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**Binary Search**

```
// return index number or -1
int binarySearch (vector<int> &nums,
int target) {
    int low = 0, high = nums.size() - 1,
    mid;
    while (low <= high)
    {
        mid = (high + low) >> 1;
        if (nums[mid] == target)
        {
            return mid;
        }
        else if (nums[mid] < target)
        {
            low = mid + 1;
        }
        else
        {
            high = mid - 1;
        }
    }
    return -1; // return high;
}
```

```
// binary search in a rotated sorted
array(vector<int>)
bool searchInARotatedSortedArray
```

```
(vector<int>&A, int key) {
    int l=0, h=A.size()-1, m;
    while (l<=h)
    {
        m = (l+h)>>1;
        if(A[m]==key){
            return true;
        }if(A[m]==A[l] &&
A[m]==A[h]){
            ++l,--h;
            continue;
        }else if(A[l] <= A[m]){
            if(A[l]<=key && key<=A[m]){
                h = m-1;
            }else{
                l = m+1;
            }
        }else{
            if(A[m]<=key &&
key<=A[h]){
                l = m+1;
            }else{
                h = m-1;
            }
        }
    }
    return false;
}
```

```
// NthRoot(2.0, 25.0)
double midPowerOfN (double mid, int
n, double m)
{
    double ans = 1.0;
    for (int i = 1; i <= n; ++i)
    {
        ans *= mid;
        if (ans > m)
            return 2.0;
    }
}
```

```

    }
    if (fabs(ans - m) < 1e-9)
        return 1.0;
    return 0.0;
}
double NthRoot (int n, double m)
{
    double l = 0.0, h = m, mid;
    double tolerance = 1e-9;
    double closest = -1.0;
    // while (h - l > tolerance)
    // for safety 100 is good
    for (int i = 0; i <= 100; ++i)
    {
        mid = (l + h) / 2.0;
        double ans = midPowerOfN(mid,
n, m);
        if (ans == 1.0)
        {
            return mid;
        }
        else if (ans == 0.0)
        {
            l = mid;
        }
        else
        {
            h = mid;
            closest = mid;
        }
    }
    return closest;
}
```

```
// Binary Exponentiation
int mod = 1e9+7;
int binaryExponentiation (int base,
int power){
    int carry = 1%mod;
    int x = base%mod;
    while(power){
        if(power&1) carry = (__int128_t)
(carry*x)%mod;
        x = (__int128_t) (x*x)%mod;
        power = power>>1;
    }
    return carry%mod;
}
```

```
// sum of digit
int sumOfDigit (int num){
    ll sum = 0;
    while(num>0){
        sum += num%10;
        num/=10;
    }
    return sum;
}
```

```
//divisors for a number
vector<int> divisorsForSingleValue
(int n){
    int i;
    vector<int> v1;
    for(i=1; i*i<=n; ++i){
        if(n%i==0){

