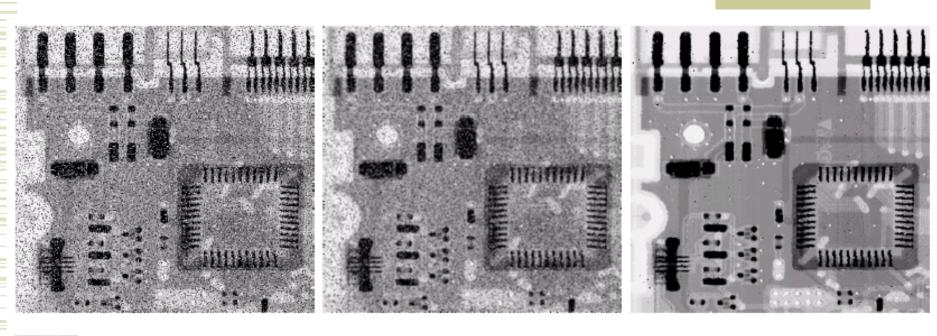
Digital Image Processing

Lecture # 3C Spatial Filtering

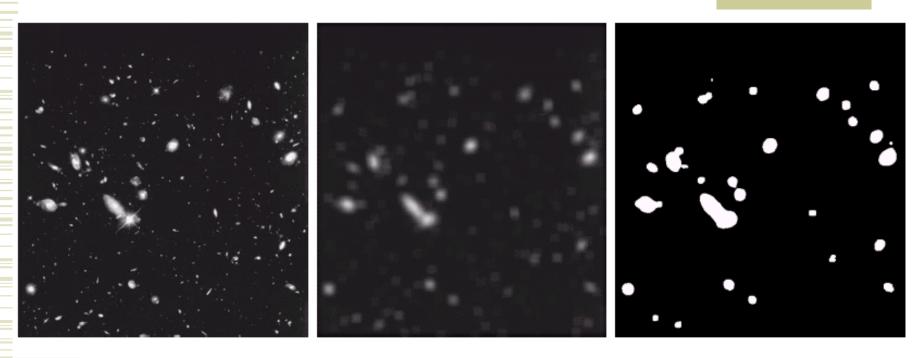
Spatial Filtering



a b c

FIGURE 3.37 (a) X-ray image of circuit board corrupted by salt-and-pepper noise. (b) Noise reduction with a 3 × 3 averaging mask. (c) Noise reduction with a 3 × 3 median filter. (Original image courtesy of Mr. Joseph E. Pascente, Lixi, Inc.)

Spatial Filtering



a b c

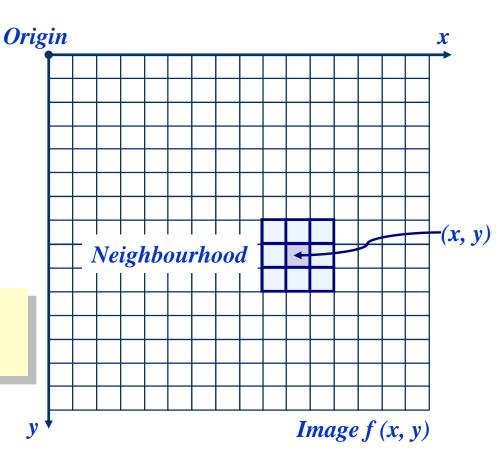
FIGURE 3.36 (a) Image from the Hubble Space Telescope. (b) Image processed by a 15 × 15 averaging mask. (c) Result of thresholding (b). (Original image courtesy of NASA.)

