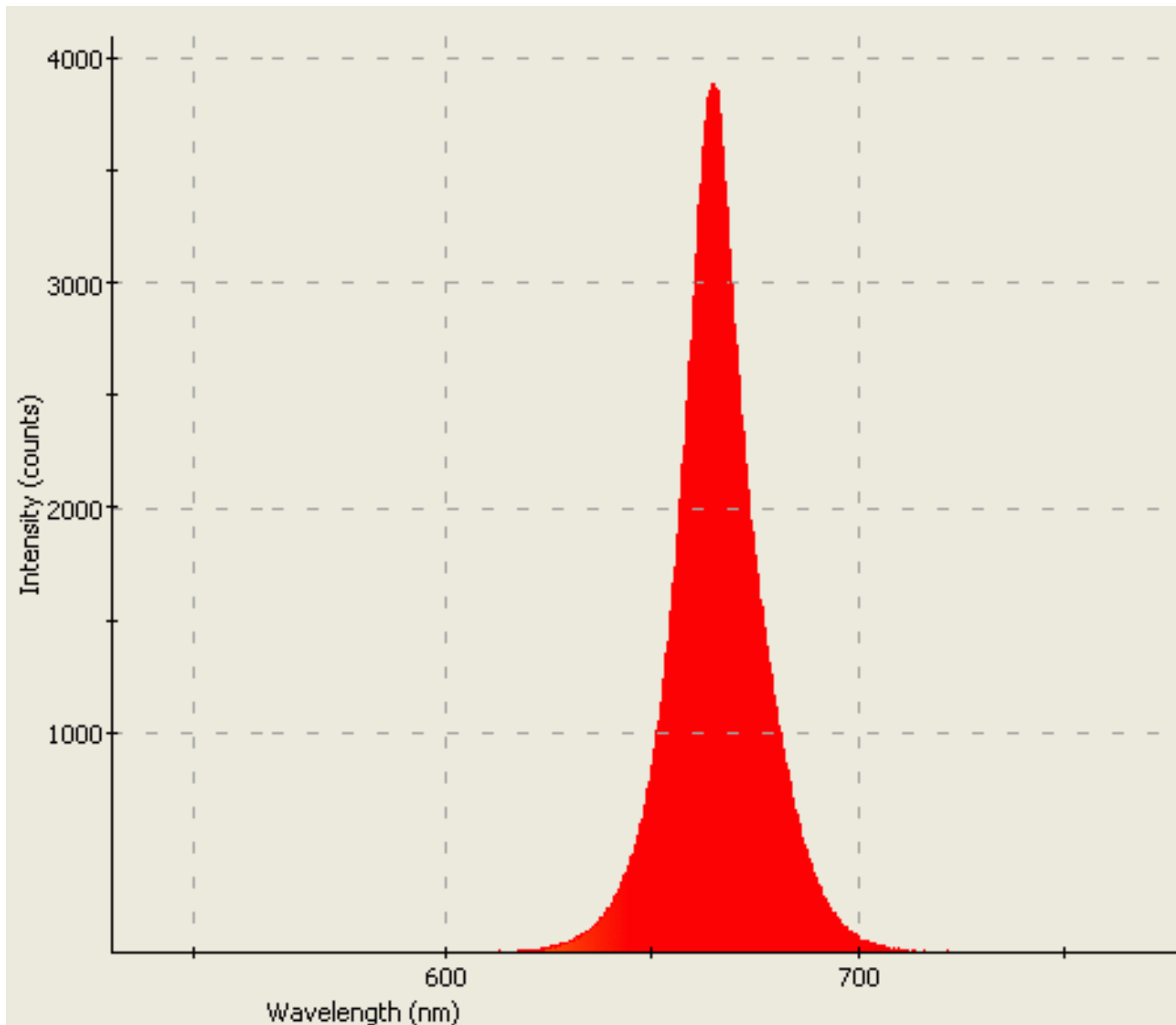
# LED – Light Emitting Diode



**Potência Irradiada:**

$$I_0 \approx k \cdot I_{LED}$$

# Espectro de LED Vermelho



<http://ledmuseum.candlepower.us/specx101.htm>

## Optoeletrônica - Fotoresistor

$$I(x, \lambda) = I_0 e^{-\alpha(\lambda) \cdot x} [W / m^2]$$

$$\alpha \approx 10^6 [m^{-1}]$$

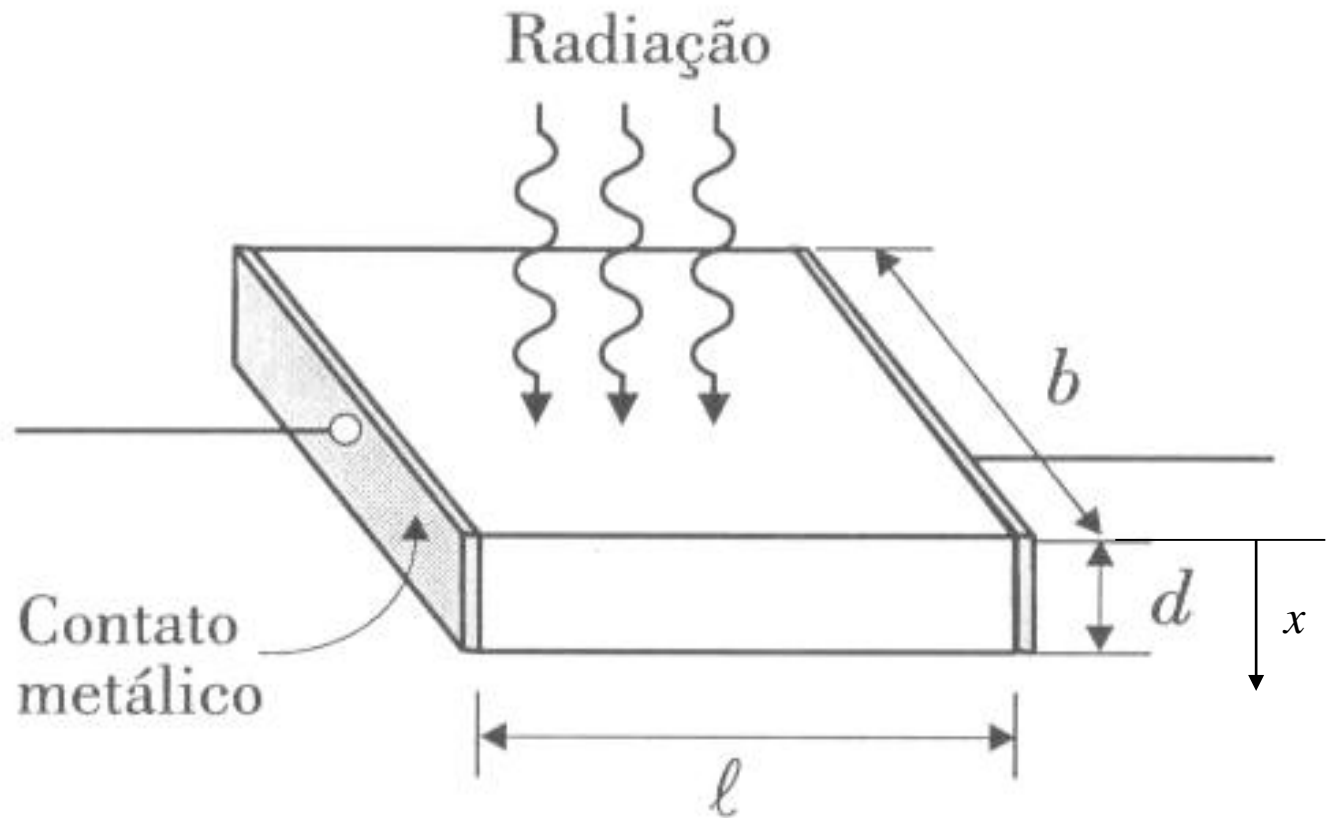


Figura 8.16: Estrutura simples de um foto-resistor, ou LDR.

## Geração de Pares Elétron-Lacuna

$$\frac{\partial \delta p}{\partial t} = \frac{\partial \delta n}{\partial t} = g = \frac{\eta I_0}{\hbar \omega d}$$

$g$  – Taxa de Geração de pares elétron-lacuna [ $\text{m}^{-3}\text{s}^{-1}$ ]

$d$  – Espessura do Semicondutor (Profundidade) [m]

$I_0$  – Radiação Incidente com **ABSORÇÃO UNIFORME** [ $\text{W}/\text{m}^2$ ]

$\eta$  – Eficiência de geração de pares elétron-lacuna

$\omega$  – Frequência Média dos Fótons [ $\text{rad}/\text{s}$ ]

**Semicondutor  
Intrínseco:**

$$n_0 = p_0 = n_i$$

$$\left\{ \begin{array}{l} p = p_0 + \delta p \quad [\text{m}^{-3}] \\ n = n_0 + \delta n \quad [\text{m}^{-3}] \end{array} \right.$$



## Geração e Recombinação de Pares Elétron-Lacuna

$$\left\{ \begin{array}{l} \frac{\partial \delta n}{\partial t} = g - r = \frac{\eta I_0}{\hbar \omega d} - \frac{\delta n}{\tau_r} \\ \frac{\partial \delta p}{\partial t} = g - r = \frac{\eta I_0}{\hbar \omega d} - \frac{\delta p}{\tau_r} \end{array} \right.$$