```

```
            v1.push_back(i);
            v1.push_back(n/i);
        }
    }
    return v1;
}
```

```
// number of combination
int nCr(int n, int r)
{
    int i, ans = 1;
    for (i = 2; i <= n; ++i)
    {
        ans *= i;
        if (i <= r || i <= (n - r))
            ans /= i;
    }
    if (r < (n - r))
    {
        for (i = 2; i <= r; ++i)
        {
            ans /= i;
        }
    }
    else
    {
        for (i = 2; i <= n - r; ++i)
        {
            ans /= i;
        }
    }
    return ans;
}
```

```
// number of permutation
int nPr (int n, int r)
{
    int i, ans = 1;
    for (i = (n - r) + 1; i <= n; ++i)
    {
        ans *= i;
    }
    return ans;
}
```

```
// Prime factorization impl
void primeFactorization (int n,
map<int, int> &m1)
{
    for (int i = 2; i * i <= n; ++i)
    {
        while (n % i == 0)
        {
            m1[i]++;
            n /= i;
        }
    }
    if (n > 1)
        m1[n]++;
}
```

```
// Sieve Prime (n log log n)
const int N = 1e6 + 9;
bool isPrime[N];
vector<int> primeNumbers;
void sieve()
{
    int i, j;
    isPrime[0] = isPrime[1] = true;
    for (i = 2; i < N; ++i)
    {
        if (!isPrime[i])
        {
            primeNumbers.push_back(i);
            for (j = i * i; j < N; j += i)
            {
                isPrime[j] = true;
            }
        }
    }
}

// sum of divisors of a number
const int N = 1e5;
vector<ll> primeNumbers;
vector<bool> isPrime(N+1, 0);
const int mod = 1e9+7;
// bigmod function
ll bigmod(ll n, ll k){
    if(k==0) return 1LL;
    ll x = bigmod(n, k/2)%mod;
    x = (x*x)%mod;
    if(k%2==1) x = (x*n)%mod;
    return x;
}
// Sieve Prime
void sieve(){
    isPrime[0] = isPrime[1] = true;
    for(ll i=2; i<N; ++i){
        if(!isPrime[i]){
            primeNumbers.push_back(i);
            for(ll j=i*i; j<N; j+=i){
                isPrime[j] = true;
            }
        }
    }
}
// sum of divisor of a number
ll sumOfDivisors(ll n){
    ll cnt, sum=1LL;
    for(ll &num: primeNumbers){
        cnt=0;
        if(num*num>n) break;
        while(n%num==0){
            n/=num;
            ++cnt;
        }
        // sum = (sum*((bigmod(num,
cnt)-1LL)/(num-1LL))%mod;
        if(cnt){
            ll a =
(bigmod(num,cnt+1)-1LL+mod)%mod
;
            ll b =
(bigmod((num-1LL),mod-2LL));
```

```
sum =
(sum*((a*b)%mod))%mod;
}
}
if(n>1){
    ll a =
(bigmod(n,2)-1LL+mod)%mod;
    ll b =
(bigmod((n-1LL),mod-2LL));
    sum = (sum*((a*b)%mod))%mod;
}
return sum;
}

// Sieve Prime O(n)
vector<bool> primeSieve (int N) {
    vector<bool> isPrimeNumber(N,
true);
    isPrimeNumber[0] =
isPrimeNumber[1] = false;
    for (int i = 4; i < N; i += 2)
        isPrimeNumber[i] = false;
    for (int i = 9; i < N; i += 6)
        isPrimeNumber[i] = false;
    for (int i = 1; 6 * i < N; ++i) {
        int x = 6 * i - 1, y = 6 * i + 1;
        if (isPrimeNumber[x])
            for (int j = 3 * x; j < N; j = x +
x + j)
                isPrimeNumber[j] = false;
        if (isPrimeNumber[y])
            for (int j = 3 * y; j < N; j = y +
y + j)
                isPrimeNumber[j] = false;
    }
    return isPrimeNumber;
}

// Generating subset of a set [1, n]
using bit mask
// TC(2^n * n) n-> 20-25
vector<vector<int>> subsets
(vector<int> &numbers_)
{
    int n = numbers_.size(), mask, i;
    int subset_cnt = (1 << n);
    vector<vector<int>> all_subsets;
    for (mask = 0; mask < subset_cnt;
++mask)
    {
        vector<int> subset;
        for (i = 0; i < n; ++i)
        {
            if ((mask & (1 << i)) != 0)
            {
                subset.push_back(numbers_[i]);
            }
        }
        all_subsets.push_back(subset);
    }
    return all_subsets;
}

// find out n is prime or not
```

```
bool isPrime (int n)
{
    if (n <= 1)
        return false;
    else if (n <= 3)
        return true;
    else if (n % 2 == 0 || n % 3 == 0)
        return false;
    for (int i = 5; i * i <= n; i += 6)
    {
        if (n % i == 0 || n % (i + 2) == 0)
            return false;
    }
    return true;
}

// findingPrimeFactors();
// Finding All Prime Factors From 1 to
N
const int N = 2020;
vector<ll> primeFactors[N];
int primeNumbers[N];
bool mp[N];
bool isPrime(ll n)
{
    if (n <= 1)
        return false;
    else if (n <= 3)
        return true;
    else if (n % 2 == 0 || n % 3 == 0)
        return false;
    for (int i = 5; i * i <= n; i += 6)
    {
        if (n % i == 0 || n % (i + 2) == 0)
            return false;
    }
    return true;
}
void findingPrimeFactors()
{
    int i, j;
    mp[2] = true;
    mp[3] = true;
    for (i = 1; 6 * i - 1 <= 1000; ++i)
    {
        ll a = (6 * i - 1), b = (6 * i + 1);
        if (isPrime(a))
            mp[a] = true;
        if (isPrime(b))
            mp[b] = true;
    }
    for (i = 1; i <= 1000; ++i)
    {
        if (mp[i])
        {
            for (j = i + i; j <= 1000; j += i)
            {
                primeFactors[j].push_back(i);
            }
        }
    }
}
int timer = 1;
```

```
// vector<vector<int>> bridges =
criticalConnections(numberOfNodes,
connections);
// dfs(0, -1, vis, adj, tin, low, bridges);
// Bridges In Graph – Using Tarjan's
Algorithm of Time In and Low Time
void dfs(int node, int parent,
vector<int> &vis, vector<int> adj[], int
tin[], int low[], vector<vector<int>>
&bridges)
{
    vis[node] = 1;
    tin[node] = low[node] = timer;
    timer++;
    for (auto &it : adj[node])
    {
        if (it == parent)
            continue;
        if (vis[it] == 0)
        {
            dfs(it, node, vis, adj, tin, low,
bridges);
            low[node] = min(low[it],
low[node]);
            if (low[it] > tin[node])
            {
                bridges.push_back({it,
node});
            }
        }
        else
        {
            low[node] = min(low[node],
low[it]);
        }
    }
}
vector<vector<int>>
criticalConnections (int n,
vector<vector<int>> &connections)
{
    vector<int> adj[n];
    for (auto it : connections)
    {
        int u = it[0], v = it[1];
        adj[u].push_back(v);
        adj[v].push_back(u);
    }
    vector<int> vis(n, 0);
    int tin[n];
    int low[n];
    vector<vector<int>> bridges;
    dfs(0, -1, vis, adj, tin, low, bridges);
    return bridges;
}
```

```
// Function to find the shortest distance
of all the vertices
// from the source vertex S.
// vector<int> res = dijkstra(V, adj,
Source);
vector<int> dijkstra (int V,
vector<vector<int>> adj[], int S)
{
```

```
// Create a priority queue for storing
the nodes as a pair {dist,node}
// where dist is the distance from
source to the node.
priority_queue<pair<int, int>,
vector<pair<int, int>>,
greater<pair<int, int>>> pq;

// Initialising distTo list with a large
number to
// indicate the nodes are unvisited
initially.
// This list contains distance from
source to the nodes.
vector<int> distTo(V, INT_MAX);

// Source initialised with dist=0.
distTo[S] = 0;
pq.push({0, S});

// Now, pop the minimum distance
node first from the min-heap
// and traverse for all its adjacent
nodes.
while (!pq.empty())
{
    int node = pq.top().second;
    int dis = pq.top().first;
    pq.pop();

    // Check for all adjacent nodes of
the popped out
// element whether the prev dist is
larger than current or not.
    for (auto it : adj[node])
    {
        int v = it[0];
        int w = it[1];
        if (dis + w < distTo[v])
        {
            distTo[v] = dis + w;

            // If current distance is
smaller,
            // push it into the queue.
            pq.push({dis + w, v});
        }
    }
}
// Return the list containing shortest
distances
// from source to all the nodes.
return distTo;
}
```

```
// Topological Sort Using BFS
Simple02
// Kahn's Algorithm
// vector<int> ans = topoSort(V, adj);
// Function to return list containing
vertices in Topological order.
vector<int> topoSort(int V,
vector<vector<int>> &adj)
{
    int indegree[V] = {0};
```

```
for (int i = 0; i < V; i++)
{
    for (auto it : adj[i])
    {
        indegree[it]++;
    }
}
queue<int> q;
for (int i = 0; i < V; i++)
{
    if (indegree[i] == 0)
    {
        q.push(i);
    }
}
vector<int> topo;
while (!q.empty())
{
    int node = q.front();
    q.pop();
    topo.push_back(node);
    // node is in your topo sort
    // so please remove it from the
indegree

    for (auto it : adj[node])
    {
        indegree[it]--;
        if (indegree[it] == 0)
            q.push(it);
    }
}
return topo;
}
```

```
// Topological Sort Using DFS
Simple01
// Function to return list containing
vertices in Topological order.
// call vector<int> ans = topoSort(V,
adj);
void dfs(int node, int vis[], stack<int>
&st, vector<vector<int>> &adj)
{
    vis[node] = 1;
    for (auto it : adj[node])
    {
        if (!vis[it])
            dfs(it, vis, st, adj);
    }
    st.push(node);
}
vector<int> topoSort (int V,
vector<vector<int>> &adj)
{
    int vis[V] = {0};
    stack<int> st;
    for (int i = 0; i < V; i++)
    {
        if (!vis[i])
        {
            dfs(i, vis, st, adj);
        }
    }
}
```

```

vector<int> ans;
while (!st.empty())
{
    ans.push_back(st.top());
    st.pop();
}
return ans;
}

// Multisource BFS For Adjacency List
int dist[N];
bool visited[N];
// Multisource BFS Function
void Multisource_BFS(vector<int>
graph[], queue<int> q)
{
    while (!q.empty())
    {
        int k = q.front();
        q.pop();
        for (auto i : graph[k])
        {
            if (!visited[i])
            {
                // Pushing the adjacent
                // with distance from current
                // vertex's distance + 1
                source = this
                q.push(i);
                dist[i] = dist[k] + 1;
                visited[i] = true;
            }
        }
    }
}

// This function calculates the distance
// of each
// vertex from nearest source
void nearestTown(vector<int>
graph[], int n, int sources[], int s)
{
    // Create a queue for BFS
    queue<int> q;
    // Mark all the source vertices as
    // visited and enqueue it
    for (int i = 0; i < s; i++)
    {
        q.push(sources[i]);
        visited[sources[i]] = true;
    }
    Multisource_BFS(graph, q);
    // Printing the distances
    for (int i = 1; i <= n; i++)
    {
        cout << i << " " << dist[i] <<
endl;
    }
}

// Multisource BFS For Adjacency
// Matrix
int multisourceBFS
(vector<vector<int>> &grid)
{
    queue<pair<int, int>> q;
    int n = grid.size(); // 6
    int m = grid[0].size(); // 5
    int vis[n][m];
    memset(vis, 0, sizeof(vis));
    // traverse boundary elements
    for (int i = 0; i < n; i++)
    {
        // if it is a land then store it in
        queue
        if (grid[i][0] == 1)
        {
            q.push({i, 0});
            vis[i][0] = 1;
        }
        if (grid[i][m - 1] == 1)
        {
            q.push({i, m - 1});
            vis[i][m - 1] = 1;
        }
    }
    for (int i = 1; i < m - 1; i++)
    {
        // if it is a land then store it in
        queue
        if (grid[0][i] == 1)
        {
            q.push({0, i});
            vis[0][i] = 1;
        }
        if (grid[n - 1][i] == 1)
        {
            q.push({n - 1, i});
            vis[n - 1][i] = 1;
        }
    }

    int delrow[] = {-1, 0, +1, 0};
    int delcol[] = {0, +1, +0, -1};

    while (!q.empty())
    {
        int row = q.front().first;
        int col = q.front().second;
        q.pop();

        // traverses all 4 directions
        for (int i = 0; i < 4; i++)
        {
            int nrow = row + delrow[i];
            int ncol = col + delcol[i];
            // check for valid coordinates
            and for land cell
            if (nrow >= 0 && nrow < n &&
ncol >= 0 && ncol < m &&
vis[nrow][ncol] == 0 &&
grid[nrow][ncol] == 1)
            {
                q.push({nrow, ncol});
                vis[nrow][ncol] = 1;
            }
        }
    }

    int cnt = 0;
    for (int i = 0; i < n; i++)
    {
        for (int j = 0; j < m; j++)
        {
            // check for unvisited land cell
            if (grid[i][j] == 1 && vis[i][j]
== 0)
                cnt++;
        }
    }
    return cnt;
}

// Bipartite Graph or Bicoloring
bool check(int start, int V, vector<int>
adj[], int color[])
{
    queue<int> q;
    q.push(start);
    color[start] = 0;
    while (!q.empty())
    {
        int node = q.front();
        q.pop();

        for (auto it : adj[node])
        {
            // if the adjacent node is yet not
            // colored
            // you will give the opposite
            // color of the node
            if (color[it] == -1)
            {
                color[it] = !color[node];
                q.push(it);
            }
            // is the adjacent guy having the
            // same color
            // someone did color it on some
            // other path
            else if (color[it] ==
color[node])
            {
                return false;
            }
        }
        return true;
    }

    bool isBipartite(int V, vector<int>
adj[])
    {
        int color[V];
        for (int i = 0; i < V; i++)
            color[i] = -1;

        for (int i = 0; i < V; i++)
        {
            // if not colored
            if (color[i] == -1)
            {
                if (check(i, V, adj, color) ==
false)
                {
                    return false; // it is not
bipartite graph