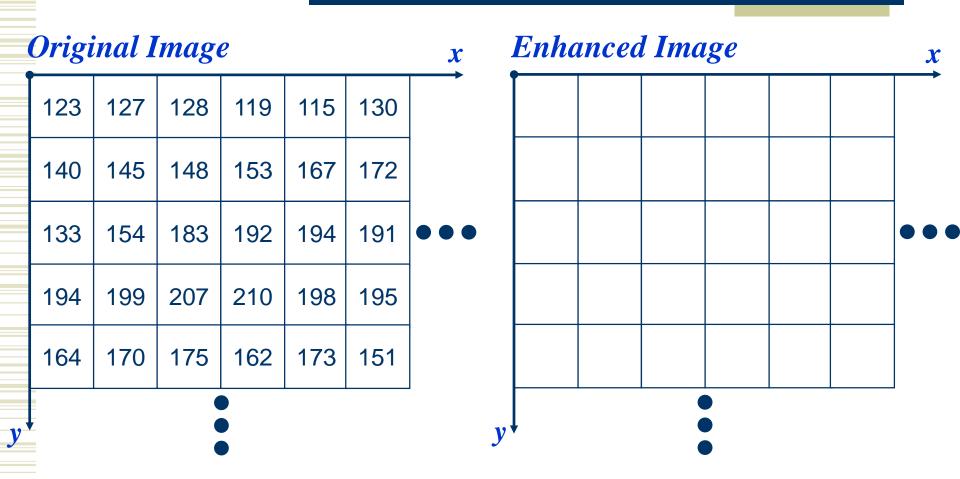
Contents

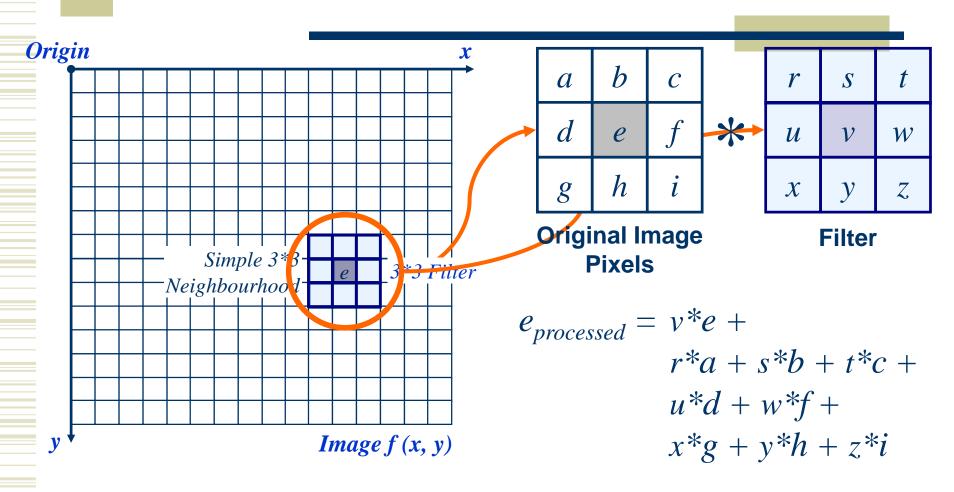
- Basics of Spatial Filtering
- Smoothing Spatial Filters
 - Average Filter
 - Median Filter

Neighbourhood operations:
Operate on a larger
neighbourhood of pixels
than point operations

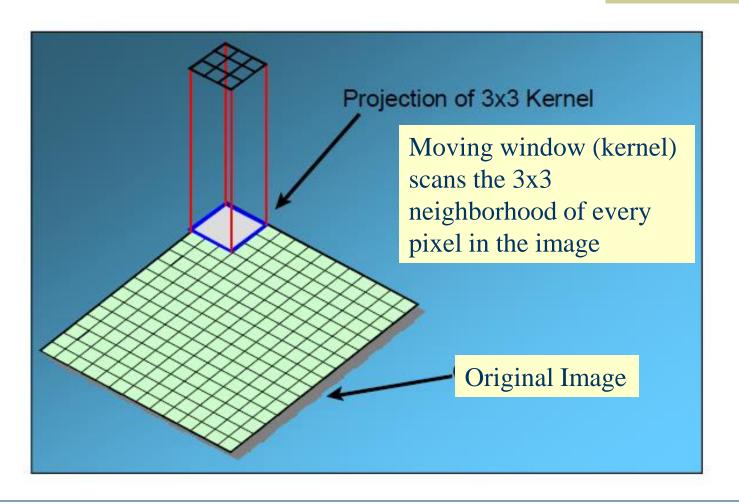
Neighbourhoods are mostly a rectangle around a central pixel

