

VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



LAB RECORD

Bio Inspired Systems (23CS5BSBIS)

Submitted by

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in partial fulfillment for the award of the degree of

BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING

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CERTIFICATE

This is to certify that the Lab work entitled “ Bio Inspired Systems (23CS5BSBIS)” carried out by **Agam Tiwari (1BM22CS023)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements of the above mentioned subject and the work prescribed for the said degree.

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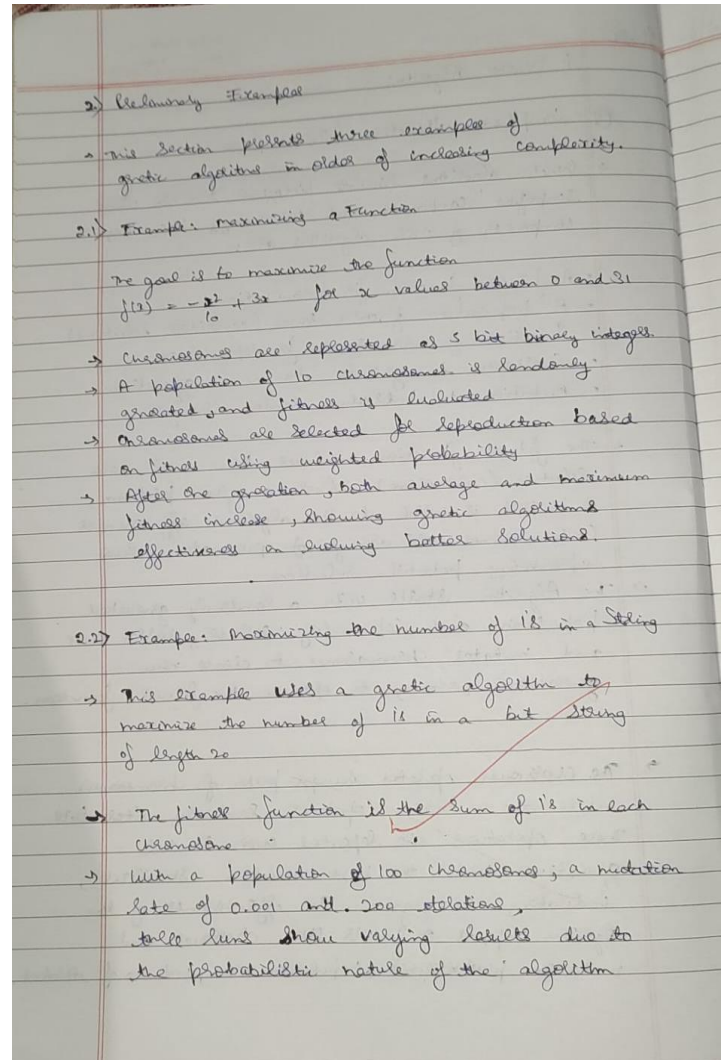
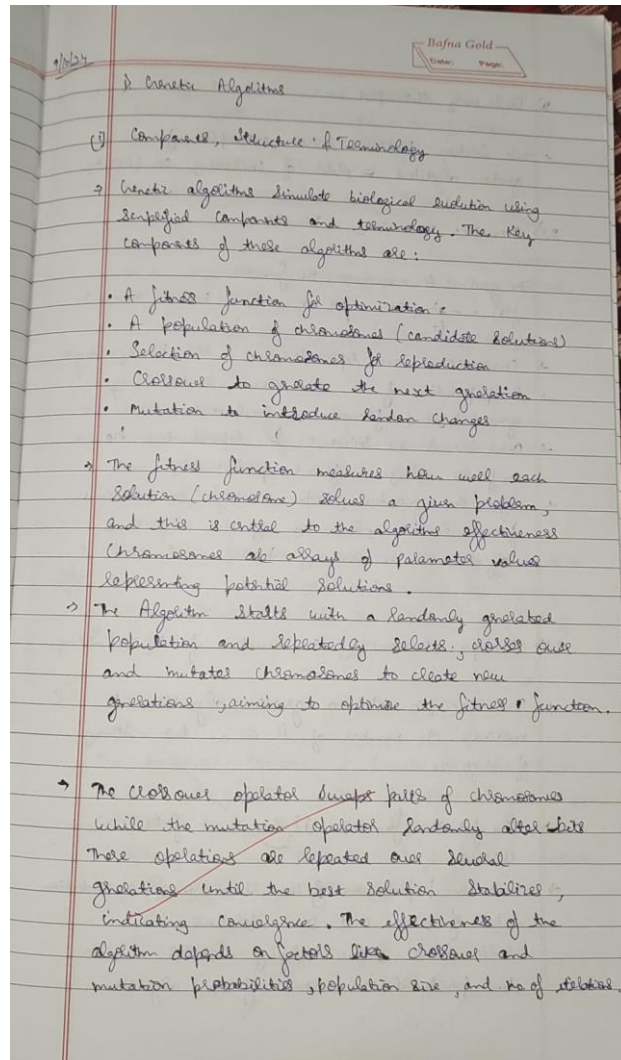
Github Link:

<https://github.com/Agam1611/BIS-LAB-5Sem>

Program 1

Genetic Algorithm for Optimization Problems

Algorithm:



Code:

```
import numpy as np

# Objective function to maximize
def fitness_function(x):
    return x**2

# Initialize parameters
population_size = 50
mutation_rate = 0.1
crossover_rate = 0.7
num_generations = 50
lower_bound = -10
upper_bound = 10

# Create initial population
def initialize_population(size, lower, upper):
    return np.random.uniform(lower, upper, size)

# Evaluate fitness for the population
def evaluate_fitness(population):
    return np.array([fitness_function(x) for x in population])

# Selection using roulette wheel selection
def select_parents(population, fitness):
    total_fitness = np.sum(fitness)
    selection_probs = fitness / total_fitness
    parents_indices = np.random.choice(len(population), size=2,
p=selection_probs)
    return population[parents_indices]

# Crossover to create offspring
def crossover(parent1, parent2):
    if np.random.rand() < crossover_rate:
        return (parent1 + parent2) / 2 # Linear crossover
    return parent1

# Mutation to introduce diversity
def mutate(offspring):
    if np.random.rand() < mutation_rate:
        return np.random.uniform(lower_bound, upper_bound)
    return offspring

# Genetic Algorithm main function
```

```

def genetic_algorithm():
    # Initialize population
    population = initialize_population(population_size, lower_bound,
upper_bound)

    for generation in range(num_generations):
        # Evaluate fitness of the population
        fitness = evaluate_fitness(population)

        # Track the best solution
        best_fitness_idx = np.argmax(fitness)
        best_solution = population[best_fitness_idx]
        best_fitness_value = fitness[best_fitness_idx]

        print(f"Generation {generation}: Best Solution = {best_solution},
Fitness = {best_fitness_value}")

        # Create the next generation
        new_population = []
        for _ in range(population_size):
            parent1, parent2 = select_parents(population, fitness)
            offspring = crossover(parent1, parent2)
            offspring = mutate(offspring)
            new_population.append(offspring)

        population = np.array(new_population)

    # Final evaluation
    final_fitness = evaluate_fitness(population)
    best_fitness_idx = np.argmax(final_fitness)
    best_solution = population[best_fitness_idx]
    best_fitness_value = final_fitness[best_fitness_idx]

    return best_solution, best_fitness_value

# Run the genetic algorithm
best_solution, best_fitness_value = genetic_algorithm()
print(f"Best Solution Found: x = {best_solution}, f(x) =
{best_fitness_value}")

```

Output :

```

Generation 0: Best Solution = -9.967365011554792, Fitness = 99.34836527356666
Generation 1: Best Solution = -9.169251894044368, Fitness = 84.07518029643623
Generation 49: Best Solution = 9.123059138454053, Fitness = 83.23020804373002
Best Solution Found: x = 9.05670095588789, f(x) = 82.02383220438064

```

Program 2

Particle Swarm Optimization for Function Optimization

Algorithm:

23/10/24 Particle Swarm Optimization

```
import numpy as np
# Step 1: Fitness Function

def fitness_function(position):
    return np.sum(position**2)

# Step 2: Initialize parameters

def initialize_parameters():
    params = {}
    'N': 50,
    'dim': 2,
    'max_iter': 100,
    'minx': -10,
    'maxx': 10,
    'w': 0.5,           # Inertia weight
    'c1': 1.5,          # Cognitive coefficient
    'c2': 2.5           # Social coefficient
    return params

# Step 3: Initialize particles

class Particle:
    def __init__(self, position, velocity):
        self.position = position
        self.velocity = velocity
        self.best_pos = position.copy()
        self.best_fitness = float('inf')
```

Particle Swarm Optimization

```
def initialize_swarm(N, dim, minx, maxx):
    swarm = []
    for _ in range(N):
        position = np.random.uniform(minx, maxx, dim)
        velocity = np.random.uniform(-1, 1, dim)
        swarm.append(Particle(position, velocity))
    return swarm

# Step 4: Evaluate Fitness

def evaluate_fitness(swarm):
    for particle in swarm:
        particle.fitness = fitness_function(particle.position)

# Step 5: Update velocities and positions

def update_particles(swarm, best_pos, swarm, w, c1, c2, minx, maxx):
    for particle in swarm:
        r1, r2 = np.random.rand(), np.random.rand()
        particle.velocity = (w * particle.velocity +
                             r1 * c1 * (particle.best_pos -
                                         particle.position) +
                             r2 * c2 * (best_pos[swarm.index(particle)] -
                                         particle.position))
        particle.position += particle.velocity
        particle.position = np.clip(particle.position, minx, maxx)
```

