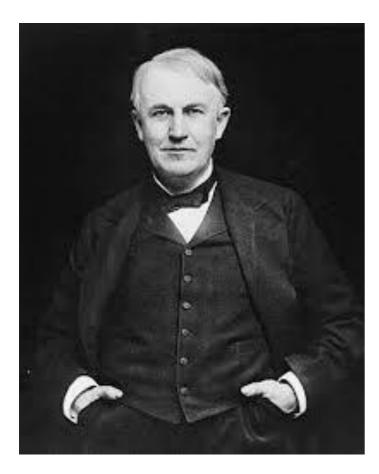
# Materiais Elétricos e Magnéticos para Engenharia

**Professor: Marcus V. Batistuta** 

Laboratório #2 **Lâmpada Elétrica de Filamento** 

1º Semestre de 2018

FGA - Universidade de Brasília



Thomas A. Edison 1847-1931



22 Outubro de 1879

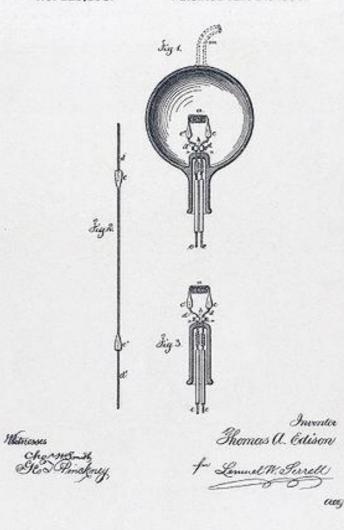




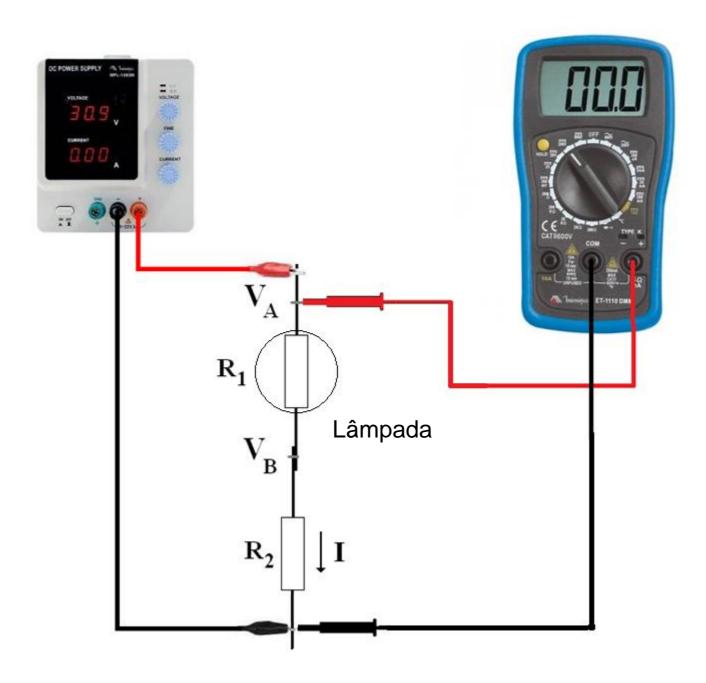
T. A. EDISON. Electric-Lamp.

No. 223,898.

Patented Jan. 27, 1880.



# Circuito de Medidas

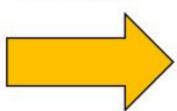


## Lâmpada Elétrica



$$P_E = IV = \frac{V^2}{R(T)} = I^2 R(T)$$





Equilíbrio Térmico (alto-aquecimento)

$$P_E \cong P_R$$

Coeficiente Térmico

$$\alpha_T = \frac{1}{R(T)} \frac{dR}{dT} \bigg|_T$$

## Radiação de Corpo Negro

$$B(\upsilon,T) = \frac{2h\upsilon^3}{c^2} \frac{1}{\frac{h\upsilon}{e^{\frac{h\upsilon}{kT}} - 1}} \left[ \frac{W.sr^{-1}m^{-2}}{Hz} \right]$$

