



Recurrent Neural Networks

Amir H. Payberah
payberah@kth.se
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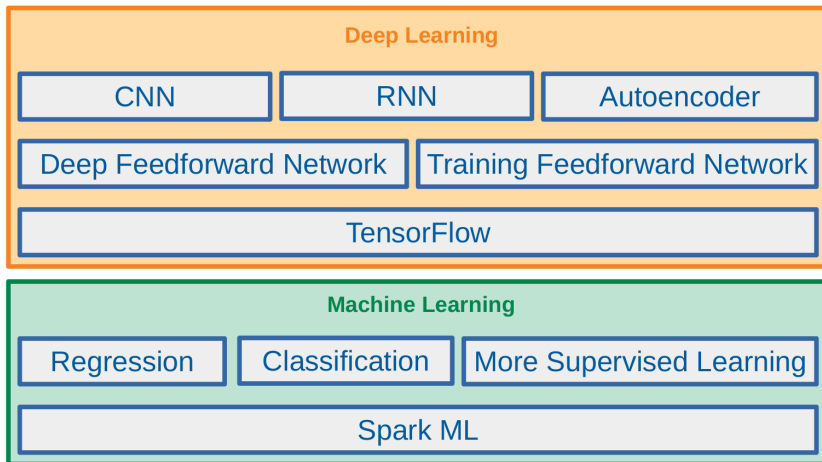




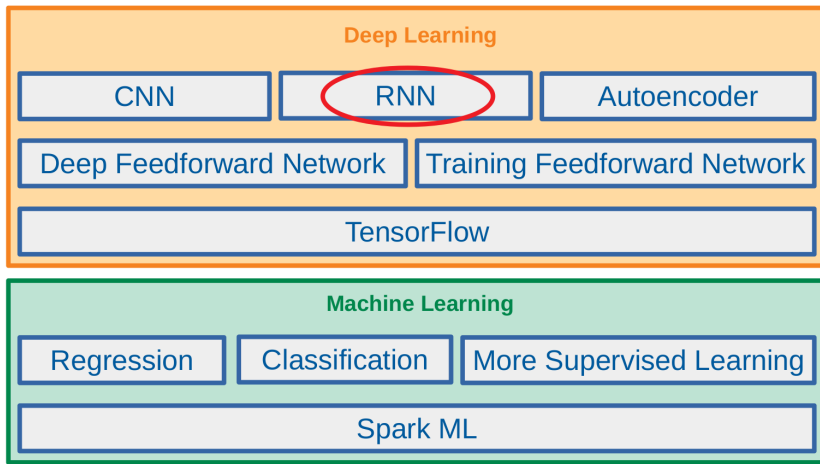
The Course Web Page

<https://id2223kth.github.io>

Where Are We?



Where Are We?



Let's Start With An Example

Google

the students opened their



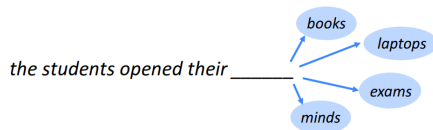
their **work**
their **books**
their **teachers**
their **homework**
their **lecturer**
their **new lecturer**

Feeling Lucky

venska

Language Modeling (1/2)

- **Language modeling** is the task of **predicting** what word comes next.

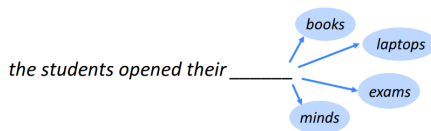


Language Modeling (2/2)

- More formally: given a sequence of words $x^{(1)}, x^{(2)}, \dots, x^{(t)}$, compute the probability distribution of the next word $x^{(t+1)}$:

$$p(x^{(t+1)} = w_j | x^{(t)}, \dots, x^{(1)})$$

- w_j is a word in vocabulary $V = \{w_1, \dots, w_v\}$.



n-gram Language Models

- ▶ the students opened their ___
- ▶ How to learn a Language Model?
- ▶ Learn a n-gram Language Model!
- ▶ A n-gram is a chunk of n consecutive words.
 - Unigrams: "the", "students", "opened", "their"
 - Bigrams: "the students", "students opened", "opened their"
 - Trigrams: "the students opened", "students opened their"
 - 4-grams: "the students opened their"
- ▶ Collect statistics about how frequent different n-grams are, and use these to predict next word.

n-gram Language Models - Example

- ▶ Suppose we are learning a 4-gram Language Model.
 - $x^{(t+1)}$ depends only on the preceding 3 words $\{x^{(t)}, x^{(t-1)}, x^{(t-2)}\}$.

~~as the proctor started the clock, the~~ students opened their _____
 discard condition on this

$$p(w_j | \text{students opened their}) = \frac{\text{students opened their } w_j}{\text{students opened their}}$$

- ▶ In the corpus:
 - "students opened their" occurred 1000 times
 - "students opened their books" occurred 400 times:
 $p(\text{books} | \text{students opened their}) = 0.4$
 - "students opened their exams" occurred 100 times:
 $p(\text{exams} | \text{students opened their}) = 0.1$

Problems with n-gram Language Models - Sparsity

$$p(w_j | \text{students opened their}) = \frac{\text{students opened their } w_j}{\text{students opened their}}$$

- ▶ What if "students opened their w_j " never occurred in data? Then w_j has probability 0!
- ▶ What if "students opened their" never occurred in data? Then we can't calculate probability for any w_j !
- ▶ Increasing n makes sparsity problems worse.
 - Typically we can't have n bigger than 5.



Problems with n-gram Language Models - Storage

$$p(w_j | \text{students opened their}) = \frac{\text{students opened their } w_j}{\text{students opened their}}$$

- ▶ For "students opened their w_j ", we need to store count for all possible 4-grams.
- ▶ The model size is in the order of $O(\exp(n))$.
- ▶ Increasing n makes model size huge.