```

```

    }
    }
}
return true; // it is bipartite graph
}

// Detect Cycle In A Undirected Graph
Using BFS
bool detect(int src, vector<int> adj[],
bool vis[])
{
    vis[src] = true;
    // store <source node, parent node>
    queue<pair<int, int>> q;
    q.push({src, -1});
    // traverse until queue is not empty
    while (!q.empty())
    {
        int node = q.front().first;
        int parent = q.front().second;
        q.pop();

        // go to all adjacent nodes
        for (auto adjacentNode :
adj[node])
        {
            // if adjacent node is unvisited
            if (!vis[adjacentNode])
            {
                vis[adjacentNode] = true;
                q.push({adjacentNode,
node});
            }
            // if adjacent node is visited and
            is not it's own parent node
            else if (parent != adjacentNode)
            {
                // yes it is a cycle
                return true;
            }
        }
    }
    // there's no cycle
    return false;
}

// Function to detect cycle in an
undirected graph.
bool isCycle(int V, vector<int> adj[])
{
    // initialize them as unvisited
    bool vis[V] = {false};
    for (int i = 0; i < V; i++)
    {
        if (!vis[i])
        {
            if (detect(i, adj, vis))
                return true;
        }
    }
    return false;
}

```

// detect cycle in a directed graph

```

// Function to perform DFS and check
for cycles in the directed graph
bool dfsCheck(int node, vector<int>
adj[], bool vis[], bool pathVis[])
{
    vis[node] = true;
    pathVis[node] = true;

    // Traverse adjacent nodes
    for (auto it : adj[node])
    {
        // When the node is not visited
        if (!vis[it])
        {
            if (dfsCheck(it, adj, vis,
pathVis))
                return true;
        }
        // If the node has been previously
        visited but it has to be visited on the
        same path
        else if (pathVis[it])
        {
            return true; // there is a cycle
        }
    }

    pathVis[node] = false;
    return false; // if there is no cycle
}

// Function to detect cycle in a directed
graph
bool isCyclic(int V, vector<int> adj[])
{
    bool vis[V] = {false}; // Array to
    track visited nodes
    bool pathVis[V] = {false}; // Array
    to track visited nodes on the current
    path

    for (int i = 0; i < V; i++)
    {
        if (!vis[i])
        {
            if (dfsCheck(i, adj, vis,
pathVis))
                return true;
        }
    }
    return false;
}

// Function to return Breadth First
Traversal of given graph.
vector<int> bfsOfGraph(int V,
vector<int> adj[])
{
    bool vis[V] = {false};
    vis[0] = true; // here we define
    source node true
    queue<int> q;
    // push the initial starting node
    q.push(0);
    vector<int> bfs;
    // iterate till the queue is empty

```

```

while (!q.empty())
{
    // get the topmost element in the
    queue
    int node = q.front();
    q.pop();
    bfs.push_back(node);
    // traverse for all its neighbors
    for (auto it : adj[node])
    {
        // if the neighbor has previously
        not been visited,
        // store in Queue and mark as
        visited
        if (!vis[it])
        {
            vis[it] = true;
            q.push(it);
        }
    }
    return bfs;
}

// Trie
struct Trie
{
    struct Trie *children[10];
    bool isend;
    Trie() {
        memset(children,
0, sizeof(children));
        isend = false;
    }
};

struct Trie *root;
void insertTrie (string s1) {
    struct Trie *cur = root;
    for (char &c: s1) {
        int index = c-'0';
        if (cur->isend) flag = false;
        if (!cur->children[index]) {
            cur->children[index] = new
Trie;
        }
        cur = cur->children[index];
    }
    cur->isend = true;
    for (int i=0; i<10; ++i) {
        if (cur->children[i]) {
            flag = false;
        }
    }
}

void dfs(ll vertex)
{
    visit[vertex] = true;
    for (auto child : graph[vertex])
    {
        if (!visit[child])
            dfs(child);
    }
}

```

```

// segment Tree
const int N = 2e5 + 2;
long long segmentTreeArray[N], tree[4 * N];
// segment Tree Array = given array
// tree = we build the array
// to call this function build(1, 0, n-1)
// node can't start from 0
void build(int node, int start, int end_)
{
    if (start == end_)
    {
        tree[node] = segmentTreeArray[start];
        return;
    }

    int mid = (start + end_) >> 1;
    build((node << 1), start, mid);
    build((node << 1) + 1, mid + 1, end_);

    // modify
    tree[node] = tree[(node << 1)] + tree[(node << 1) + 1];
    // tree[node] = max(tree[(node << 1)], tree[(node << 1) + 1]);
    // tree[node] = min(tree[(node << 1)], tree[(node << 1) + 1]);
}

// to find sum from l to r
// query(1, 0, n - 1, l-1, r-1);
long long query(int node, int start, int en, const int &l, const int &r)
{
    // l...r > start...en    start...en < l...r no overlap
    if (start > r || en < l)
    {
        return 0LL;
    }
    // l start...en r complete overlap
    if (l <= start && r >= en)
    {
        return tree[node];
    }
    // start l en r partial overlap
    // l start r en
    int mid = (start + en) >> 1;
    long long q1 = query(node << 1, start, mid, l, r);
    long long q2 = query((node << 1) + 1, mid + 1, en, l, r);

    return q1 + q2;
    // return max(q1, q2);
    // return min(q1, q2);
}

// to update query
// update(1, 0, n - 1, index-1, val);
void update(int node, int st, int en, const int &idx, const long long &val)

```

```

{
    if (st == en)
    {
        segmentTreeArray[st] = val;
        tree[node] = val;
        return;
    }
    int mid = (st + en) >> 1;
    if (idx <= mid)
    {
        update((node << 1), st, mid, idx, val);
    }
    else
    {
        update((node << 1) + 1, mid + 1, en, idx, val);
    }

    tree[node] = tree[(node << 1)] + tree[(node << 1) + 1];
    // tree[node] = max(tree[(node << 1)], tree[(node << 1) + 1]);
    // tree[node] = min(tree[(node << 1)], tree[(node << 1) + 1]);
}

vector<long long>
maximumSumSubmatrix (int r, int c, vector<vector<long long>> &v1)
{
    long long **prefix = new long long *[r];
    for (int i = 0; i < r; ++i)
    {
        prefix[i] = new long long;
        for (int j = 0; j < c; ++j)
        {
            prefix[i][j] = 0;
        }
    }
    for (int i = 0; i < r; ++i)
    {
        for (int j = 0; j < c; ++j)
        {
            if (j == 0)
            {
                prefix[i][j] = v1[i][j];
            }
            else
            {
                prefix[i][j] = v1[i][j] + prefix[i][j - 1];
            }
        }
    }
    vector<long long> solution(5);
    long long val, st, en, ans;
    // long long maxSum = LLONG_MIN, startx, starty, endx, endy;
    // solution[0,...,4] = {maxSum, start_x, start_y, end_x, end_y}
    solution[0] = LLONG_MIN;
    for (int i = 0; i < c; ++i)

```

```

{
    for (int j = i; j < c; ++j)
    {
        vector<long long> v2;
        for (int k = 0; k < r; ++k)
        {
            if (i == 0)
            {
                val = prefix[k][j];
            }
            else
            {
                val = prefix[k][j] - prefix[k][i - 1];
            }
            v2.push_back(val);
        }
        ans = kadaneAlorithm(v2, st, en);
        if (ans > solution[0])
        {
            solution[0] = ans, solution[1] = st, solution[2] = i, solution[3] = en, solution[4] = j;
        }
    }
}
return solution;
}

long long kadaneAlorithm (vector<long long> &v1, long long &finalStart, long long &finalEnd)
{
    long long currentSum = 0, maxSum = LLONG_MIN, n = v1.size(), start = 0;
    for (int i = 0; i < n; ++i)
    {
        currentSum += v1[i];
        if (currentSum > maxSum)
        {
            maxSum = currentSum;
            finalStart = start;
            finalEnd = i;
        }
        if (currentSum < 0)
        {
            currentSum = 0;
            start = i + 1;
        }
    }
    return maxSum;
}

long long LargestSumContiguousSubarray (ll ar[], ll arraySize, ll &subarrayStart, ll &subarrayEnd)
{
    long long sum = 0, mx = LLONG_MIN, start = -1;
    for (int i = 0; i < arraySize; ++i)
    {
        if (sum == 0)
        {
            start = i;