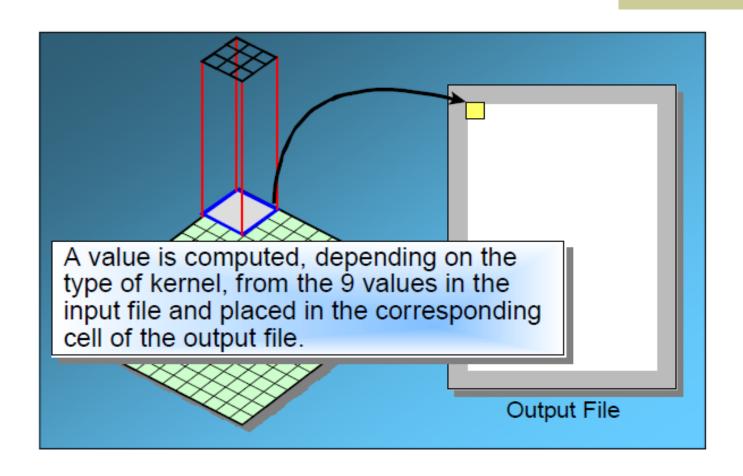


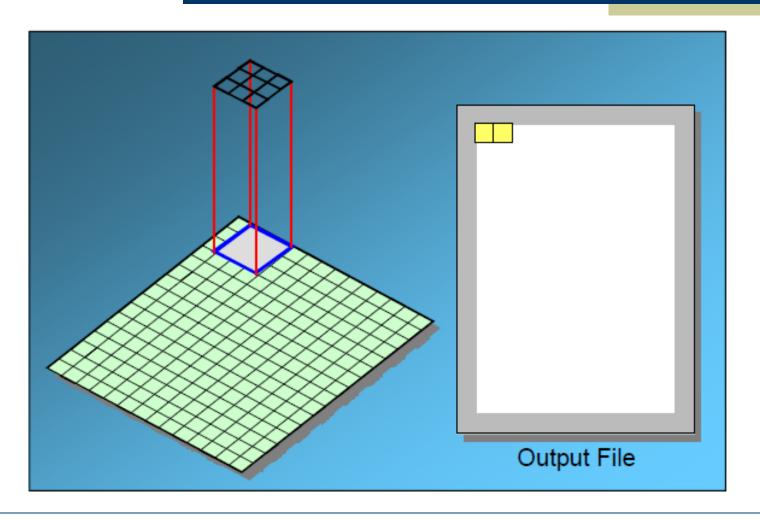


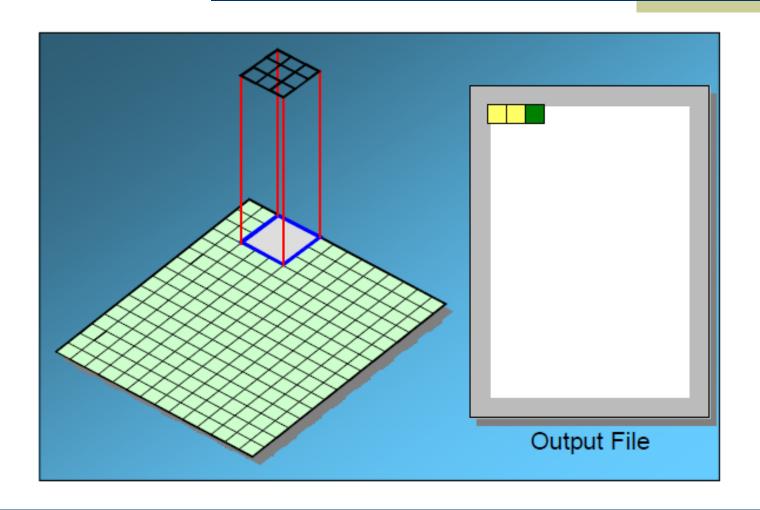


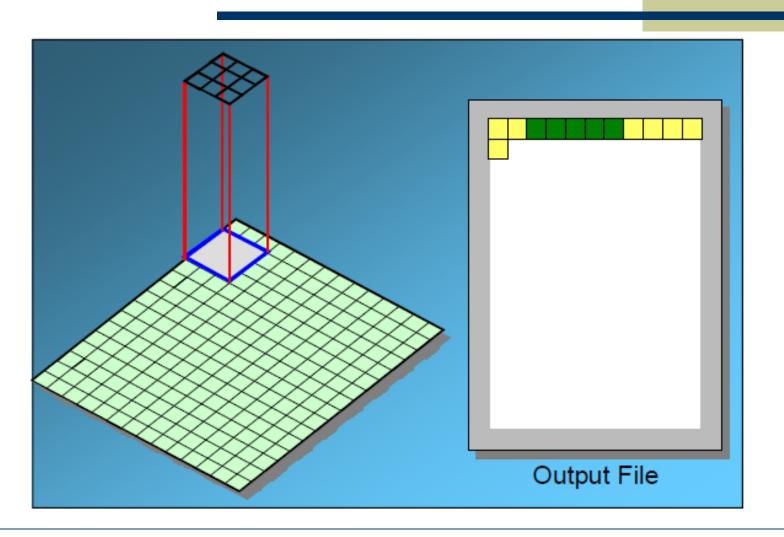
The above is repeated for every pixel in the original image to generate the filtered image