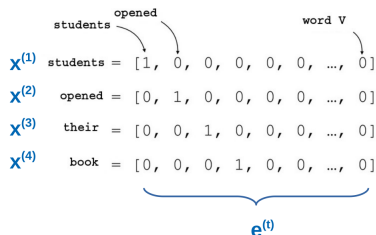
Can We Build a Neural Language Model? (1/3)

► Recall the **Language Modeling** task:

- **Input:** sequence of words $x^{(1)}, x^{(2)}, \dots, x^{(t)}$
- **Output:** probability dist of the next word $p(x^{(t+1)} = w_j | x^{(t)}, \dots, x^{(1)})$

► **One-Hot encoding**

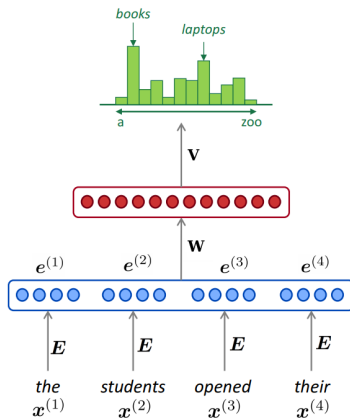
- Represent a **categorical variable** as a **binary vector**.
- All recodes are **zero**, except the index of the integer, which is **one**.
- Each embedded word $e^{(t)} = E^T x^{(t)}$ is a **one-hot vector** of size **vocabulary size**.



Can We Build a Neural Language Model? (2/3)

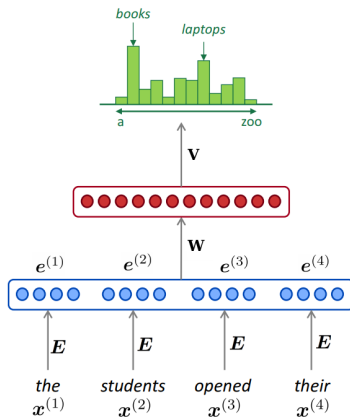
► A MLP model

- **Input:** words $x^{(1)}, x^{(2)}, x^{(3)}, x^{(4)}$
- **Input layer:** one-hot vectors $e^{(1)}, e^{(2)}, e^{(3)}, e^{(4)}$
- **Hidden layer:** $h = f(w^T e)$, f is an activation function.
- **Output:** $\hat{y} = \text{softmax}(v^T h)$



Can We Build a Neural Language Model? (3/3)

- ▶ Improvements over n-gram LM:
 - No sparsity problem
 - Model size is $O(n)$ not $O(\exp(n))$
- ▶ Remaining problems:
 - It is fixed 4 in our example, which is small
 - We need a neural architecture that can process any length input



Recurrent Neural Networks (RNN)

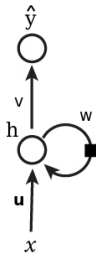


Recurrent Neural Networks (1/4)

- ▶ The idea behind **Recurrent neural networks (RNN)** is to make use of **sequential data**.
 - Until here, we assume that **all inputs (and outputs)** are **independent** of each other.
 - It is a **bad idea** for many tasks, e.g., **predicting the next word in a sentence** (it's better to know which words came before it).
- ▶ They can analyze **time series data** and predict **the future**.
- ▶ They can work on **sequences of arbitrary lengths**, rather than on **fixed-sized inputs**.

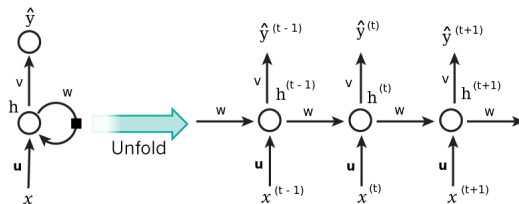
Recurrent Neural Networks (2/4)

- ▶ Neurons in an **RNN** have **connections pointing backward**.
- ▶ RNNs have **memory**, which captures **information** about what **has been calculated so far**.



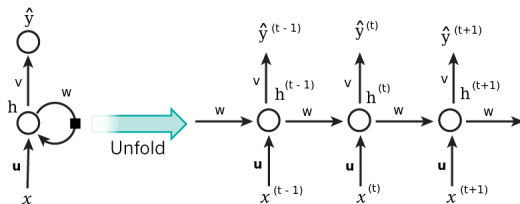
Recurrent Neural Networks (3/4)

- ▶ **Unfolding the network**: represent a network against the time axis.
 - We write out the network for the **complete sequence**.
- ▶ For example, if the sequence we care about is a **sentence of three words**, the network would be **unfolded into a 3-layer** neural network.
 - One layer for **each word**.



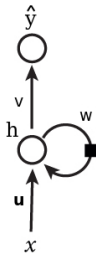
Recurrent Neural Networks (4/4)

- ▶ $h^{(t)} = f(\mathbf{u}^\top \mathbf{x}^{(t)} + \mathbf{w}h^{(t-1)})$, where f is an activation function, e.g., **tanh** or **ReLU**.
- ▶ $\hat{y}^{(t)} = g(\mathbf{v}h^{(t)})$, where g can be the **softmax** function.
- ▶ $\text{cost}(y^{(t)}, \hat{y}^{(t)}) = \text{cross_entropy}(y^{(t)}, \hat{y}^{(t)}) = -\sum y^{(t)} \log \hat{y}^{(t)}$
- ▶ $y^{(t)}$ is the **correct** word at time step t , and $\hat{y}^{(t)}$ is the **prediction**.



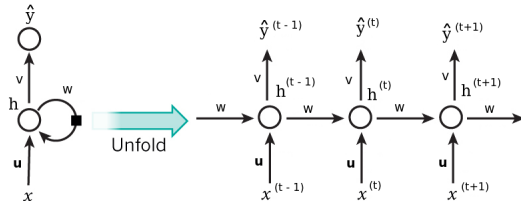
Recurrent Neurons - Weights (1/4)

- ▶ Each recurrent neuron has **three sets of weights**: u , w , and v .