Code:

```
import numpy as np

# Step 1: Define the Problem
def fitness_function(position):
    # Example: Minimize the Sphere function
    return np.sum(position**2)

# Step 2: Initialize Parameters
def initialize_parameters():
    params = {
        'N': 50,          # Number of particles
        'dim': 2,          # Dimensionality of the problem
        'max_iter': 200,   # Maximum number of iterations
        'minx': -10,       # Minimum bound for position
        'maxx': 10,        # Maximum bound for position
        'w': 0.5,          # Inertia weight
        'c1': 1.5,          # Cognitive coefficient
        'c2': 1.5          # Social coefficient
    }
    return params

# Step 3: Initialize Particles
class Particle:
    def __init__(self, position, velocity):
        self.position = position
        self.velocity = velocity
        self.bestPos = position.copy()
        self.bestFitness = float('inf')

def initialize_swarm(N, dim, minx, maxx):
    swarm = []
    for _ in range(N):
        position = np.random.uniform(minx, maxx, dim)
        velocity = np.random.uniform(-1, 1, dim)
        swarm.append(Particle(position, velocity))
    return swarm

# Step 4: Evaluate Fitness
def evaluate_fitness(swarm):
    for particle in swarm:
        particle.fitness = fitness_function(particle.position)

# Step 5: Update Velocities and Positions
def update_particles(swarm, best_pos_swarm, w, c1, c2, minx, maxx):
```



```

    for particle in swarm:
        r1, r2 = np.random.rand(), np.random.rand()
        particle.velocity = (w * particle.velocity +
                             r1 * c1 * (particle.bestPos - particle.position)
                             r2 * c2 * (best_pos_swarm - particle.position))
        particle.position += particle.velocity
        # Clip position to be within bounds
        particle.position = np.clip(particle.position, minx, maxx)

# Step 6: Iterate
def pso():
    params = initialize_parameters()
    swarm = initialize_swarm(params['N'], params['dim'], params['minx'],
                             params['maxx'])
    best_pos_swarm = swarm[0].position.copy()
    best_fitness_swarm = float('inf')

    for _ in range(params['max_iter']):
        evaluate_fitness(swarm)

        for particle in swarm:
            if particle.fitness < particle.bestFitness:
                particle.bestFitness = particle.fitness
                particle.bestPos = particle.position.copy()
            if particle.fitness < best_fitness_swarm:
                best_fitness_swarm = particle.fitness
                best_pos_swarm = particle.position.copy()

        update_particles(swarm, best_pos_swarm, params['w'], params['c1'],
                        params['c2'], params['minx'], params['maxx'])

    # Step 7: Output the Best Solution
    return best_pos_swarm, best_fitness_swarm

best_position, best_fitness = pso()

print("Best Position:", best_position)
print("Best Fitness:", best_fitness)

```

Output :

```

Best Position: [-9.19971249e-25  1.71937901e-24]
Best Fitness: 3.802611270068504e-48

```

Program 3

Ant Colony Optimization for the Traveling Salesman Problem

Algorithm:

```
30/10/24 Ant Colony Optimization for the TSP

import numpy as np
import random

class AntColony:
    def __init__(self, cities, num_ants=10, alpha=1.0,
                 beta=2.0, rho=0.5, iterations=100):
        self.cities = cities
        self.num_ants = num_ants
        self.alpha = alpha
        self.beta = beta
        self.rho = rho
        self.iterations = iterations
        self.num_cities = len(cities)
        self.pheromone = np.zeros((self.num_cities,
                                     self.num_cities))
        self.distance = self.calculate_distance()

    def calculate_distance(self):
        distances = np.zeros((self.num_cities,
                               self.num_cities))
        for i in range(self.num_cities):
            for j in range(i+1, self.num_cities):
                distances[i][j] = distances[j][i]

        return distances
```

```
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def select_next_city(self, current_city, visited):
    probabilities = []
    for next_city in range(self.num_cities):
        if next_city not in visited:
            pheromone = self.pheromone[
                [current_city][next_city]] ** self.alpha
            heuristic = (1 / self.distance[
                [current_city][
                    next_city]]) ** self.beta
            probabilities.append(pheromone *
                                  heuristic)

    else:
        probabilities.append(0)

    total = sum(probabilities)
    probabilities = [p / total for p in
                     probabilities]
    return np.random.choice(range(self.num_cities),
                             p=probabilities)

def construct_solution(self):
    for _ in range(self.num_ants):
        visited = [0]
        current_city = 0
        for _ in range(1, self.num_cities):
            next_city = self.select_next_city(
                current_city, visited)
            visited.append(next_city)
            current_city = next_city
        visited.append(0)
        yield visited
```