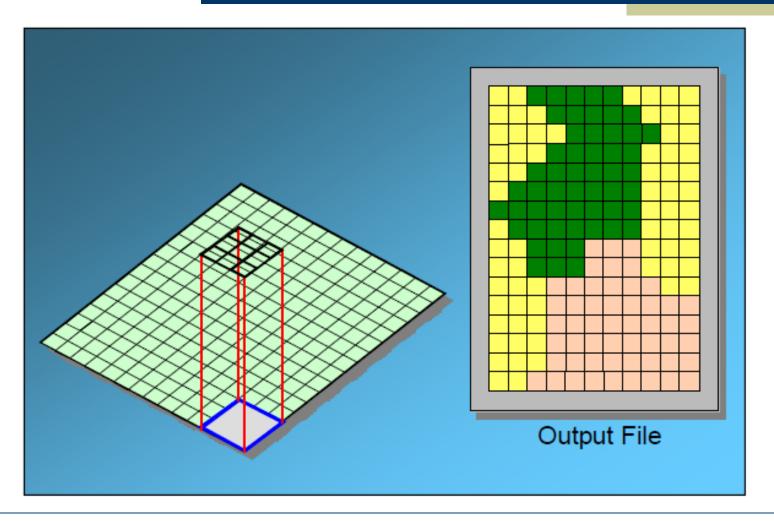












Mask operation near the image border: Problem arises when part of the mask is located outside the image plane

Discard the problem pixels (e.g. 512x512 input 510x510 output if mask size is 3x3)

Zero padding: Expand the input image by padding zeros (512x512 original image, 514x514 padded image, 512x512 output)

Zero padding is not recommended as it creates artificial lines or edges on the border **Pixel replication: We**

normally use the gray levels of border pixels to fill up the expanded region (for 3x3 mask). For larger masks a border region equal to half of the mask size is mirrored on the expanded region.

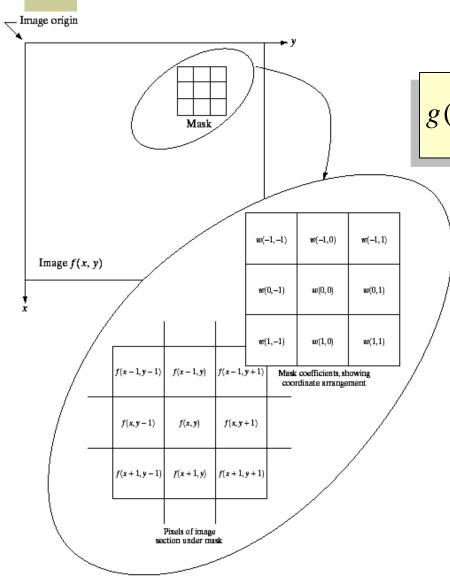
Mask operation near the border: Pixel replication

_								
	102	102	130	143	123	115		
	102	102	130	143	123	115		
	93	93						
	98	98						
	82	82						
	65	65						
	^							
Expanded area Original image size					size			

Engr. Afzal Ahmed

(shaded area)

- ◆ The output intensity value at (x,y) depends not only on the input intensity value at (x,y) but also on the specified number of neighboring intensity values around (x,y)
- Spatial masks (also called window, filter, kernel, template) are used and convolved over the entire image for local enhancement (spatial filtering)
- The size of the masks determines the number of neighboring pixels which influence the output value at (x,y)
- The values (coefficients) of the mask determine the nature and properties of enhancing technique



$$g(x, y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s, t) f(x+s, y+t)$$

where
$$a = \frac{m-1}{2}$$
, $b = \frac{n-1}{2}$
 $x = 0, 1, 2, ..., M-1, y = 0, 1, 2, ..., N-1$