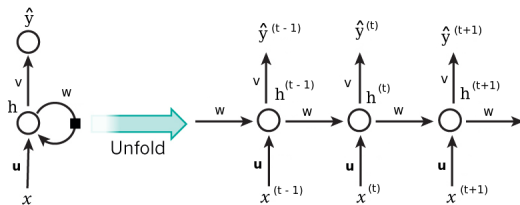
Recurrent Neurons - Weights (2/4)

- ▶ u : the weights for the inputs $x^{(t)}$.
- ▶ $x^{(t)}$: is the input at time step t .
- ▶ For example, $x^{(1)}$ could be a one-hot vector corresponding to the first word of a sentence.



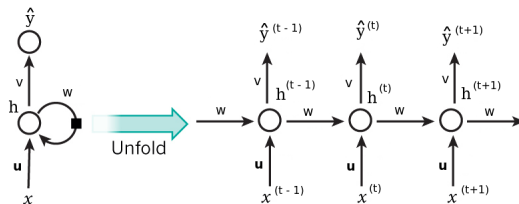
Recurrent Neurons - Weights (3/4)

- ▶ w : the weights for the hidden state of the previous time step $h^{(t-1)}$.
- ▶ $h^{(t)}$: is the hidden state (memory) at time step t .
 - $h^{(t)} = \tanh(u^T x^{(t)} + wh^{(t-1)})$
 - $h^{(0)}$ is the initial hidden state.



Recurrent Neurons - Weights (4/4)

- ▶ v : the weights for the hidden state of the current time step $h^{(t)}$.
- ▶ $\hat{y}^{(t)}$ is the output at step t .
- ▶ $\hat{y}^{(t)} = \text{softmax}(vh^{(t)})$
- ▶ For example, if we wanted to predict the next word in a sentence, it would be a vector of probabilities across our vocabulary.

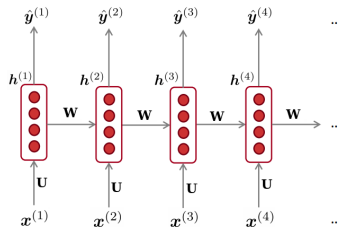
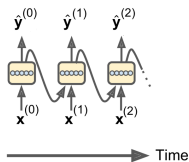
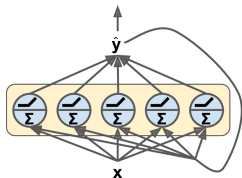


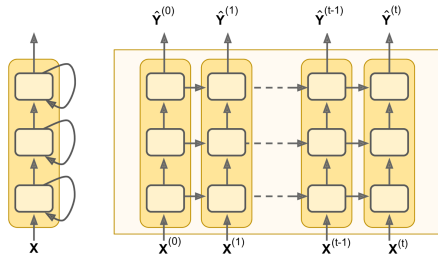
Layers of Recurrent Neurons

- At each time step t , every neuron of a **layer** receives both the **input vector** $\mathbf{x}^{(t)}$ and the **output vector** from the previous time step $\mathbf{h}^{(t-1)}$.

$$\mathbf{h}^{(t)} = \tanh(\mathbf{u}^T \mathbf{x}^{(t)} + \mathbf{w}^T \mathbf{h}^{(t-1)})$$

$$\mathbf{y}^{(t)} = \text{sigmoid}(\mathbf{v}^T \mathbf{h}^{(t)})$$

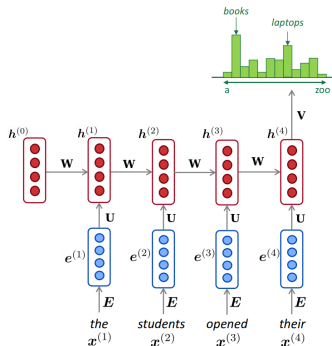
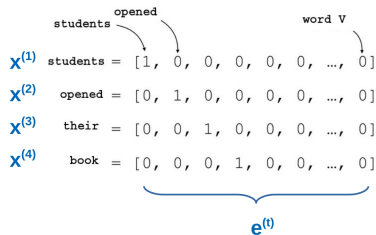




Let's Back to Language Model Example

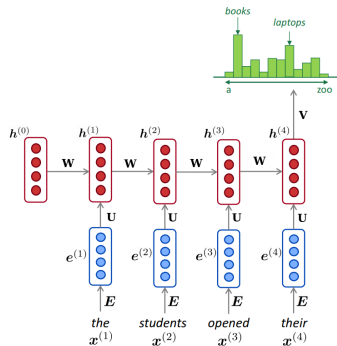
A RNN Neural Language Model (1/2)

- ▶ The input \mathbf{x} will be a **sequence of words** (each $\mathbf{x}^{(t)}$ is a **single word**).
- ▶ Each embedded word $\mathbf{e}^{(t)} = \mathbf{E}^T \mathbf{x}^{(t)}$ is a **one-hot vector** of size **vocabulary size**.

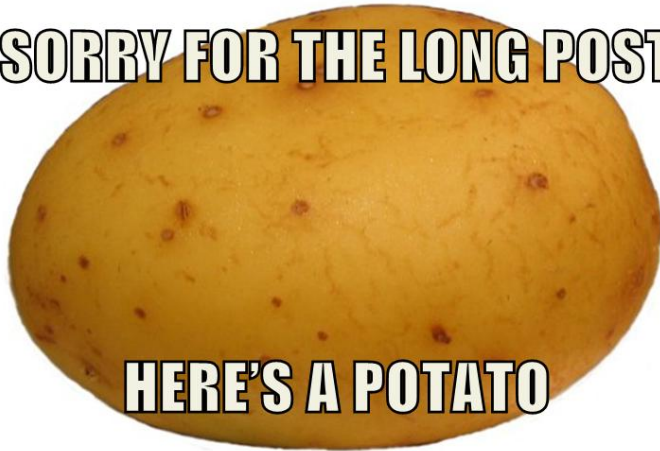


A RNN Neural Language Model (2/2)

- ▶ Let's recap the equations for the RNN:
 - $h^{(t)} = \tanh(u^T e^{(t)} + w h^{(t-1)})$
 - $\hat{y}^{(t)} = \text{softmax}(v h^{(t)})$
- ▶ The output $\hat{y}^{(t)}$ is a vector of **vocabulary size** elements.
- ▶ Each element of $\hat{y}^{(t)}$ represents the **probability** of that word being the **next word** in the sentence.