Code:

```
import numpy as np
import random

class AntColony:
    def __init__(self, cities, num_ants=10, alpha=1.0, beta=2.0, rho=0.5,
iterations=100):
        self.cities = cities
        self.num_ants = num_ants
        self.alpha = alpha
        self.beta = beta
        self.rho = rho
        self.iterations = iterations
        self.num_cities = len(cities)
        self.pheromone = np.ones((self.num_cities, self.num_cities))
        self.distance = self.calculate_distances()
    def calculate_distances(self):
        distances = np.zeros((self.num_cities, self.num_cities))
        for i in range(self.num_cities):
            for j in range(i + 1, self.num_cities):
                distances[i][j] = distances[j][i] =
np.linalg.norm(np.array(self.cities[i]) - np.array(self.cities[j]))
        return distances
    def select_next_city(self, current_city, visited):
        probabilities = []
        for next_city in range(self.num_cities):
            if next_city not in visited:
                pheromone = self.pheromone[current_city][next_city] **
self.alpha
                heuristic = (1 / self.distance[current_city][next_city]) **
self.beta
                probabilities.append(pheromone * heuristic)
        else:
            probabilities.append(0)
        total = sum(probabilities)
        probabilities = [p / total for p in probabilities]
        return np.random.choice(range(self.num_cities), p=probabilities)
    def construct_solution(self):
        for _ in range(self.num_ants):
            visited = [0]
            current_city = 0
            for _ in range(1, self.num_cities):
                next_city = self.select_next_city(current_city, visited)
                visited.append(next_city)
                current_city = next_city
            visited.append(0) # Return to starting city
```

```

        yield visited
    def update_pheromones(self, solutions):
        self.pheromone *= (1 - self.rho) # Evaporation
        for solution in solutions:
            length = self.calculate_tour_length(solution)
            pheromone_deposit = 1 / length
            for i in range(len(solution) - 1):
                self.pheromone[solution[i]][solution[i + 1]] +=
pheromone_deposit
    def calculate_tour_length(self, solution):
        return sum(self.distance[solution[i]][solution[i + 1]] for i in
range(len(solution) - 1))

    def run(self):
        best_solution = None
        best_length = float('inf')
        for _ in range(self.iterations):
            solutions = list(self.construct_solution())
            self.update_pheromones(solutions)
            for solution in solutions:
                length = self.calculate_tour_length(solution)
                if length < best_length:
                    best_length = length
                    best_solution = solution
        return best_solution, best_length
cities = [(0, 0), (1, 2), (2, 1), (4, 4), (2, 4)]
aco = AntColony(cities)
best_route, best_distance = aco.run()
print("Best Route:", best_route)
print("Best Distance:", best_distance)

```

Output :

Best Route: [0, 1, 4, 3, 2, 0]

Best Distance: 12.313755207963359

Program 4

Cuckoo Search (CS)

Algorithm:

20/11/24 Cuckoo Search Algorithm

```

import numpy as np
import math

def objective_function(x):
    return np.sum(x**2)

def Levy_flight(beta=1.5, size=1):
    signa = (math.gamma(1+beta) * np.sin(
        np.pi * beta/2)) /
        math.gamma((1+beta)/2) * beta *
        (2 ** ((beta-1)/2)) ** (1/beta)
    u = np.random.normal(0, signa * u, size)
    v = np.random.normal(0, 1, size)
    step = u / (np.abs(v) ** (1/beta))
    return step

def Cuckoo_Search(obj_fun, dim, lb, ub, num_nests,
                  max_iter=100, pa=0.25):
    nests = np.random.rand(num_nests, dim)
    * (ub-lb) + lb
    fitness = np.apply_along_axis(objective_function, 1, nests)

    best_nest_idx = np.argmin(fitness)
    best_nest = nests[best_nest_idx]
    best_fitness = fitness[best_nest_idx]

    for iteration in range(max_iter):
        for i in range(num_nests):
            step = Levy_flight(size=dim)
            new_nest = nests[i] + 0.01 * step
            new_nest = np.clip(new_nest, lb, ub)
            new_fitness = obj_fun(new_nest)

            if new_fitness < fitness[i]:
                nests[i] = new_nest
                fitness[i] = new_fitness

        return best_nest, best_fitness

dim = 5
lb = -5
ub = 5
best_solution, best_fitness = Cuckoo_Search(obj_fun, dim,
                                           lb, ub, num_nests=25,
                                           max_iter=100, pa=0.25)

print(f"Best Solution: {best_solution}")
print(f"Best Fitness: {best_fitness}")

```

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```

new_nest = nests[i] + 0.01 * step
new_nest = np.clip(new_nest, lb, ub)
new_fitness = obj_fun(new_nest)

if new_fitness < fitness[i]:
    nests[i] = new_nest
    fitness[i] = new_fitness

for i in range(num_nests):
    if np.random.rand(1) < pa:
        nests[i] = np.random.rand(dim)
        * (ub-lb) + lb
        fitness[i] = obj_fun(nests[i])

return best_nest, best_fitness

dim = 5
lb = -5
ub = 5
best_solution, best_fitness = Cuckoo_Search(obj_fun, dim,
                                           lb, ub, num_nests=25,
                                           max_iter=100, pa=0.25)

print(f"Best Solution: {best_solution}")
print(f"Best Fitness: {best_fitness}")

Output:
Best Solution : [0.6498, 0.596, 2.015, 0.9398, 0.3198]
Best Fitness : 5.8814

```


Code:

```
import numpy as np
import math
# Objective function to optimize (example: Sphere function)
def objective_function(x):
    return np.sum(x**2)

# Lévy Flight distribution
def levy_flight(beta=1.5, size=1):
    sigma_u = (math.gamma(1 + beta) * np.sin(np.pi * beta / 2) /
               math.gamma((1 + beta) / 2) * beta * (2 ** ((beta - 1) /
2)))**(1 / beta)
    u = np.random.normal(0, sigma_u, size)
    v = np.random.normal(0, 1, size)
    step = u / (np.abs(v) ** (1 / beta))
    return step

