

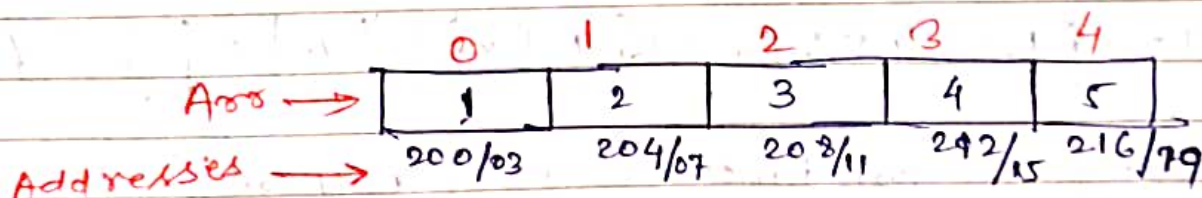
Arrays Representation

Array:- Array is a collection of elements. & all the elements are same data types, grouped under one name.

eg: `int arr[5] = {1, 2, 3, 4, 5}` Index values.
↑
Size of Array

* arrays are vectors vector values

* If a single 'int' value take 4 bytes then the above array will take $4 \times 5 (\text{Size}) = 20$ bytes.



of the
values inside
array

* we can access the element of array using index value. or assign

eg: `cout << A[2];` // o/p = 3.

* Declaration of Array *

`int arr[5] = {1, 2, 3, 4, 5};` `arr` →

| | | | | |
|---|---|---|---|---|
| 0 | 1 | 2 | 3 | 4 |
| 1 | 2 | 3 | 4 | 5 |

↓
Declaration + Initialization

`int arr[5];` /* Declaration */ with array size 5.

↳ `arr` →

| | | | | |
|---|---|---|---|---|
| 0 | 1 | 2 | 3 | 4 |
| ? | ? | - | - | - |

↳ any garbage value.

`int arr[5] = {1, 2};` `arr` →

| | | | | |
|---|---|---|---|---|
| 0 | 1 | 2 | 3 | 4 |
| 1 | 2 | 0 | 0 | 0 |

`int arr[5] = {0};` `arr` →

| | | | | |
|---|---|---|---|---|
| 0 | 1 | 2 | 3 | 4 |
| 0 | 0 | 0 | 0 | 0 |

`int arr[6] = {1, 2, 3, 4, 5, 6};` →

| | | | | | |
|---|---|---|---|---|---|
| 0 | 1 | 2 | 3 | 4 | 5 |
| 1 | 2 | 3 | 4 | 5 | 6 |

* During the run time the array will be created inside the memory (Stack/Heap) and assigning the values.

* using for loop we can traverse inside the array and we can easily access the element.
eg!

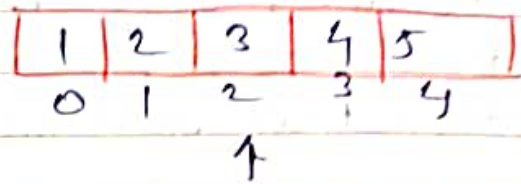
```
for (int i = 0; i < 6; i++) {  
    cout << A[i] << " ";  
}
```

o/p: 1 2 3 4 5 6

* Multiple ways to accessing the elements.

cout << 2[A];

cout << *(A+2);



* Address of the element inside array is contiguous.

Static v/s Dynamic Array

```
void main()
```

```
{
```

```
    int A[5];
```

→ This array will create inside stack.

* the size of the array was decided at the compile time.

* Memory is allocated at the runtime.

* we can create any size of array during runtime.

In C++ and it

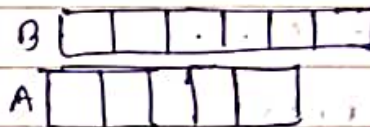
will created inside stack only.

eg:

```
int n;
```

```
cin >> n; // input :- 5
```

```
int B[n];
```



```
main() {
```

```
    --
```

```
    --
```

```
}
```

* The array which is created inside heap memory, that's array size and memory, both are decided at runtime.

* we can use "new" keyword for creating an array inside heap memory.

* For accessing anything which is inside heap memory we required pointer variables or the pointers.
int * ptr;

* we cannot access the objects which are created inside heap without pointers.