SORRY FOR THE LONG POST



HERE'S A POTATO

RNN in TensorFlow

RNN in TensorFlow (1/3)

► Manul implementation of an RNN

```
# make the dataset
n_inputs = 3
n_neurons = 5

X0_batch = np.array([[0, 1, 2], [3, 4, 5], [6, 7, 8], [9, 0, 1]]) # t = 0
X1_batch = np.array([[9, 8, 7], [0, 0, 0], [6, 5, 4], [3, 2, 1]]) # t = 1

X0 = tf.placeholder(tf.float32, [None, n_inputs])
X1 = tf.placeholder(tf.float32, [None, n_inputs])

# build the network
Wx = tf.Variable(tf.random_normal(shape=[n_inputs, n_neurons], dtype=tf.float32))
Wh = tf.Variable(tf.random_normal(shape=[n_neurons, n_neurons], dtype=tf.float32))
b = tf.Variable(tf.zeros([1, n_neurons], dtype=tf.float32))

h0 = tf.tanh(tf.matmul(X0, Wx) + b)
h1 = tf.tanh(tf.matmul(h0, Wh) + tf.matmul(X1, Wx) + b)
```


RNN in TensorFlow (2/3)

- Use `dynamic_rnn`

```
n_inputs = 3
n_neurons = 5
n_steps = 2

X_batch = np.array([
    # t = 0      t = 1
    [[0, 1, 2], [9, 8, 7]], # instance 1
    [[3, 4, 5], [0, 0, 0]], # instance 2
    [[6, 7, 8], [6, 5, 4]], # instance 3
    [[9, 0, 1], [3, 2, 1]], # instance 4
])

X = tf.placeholder(tf.float32, [None, n_steps, n_inputs])

# build the network
basic_cell = tf.contrib.rnn.BasicRNNCell(num_units=n_neurons)
outputs, states = tf.nn.dynamic_rnn(basic_cell, X, dtype=tf.float32)
```

► Multi-layer RNN

```
layers = [tf.contrib.rnn.BasicRNNCell(num_units=n_neurons, activation=tf.nn.relu)
          for layer in range(n_layers)]

multi_layer_cell = tf.contrib.rnn.MultiRNNCell(layers)

outputs, states = tf.nn.dynamic_rnn(multi_layer_cell, X, dtype=tf.float32)

states_concat = tf.concat(axis=1, values=states)

logits = tf.layers.dense(states_concat, n_outputs)
```

Training RNNs

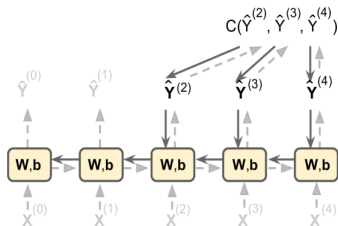


Training RNNs

- ▶ To **train an RNN**, we should **unroll it through time** and then simply use **regular backpropagation**.
- ▶ This strategy is called **backpropagation through time (BPTT)**.

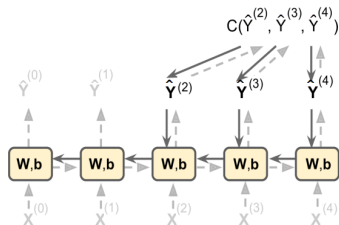
Backpropagation Through Time (1/3)

- ▶ To train the model using **BPTT**, we go through the following steps:
 - ▶ 1. **Forward pass** through the **unrolled network** (represented by the dashed arrows).
 - ▶ 2. The **cost function** is $C(\hat{y}^{t_{\min}}, \hat{y}^{t_{\min}+1}, \dots, \hat{y}^{t_{\max}})$, where t_{\min} and t_{\max} are the first and last output time steps, **not counting the ignored outputs**.



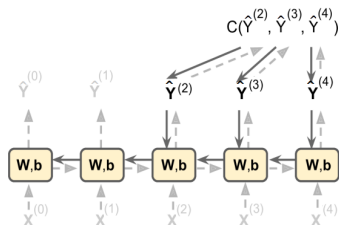
Backpropagation Through Time (2/3)

- ▶ 3. **Propagate backward** the gradients of that cost function through the **unrolled network** (represented by the solid arrows).
- ▶ 4. The **model parameters** are **updated** using the gradients computed during BPTT.

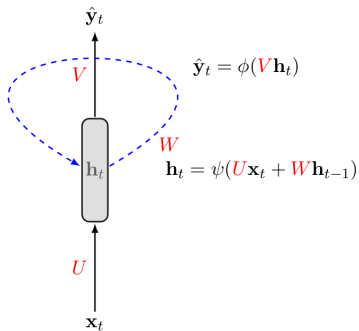


Backpropagation Through Time (3/3)

- ▶ The gradients **flow backward** through **all the outputs** used by the cost function, **not just through the final output**.
- ▶ For example, in the following figure:
 - The **cost function** is computed using the **last three outputs**, $\hat{y}^{(2)}$, $\hat{y}^{(3)}$, and $\hat{y}^{(4)}$.
 - Gradients flow through these three outputs, but **not through** $\hat{y}^{(0)}$ and $\hat{y}^{(1)}$.