# Cuckoo Search Algorithm
def cuckoo_search(objective_function, dim, lower_bound, upper_bound,
num_nests=25, max_iter=100, pa=0.25):
    # Initialize nests with random solutions within bounds
    nests = np.random.rand(num_nests, dim) * (upper_bound - lower_bound) +
lower_bound
    fitness = np.apply_along_axis(objective_function, 1, nests)

    # Initialize the best solution
    best_nest_idx = np.argmin(fitness)
    best_nest = nests[best_nest_idx]
    best_fitness = fitness[best_nest_idx]

    # Iterate for a fixed number of generations or until convergence
    for iteration in range(max_iter):
        for i in range(num_nests):
            # Generate a new solution using Lévy flight
            step = levy_flight(size=dim)
            new_nest = nests[i] + 0.01 * step
            new_nest = np.clip(new_nest, lower_bound, upper_bound)

            # Evaluate the new solution
            new_fitness = objective_function(new_nest)

            # If the new solution is better, replace the old solution
            if new_fitness < fitness[i]:
                nests[i] = new_nest
                fitness[i] = new_fitness
```

```

        # Abandon the worst nests
        for i in range(num_nests):
            if np.random.rand() < pa: # Probability to abandon
                nests[i] = np.random.rand(dim) * (upper_bound - lower_bound)
+ lower_bound
                fitness[i] = objective_function(nests[i])

        # Find the current best nest
        best_nest_idx = np.argmin(fitness)
        best_nest = nests[best_nest_idx]
        best_fitness = fitness[best_nest_idx]

        # print(f"Iteration {iteration+1}, Best Fitness: {best_fitness}")

    return best_nest, best_fitness

# Example usage of Cuckoo Search

# Define the problem dimensions and bounds
dim = 5 # Dimension of the solution space
lower_bound = -5 # Lower bound of the search space
upper_bound = 5 # Upper bound of the search space

# Run Cuckoo Search
best_solution, best_fitness = cuckoo_search(objective_function, dim,
lower_bound, upper_bound, num_nests=25, max_iter=100, pa=0.25)

print(f"Best Solution: {best_solution}")
print(f"Best Fitness: {best_fitness}")

```

Output :

```

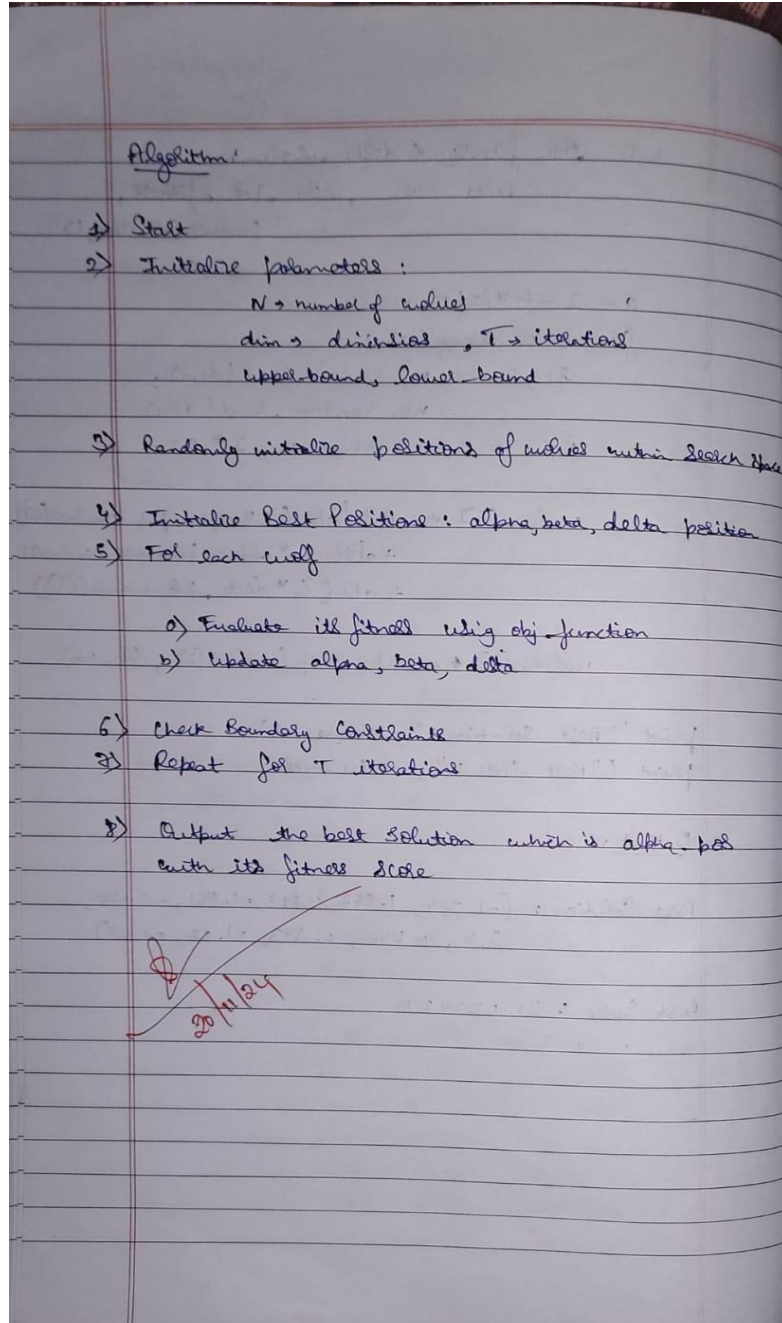
Best Solution: [0.64982748 0.55961241 2.01501756 0.93987275 0.31984962]
Best Fitness: 5.78140211553397

```

Program 5

Grey Wolf Optimizer (GWO)

Algorithm:



Code:

```
import numpy as np

# Objective function (example: Sphere function)
def objective_function(x):
    return np.sum(x**2)
N, dim, T = 30, 10, 100 # Number of wolves, dimensions, iterations
lower_bound, upper_bound = -10, 10

wolves = np.random.uniform(lower_bound, upper_bound, (N, dim))

alpha_pos, beta_pos, delta_pos = np.zeros(dim), np.zeros(dim), np.zeros(dim)
alpha_score, beta_score, delta_score = float('inf'), float('inf'), float('inf')
for t in range(T):
    for i in range(N):
        fitness = objective_function(wolves[i]) # Evaluate fitness
        if fitness < alpha_score:
            delta_score, delta_pos = beta_score, beta_pos.copy()
            beta_score, beta_pos = alpha_score, alpha_pos.copy()
            alpha_score, alpha_pos = fitness, wolves[i].copy()
        elif fitness < beta_score:
            delta_score, delta_pos = beta_score, beta_pos.copy()
            beta_score, beta_pos = fitness, wolves[i].copy()
        elif fitness < delta_score:
            delta_score, delta_pos = fitness, wolves[i].copy()
    a = 2 - t * (2 / T)
    for i in range(N):
        r1, r2 = np.random.rand(dim), np.random.rand(dim)
        A, C = 2 * a * r1 - a, 2 * r2
        wolves[i] += A * (abs(C * alpha_pos - wolves[i]) +
                        abs(C * beta_pos - wolves[i]) +
                        abs(C * delta_pos - wolves[i]))

        wolves[i] = np.clip(wolves[i], lower_bound, upper_bound)
print("Best Solution:", alpha_pos)
print("Best Score:", alpha_score)
```

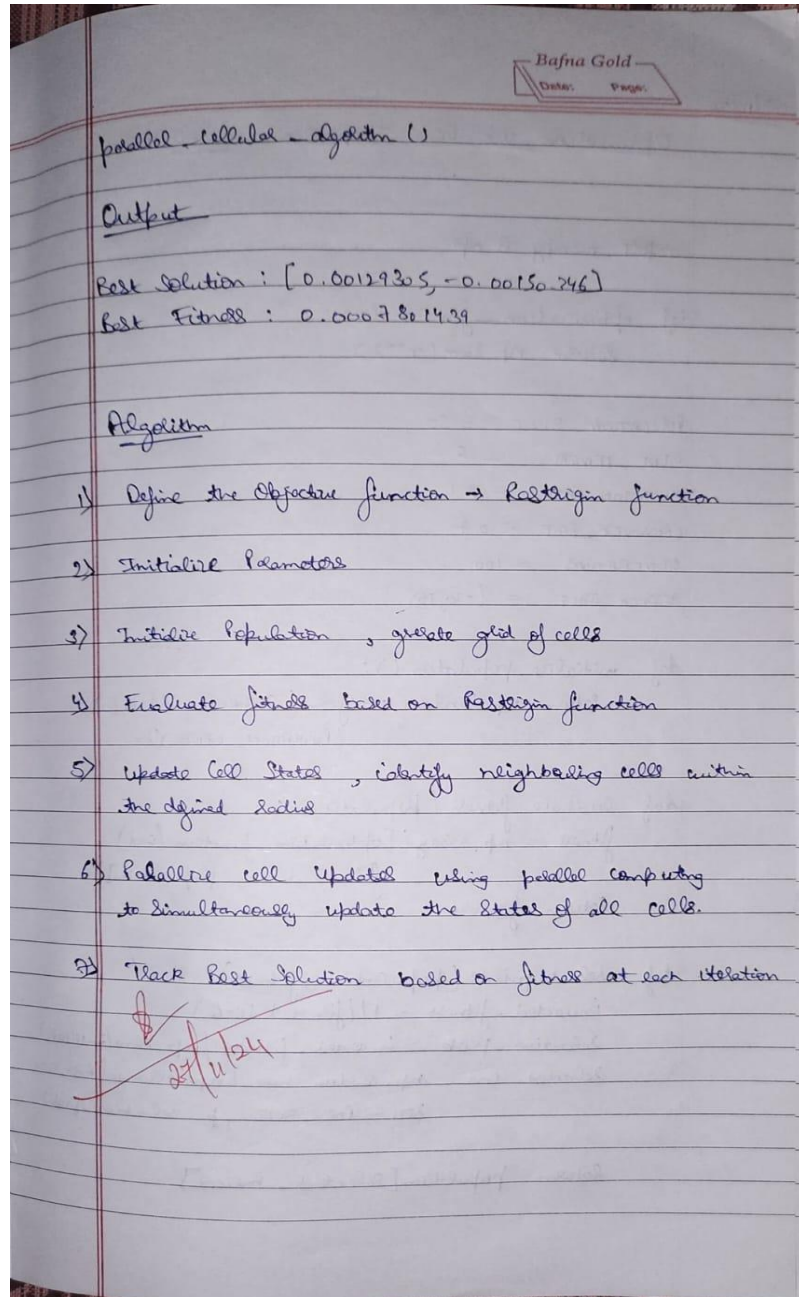
Output :