Filtering can be given in equation form as shown above

- ◆ Given the 3×3 mask with coefficients: w₁, w₂,..., w₂
- ◆ The mask cover the pixels with gray levels: z₁, z₂,..., z₂

\mathbf{w}_1	\mathbf{w}_2	\mathbf{w}_3
W_4	W_5	\mathbf{w}_{6}
W_7	W ₈	W ₉

\mathbf{z}_1	\mathbf{Z}_2	\mathbf{z}_3
\mathbf{Z}_4	\mathbf{Z}_5	Z ₆
Z ₇	z_8	Z_9

$$z \longleftarrow z_1 w_1 + z_2 w_2 + z_3 w_3 + \dots + z_9 w_9 = \sum_{i=1}^9 z_i w_i$$

• z gives the output intensity value for the processed image (to be stored in a new array) at the location of z_5 in the input image

Smoothing Spatial Filters

- For blurring/noise reduction
- ◆Blurring is usually used in preprocessing steps, e.g., to remove small details from an image prior to object extraction, or to bridge small gaps in lines or curves
- ◆Equivalent to Low-pass spatial filtering in frequency domain because smaller (high frequency) details are removed based on neighborhood averaging (averaging filters)

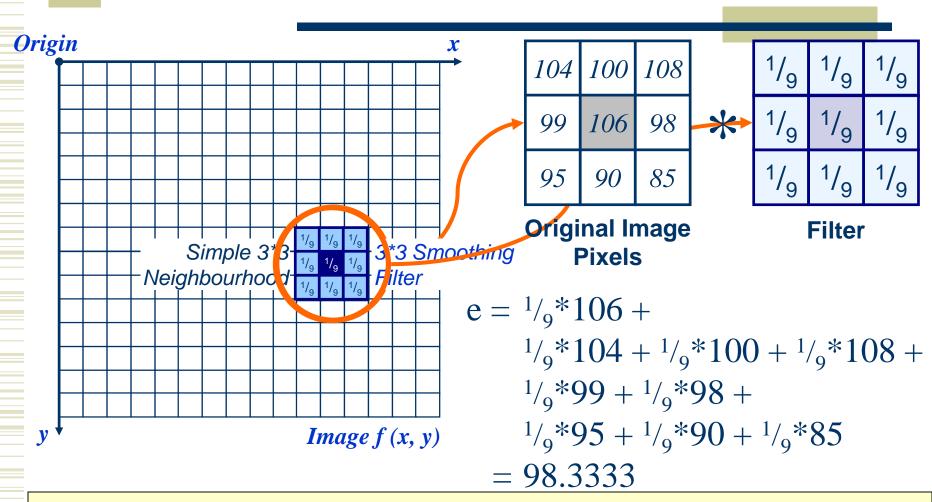
Smoothing Spatial Filters

Simply average all of the pixels in a neighbourhood around a central value

1/9	1/9	1/9
1/9	1/9	1/9
1/9	1/9	1/9

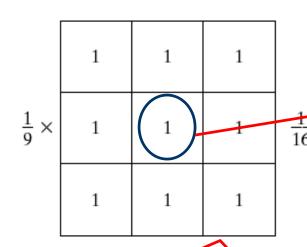
Simple averaging filter

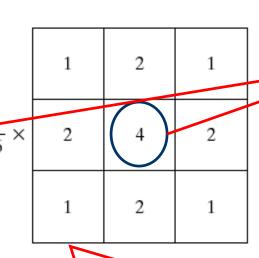
Average Filter



The above is repeated for every pixel in the original image to generate the smoothed image