BPTT Step by Step (1/20)





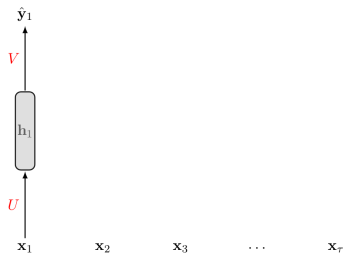
BPTT Step by Step (2/20)

x_1 x_2 x_3 ... x_r

BPTT Step by Step (3/20)

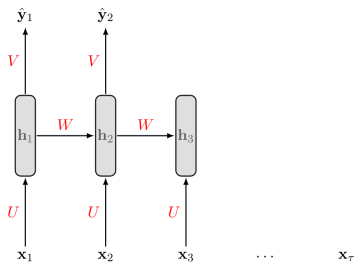


BPTT Step by Step (4/20)

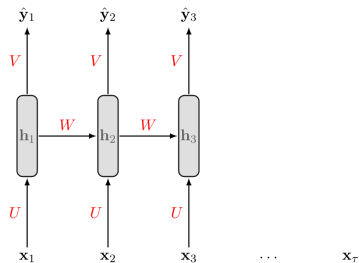




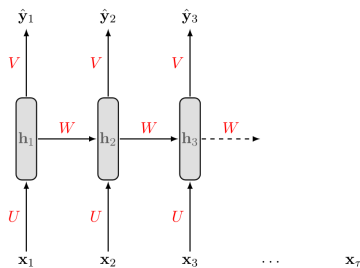
BPTT Step by Step (7/20)



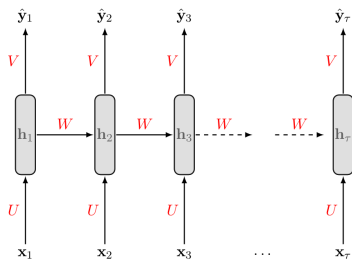
BPTT Step by Step (8/20)



BPTT Step by Step (9/20)

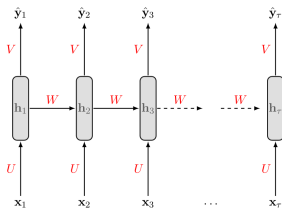


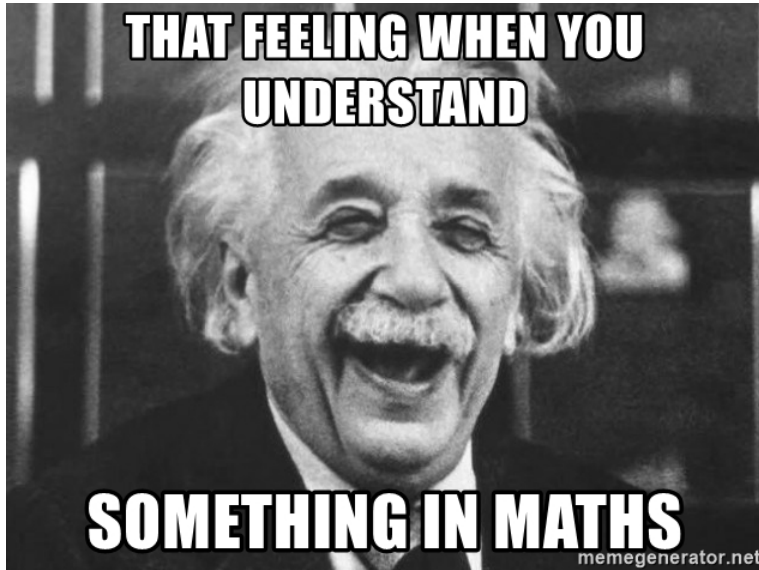
BPTT Step by Step (11/20)



$$\hat{y}^{(t)} = \text{softmax}(z^{(t)})$$

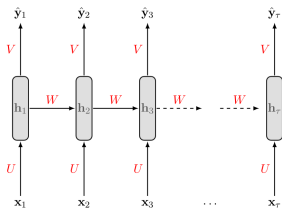
$$J^{(t)} = \text{cross_entropy}(y^{(t)}, \hat{y}^{(t)}) = - \sum y^{(t)} \log \hat{y}^{(t)}$$





$$J^{(t)} = \text{cross_entropy}(y^{(t)}, \hat{y}^{(t)}) = - \sum y^{(t)} \log \hat{y}^{(t)}$$

- ▶ We treat the full sequence as one training example.
- ▶ The total error E is just the sum of the errors at each time step.
- ▶ E.g., $E = J^{(1)} + J^{(2)} + \dots + J^{(t)}$



BPTT Step by Step (14/20)

- ▶ $J^{(t)}$ is the **total cost**, so we can say that a **1-unit increase** in \mathbf{v} , \mathbf{w} or \mathbf{u} will impact each of $J^{(1)}$, $J^{(2)}$, until $J^{(t)}$ individually.
- ▶ The **gradient** is equal to the **sum of the respective gradients** at **each time step t** .
- ▶ For example if $t = 3$ we have: $E = J^{(1)} + J^{(2)} + J^{(3)}$

$$\frac{\partial E}{\partial \mathbf{v}} = \sum_t \frac{\partial J^{(t)}}{\partial \mathbf{v}} = \frac{\partial J^{(3)}}{\partial \mathbf{v}} + \frac{\partial J^{(2)}}{\partial \mathbf{v}} + \frac{\partial J^{(1)}}{\partial \mathbf{v}}$$

$$\frac{\partial E}{\partial \mathbf{w}} = \sum_t \frac{\partial J^{(t)}}{\partial \mathbf{w}} = \frac{\partial J^{(3)}}{\partial \mathbf{w}} + \frac{\partial J^{(2)}}{\partial \mathbf{w}} + \frac{\partial J^{(1)}}{\partial \mathbf{w}}$$

$$\frac{\partial E}{\partial \mathbf{u}} = \sum_t \frac{\partial J^{(t)}}{\partial \mathbf{u}} = \frac{\partial J^{(3)}}{\partial \mathbf{u}} + \frac{\partial J^{(2)}}{\partial \mathbf{u}} + \frac{\partial J^{(1)}}{\partial \mathbf{u}}$$

BPTT Step by Step (15/20)

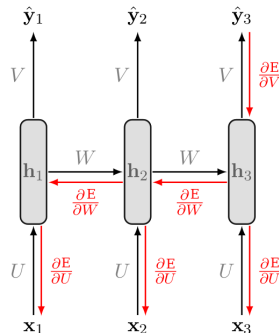
- ▶ Let's start with $\frac{\partial E}{\partial v}$.
- ▶ A change in v will only **impact** $J^{(3)}$ at time $t = 3$, because it plays no role in computing the value of anything other than $z^{(3)}$.