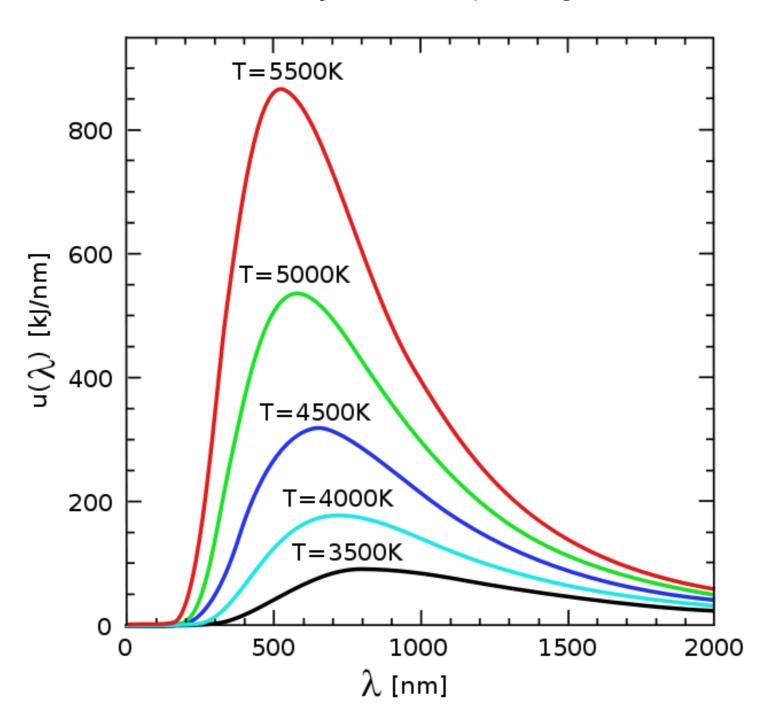
$$E(\lambda,T) = \frac{2hc^2}{\lambda^5} \frac{1}{\frac{hc}{e^{\frac{hc}{\lambda kT}} - 1}} \left[ \frac{W.sr^{-1}.m^{-2}}{m} \right]$$
Lei de Planck

$$P_{\scriptscriptstyle R} = A \, {arepsilon} \sigma T^4$$
 [W] Lei de Stefan-Boltzmann

$$\sigma = 5.67 \times 10-8 \text{ [W m}^{-2} \text{ K}^{-4} \text{]}$$

$$\varepsilon \approx 1$$
 Emissividade

# Radiação de Corpo Negro



### Radiação de Filamento

Ponto de Máximo: 
$$\frac{dB(\lambda,T)}{d\lambda} = 0$$

$$\lambda_{\text{max}} T = 2897,756 \text{ [}\mu\text{m.K]}$$

Temperatura Ideal (Centro da Banda Visível):

$$\lambda_{\text{max}} = \frac{0.7 + 0.4}{2} = 0.55 \text{ [µm]}$$

$$T = \frac{2897,756}{0,55} = 5268,6473$$
 [K]