```



```

    }
    sum += ar[i];
    if(mx<sum){
        mx = sum;
        subarrayStart = start;
        subarrayEnd = i;
    }
    if(sum<0){
        sum=0;
    }
}
return mx;
}

vector<long long>
jobSequencingProblem
(vector<vector<long long>> &v1, int
n)
{
    sort(v1.begin(), v1.end(),
[&](vector<long long> &a,
vector<long long> &b){
        return a[1]<b[1];
    });
    priority_queue<vector<long
long>, vector<vector<long long>>,
CustomComparator> pq;
    long long mxProfit = 0,
    numberOfWorkDone = 0;
    int slot_available;
    for (int i = n-1; i >= 0; --i)
    {
        slot_available = v1[i][1] -
(i>0?v1[i-1][1]:0);
        pq.push(v1[i]);
        while (slot_available>0 &&
pq.size()>0)
        {
            vector<long long> v2 =
pq.top();
            pq.pop();
            mxProfit += v2[2];
            numberOfWorkDone++;
            slot_available--;
        }
    }
    return {numberOfWorkDone,
mxProfit};
}

```

```

vector<int> jobSequencingProblem
(vector<vector<int>> &v1, int n)
{
    // v1 is vector first index -> id
    // v1 is vector second index -> dead
    Line
    // v1 is vector profit index -> profit
    sort(v1.begin(), v1.end(),
[&](vector<int> &a, vector<int> &b)
{ return a[2] > b[2]; });
    int mx_dead = -1;
    for (int i = 0; i < n; ++i)
    {
        if (mx_dead < v1[i][1])

```

```

        mx_dead = v1[i][1];
    }
    vector<int> v2(mx_dead + 1, -1);
    int mxProfit = 0,
    numberOfWorkDone = 0;
    for (int i = 0; i < n; ++i)
    {
        for (int j = v1[i][1]; j > 0; --j)
        {
            if (v2[j] == -1)
            {
                v2[j] = v1[i][0];
                ++numberOfWorkDone;
                mxProfit += v1[i][2];
                break;
            }
        }
    }
    return {numberOfWorkDone,
mxProfit};
}

```

```

const int N = 2 * 1e5 + 10;
int dp[N], arr[N];
// remember to memset(dp, -1,
sizeof(dp))
// index should be start from 0 to n
// loop(i,0,n) ans =
max(ans, DP_LCS(i));
// index = longest Subsequence 0 to
index
int DP_LCS (int int index)
{
    // base case
    // ---
    // if data already exists.
    if (dp[index] != -1)
        return dp[index];
    int length = 1;
    for (int i = 0; i < index; ++i)
    {
        if (arr[index]>arr[i])
            length = max(length,
DP_LCS(i) + 1);
    }
    // return and store dating
    return dp[index] = length;
}

```

```

const int N = 2 * 1e5 + 10;
long long dp[N], height[N];
// remember to memset(dp, -1,
sizeof(dp))
// ending point is where frog is now
// k is maximum length frog can jump
long long DP_Jumps (long long int
endingPoint, long long k)
{
    // base case
    if (endingPoint <= 0)
        return 0;
    // if data is already exist.
    if (dp[endingPoint] != -1)
        return dp[endingPoint];

```

```

    long long cost = 1e15;
    for (int i = 1; i <= k; ++i)
    {
        if (endingPoint-i>=0)
            cost = min(cost,
DP_Jumps(endingPoint - i, k) +
abs(height[endingPoint] -
height[endingPoint - i]));
    }
    // return and store dating
    return dp[endingPoint] = cost;
}

```

```

vector<int> divisorsForSingleValue
(int n){
    int i;
    vector<int> v1;
    for(i=1; i*i<=n; ++i){
        if(n%i==0){
            v1.push_back(i);
            v1.push_back(n/i);
        }
    }
    --i;
    if(i*i==n){
        v1.pop_back();
    }
    return v1;
}

```

```

void bfs_distance(ll root, vector<ll>
&distance)
{
    ll x;
    queue<ll> q;
    q.push(root);
    distance[root] = 0;
    visited.assign(N, false);
    while (!q.empty())
    {
        ll current = q.front();
        q.pop();
        visited[current] = true;
        for (auto child : graph[current])
        {
            if (!visited[child])
            {
                q.push(child);
                distance[child] =
distance[current] + 1;
            }
        }
    }
}

```

```

vector<vector<int>>
printMaxActivities
(vector<vector<int>> &v1, int n)
{
    //v1.push_back({index[i], start[i],
finish[i]});
    // index[] array is at 0 index of v1
    // start[] array is at 1 index of v1
    // finish[] array is at 2 index of v1
    int i=0, j;

```

```

vector<vector<int>> ansVector;
sort(v1.begin(), v1.end(),
[&](vector<int> &a, vector<int> &b){
    return a[2]<b[2];
});
ansVector.push_back({v1[i][0],
v1[i][1], v1[i][2]});
    for (j = 1; j < n; j++) {
        if(v1[j][1] >=
v1[i][2]) {
ansVector.push_back({v1[j][0],
v1[j][1], v1[j][2]});
        i = j;
    }
    }
    return ansVector;
}

```

```

int gcd (int m, int n){
    int r = 0, a, b;
    a = (m > n) ? m : n;
    b = (m < n) ? m : n;
    r = b;
    while (a % b != 0)
    {
        r = a % b;
        a = b;
        b = r;
    }
    return r;
}
int lcm (int m, int n){
    int a;
    a = (m > n) ? m : n;
    while (true)
    {
        if (a % m == 0 && a % n == 0)
            return a;
        ++a;
    }
}
long lcm(long x, long y)
{
    return (x * (y / gcd(x, y)));
}

```

```

// sieveDivisorsCount();
// for(int i=0; i<N; ++i){
// cout << i << " " << countDivisors[i]
// << "\n";}
const int N = 1e6 + 5;
int countDivisors[N + 5];
void sieveDivisorsCount()
{
    int i, j;
    for (i = 2; i < N; i++)
    {
        for (j = i; j < N; j += i)
        {
            countDivisors[j]++;
        }
    }
}

```

```

}

// Finding Sum Of Two Index Value Is
Equal Of Target Value
// A is sorted vector
// if there any two value with sum X
return 1 nor 0
int isPairSum_TwoPointer
(vector<int> &A, int X)
{
    int i = 0; // represents first
pointer
    int j = A.size() - 1; // represents
second pointer
    while (i < j)
    {
        if (A[i] + A[j] == X)
            return 1; // If we find a pair
// If sum of elements at current
// pointers is less, we move
towards
// higher values by doing i++
        else if (A[i] + A[j] < X)
            i++;
// If sum of elements at current
// pointers is more, we move
towards
// lower values by doing j--
        else
            j--;
    }
    return 0;
}

```

```

// order set
#include
<ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template <class T>
using oset = tree<T, null_type,
less<T>, rb_tree_tag,
tree_order_statistics_node_update>;
// oset <ll> s; --> Declare ordered set
// s.order_of_key(val) --> index of
value val
//*(s.find_by_order(ind)) --> value at
index ind

```

```

// Multiplicative modulus
long long mulmod(long long a, long
long b, long long m) {
    long long res = 0; // Initialize the
result

```

```

    a %= m;
    while (b > 0) {
        // If b is odd, add a to the result
        if (b % 2 == 1) {
            res = (res + a) % m;
        }
    }
}

```

```

// Double a and reduce b by half
a = (a * 2) % m;
b /= 2;
}

return res;
}

```

```

// Power value modulus
long long mod_pow(long long base,
long long exp, long long mod) {
    long long result = 1;
    while (exp > 0) {
        if (exp % 2 == 1) {
            result = (result * base) % mod;
        }
        base = (base * base) % mod;
        exp /= 2;
    }
    return result;
}

```

```

// Sieve of Erastones
void sieveOfEratosthenes()
{
    primes[1] = 1;
    for (int i = 2; i * i <= N; i++)
    {
        if (primes[i])
            continue;
        primes[i] = i;
        for (int j = i * i; j <= N; j += i)
        {
            if (!primes[j])
                primes[j] = i;
        }
    }
}