$$\frac{\partial E}{\partial v} = \sum_t \frac{\partial J^{(t)}}{\partial v} = \frac{\partial J^{(3)}}{\partial v} + \frac{\partial J^{(2)}}{\partial v} + \frac{\partial J^{(1)}}{\partial v}$$

$$\frac{\partial J^{(3)}}{\partial v} = \frac{\partial J^{(3)}}{\partial \hat{y}^{(3)}} \frac{\partial \hat{y}^{(3)}}{\partial z^{(3)}} \frac{\partial z^{(3)}}{\partial v}$$

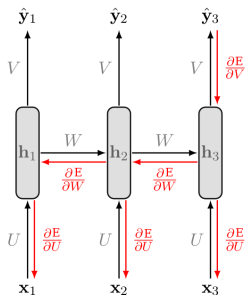
$$\frac{\partial J^{(2)}}{\partial v} = \frac{\partial J^{(2)}}{\partial \hat{y}^{(2)}} \frac{\partial \hat{y}^{(2)}}{\partial z^{(2)}} \frac{\partial z^{(2)}}{\partial v}$$

$$\frac{\partial J^{(1)}}{\partial v} = \frac{\partial J^{(1)}}{\partial \hat{y}^{(1)}} \frac{\partial \hat{y}^{(1)}}{\partial z^{(1)}} \frac{\partial z^{(1)}}{\partial v}$$



BPTT Step by Step (16/20)

- ▶ Let's compute the derivatives of $\frac{\partial J}{\partial \mathbf{w}}$ and $\frac{\partial J}{\partial \mathbf{u}}$, which are **computed the same**.
- ▶ A change in \mathbf{w} at $t = 3$ will impact our cost J in 3 separate ways:
 1. When computing the value of $\mathbf{h}^{(1)}$.
 2. When computing the value of $\mathbf{h}^{(2)}$, which depends on $\mathbf{h}^{(1)}$.
 3. When computing the value of $\mathbf{h}^{(3)}$, which depends on $\mathbf{h}^{(2)}$, which depends on $\mathbf{h}^{(1)}$.

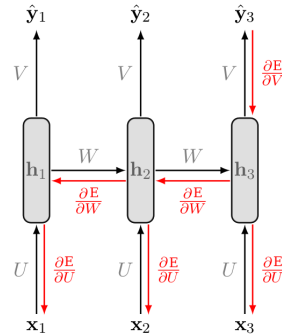


BPTT Step by Step (17/20)

- we compute our individual gradients as:

$$\sum_t \frac{\partial J^{(t)}}{\partial \mathbf{w}} = \frac{\partial J^{(3)}}{\partial \mathbf{w}} + \frac{\partial J^{(2)}}{\partial \mathbf{w}} + \frac{\partial J^{(1)}}{\partial \mathbf{w}}$$

$$\frac{\partial J^{(1)}}{\partial \mathbf{w}} = \frac{\partial J^{(1)}}{\partial \hat{\mathbf{y}}^{(1)}} \frac{\partial \hat{\mathbf{y}}^{(1)}}{\partial \mathbf{z}^{(1)}} \frac{\partial \mathbf{z}^{(1)}}{\partial \mathbf{h}^{(1)}} \frac{\partial \mathbf{h}^{(1)}}{\partial \mathbf{s}^{(1)}} \frac{\partial \mathbf{s}^{(1)}}{\partial \mathbf{w}}$$



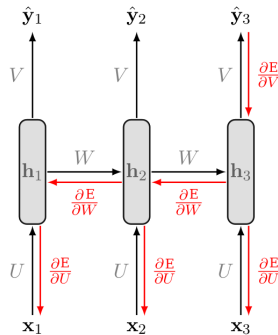
BPTT Step by Step (18/20)

- we compute our individual gradients as:

$$\sum_t \frac{\partial J^{(t)}}{\partial \mathbf{w}} = \frac{\partial J^{(3)}}{\partial \mathbf{w}} + \frac{\partial J^{(2)}}{\partial \mathbf{w}} + \frac{\partial J^{(1)}}{\partial \mathbf{w}}$$

$$\frac{\partial J^{(2)}}{\partial \mathbf{w}} = \frac{\partial J^{(2)}}{\partial \hat{\mathbf{y}}^{(2)}} \frac{\partial \hat{\mathbf{y}}^{(2)}}{\partial \mathbf{z}^{(2)}} \frac{\partial \mathbf{z}^{(2)}}{\partial \mathbf{h}^{(2)}} \frac{\partial \mathbf{h}^{(2)}}{\partial \mathbf{s}^{(2)}} \frac{\partial \mathbf{s}^{(2)}}{\partial \mathbf{w}} +$$

$$\frac{\partial J^{(2)}}{\partial \hat{\mathbf{y}}^{(2)}} \frac{\partial \hat{\mathbf{y}}^{(2)}}{\partial \mathbf{z}^{(2)}} \frac{\partial \mathbf{z}^{(2)}}{\partial \mathbf{h}^{(2)}} \frac{\partial \mathbf{h}^{(2)}}{\partial \mathbf{s}^{(2)}} \frac{\partial \mathbf{s}^{(2)}}{\partial \mathbf{h}^{(1)}} \frac{\partial \mathbf{h}^{(1)}}{\partial \mathbf{s}^{(1)}} \frac{\partial \mathbf{s}^{(1)}}{\partial \mathbf{w}}$$



BPTT Step by Step (19/20)

