(REVISED COURSE)

QP Code: 11859

(3 Hours)

Total Marks: 80

N. B.: (1) Question No.1 is compulsory.

- (2) Attempt any three questions of the remaining five.
- (3) figures to the right indicate full marks.

1. (a) Evaluate
$$\int_{0}^{2} x^{4} (8-x^{3})^{-1/3} dx$$

(b) Solve
$$\frac{d^4y}{dx^4} + 2\frac{d^2y}{dx^2} + y = 0$$

(c) Prove that
$$E = 1 + \Delta = e^{4D}$$

(d) Solve
$$\left[x \sqrt{x^2 + y^2} - y \right] dx + \left[y \sqrt{x^2 + y^2} - x \right] dy = 0$$

(e) Change to polar coordinates and evaluate
$$\int_{0}^{2 \text{ ax} - x^{2}} \frac{x}{\sqrt{x^{2} + y^{2}}} dy dx$$

(f) Evaluate
$$\int_{\partial \partial}^{1} e^{x+y} dy dx$$
.

2. (a) Solve
$$\frac{dy}{dx} + x \sin 2y = x^3 \cos^2 y$$

(b) Change the order of integration and evaluate
$$\int_{0}^{a} \int_{y^{2}/a}^{y} \frac{y}{(a-x)\sqrt{ax-y^{2}}} dxdy$$

(c) Prove that
$$\int_{\partial}^{\infty} \cos \lambda x \left(e^{-ax} - e^{-bx} \right) dx = \frac{1}{2} \log \left(\frac{b^2 + \lambda^2}{a^2 + \lambda^2} \right), \text{ a>0, b>0 using DUIS}$$
 8 rule

3. (a) Evaluate
$$\iiint_{x^2 + y^2 + z^2 = a^2} \frac{dx dy dz}{x^2 + y^2 + z^2}$$
 throughout the volume of the sphere

(b) Find the area common to the cardiods
$$r = a(1+\cos\theta)$$
 and $r = a(1-\cos\theta)$.

$$\frac{d^2y}{dx^2} - 4\frac{dy}{dx} + 4y = e^{2x} \sec^2 x$$

4. (a) Find the length of one arc of the cycloid
$$x = a(\theta - \sin \theta)$$
 and $y = a(1 + \cos \theta)$

(b) Solve
$$\frac{d^2y}{dx^2} + 2y = x^2e^{3x} + e^x \cos x$$

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- (c) Apply Runge- kutla method of fourth order to find an approximate value of y at x = 1.2 if $\frac{dy}{dx} = x^2 + y^2$, given that y = 1.5 when x = 1 choosing h = 0.1
- 5. (a) Solve $[xy^2 e^{1/x^3}] dx yx^2 dy = 0$
 - (b) If y satisfies the equation $\frac{dy}{dx} = x^2y 1$ and with y = 1 when x = 0, using 5 Taylor's series method for y about x = 0, find y when x = 0.1 and x = 0.2
 - (c) Compute the value of the definite integral $\int_{-1}^{1} \frac{dx}{1+x^2}$ by using
 - (i) Trapezoidal rule
 - (ii) Simpson's $\left(\frac{1}{3}\right)^{rd}$ rule
 - (iii) Simpson's $(\frac{3}{8})^{th}$ rule. Compare result with exact values.
- 6. (a) A radial displacement 'u' in rotating a disc at a distance 'r' from the axis in given by $\frac{d^2u}{dr^2} + \frac{1}{r}\frac{du}{dr} \frac{u}{r^2} + kr = 0$. Find the displacement given u = 0 when r = 0 and r = a
 - (b) Evaluate $\iint x^2 dxdy$ over the region bounded by $xy = a^2$, x = 2a, y = 0 and y = x 6 in the first quadrant.
 - (c) Find the volume of the tetrahecron bounded by the co-ordinate planes and the plane $\frac{x}{2} + \frac{y}{3} + \frac{z}{4} = 1$