$\tau_r$  – Tempo de Recombinação [s]

$r$  – Taxa de Recombinação [ $1/\text{m}^3.\text{s}$ ]

**Regime Estacionário:**  $g = r \longrightarrow \frac{\partial}{\partial t} = 0$

**Semicondutor Intrínseco:**  $\delta p = \delta n = g \tau_r = \frac{\eta I_0 \tau_r}{\hbar \omega d}$

## Geração e Recombinação de Pares Elétron-Lacuna

$$\sigma = n.e.\mu_n + p.e.\mu_p = (n_0 + \delta n).e.\mu_n + (p_0 + \delta p).e.\mu_p$$

$\sigma$  – Condutividade [S/m]

$\mu$  – Mobilidades de Elétrons e Lacunas

$$\sigma = n.e.\mu_n + p.e.\mu_p = (n_i + \Delta)e(\mu_n + \mu_p)$$

$$\Delta = \frac{\eta I_0 \tau_r}{\hbar \omega d} = C.I_0$$

$$I_0 \approx k.I_{LED}$$

$$\sigma = (n_i + C.I_0)e(\mu_n + \mu_p)$$

# Concentração Intrínseca vs. Temperatura

$$n_i = p_i = \sqrt{n_i p_i} = (N_c N_v)^{1/2} e^{-E_g/2k_B T}$$

$$n = N_c e^{-(E_c - E_F)/k_B T}$$

$$p = N_v e^{-(E_F - E_v)/k_B T}$$

$$N_c = 2 \left( \frac{m_c^* k_B T}{2\pi \hbar^2} \right)^{3/2}$$

$$N_v = 2 \left( \frac{m_v^* k_B T}{2\pi \hbar^2} \right)^{3/2}$$

**Assumindo Invariante: Temperatura ~ 300 K**

## Corrente vs. Tensão no LDR

$$\sigma = (n_i + C.I_0).e(\mu_n + \mu_p)$$

$$I = G.V \quad \frac{1}{R} = G = \frac{A\sigma}{l} \quad I = \frac{A\sigma}{l} V$$

$$I = \frac{A\sigma}{l} V = \left[ \frac{A}{l} (n_i + C.I_0).e(\mu_n + \mu_p) \right].V$$

$$I = \left[ \frac{A}{l} (n_i + C.k.I_{LED}).e(\mu_n + \mu_p) \right].V$$

$$I_{LDR} = [C_1.I_{LED} + C_2].V_{LDR}$$

## **Desafio: Ganho de Corrente, Tensão e Potência**

$$I_{LDR} = [C_1 \cdot I_{LED} + C_2] \cdot V_{LDR}$$

1) Possível ?  $i_{LDR} > i_{LED}$

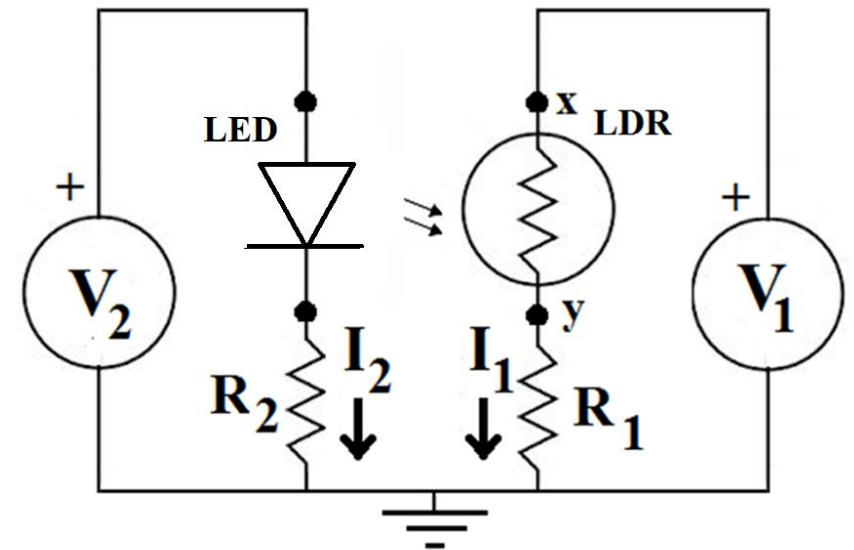
$$G_i = i_{LDR} / i_{LED}$$

2) Possível ?  $v_{LDR} > v_{LED}$

$$G_v = v_{LDR} / v_{LED}$$

3) Possível ?  $i_{LDR} v_{LDR} > i_{LED} v_{LED}$

$$G = (i_{LDR} v_{LDR}) / (i_{LED} v_{LED})$$



**Pequenos sinais em regime permanente senoidal.**