Ponto de fusão do tungstênio = 3695 K Ponto de Sublimação do Carbono = 3915 K

## Olho Humano

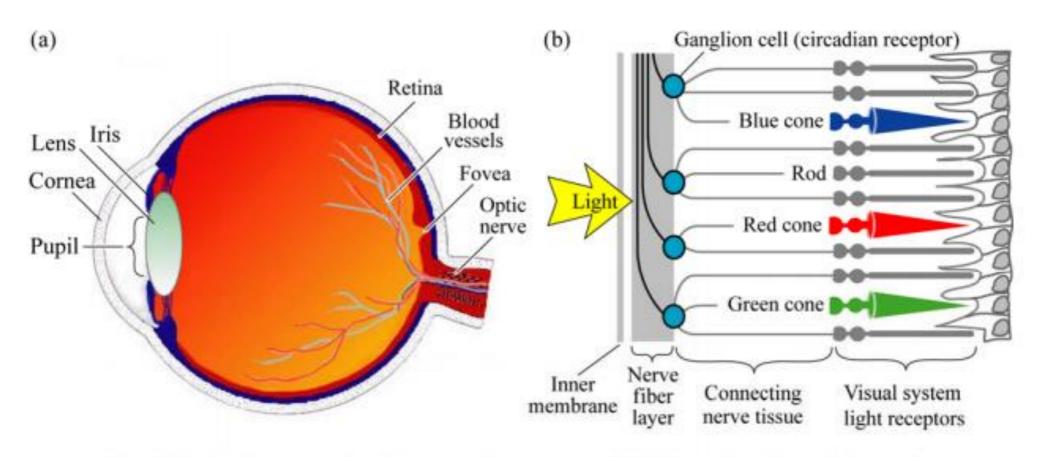
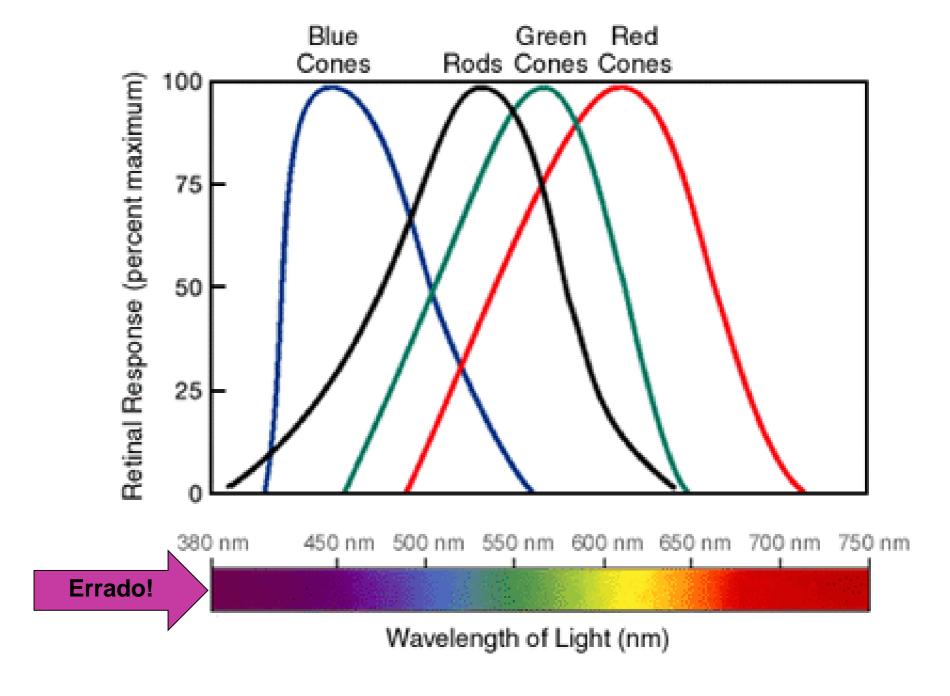


Fig. 16.1. (a) Cross section through a human eye. (b) Schematic view of the retina including rod and cone light receptors (adapted from Encyclopedia Britannica, 1994).

## Sensibilidade da Visão



# Espectro de Sensibilidade do Olho Humano

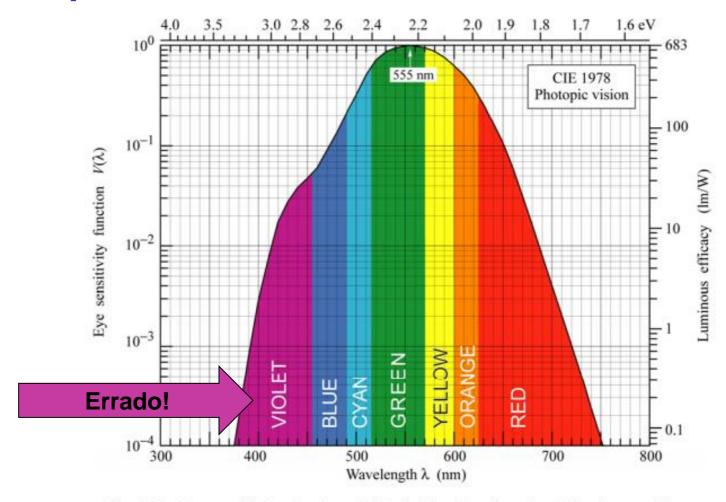
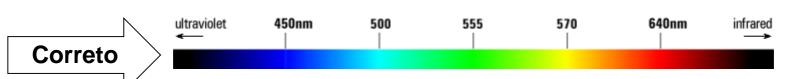
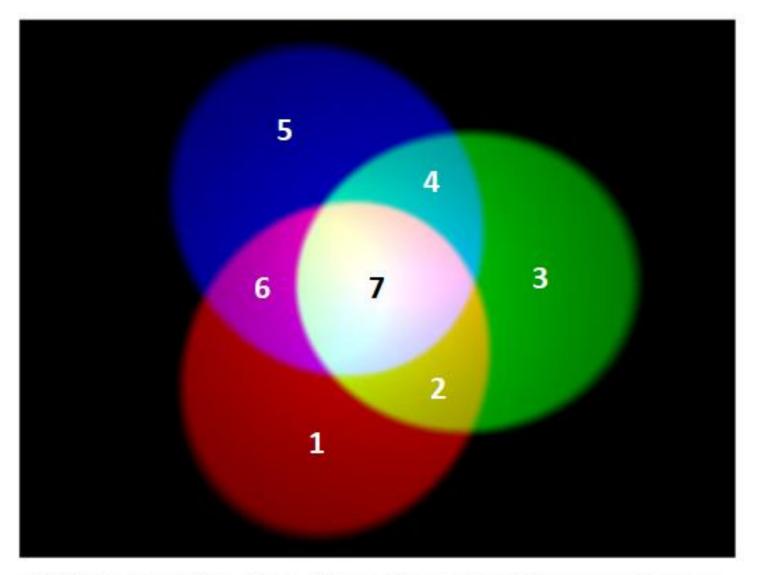