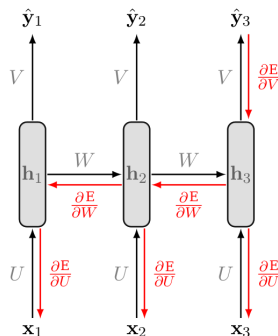
- we compute our individual gradients as:

$$\sum_t \frac{\partial J^{(t)}}{\partial \mathbf{w}} = \frac{\partial J^{(3)}}{\partial \mathbf{w}} + \frac{\partial J^{(2)}}{\partial \mathbf{w}} + \frac{\partial J^{(1)}}{\partial \mathbf{w}}$$

$$\frac{\partial J^{(3)}}{\partial \mathbf{w}} = \frac{\partial J^{(3)}}{\partial \hat{\mathbf{y}}^{(3)}} \frac{\partial \hat{\mathbf{y}}^{(3)}}{\partial \mathbf{z}^{(3)}} \frac{\partial \mathbf{z}^{(3)}}{\partial \mathbf{h}^{(3)}} \frac{\partial \mathbf{h}^{(3)}}{\partial \mathbf{s}^{(3)}} \frac{\partial \mathbf{s}^{(3)}}{\partial \mathbf{w}} +$$

$$\frac{\partial J^{(3)}}{\partial \hat{\mathbf{y}}^{(3)}} \frac{\partial \hat{\mathbf{y}}^{(3)}}{\partial \mathbf{z}^{(3)}} \frac{\partial \mathbf{z}^{(3)}}{\partial \mathbf{h}^{(3)}} \frac{\partial \mathbf{h}^{(3)}}{\partial \mathbf{s}^{(3)}} \frac{\partial \mathbf{s}^{(3)}}{\partial \mathbf{h}^{(2)}} \frac{\partial \mathbf{h}^{(2)}}{\partial \mathbf{s}^{(2)}} \frac{\partial \mathbf{s}^{(t)}}{\partial \mathbf{w}} +$$

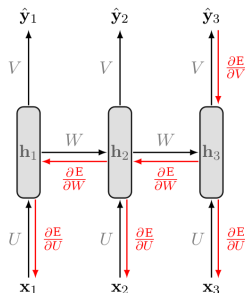
$$\frac{\partial J^{(3)}}{\partial \hat{\mathbf{y}}^{(3)}} \frac{\partial \hat{\mathbf{y}}^{(3)}}{\partial \mathbf{z}^{(3)}} \frac{\partial \mathbf{z}^{(3)}}{\partial \mathbf{h}^{(3)}} \frac{\partial \mathbf{h}^{(3)}}{\partial \mathbf{s}^{(3)}} \frac{\partial \mathbf{s}^{(3)}}{\partial \mathbf{h}^{(2)}} \frac{\partial \mathbf{h}^{(2)}}{\partial \mathbf{s}^{(2)}} \frac{\partial \mathbf{s}^{(2)}}{\partial \mathbf{h}^{(1)}} \frac{\partial \mathbf{h}^{(1)}}{\partial \mathbf{s}^{(1)}} \frac{\partial \mathbf{s}^{(1)}}{\partial \mathbf{w}}$$



BPTT Step by Step (20/20)

- More generally, a change in \mathbf{w} will impact our cost $J^{(t)}$ on t separate occasions.

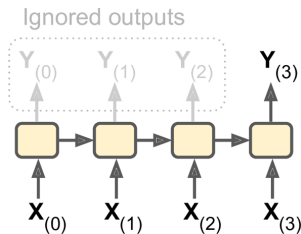
$$\frac{\partial J^{(t)}}{\partial \mathbf{w}} = \sum_{k=1}^t \frac{\partial J^{(t)}}{\partial \hat{\mathbf{y}}^{(t)}} \frac{\partial \hat{\mathbf{y}}^{(t)}}{\partial \mathbf{z}^{(t)}} \frac{\partial \mathbf{z}^{(t)}}{\partial \mathbf{h}^{(t)}} \left(\prod_{j=k+1}^t \frac{\partial \mathbf{h}^{(j)}}{\partial \mathbf{s}^{(j)}} \frac{\partial \mathbf{s}^{(j)}}{\partial \mathbf{h}^{(j-1)}} \right) \frac{\partial \mathbf{h}^{(k)}}{\partial \mathbf{s}^{(k)}} \frac{\partial \mathbf{s}^{(k)}}{\partial \mathbf{w}}$$



RNN Design Patterns

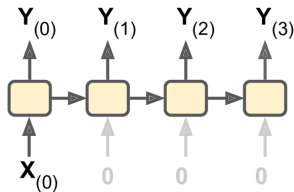
RNN Design Patterns - Sequence-to-Vector

- ▶ **Sequence-to-vector** network: takes a **sequence of inputs**, and ignore all outputs except for **the last one**.
- ▶ E.g., you could feed the network a **sequence of words** corresponding to a movie review, and the network would output a **sentiment score**.



RNN Design Patterns - Vector-to-Sequence

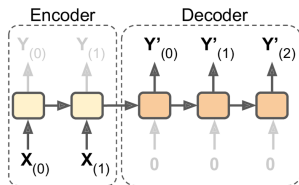
- ▶ **Vector-to-sequence** network: takes a **single input** at the first time step, and let it **output a sequence**.
- ▶ E.g., the input could be an **image**, and the output could be a **caption for that image**.



-

RNN Design Patterns - Encoder-Decoder

- ▶ **Encoder-decoder** network: a **sequence-to-vector** network (**encoder**), followed by a **vector-to-sequence** network (**decoder**).
- ▶ E.g., **translating** a sentence from one language to another.
- ▶ You would feed the network **a sentence in one language**, the encoder would convert this sentence into a **single vector representation**, and then the decoder would decode this vector into a sentence in another language.



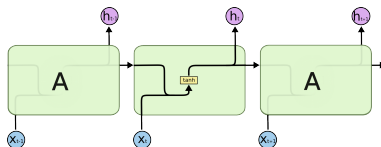
LSTM

RNN Problems

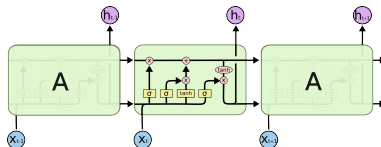
- ▶ Sometimes we only need to look at **recent information** to perform the present task.
 - E.g., **predicting the next word** based on the previous ones.
- ▶ In such cases, where the **gap between the relevant information and the place that it's needed** is **small**, RNNs can learn to use the past information.
- ▶ But, as that **gap grows**, RNNs become **unable to learn** to connect the information.
- ▶ RNNs may suffer from the **vanishing/exploding gradients problem**.
- ▶ To solve these problem, **long short-term memory (LSTM)** have been introduced.
- ▶ In LSTM, the network can learn **what to store** and **what to throw away**.