Average Filter





Consider the output pixel is positioned at the center

Box Filter all coefficients are equal

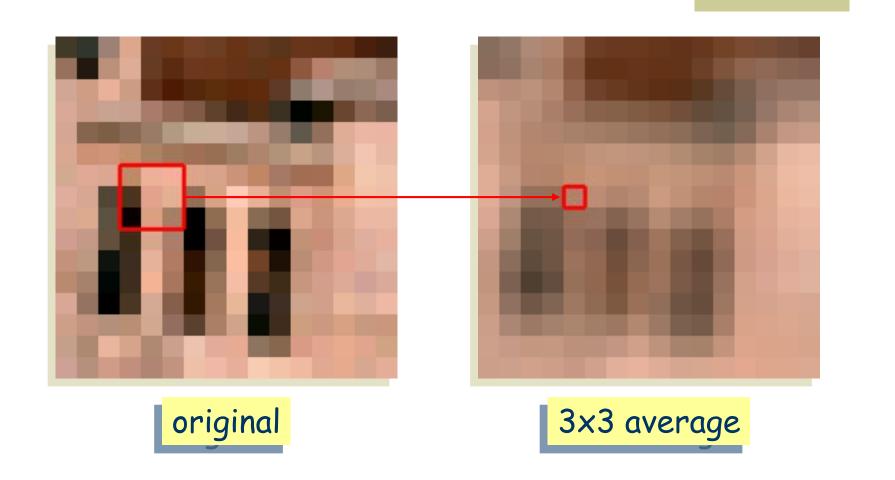
Weighted Average give more (less) weight to near (away from) the output location

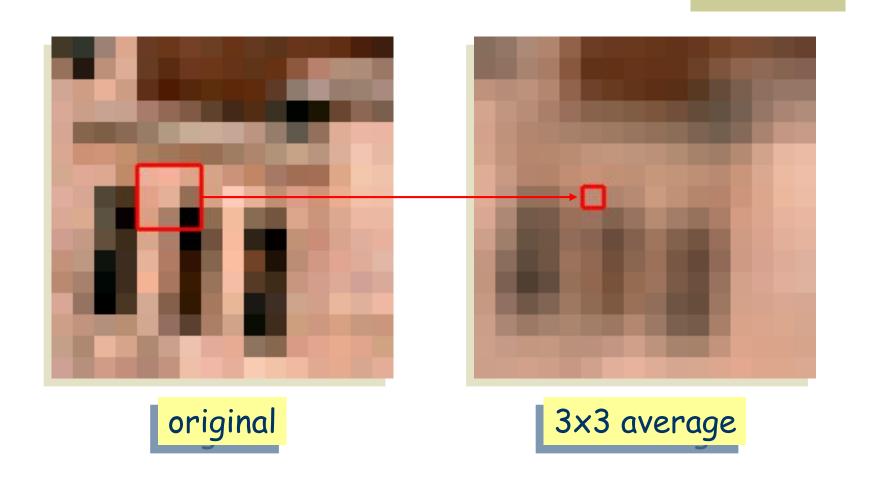


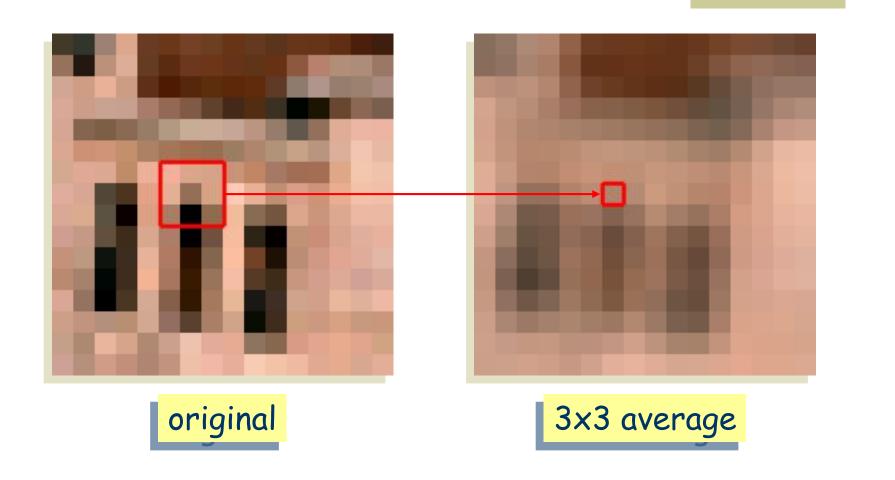
original



3x3 average

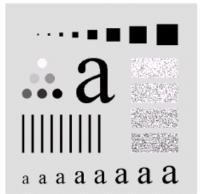


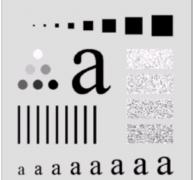




Original image

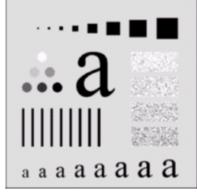
Size: 500x500





Smooth by 3x3 box filter

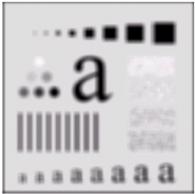
Smooth by 5x5 box filter





Smooth by 9x9 box filter

Smooth by 15x15 box filter





Smooth by 35x35 box filter

Notice how detail begins to disappear

Order-Statistic Filtering

- Output is based on order of gray levels in the masked area
- Some simple neighbourhood operations include:
 - Min: Set the pixel value to the minimum in the neighbourhood
 - Max: Set the pixel value to the maximum in the neighbourhood
 - Median: The median value of a set of numbers is the midpoint value in that set