Fig. 16.7. Eye sensitivity function,  $V(\lambda)$ , (left-hand ordinate) and luminous efficacy, measured in lumens per watt of optical power (right-hand ordinate).  $V(\lambda)$  is maximum at 555 nm (after 1978 CIE data).

https://www.ecse.rpi.edu/~schubert/Light-Emitting-Diodes-dot-org/Sample-Chapter.pdf

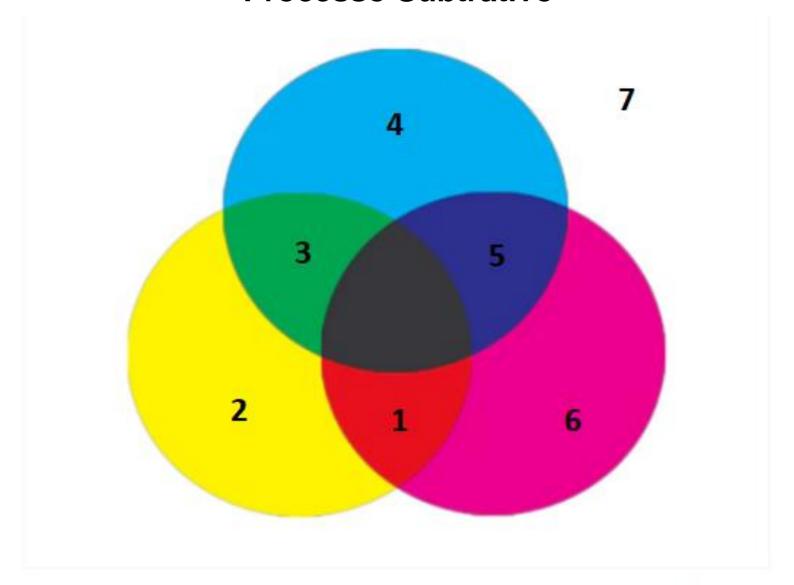


#### **Processo Aditivo**



Additive color mixing. If you (like me) have a hard time wrapping your head around how red and green mix together to make yellow, watch this YouTube video.

#### **Processo Subtrativo**



Subtractive color mixing is pretty close to the paint mixing we did in grade school. This video does a great job visualizing the "subtractive" part of it.