```

```

// Number of Divisors of a number
long long numberOfDivisors(long
long num) {
    long long total = 1;
    for (int i = 2; (long long)i * i <=
num; i++) {
        if (num % i == 0) {
            int e = 0;
            do {
                e++;
                num /= i;
            } while (num % i == 0);
            total *= e + 1;
        }
    }
    if (num > 1) {
        total *= 2;
    }
    return total;
}

```

```
// DSU TC (alpha * n)
const int N = 1e5 + 10;
vector<int> parent(N), sizeDSU(N),
rankDSU(N);
void disjointSet(int n)
{
    rankDSU.resize(n + 1);
    parent.resize(n + 1);
    sizeDSU.resize(n + 1);
    for (int i = 0; i <= n; i++)
    {
        parent[i] = i;
        sizeDSU[i] = 1;
        rankDSU[i] = 0;
    }
}
void makeDSU(int i)
{
    parent[i] = i;
    sizeDSU[i] = 1;
}
int findParent(int p)
{
    if (p == parent[p])
        return p;
    // Path Compression
    return parent[p] =
findParent(parent[p]);
}
void unionBySize(int a, int b)
{
    int parentOfa = findParent(a);
    int parentOfb = findParent(b);
    if (parentOfa != parentOfb)
    {
        // Union by size
        if (sizeDSU[parentOfa] <
sizeDSU[parentOfb])
            swap(parentOfa, parentOfb);
        parent[parentOfb] = parentOfa;
        sizeDSU[parentOfa] +=
sizeDSU[parentOfb];
    }
}
void unionByRank(int a, int b)
{
    int parentOfa = findParent(a);
    int parentOfb = findParent(b);
    if (parentOfa == parentOfb)
        return;
    if (rankDSU[parentOfa] <
rankDSU[parentOfb])
    {
        parent[parentOfa] = parentOfb;
    }
    else if (rankDSU[parentOfb] <
rankDSU[parentOfa])
    {
        parent[parentOfb] = parentOfa;
    }
    else
    {
        parent[parentOfb] = parentOfa;
        rankDSU[parentOfa]++;
    }
}
}
```

```
// auto v2 = kruskal_MST(v1, n);
int total_cost;
vector<array<int, 3>> kruskal_MST
(vector<vector<array<int, 2>>> &adj,
int noNode)
{
    vector<array<int, 3>> gra, mst;
    int u, v, w, n = adj.size(), i, j;
    disjointSet(n);
    for (i = 1; i < n; i++)
    {
        for (auto &[v, w] : adj[i])
        {
            gra.push_back({w, i, v});
        }
    }
    sort(gra.begin(), gra.end());
    total_cost = 0;
    for (auto &[w, u, v] : gra)
    {
        if (findParent(u) == findParent(v))
            continue;
        unionBySize(u, v);
        total_cost += w;
        mst.push_back({w, u, v});
    }
    return mst;
}
```

```
// Prim's Algorithm MST
// Function to find sum of weights of
edges of the Minimum Spanning Tree.
int spanningTree(int V,
vector<vector<int>> adj[])
{
    priority_queue<pair<int, int>,
vector<pair<int, int>>,
greater<pair<int, int>>> pq;
    vector<int> vis(V, 0);
    // {wt, node}
    pq.push({0, 0});
    int sum = 0;
    while (!pq.empty())
    {
        auto it = pq.top();
        pq.pop();
        int node = it.second;
        int wt = it.first;

        if (vis[node] == 1)
            continue;
        // add it to the mst
        vis[node] = 1;
        sum += wt;
        for (auto it : adj[node])
        {
            int adjNode = it[0];
            int edW = it[1];
            if (!vis[adjNode])
            {
                pq.push({edW, adjNode});
            }
        }
    }
}
```

```
return sum;
}

// Maximum Sum Of Subarray
// maximumSumOfSubarray(v1)
int maximumSumOfSubarray (int
v1[])
{
    int sum2 = INT_MIN, i, sum1 = 0, n
= sizeof(v1);
    for (i = 0; i < n; ++i)
    {
        sum1 += v1[i];
        sum2 = max(sum2, sum1);
        if (sum1 < 0)
            sum1 = 0;
    }
    return sum2;
}
```

```
// Diameter Of Tree
// diameterOfTree(v1)
int mx = 1, node = 1;
void dfs(int i, int depth, bool vis[], int
dis[], vector<vector<int>> &adj)
{
    vis[i] = true;
    dis[i] = depth;
    if (depth > mx)
    {
        mx = depth;
        node = i;
    }
    for (auto &c : adj[i])
    {
        if (!vis[c])
            dfs(c, depth + 1, vis, dis, adj);
    }
}
int diameterOfTree
(vector<vector<int>> &adj)
{
    int n = adj.size();
    bool vis[n];
    int dis[n];
    memset(vis, false, sizeof(vis));
    memset(dis, 0, sizeof(dis));
    // dfs(root, 0)
    dfs(1, 0, vis, dis, adj);
    memset(vis, false, sizeof(vis));
    memset(dis, 0, sizeof(dis));
    dfs(node, 0, vis, dis, adj);
    return mx;
}
```

```
// Subtree Size
// subtreeSizeCall(v1)
int dfs(int i, bool vis[], vector<int>
&subtreeSize, vector<vector<int>>
&adj)
```

```
{
    vis[i] = true;
    int child = 1;
    for (auto &c : adj[i])
    {
        if (!vis[c])
            child += dfs(c, vis, subtreeSize,
adj);
    }
    return subtreeSize[i] = child;
}
vector<int>
subtreeSizeCall(vector<vector<int>>
&adj)
{
    int n = adj.size();
    bool vis[n];
    vector<int> subtreeSize(n);
    memset(vis, false, sizeof(vis));
    // dfs(root)
    n = dfs(0, vis, subtreeSize, adj);
    return subtreeSize;
}
```

```
/*
** Below code is the basic structure
of sparse table range query
implementation
*/
```

```
const int MAXN = 1e9; // immutable
array max size

const int K = 25; // K =
2^(log(MAXN)) that is the max size of
the immutable array
```

```
int N = 6; // the size of the array
int st[K+1][MAXN]; // sparse table
array<int, 6> arr; // the given array
```

```
int f(int a, int b) {
    // This function is used to elaborate
the min query/ max query/ sum query
    // or Other action regarding min max
of a range specified at sparsetable
```

```
    return 0;
}
```

```
void sparseTable() {
    copy(arr.begin(), arr.end(), st[0]);
```

```
    for (int i = 1; i <= K; i++)
        for (int j = 0; j + (1 << i) <= N;
j++)
            st[i][j] = f(st[i - 1][j], st[i - 1][j
+ (1 << (i - 1))]);
}
```

```
/*
** Below code is for range sum
query
*/
```

```
const int MAXN = 1e9; // immutable
array max size
const int K = 25; // K =
2^(log(MAXN)) that is the max size of
the immutable array
int N = 6; // the size of the array
long long st[K + 1][MAXN];
array<int, 6> arr; // the given array
```

```
void sparseTable() {
    copy(arr.begin(), arr.end(), st[0]);
```

```
    for (int i = 1; i <= K; i++)
        for (int j = 0; j + (1 << i) <= N;
j++)
            st[i][j] = st[i - 1][j] + st[i - 1][j
+ (1 << (i - 1))];
}
```

```
int getSum(int L, int R) { // O(K)
    long long sum = 0;
    for (int i = K; i >= 0; i--) {
        if ((1 << i) <= R - L + 1) {
            sum += st[i][L];
            L += 1 << i;
        }
    }
    return sum;
}
```

```
/*
** Below code is for range min
query
*/

const int MAXN = 1e9; // immutable
array max size
const int K = 25; // K =
2^(log(MAXN)) that is the max size of
the immutable array
int N = 6; // the size of the array
long long st[K + 1][MAXN];
array<int, 6> arr; // the given array
int lg[MAXN+1];
```

```
void precomputeLogarithms() {
    lg[1] = 0;
    for (int i = 2; i <= MAXN; i++)
        lg[i] = lg[i/2] + 1;
}
```

```
void sparseTable() {
    copy(arr.begin(), arr.end(), st[0]);

    for (int i = 1; i <= K; i++)
        for (int j = 0; j + (1 << i) <= N;
j++)
            st[i][j] = min(st[i - 1][j], st[i -
1][j + (1 << (i - 1))]);
}
```

```
int getMinQuery(int L, int R) {
    int i = lg[R - L + 1];
    int minimum = min(st[i][L], st[i][R -
(1 << i) + 1]);
}
```

```
    return minimum;
}
```

```
/*
** Below code is for BIT that
calculates sum in 1D array
** Time Complexity: O(log(n)) // here
n is the size of array
** Space Complexity: O(n)
*/
```

```
struct FenwickTree {
    vector<int> bit; // binary indexed
tree
    int n;
```

```
FenwickTree(int n) {
    this->n = n;
    bit.assign(n, 0);
}
```

```
FenwickTree(vector<int> const &a)
: FenwickTree(a.size()) {
    for (size_t i = 0; i < a.size(); i++)
        add(i, a[i]);
}
```

```
int sum(int r) {
    int ret = 0;
    for (; r >= 0; r = (r & (r + 1)) - 1)
        ret += bit[r];
    return ret;
}
```

```
int sum(int l, int r) {
    return sum(r) - sum(l - 1);
}
```

```
void add(int idx, int delta) {
    for (; idx < n; idx = idx | (idx + 1))
        bit[idx] += delta;
}
};
```

```
/*
** Below code is for BIT that
calculates minimum of [0, r] in 1D
array
** Time Complexity: O(log(n)) // here
n is the size of array
** Space Complexity: O(n)
*/
```

```
struct FenwickTreeMin {
    vector<int> bit;
    int n;
    const int INF = (int)1e9;

    FenwickTreeMin(int n) {
        this->n = n;
        bit.assign(n, INF);
    }
}
```

```
FenwickTreeMin(vector<int> a) :
FenwickTreeMin(a.size()) {
    for (size_t i = 0; i < a.size(); i++)
```

```

        update(i, a[i]);
    }

    int getmin(int r) {
        int ret = INF;
        for (; r >= 0; r = (r & (r + 1)) - 1)
            ret = min(ret, bit[r]);
        return ret;
    }

    void update(int idx, int val) {
        for (; idx < n; idx = idx | (idx + 1))
            bit[idx] = min(bit[idx], val);
    }
};

/*
** Below code is for BIT that
calculates sum using 1-based indexing
in 1D array
** Time Complexity: O(log(n)) // here
n is the size of array
** Space Complexity: O(n)
*/

struct FenwickTreeOneBasedIndexing {
    vector<int> bit; // binary indexed
    tree
    int n;

    FenwickTreeOneBasedIndexing(int
n) {
        this->n = n + 1;
        bit.assign(n + 1, 0);
    }

    FenwickTreeOneBasedIndexing(vector
<int> a)
    :
    FenwickTreeOneBasedIndexing(a.size(
)) {
        for (size_t i = 0; i < a.size(); i++)
            add(i, a[i]);
    }

    int sum(int idx) {
        int ret = 0;
        for (++idx; idx > 0; idx -= idx &
-idx)
            ret += bit[idx];
        return ret;
    }

    int sum(int l, int r) {
        return sum(r) - sum(l - 1);
    }

    void add(int idx, int delta) {
        for (++idx; idx < n; idx += idx &
-idx)
            bit[idx] += delta;
    }
};