Eg:

```
void main()
```

```
int ar[5];
```

```
int *ptr;
```

* the pointer variable is created inside stack and it will store the address of the object/array.

```
ptr = new int[5];
```

* we can access the heap object using pointer.

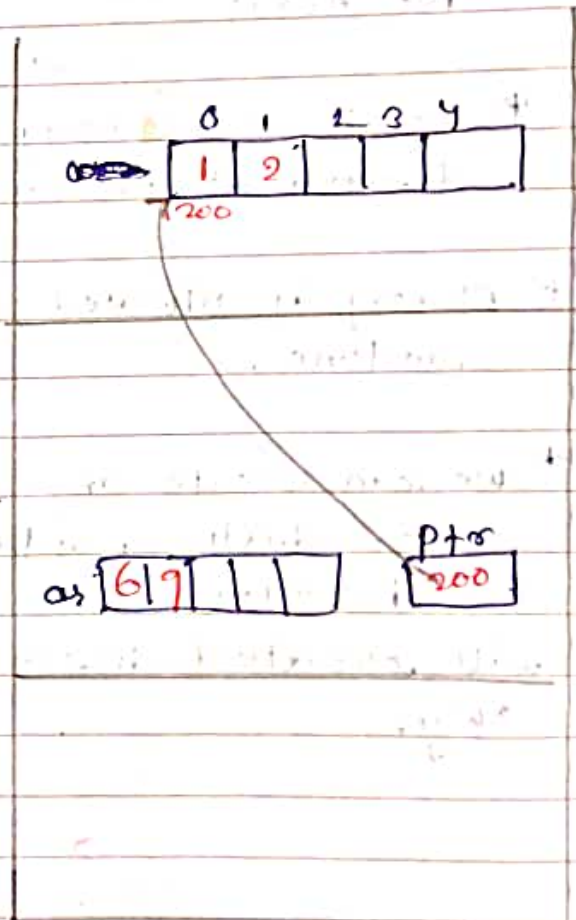
eg:

```
ptr[0] = 1;
```

```
ptr[1] = 2;
```

```
ar[0] = 6;
```

```
ar[1] = 9;
```



In 'C' language we can create array inside heap such way.

```
int arr[5];
```

```
int *ptr;
```

```
ptr = (int *) malloc (5 * sizeof(int));
```

* After the execution of program ^{or} if the memory of heap not required then we must deallocate the memory from heap.

* If we cannot do it, then it may cause memory ~~leak~~ leak.

* In c++ we can delete the unused memory using delete keyword.

eg: `delete []p;`

* In 'C' language we use free:

eg:

`free(p);`

* Once the array of some size is created (heap/stack) then it cannot be resize.

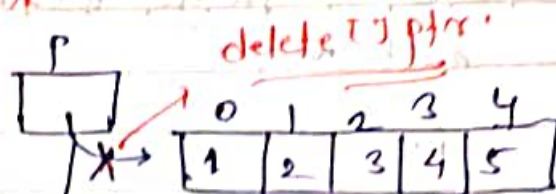
* If we want to increase the size of the array then it is possible only inside heap, but the same array's size cannot be increased.

↳ There is some alternative ways, to increase.

* Inside stack the size of the array cannot increase.

* How to Increase Array Size *

int *ptr = new int[5];



int *ptr2 = new int[newsize];

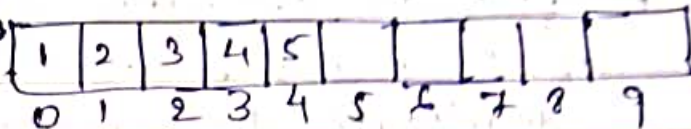
eg: newsize = 10;

for (int i=0; i<5; ++i)

ptr2[i] = ptr[i];

ptr = ptr2; ptr2 = NULL;

*ptr2



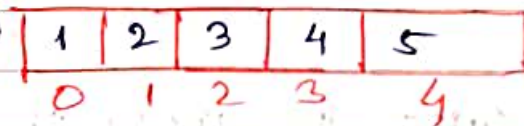
ptr = ptr2;

* If we want to increase the size then create another array with bigger size and copy all the elements from previous to new array.