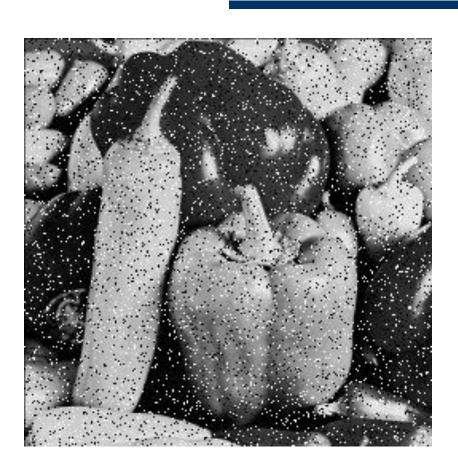
10	20	20
20	15	20
20	25	100

Sort the values
Determine the median

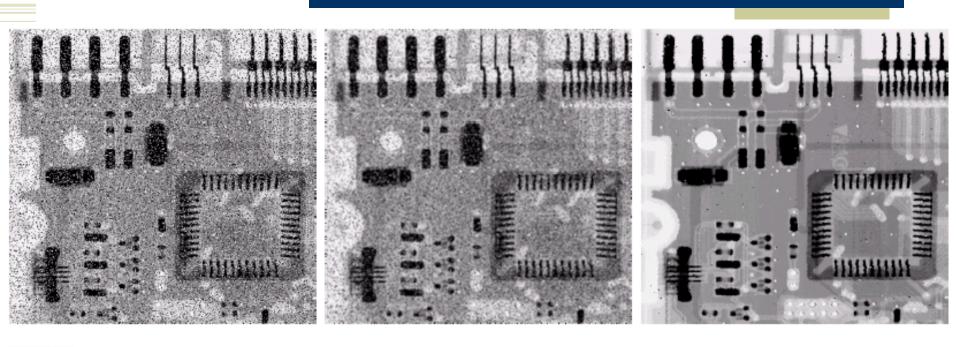
Median = ?20

- Particularly effective when
 - The noise pattern consists of strong impulse noise (salt-and-pepper)

Salt and Pepper Noise

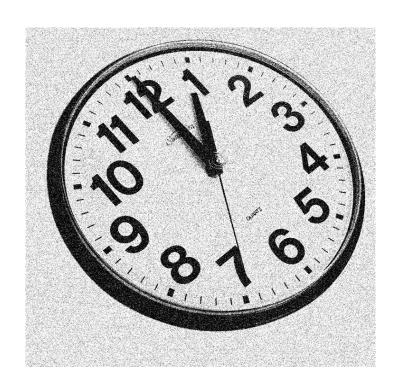






a b c

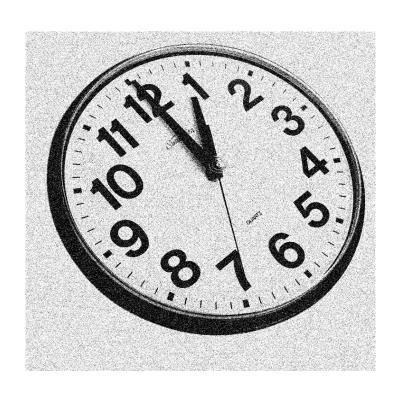
FIGURE 3.37 (a) X-ray image of circuit board corrupted by salt-and-pepper noise. (b) Noise reduction with a 3 × 3 averaging mask. (c) Noise reduction with a 3 × 3 median filter. (Original image courtesy of Mr. Joseph E. Pascente, Lixi, Inc.)