```

```

// Lexicographical next balanced
sequence of a given string
bool next_balanced_sequence(string &
s) {
    int n = s.size();
    int depth = 0;
    for (int i = n - 1; i >= 0; i--) {
        if (s[i] == '(')
            depth--;
        else
            depth++;

        if (s[i] == '(' && depth > 0) {
            depth--;
            int open = (n - i - 1 - depth) / 2;
            int close = n - i - 1 - open;
            string next = s.substr(0, i) + ')' +
string(open, '(') + string(close, ')');
            s.swap(next);
            return true;
        }
    }
    return false;
}

```

```

// Finding kth balanced string
sequence
string kth_balanced(int n, int k) {
    vector<vector<int>> d(2*n+1,
vector<int>(n+1, 0));
    d[0][0] = 1;
    for (int i = 1; i <= 2*n; i++) {
        d[i][0] = d[i-1][1];
        for (int j = 1; j < n; j++)
            d[i][j] = d[i-1][j-1] +
d[i-1][j+1];
        d[i][n] = d[i-1][n-1];
    }

    string ans;
    int depth = 0;
    for (int i = 0; i < 2*n; i++) {
        if (depth + 1 <= n &&
d[2*n-i-1][depth+1] >= k) {
            ans += '(';
            depth++;
        } else {
            ans += ')';
            if (depth + 1 <= n)
                k -= d[2*n-i-1][depth+1];
            depth--;
        }
    }
    return ans;
}

```

```

// inversion count of the array
calculating each element inversion
using mergeSort
int _mergeSort(int arr[], int temp[], int
left, int right);
int merge(int arr[], int temp[], int left,
int mid,
int right);

```

```

// This function sorts the
// input array and returns the
// number of inversions in the array
int mergeSort(int arr[], int array_size)
{
    int temp[array_size];
    return _mergeSort(arr, temp, 0,
array_size - 1);
}

```

```

// An auxiliary recursive function
// that sorts the input array and
// returns the number of inversions in
the array.
int _mergeSort(int arr[], int temp[], int
left, int right)
{
    int mid, inv_count = 0;
    if (right > left) {
        // Divide the array into two parts
        and
        // call _mergeSortAndCountInv()
        // for each of the parts
        mid = (right + left) / 2;
    }
}

```

```

// Inversion count will be sum of
// inversions in left-part, right-part
// and number of inversions in
merging
inv_count += _mergeSort(arr,
temp, left, mid);
inv_count += _mergeSort(arr,
temp, mid + 1, right);

// Merge the two parts
inv_count += merge(arr, temp,
left, mid + 1, right);
}
return inv_count;
}

```

```

// This function merges two sorted
arrays
// and returns inversion count in the
arrays.
int merge(int arr[], int temp[], int left,
int mid,
int right)
{
    int i, j, k;
    int inv_count = 0;

    i = left;
    j = mid;
    k = left;
    while ((i <= mid - 1) && (j <=
right)) {
        if (arr[i] <= arr[j]) {
            temp[k++] = arr[i++];
        }
        else {
            temp[k++] = arr[j++];
        }
    }

    // this is tricky -- see above
// explanation/diagram for
merge()

```

```

        inv_count = inv_count + (mid -
i);
    }
}

// Copy the remaining elements of
left subarray
// (if there are any) to temp
while (i <= mid - 1)
    temp[k++] = arr[i++];

// Copy the remaining elements of
right subarray
// (if there are any) to temp
while (j <= right)
    temp[k++] = arr[j++];

// Copy back the merged elements to
original array
for (i = left; i <= right; i++)
    arr[i] = temp[i];

return inv_count;
}

```

**// Euler totient phi(n)**, time complexity:  $O(\sqrt{n})$

```

int phi(int n) {
    int result = n;
    for (int i = 2; i * i <= n; i++) {
        if (n % i == 0) {
            while (n % i == 0)
                n /= i;
            result -= result / i;
        }
    }
    if (n > 1)
        result -= result / n;
    return result;
}

```

**// Segment Tree Lazy Propagation**

addition

// here, a[] is the 1-based array from question

```

const int MAXN = int(1e9);
long long t[4*MAXN];

```

```

void build(int a[], int v, int tl, int tr) {
    if (tl == tr) {
        t[v] = a[tl];
    } else {
        int tm = (tl + tr) / 2;
        build(a, v*2, tl, tm);
        build(a, v*2+1, tm+1, tr);
        t[v] = 0;
    }
}

```

```

void update(int v, int tl, int tr, int l, int
r, int add) {
    if (l > r)
        return;
    if (l == tl && r == tr) {
        t[v] += add;
    } else {

```

```

        int tm = (tl + tr) / 2;
        update(v*2, tl, tm, l, min(r, tm),
add);
        update(v*2+1, tm+1, tr, max(l,
tm+1), r, add);
    }
}

```

```

int get(int v, int tl, int tr, int pos) {
    if (tl == tr)
        return t[v];
    int tm = (tl + tr) / 2;
    if (pos <= tm)
        return t[v] + get(v*2, tl, tm, pos);
    else
        return t[v] + get(v*2+1, tm+1, tr,
pos);
}

```

**// Segment Tree Lazy Propagation**

addition and querying for maximum

// here, a[] is the 1-based array from question

```

const int MAXN = int(2e5);
const int INF = int(1e9);
long long t[4*MAXN];
long long lazy[4*MAXN];

```

```

void build(int a[], int v, int tl, int tr) {
    if (tl == tr) {
        t[v] = a[tl];
    } else {
        int tm = (tl + tr) / 2;
        build(a, v*2, tl, tm);
        build(a, v*2+1, tm+1, tr);
        t[v] = max(t[v*2], t[v*2+1]);
    }
}