* then, delete[] ptr, pointer, and assign "ptr = ptr2" so, first pointer also points to the new array and make second pointer NULL, so, it will remove and the previous array deleted from the memory.

Eg:

int *p = new int[5];



int *q = new int[10];



for (int i=0; i<5; ++i)

q[i] = p[i]; // all the element copied to q

delete[] p

p = q;

q = NULL;

Now the p pointing to the new array.

2D Array

2-Dimension Array

* Declaration of 2D Array!

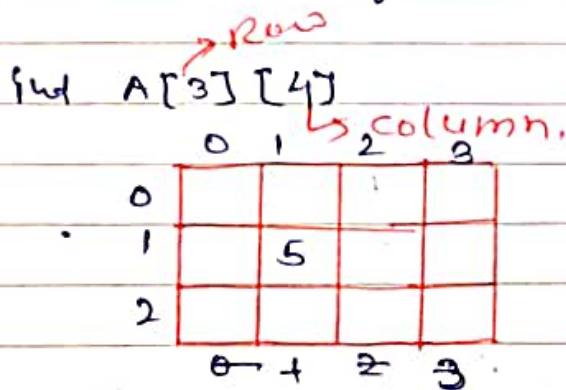
"Method 1:"

① `int A[3][4];`

`int B[3][4] = { {1, 2, 3, 4}, {2, 4, 6, 8}, {3, 6, 9, 12} }`

// Initialization & Declaration.

Representation of 2D Array:

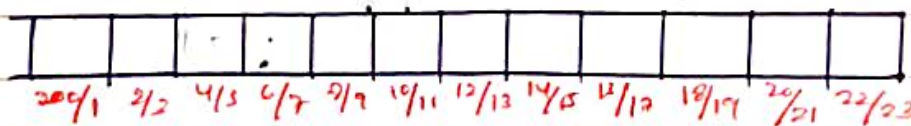


we can access element inside a 2D array using both i row and column.

Eg:

`A[1][1] = 5;`

* 2D Array Represent inside memory:



suppose

`int = 2 byte`

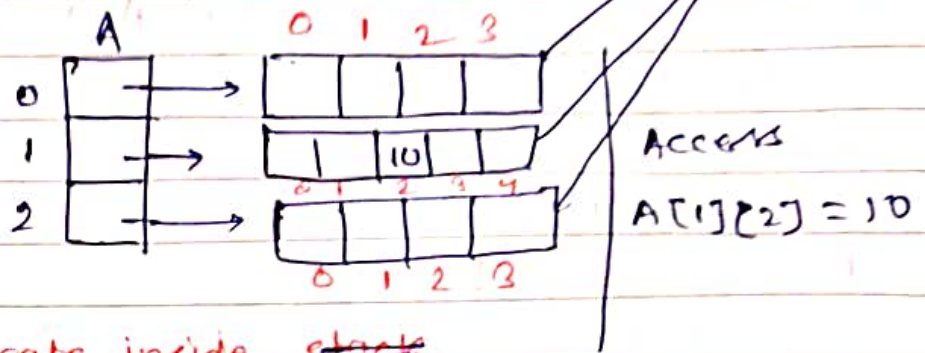
→ Addresses.

* this 2D array is created inside stack.

* Method 2 *

Array of integer pointers (stack)

int *A[3];
* using pointers *



* this array is also create inside stack
Eg: int *A[3];

A[0] = new int[4];

A[1] = new int[4];

A[2] = new int[4];

* Method 3 *

* using double pointer.

int **A; Declaration

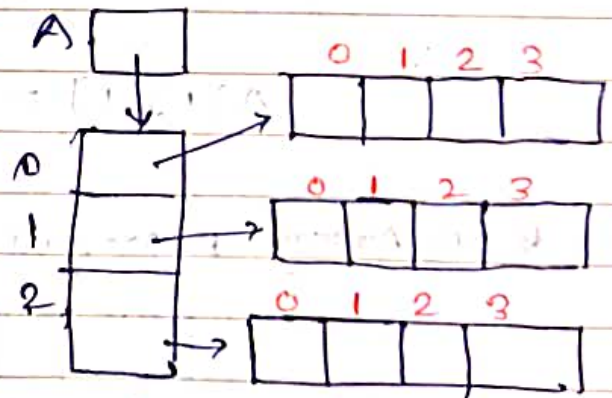
A = new int *[3]; inside heap

A[0] = new int[4];

A[1] = new int[4];

A[2] = new int[4];

inside heap



* Accessing any 2D Array, we can use nested for loops.