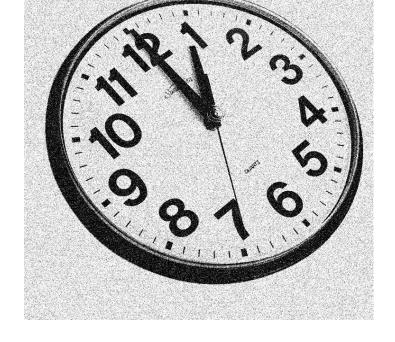


Noisy



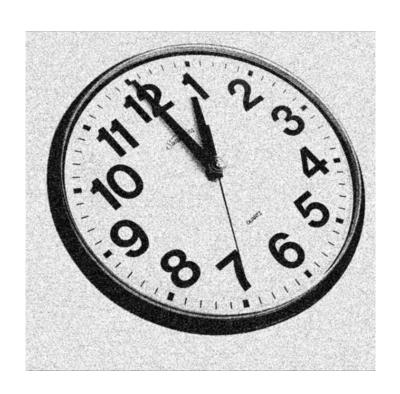
Original



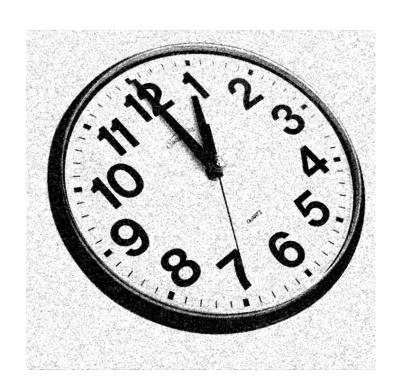


Noisy

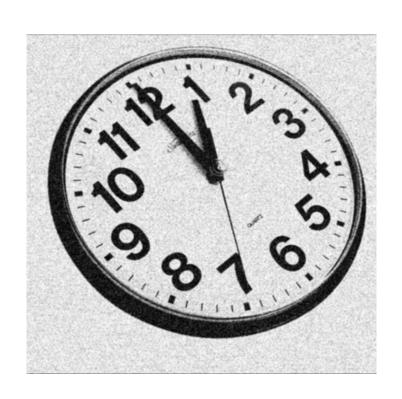
Noisy



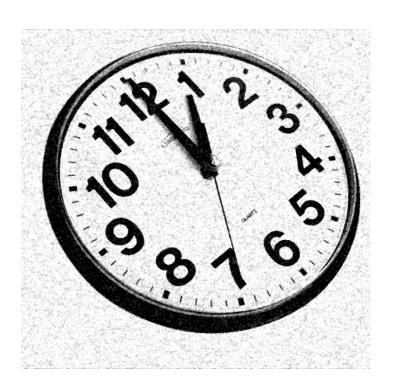
3x3-blur x 1



3x3-median x 1



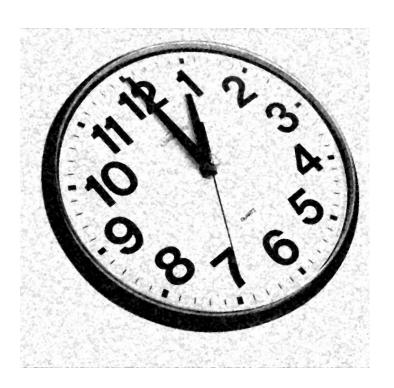
3x3-blur x 2



3x3-median x 2



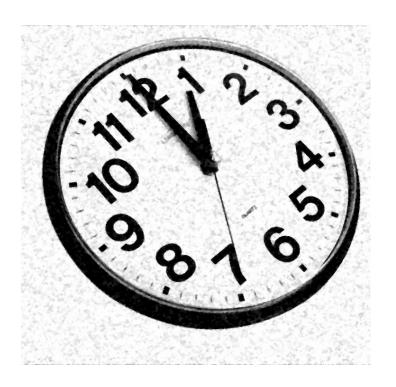
3x3-blur x 5



3x3-median x 5



3x3-blur x 10



3x3-median x 10

Acknowledgements

- Digital Image Processing", Rafael C. Gonzalez & Richard E. Woods, Addison-Wesley, 2002
- Peters, Richard Alan, II, Lectures on Image Processing, Vanderbilt University, Nashville, TN,
 April 2008
- Brian Mac Namee, Digitial Image Processing, School of Computing, Dublin Institute of Technology
- Computer Vision for Computer Graphics, Mark Borg