RNN Basic Cell vs. LSTM

- ▶ Without looking inside the box, the **LSTM** cell looks exactly like a **basic cell**.
- ▶ The repeating module in a **standard RNN** contains a **single layer**.

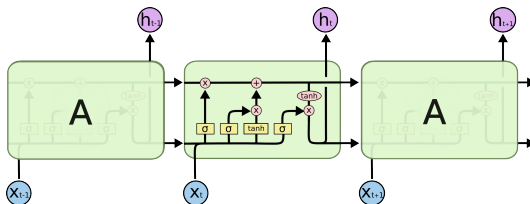


- ▶ The repeating module in an **LSTM** contains **four interacting layers**.

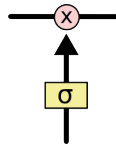


LSTM (1/2)

- In LSTM **state** is split in **two vectors**:
1. $h^{(t)}$ (**h** stands for **hidden**): the **short-term** state
 2. $c^{(t)}$ (**c** stands for **cell**): the **long-term** state



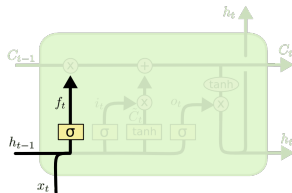
-
- The diagram illustrates the internal structure of an LSTM cell. It shows the flow of information through various gates and the cell state. The inputs are x_t and the hidden state from the previous time step h_{t-1} . The cell state from the previous time step C_{t-1} is also shown. The cell state is updated by adding the output of the cell input gate (i_t) and multiplying the previous cell state by the output of the forget gate (f_t). The output gate (o_t) produces the final hidden state h_t by applying a \tanh activation to the cell state.



Step-by-Step LSTM Walk Through (1/4)

- ▶ **Step one:** decides **what information** we are going to **throw away** from the **cell state**.
- ▶ This decision is made by a **sigmoid layer**, called the **forget gate** layer.
- ▶ It looks at $\mathbf{h}^{(t-1)}$ and $\mathbf{x}^{(t)}$, and outputs a number between 0 and 1 for each number in the cell state $\mathbf{c}^{(t-1)}$.
 - 1 represents **completely keep this**, and 0 represents **completely get rid of this**.

$$f^{(t)} = \sigma(\mathbf{u}_f^T \mathbf{x}^{(t)} + \mathbf{w}_f \mathbf{h}^{(t-1)})$$

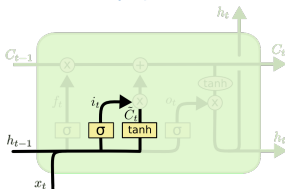


Step-by-Step LSTM Walk Through (2/4)

- ▶ **Second step:** decides **what new information** we are going to **store** in the **cell state**. This has two parts:
 - ▶ 1. A **sigmoid layer**, called the **input gate** layer, decides **which values** we will update.
 - ▶ 2. A **tanh layer** creates a vector of **new candidate values** that could be added to the state.

$$i_t = \sigma(\mathbf{u}_i^T \mathbf{x}^{(t)} + \mathbf{w}_i \mathbf{h}^{(t-1)})$$

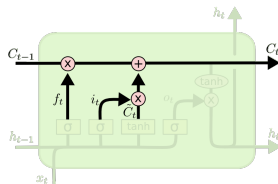
$$\tilde{c}_t = \tanh(\mathbf{u}_c^T \mathbf{x}^{(t)} + \mathbf{w}_c \mathbf{h}^{(t-1)})$$



Step-by-Step LSTM Walk Through (3/4)

- ▶ **Third step:** updates the old cell state $c^{(t-1)}$, into the new cell state $c^{(t)}$.
- ▶ We multiply the old state by $f^{(t)}$, forgetting the things we decided to forget earlier.
- ▶ Then we add it $i^{(t)} \otimes \tilde{c}^{(t)}$.
- ▶ This is the new candidate values, scaled by how much we decided to update each state value.

$$c^{(t)} = f^{(t)} \otimes c^{(t-1)} + i^{(t)} \otimes \tilde{c}^{(t)}$$

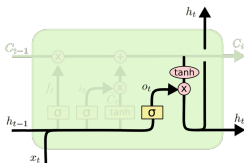


Step-by-Step LSTM Walk Through (4/4)

- **Fourth step:** decides about the **output**.
- First, runs a **sigmoid layer** that decides **what parts of the cell state** we are going to **output**.
- Then, puts the cell state through **tanh** and multiplies it by the output of the **sigmoid gate (output gate)**, so that it **only outputs the parts it decided to**.

$$o^{(t)} = \sigma(\mathbf{u}_o^T \mathbf{x}^{(t)} + \mathbf{w}_o \mathbf{h}^{(t-1)})$$

$$\hat{\mathbf{y}}^{(t)} = \mathbf{h}^{(t)} = o^{(t)} \otimes \tanh(\mathbf{c}^{(t)})$$





LSTM in TensorFlow

► Multi-layer LSTM

```
lstm_cells = [tf.contrib.rnn.BasicLSTMCell(num_units=n_neurons) for layer in range(n_layers)]  
multi_cell = tf.contrib.rnn.MultiRNNCell(lstm_cells)  
  
outputs, states = tf.nn.dynamic_rnn(multi_cell, X, dtype=tf.float32)  
  
top_layer_h_state = states[-1][1]  
  
logits = tf.layers.dense(top_layer_h_state, n_outputs)
```

Summary



Summary

- ▶ RNN
- ▶ Unfolding the network
- ▶ Three weights
- ▶ Backpropagation through time
- ▶ RNN design patterns
- ▶ LSTM



Reference

- ▶ Ian Goodfellow et al., Deep Learning (Ch. 10)
- ▶ Aurélien Géron, Hands-On Machine Learning (Ch. 14)
- ▶ Understanding LSTM Networks
<http://colah.github.io/posts/2015-08-Understanding-LSTMs>
- ▶ CS224d: Deep Learning for Natural Language Processing
<http://cs224d.stanford.edu>

Questions?