```
Best Solution: [-1.28434275  1.94786008  0.82301541 -1.85113457 -2.08806377
 3.74582237
 0.84065243  0.8938704  -1.22271966 -0.29007149]
Best Score: 31.023829961456407
```

Program 6

Parallel Cellular Algorithms and Programs

Algorithm:



Code:

```
import numpy as np
import random
import concurrent.futures

def rastrigin(x):
    A = 10
    return A * len(x) + sum([(xi ** 2 - A * np.cos(2 * np.pi * xi)) for xi in x])

GRID_SIZE = (10, 10)
DIM = 2
RADIUS = 1
ITER = 100
BEST = None

def init_grid(size, dim):
    return [[np.random.uniform(-5.12, 5.12, size=(dim,)) for _ in range(size[1])] for _ in range(size[0])]

def fitness(cell):
    return rastrigin(cell)

def update_state(grid, i, j, radius):
    curr = grid[i][j]
    fitness_curr = fitness(curr)
    neighbors = [grid[ni][nj] for dx in range(-radius, radius+1) for dy in range(-radius, radius+1)
                  if 0 <= (ni := i+dx) < len(grid) and 0 <= (nj := j+dy) < len(grid[0]) and (dx or dy)]
    if neighbors:
        best_neigh = min(neighbors, key=fitness)
        return curr + 0.1 * (best_neigh - curr)
    return curr

def run_iteration(grid, radius):
    new_grid = [[None for _ in range(len(grid[0]))] for _ in range(len(grid))]
    with concurrent.futures.ThreadPoolExecutor() as ex:
        futures = [ex.submit(update_state, grid, i, j, radius) for i in range(len(grid)) for j in range(len(grid[0]))]
        for idx, future in enumerate(futures):
            i, j = divmod(idx, len(grid[0]))
            new_grid[i][j] = future.result()
    return new_grid
```

```

def track_best(grid):
    global BEST
    best_cell, best_fitness = None, float('inf')
    for row in grid:
        for cell in row:
            f = fitness(cell)
            if f < best_fitness:
                best_fitness = f
                best_cell = cell
    if BEST is None or best_fitness < fitness(BEST):
        BEST = best_cell

def parallel_cellular_algorithm():
    global BEST
    grid = init_grid(GRID_SIZE, DIM)
    for _ in range(ITER):
        grid = run_iteration(grid, RADIUS)
        track_best(grid)
        print(f"Best Fitness: {fitness(BEST)}")
    print("Best Solution:", BEST)
    print("Best Fitness:", fitness(BEST))

parallel_cellular_algorithm()

```

Output :