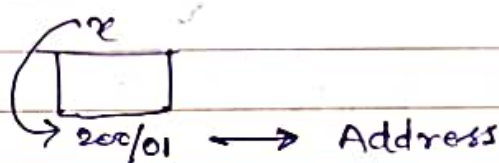
eg: `for (int i=0; i<3; ++i) {`

`for (int j=0; j<4; ++j) {`

`code of program
*/
}`

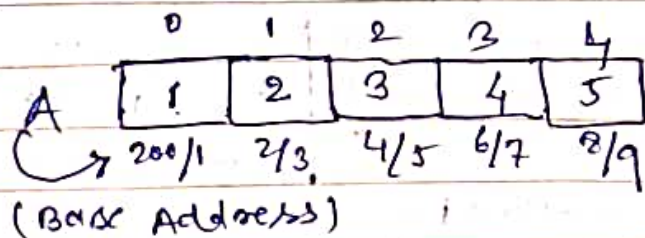
Array In Compiler

`int x = 10;`



* During execution the memory is allocated for the variables and it stores its corresponding address.

`int A[] = {1, 2, 3, 4, 5}`



`A[3] = 4`

formula

$$\text{add}(A[3]) = L_0 + 3 * \text{Size of (int)}$$

$$= 200 + 3 * 6$$

$$\text{add}(A[3]) = \boxed{206}$$

2, 4 byte

* $\text{Add}(A[i]) = \boxed{Lo + \text{index} * \text{sizeof}(\text{int})}$

Base Address \rightarrow 0 based indexing \rightarrow size of Data Type

index value

* 1 based indexing

$\text{Add}(A[i]) = \boxed{Lo + (\text{index} - 1) * \text{sizeof}(\text{int})}$

* Row Major formula * 2D *

`int A[3][4];`

eg! here `int = 2 byte`.

| | 0 | 1 | 2 | 3 |
|---|----------|----------|----------|----------|
| 0 | a_{00} | a_{01} | a_{02} | a_{03} |
| 1 | a_{10} | a_{11} | a_{12} | a_{13} |
| 2 | a_{20} | a_{21} | a_{22} | a_{23} |

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |
|---|-------|-----|-----|-----|-----|-------|-------|-------|-------|-------|-------|-------|----|----|----|----|----|----|----|----|----|----|----|----|
| A | | | | | | | | | | | | | | | | | | | | | | | | |
| | 200/1 | 2/3 | 4/5 | 6/7 | 8/9 | 10/11 | 12/13 | 14/15 | 16/17 | 18/19 | 20/21 | 22/23 | | | | | | | | | | | | |

This is how during execution 2D array look like in the compiler.

It will store the element row by row.

eg!

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
|-------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| Row 0 | a_{00} | a_{01} | a_{02} | a_{03} | a_{10} | a_{11} | a_{12} | a_{13} | a_{20} | a_{21} | a_{22} | a_{23} |
| Row 1 | | | | | | | | | | | | |
| Row 2 | | | | | | | | | | | | |

| | 0 | 1 | 2 | 3 |
|---|----------|----------|----------|----------|
| 0 | a_{00} | a_{01} | a_{02} | a_{03} |
| 1 | a_{10} | a_{11} | a_{12} | a_{13} |
| 2 | a_{20} | a_{21} | a_{22} | a_{23} |

$$\begin{aligned} \text{Add}[A[1][2]] &= 200 + [4+2] * 2 \\ &= 200 + 6 * 2 \\ &= 212 \end{aligned}$$

| | 0 | 1 | 2 | 3 | |
|---|---|---|---|---|---|
| 0 | | | | | 0 |
| 1 | | | | | 1 |
| 2 | | | | | 2 |

$$\begin{aligned} \text{Add}[A[2][1]] &= 200 + [2+4+1] * 2 \\ &= 200 + [9] * 2 \\ &= 218 \end{aligned}$$