# 7 Cores + Preto (Nenhuma Cor) ou Branco (Todas as Cores) Aditivo Subtrativo

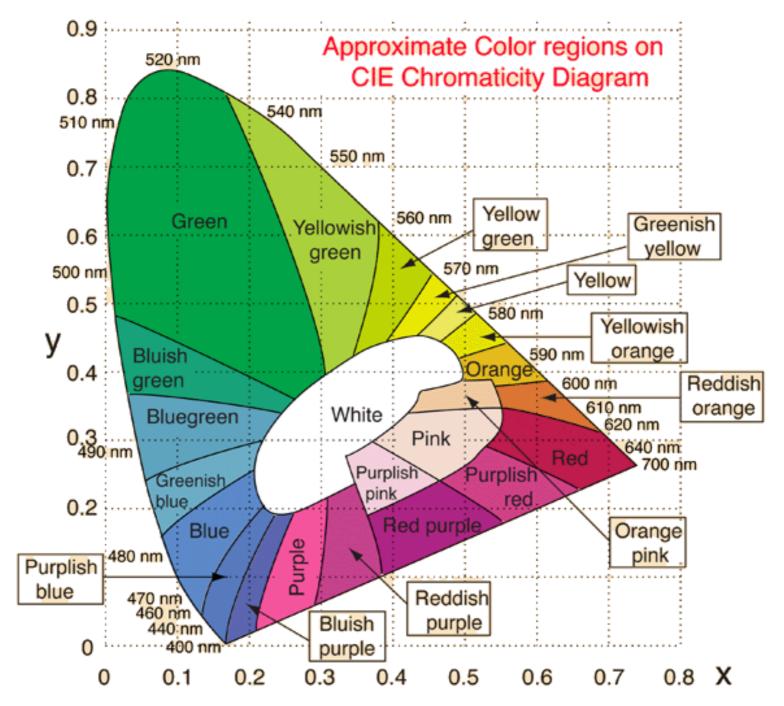
$$N = 3 \Rightarrow R,G,B$$
 (Retina, 1 bit por cor)

Ligado/Desligado

$$2^3 = 8$$

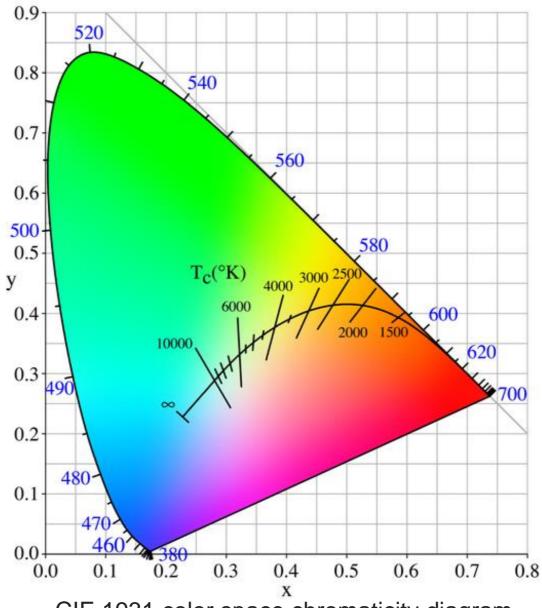
```
Processo Aditivo:
(2 níveis - 0 ou 1)
R G B
  0 0 Preto
  0 0 Vermelho
  1 0 Amarelo
 1 0 Verde
 1 1 Ciano
  0 1 Azul
  0 1 Violeta
  1 1 Branco
```

Não existe na sequência do espectro!



http://hyperphysics.phy-astr.gsu.edu/hbase/vision/cie.html

## Radiação de Corpo Negro



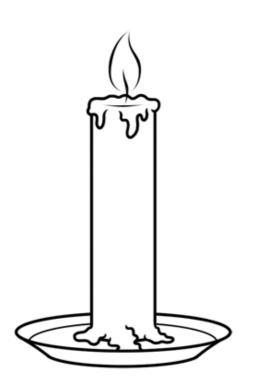
CIE 1931 color space chromaticity diagram

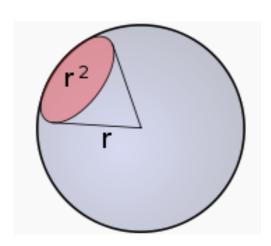
Ponto de fusão do tungstênio = 3695 K Ponto de Sublimação do Carbono = 3915 K

# Candela e Lúmen

A candela é a intensidade luminosa, numa dada direção, de uma fonte que emite uma radiação monocromática de frequência 540 x 10<sup>12</sup> hertz e que tem uma intensidade radiante nessa direção

de  $\frac{1}{683}$  watt por esferorradiano (sr).