```

```

void push(int v) {
    t[v*2] += lazy[v];
    lazy[v*2] += lazy[v];
    t[v*2+1] += lazy[v];
    lazy[v*2+1] += lazy[v];
    lazy[v] = 0;
}

```

```

void update(int v, int tl, int tr, int l, int
r, int addend) {
    if (l > r)
        return;
    if (l == tl && tr == r) {
        t[v] += addend;
        lazy[v] += addend;
    } else {
        push(v);
        int tm = (tl + tr) / 2;
        update(v*2, tl, tm, l, min(r, tm),
addend);
        update(v*2+1, tm+1, tr, max(l,
tm+1), r, addend);
        t[v] = max(t[v*2], t[v*2+1]);
    }
}

```

```

int query(int v, int tl, int tr, int l, int r) {

```

```

    if (l > r)
        return -INF;
    if (l == tl && tr == r)
        return t[v];
    push(v);
    int tm = (tl + tr) / 2;
    return max(query(v*2, tl, tm, l,
min(r, tm)),
        query(v*2+1, tm+1, tr, max(l,
tm+1), r));
}

```

**// Persistent Segment Tree that**

records history of each range

```

struct Vertex {

```

```

    Vertex *l, *r;
    int sum;

```

```

    Vertex(int val) : l(nullptr), r(nullptr),
sum(val) {}

```

```

    Vertex(Vertex *l, Vertex *r) : l(l),
r(r), sum(0) {}

```

```

    if (!l) sum += l->sum;
    if (!r) sum += r->sum;
}

```

```

};

```

```

Vertex* build(int a[], int tl, int tr) {
    if (tl == tr)
        return new Vertex(a[tl]);
    int tm = (tl + tr) / 2;
    return new Vertex(build(a, tl, tm),
build(a, tm+1, tr));
}

```

```

int get_sum(Vertex* v, int tl, int tr, int
l, int r) {
    if (l > r)
        return 0;
    if (l == tl && tr == r)
        return v->sum;
    int tm = (tl + tr) / 2;
    return get_sum(v->l, tl, tm, l, min(r,
tm))
        + get_sum(v->r, tm+1, tr, max(l,
tm+1), r);
}

```

```

Vertex* update(Vertex* v, int tl, int tr,
int pos, int new_val) {

```

```

    if (tl == tr)
        return new Vertex(new_val);
    int tm = (tl + tr) / 2;
    if (pos <= tm)
        return new Vertex(update(v->l, tl,
tm, pos, new_val), v->r);
    else
        return new Vertex(v->l,
update(v->r, tm+1, tr, pos, new_val));
}

```

**// Fermat's theorem impl**

// Here, binpower(...) function refers the binary exponentiation

```
bool probablyPrimeFermat(int n, int
iter=5) {
    if (n < 4)
        return n == 2 || n == 3;

    for (int i = 0; i < iter; i++) {
        int a = 2 + rand() % (n - 3);
        if (binpower(a, n - 1, n) != 1)
            return false;
    }
    return true;
}
```

#### // Miller Robin theorem impl

```
using u64 = uint64_t;
using u128 = __uint128_t;

u64 binpower(u64 base, u64 e, u64
mod) {
    u64 result = 1;
    base %= mod;
    while (e) {
        if (e & 1)
            result = (u128)result * base %
mod;
        base = (u128)base * base % mod;
        e >>= 1;
    }
    return result;
}
```

```
bool check_composite(u64
n, u64 a, u64 d, int s) {
    u64 x = binpower(a, d, n);
    if (x == 1 || x == n - 1)
        return false;
    for (int r = 1; r < s; r++) {
        x = (u128)x * x % n;
        if (x == n - 1)
            return false;
    }
    return true;
};
```

```
bool MillerRabin(u64 n, int
iter=5) { // returns true if n
is probably prime, else
returns false.
```

```
    if (n < 4)
        return n == 2 || n == 3;

    int s = 0;
    u64 d = n - 1;
    while ((d & 1) == 0) {
        d >>= 1;
        s++;
    }

    for (int i = 0; i < iter; i++) {
        int a = 2 + rand() % (n - 3);
        if (check_composite(n, a, d, s))
            return false;
    }
}
```

```
    return true;
}
```

#### // Finding Articulation Point of forest like graph

```
int n; // number of nodes
vector<vector<int>> adj; // adjacency
list of graph

vector<bool> visited;
vector<int> tin, low;
int timer;

void dfs(int v, int p = -1) {
    visited[v] = true;
    tin[v] = low[v] = timer++;
    int children=0;
    for (int to : adj[v]) {
        if (to == p) continue;
        if (visited[to]) {
            low[v] = min(low[v], tin[to]);
        } else {
            dfs(to, v);
            low[v] = min(low[v], low[to]);
            if (low[to] >= tin[v] && p != -1)
                IS_CUTPOINT(v);
            ++children;
        }
    }
    if (p == -1 && children > 1)
        IS_CUTPOINT(v);
}

void find_cutpoints() {
    timer = 0;
    visited.assign(n, false);
    tin.assign(n, -1);
    low.assign(n, -1);
    for (int i = 0; i < n; ++i) {
        if (!visited[i])
            dfs(i);
    }
}
```

#### // This code refers to the count of Longest Increasing Subsequence in an array

```
// Time Complexity: O(nlogn)
int lis(vector<int> const& a) {
    int n = a.size();
    const int INF = 1e9;
    vector<int> d(n+1, INF);
    d[0] = -INF;

    for (int i = 0; i < n; i++) {
        int l = upper_bound(d.begin(),
d.end(), a[i]) - d.begin();
        if (d[l-1] < a[i] && a[i] < d[l])
            d[l] = a[i];
    }

    int ans = 0;
    for (int l = 0; l <= n; l++) {
        if (d[l] < INF)
```

```
        ans = l;
    }
    return ans;
}
```

#### // This is the impl of KMP pattern

```
matching of a substring to string
// Time Complexity: O(n)
vector<int> prefix_function(string s) {
    int n = (int)s.length();
    vector<int> pi(n);
    for (int i = 1; i < n; i++) {
        int j = pi[i-1];
        while (j > 0 && s[i] != s[j])
            j = pi[j-1];
        if (s[i] == s[j])
            j++;
        pi[i] = j;
    }
    return pi;
}
```