$A[2][1]$

Formula:

$$\text{Add}[A[i][j]] = L_0 + [i * \text{column} + j] * \text{sizeof}(\text{int})$$

Base Address

* Column-major Representation:

`int A[3][4];`

* In column-major form all the elements are represented column by column.

| | 0 | 1 | 2 | 3 | → cols |
|---|----------|----------|----------|----------|--------|
| 0 | a_{00} | a_{01} | a_{02} | a_{03} | |
| 1 | a_{10} | a_{11} | a_{12} | a_{13} | |
| 2 | a_{20} | a_{21} | a_{22} | a_{23} | |

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| a_{00} | a_{10} | a_{20} | a_{01} | a_{11} | a_{21} | a_{02} | a_{12} | a_{22} | a_{03} | a_{13} | a_{23} |
| 00/1 | 2/3 | 4/5 | 6/7 | 8/9 | 10/11 | 12/13 | 14/15 | 16/17 | 18/19 | 20/21 | 22/23 |
| col-0 | | | col-1 | | | col-2 | | | col-3 | | |

| | | | | |
|---|----------|----------|----------|----------|
| 0 | a_{00} | a_{01} | a_{02} | a_{03} |
| 1 | a_{10} | a_{11} | a_{12} | a_{13} |
| 2 | a_{20} | a_{21} | a_{22} | a_{23} |

Assume that
`int = 2 byte`

| col 0 | | | col 1 | | | col 2 | | | col 3 | | |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| a ₀₀ | a ₁₀ | a ₂₀ | a ₀₁ | a ₁₁ | a ₂₁ | a ₀₂ | a ₁₂ | a ₂₂ | a ₀₃ | a ₁₃ | a ₂₃ |
| 200/1 | 0/8 | 4/5 | 4/7 | 4/9 | 10/6 | 14/13 | 14/15 | 14/17 | 18/16 | 24/11 | 24/23 |

Formula:-

$$A[i][j] = 200 + [2 + 3 + 1] * 2$$

$$= 200 + 14$$

$$= 214$$

| | 1 | 2 | 3 |
|---|-----------------|-----------------|-----------------|
| 0 | a ₀₀ | a ₀₁ | a ₀₂ |
| 1 | a ₁₀ | a ₁₁ | a ₁₂ |
| 2 | a ₂₀ | a ₂₁ | a ₂₂ |

$$A[2][3] = 200 + [3 + 3 + 1] * 2$$

$$= 200 + 20$$

$$= 220$$

int[3][4]
 ↓ ↓
 m n

$A[i][j] = L_0 + [j + m + i] * \text{sizeof(int)}$ → column major
 $A[i][j] = L_0 + [i * n + j] * \text{sizeof(int)}$ → row major
 ↓
 Base Address

Formula:
 $A[i][j] = L_0 + [j + m + i] * \text{sizeof(int)}$ → column Major
 (Annotations: L₀ is base, j is column, m is no. of element in each row, i is row no, sizeof(int) is size of data type)

$A[i][j] = L_0 + [i * n + j] * \text{sizeof(int)}$
 (Annotations: L₀ is base, i is row, n is no. of elem in each col, j is column, sizeof(int) is size of data type)

* column major for n dimension *

Reverse of
row major

$$L_0 + i_4 + i_3 * d_4 + i_2 * d_3 * d_4 + i_1 * d_2 * d_3 * d_4$$

$$L_0 + i_4 + i_3$$

$$L_0 + i_4 + d_4 (i_3 + i_2 * d_3 + i_1 * d_2 * d_3)$$

$$L_0 + i_4 + d_4 [i_3 + d_3 * (i_2 + i_1 * d_2)]$$

↳ Time Taken by this formula = $(n-1) = O(n)$

* Formula for 3D array *

eg: `int A[l][m][n];`

row-major

$$\text{addr}(A[i][j][k]) = \text{@}$$

$$L_0 + [i * m * n + j * n + k] * w$$

Column-major mapping!

$$\text{addr}(A[i][j][k]) = L_0 + [k * l * m + j * l + i] * w$$