1 cd- 1 sr = 1 lm

Isotrópica: 1 candela =  $4\pi$  lúmens

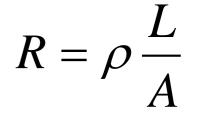
Vela: ~1 candela

Esfera:  $A = 4\pi r^2$ 

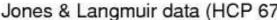
# Eficiência e Eficácia

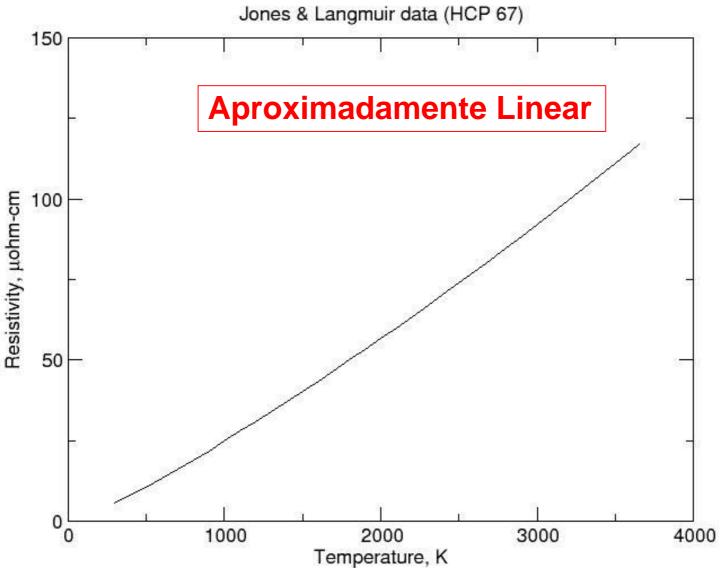
Туре	Overall luminous efficiency	Overall luminous efficacy (lm/W)
40 W tungsten incandescent	1.9%	12.6 <sup>[1]</sup>
60 W tungsten incandescent	2.1%	14.5 <sup>[1]</sup>
100 W tungsten incandescent	2.6%	17.5 <sup>[1]</sup>
glass halogen	2.3%	16
quartz halogen	3.5%	24
photographic and projection lamps with very high filament temperatures and short lifetimes	5.1%	35 <sup>[53]</sup>
ideal black-body radiator at 4000 K (or a class K star like Arcturus)	7.0%	47.5
ideal black-body radiator at 7000 K (or a class F star like Procyon)	14%	95
ideal monochromatic 555 nm (green) source	100%	683 <sup>[54]</sup>

## Resistividade do Tungstênio



## Resistivity of tungsten





# Modelo para a Lâmpada Elétrica

$$V=RI$$
  $R(T)=
ho(T)rac{L}{A}$   $ho(T)\cong K_TT$  Aprox. Linear  $R(T)=K_TTrac{L}{A}=K'_TT$ 

$$P_E = IV = \frac{V^2}{R(T)} = I^2 R(T) = \frac{V^2}{K'_T T} = I^2 K'_T T$$

$$P_E \cong P_R$$
 
$$P_R = A \varepsilon \sigma T^4$$

$$I^{2}K'_{T}T \cong A\varepsilon\sigma T^{4}$$
 
$$\frac{V^{2}}{K'_{T}T} \cong A\varepsilon\sigma T^{4}$$

$$I^2 \cong \frac{A\varepsilon\sigma}{K'_T} T^3$$

$$V^2 \cong K'_T A \varepsilon \sigma T^5$$

$$I \cong \sqrt{\frac{A\varepsilon\sigma}{K'_T}}T^{\frac{3}{2}}$$

$$I \cong \sqrt{\frac{A\varepsilon\sigma}{K'_T}} T^{\frac{3}{2}} \qquad V \cong \sqrt{K'_T A\varepsilon\sigma} T^{\frac{5}{2}}$$

$$I \cong K_I T^{\frac{3}{2}}$$

$$I \cong K_I T^{\frac{3}{2}} \qquad V \cong K_V T^{\frac{5}{2}}$$

Verificando: 
$$R(T) = \frac{V}{I} \cong \frac{K_V T^{\frac{5}{2}}}{K_I T^{\frac{3}{2}}} = K'_T T$$
 Aprox. Linear

$$I \cong K_{I}T^{\frac{3}{2}} \qquad V \cong K_{V}T^{\frac{5}{2}}$$

$$V^{\frac{2}{5}} \cong (K_{V})^{\frac{2}{5}}T \qquad T = \frac{V^{\frac{5}{2}}}{(K_{V})^{\frac{2}{5}}}$$

$$I \cong K_{I} \left( \frac{V^{\frac{2}{5}}}{(K_{V})^{\frac{2}{5}}} \right)^{\frac{3}{2}} \qquad I \cong \left( \frac{K_{I}}{(K_{V})^{\frac{3}{5}}} \right) V^{\frac{3}{5}}$$

$$I \cong KV^{\frac{3}{5}}$$

**Não-linear**