#### // An LCA implementation in graph using Binary Lifting

```
// Time Complexity: O(log(n))
int n, l;
vector<vector<int>> adj;

int timer;
vector<int> tin, tout;
vector<vector<int>> up;

void dfs(int v, int p)
{
    tin[v] = ++timer;
    up[v][0] = p;
    for (int i = 1; i <= l; ++i)
        up[v][i] = up[up[v][i-1]][i-1];

    for (int u : adj[v]) {
        if (u != p)
            dfs(u, v);
    }
}
```

```
    tout[v] = ++timer;
}

bool is_ancestor(int u, int v)
{
    return tin[u] <= tin[v] && tout[u]
>= tout[v];
}
```

```
int lca(int u, int v)
{
    if (is_ancestor(u, v))
        return u;
    if (is_ancestor(v, u))
        return v;
    for (int i = l; i >= 0; --i) {
        if (!is_ancestor(up[u][i], v))
            u = up[u][i];
    }
    return up[u][0];
}
```

```

void preprocess(int root) {
    tin.resize(n);
    tout.resize(n);
    timer = 0;
    l = ceil(log2(n));
    up.assign(n, vector<int>(l + 1));
    dfs(root, root);
}

//can be put in a knapsack of capacity W
// here, wt is the weight array, val is the
// value array of each item, and n is no of
// item
// w is the capacity
int knapSack(int W, int wt[], int val[],
int n) {

    // Base Case
    if (n == 0 || W == 0)
        return 0;

    // If weight of the nth item is more
    // than Knapsack capacity W, then
    // this item cannot be included
    // in the optimal solution
    if (wt[n - 1] > W)
        return knapSack(W, wt, val, n -
1);

    // Return the maximum of two cases:
    // (1) nth item included
    // (2) not included
    else
        return max(
            val[n - 1]
            + knapSack(W - wt[n - 1],
            wt, val, n - 1),
            knapSack(W, wt, val, n - 1));
}

// Using substring Hash
int count_unique_substrings (string
const& s) {
    int n = s.size();

    const int p = 31;
    const int m = 1e9 + 9;
    vector<long long> p_pow(n);
    p_pow[0] = 1;
    for (int i = 1; i < n; i++)
        p_pow[i] = (p_pow[i-1] * p) % m;

    vector<long long> h(n + 1, 0);
    for (int i = 0; i < n; i++)
        h[i+1] = (h[i] + (s[i] - 'a' + 1) *
p_pow[i]) % m;

    int cnt = 0;
    for (int l = 1; l <= n; l++) {
        unordered_set<long long> hs;
        for (int i = 0; i <= n - l; i++) {
            long long cur_h = (h[i + l] + m
- h[i]) % m;

            cur_h = (cur_h * p_pow[n-i-1])
% m;
            hs.insert(cur_h);
        }
        cnt += hs.size();
    }
    return cnt;
}

// Polynomial Rolling Hash impl of a
// string with low collision rate
long long compute_hash(string const&
s) {
    const int p = 31;
    const int m = 1e9 + 9;
    long long hash_value = 0;
    long long p_pow = 1;
    for (char c : s) {
        hash_value = (hash_value + (c -
'a' + 1) * p_pow) % m;
        p_pow = (p_pow * p) % m;
    }
    return hash_value;
}

// The number of relative primes in a
// given interval
// Using inclusion & exclusion
principle
int solve (int n, int r) {
    vector<int> p;
    for (int i=2; i*i<=n; ++i)
        if (n % i == 0) {
            p.push_back (i);
            while (n % i == 0)
                n /= i;
        }
    if (n > 1)
        p.push_back (n);

    int sum = 0;
    for (int msk=1; msk<(1<<p.size());
++msk) {
        int mult = 1,
        bits = 0;
        for (int i=0; i<(int)p.size(); ++i)
            if (msk & (1<<i)) {
                ++bits;
                mult *= p[i];
            }

        int cur = r / mult;
        if (bits % 2 == 1)
            sum += cur;
        else
            sum -= cur;
    }

    return r - sum;
}

// Permutation, Combination,
// Inverse Exponentiation, Binary
// Exponentiation
const int N = 5e5 + 10, mod = 1e9 + 7;
ll fact[N];
/*
fact[0] = 1;
for (int i = 1; i < N; ++i)
{
    fact[i] = (fact[i - 1] * i) % mod;
}
*/
long long inverseExponentiation(long
long a)
{
    return ((a <= 1) ? (a) : mod - (mod /
a) * inverseExponentiation(mod % a)
% mod);
}
long long combination(long long n,
long long r)
{
    return (fact[n] *
inverseExponentiation(fact[r]) % mod)
* inverseExponentiation(fact[n - r]) %
mod;
}
long long permutation(long long n,
long long r)
{
    return (fact[n] *
inverseExponentiation(fact[n - r]) %
mod);
}
long long binaryExponentiation(long
long base, long long power)
{
    long long carry = 1 % mod;
    long long x = base % mod;
    while (power)
    {
        if (power & 1)
            carry = (__int128_t)(carry * x)
% mod;
        x = (__int128_t)(x * x) % mod;
        power = power >> 1;
    }
    return carry % mod;
}

// Chinese Remainder Theorem(CRT),
// modularInverse, extendedGCD
// Function to calculate gcd and
// extended gcd
ll extendedGCD(ll a, ll b, ll &x, ll &y)
{
    if (b == 0)
    {
        x = 1;
        y = 0;
        return a;
    }
    ll x1, y1;
    ll gcd = extendedGCD(b, a % b, x1,
y1);

```



```

    x = y1;
    y = x1 - (a / b) * y1;
    return gcd;
}

// Function to compute modular inverse
of 'a' under modulo 'm'
ll modularInverse(ll a, ll m)
{
    ll x, y;
    ll gcd = extendedGCD(a, m, x, y);
    if (gcd != 1)
    {
        return -1;
    }
    return (x % m + m) % m;
}

// Chinese Remainder Theorem
implementation
// ans =
chineseRemainderTheorem(rem, num);
ll
chineseRemainderTheorem(vector<ll>
&rem, vector<ll> &num)
{
    ll prod = 1LL;
    for (ll ni : num)
        prod *= ni;

    ll result = 0;
    for (size_t i = 0; i < rem.size(); i++)
    {
        ll partialProd = prod / num[i];
        ll inv =
modularInverse(partialProd, num[i]);

        result += rem[i] * partialProd *
inv;
        result %= prod;
    }
    return (result + prod) % prod;
}

-----

// Trailing zero number of n ! :
ll findTrailingZerosOf_n_Factorial(ll n)
{
    if (n < 0)
        return -1;
    ll count = 0;
    for (ll i = 5; n / i >= 1; i *= 5)
        count += n / i;
    return count;
}

-----

// Inversion Count : O(nlogn)
void solve(ll t)
{
    ll n;
    cin >> n;
    ll s[n];
    for (int i = 0; i < n; i++)
        cin >> s[i];

    ll s1 = 0;
    ordered_set o_set;
    for (ll i = n - 1; i >= 0; i--)
    {
        s1 += o_set.order_of_key(s[i]);
        o_set.insert(s[i]);
    }
    cout << s1 << endl;
}

// Order set :
#include
<ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

#define ordered_set tree<int, null_type,
less<int>, rb_tree_tag,
tree_order_statistics_node_update>
ordered_set o_set;
/ insert function to insert in
// ordered set same as SET STL
o_set.insert(5);
o_set.insert(1);
o_set.insert(2);

// Finding the second smallest element
// in the set using * because
// find_by_order returns an iterator
cout << *(o_set.find_by_order(1)) <<
endl;

// Finding the number of elements
// strictly less than k=4
cout << o_set.order_of_key(4) <<
endl;

// Finding the count of elements less
// than or equal to 4 i.e. strictly less
// than 5 if integers are present
cout << o_set.order_of_key(5) <<
endl;

// Deleting 2 from the set if it exists
if (o_set.find(2) != o_set.end())
    o_set.erase(o_set.find(2));

// Now after deleting 2 from the set
// Finding the second smallest element
in the set
cout << *(o_set.find_by_order(1)) <<
endl;

// Finding the number of
// elements strictly less than k=4
cout << o_set.order_of_key(4) <<
endl;

```

-> next\_permutation(s1.begin(), s1.end()); s1 = "ABC" -> s1 = "ACB"; ইহা s1 string এর index/character swap করে।

-> \_\_builtin\_popcount(Bit\_int01); Bit\_int01 = 10; -> 2 ইহা Bit\_int01 এর 1 বিট গণনা করে।

-> v.erase(unique(v.begin(), v.end()), v.end()) ইহা সব প্রতিলিপি মুছে ফেলে।

-> n তম পদ =  $a + (n-1) * d$

-> প্রথম n তম পদের সমষ্টি,  $S_n = (n/2) * \{2*a + (n-1)*d\}$

-> n তম পদ =  $a * r^{(n-1)}$

-> প্রথম n তম পদের সমষ্টি,  $S_n = (a) * \{ (r^n - 1) / (r - 1) \}$  if  $r > 1$   
 $S_n = (a) * \{ (1 - r^n) / (1 - r) \}$  if  $r < 1$

->  $A^{(p-1)} = 1 \text{ mod } (M)$  — Fermat theorem

-> Sum of divisor =  $\{(P1^{(n1+1)}-1)/(p1-1)\} * \{(P2^{(n2+1)}-1)/(p2-1)\} * \dots * \{(Pn^{(nn+1)}-1)/(pn-1)\}$  // here n is the number of P that can divide the value.

-> Number of divisor of  $P1^a * P2^b * \dots * Pn^v = (a+1) * (b+1) * \dots * (v+1)$

->  $1^2 + 2^2 + \dots + n^2 = \{ n * (n+1) * (2*n+1) \} / 6$

->  $(a * 1/b) \% \text{mod} = (a * \text{bigmod}(b, m-2, m)) \text{ mod } m$

->  $a = \log_b c \Rightarrow b^a = c$

->  $nC0 + nC1 + nC2 + \dots + nCn = 2^n$

->  $nC0 + nC2 + nC4 + \dots = nC1 + nC3 + nC5 + \dots = 2^{(n-1)}$

->  $A \text{ xor } B = A \oplus B$

->  $a*x^2 + b*x + c = \{ -b \pm \text{Square Root}(b^2 - 4*a*c) \} / (2 * a)$

-> #define PI 2.0 \* acos(0.0)

-> upper\_bound(v.begin(), v.end(), value)-v.begin(); // return the index where you can store new value.

-> sort(v1.begin(), v1.end(), [&](vector<long long> &a, vector<long long> &b){  
return a[1]<b[1]; });

->