```

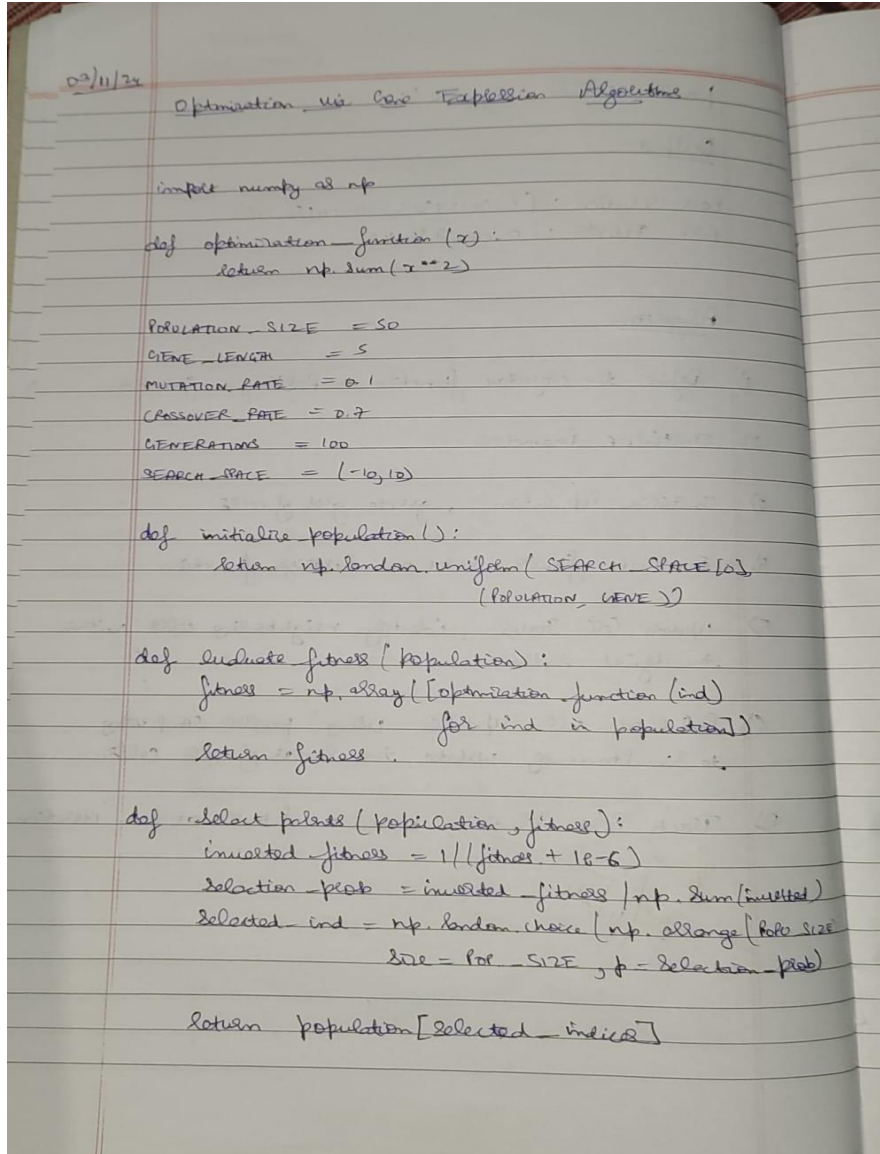
Best Fitness: 2.4309484366586602
Best Fitness: 2.4309484366586602
Best Fitness: 0.0007801439196555293
Best Fitness: 0.0007801439196555293
Best Fitness: 0.0007801439196555293
Best Solution: [ 0.00129305 -0.00150346]
Best Fitness: 0.0007801439196555293

```

Program 7

Optimization via Gene Expression Algorithms

Algorithm:



Handwritten code for a Gene Expression Algorithm in Python, written on lined paper. The code defines an optimization function and a series of helper functions for population management.

```
02/11/24
Optimization via Gene Expression Algorithms

import numpy as np

def optimization_function(x):
    return np.sum(x**2)

POPULATION_SIZE = 50
GENE_LENGTH = 5
MUTATION_RATE = 0.1
CROSSOVER_RATE = 0.7
GENERATIONS = 100
SEARCH_SPACE = (-10, 10)

def initialize_population():
    return np.random.uniform(SEARCH_SPACE[0],
                              SEARCH_SPACE[1],
                              (POPULATION_SIZE, GENE_LENGTH))

def evaluate_fitness(population):
    fitness = np.array([optimization_function(ind)
                        for ind in population])
    return fitness

def select_parents(population, fitness):
    inverted_fitness = 1 / (fitness + 1e-6)
    selection_prob = inverted_fitness / np.sum(inverted_fitness)
    selected_ind = np.random.choice(np.arange(POPULATION_SIZE),
                                    p=selection_prob)

    return population[selected_ind]
```

Code:

```
import numpy as np

# Define the mathematical function to optimize (example: minimize  $f(x) = x^2$ )
def optimization_function(x):
    return np.sum(x**2) # Modify this for other functions to optimize

# Parameters
POPULATION_SIZE = 50 # Number of individuals
GENE_LENGTH = 5 # Number of genes (dimensions of the problem)
MUTATION_RATE = 0.1 # Probability of mutation
CROSSOVER_RATE = 0.7 # Probability of crossover
GENERATIONS = 100 # Number of generations
SEARCH_SPACE = (-10, 10) # Range of values for genes

# Initialize Population
def initialize_population():
    return np.random.uniform(SEARCH_SPACE[0], SEARCH_SPACE[1],
                              (POPULATION_SIZE, GENE_LENGTH))

# Evaluate Fitness (lower is better for minimization)
def evaluate_fitness(population):
    fitness = np.array([optimization_function(ind) for ind in population])
    return fitness

# Selection (Roulette Wheel Selection)
def select_parents(population, fitness):
    # Convert fitness to probabilities (lower fitness is better)
    inverted_fitness = 1 / (fitness + 1e-6) # Avoid division by zero
    selection_prob = inverted_fitness / np.sum(inverted_fitness)
    selected_indices = np.random.choice(np.arange(POPULATION_SIZE),
                                         size=POPULATION_SIZE, p=selection_prob)
    return population[selected_indices]

# Crossover (Blend Crossover)
def crossover(parents):
    offspring = np.empty_like(parents)
    for i in range(0, POPULATION_SIZE, 2):
        p1, p2 = parents[i], parents[i+1]
        if np.random.rand() < CROSSOVER_RATE:
            alpha = np.random.rand() # Blending factor
            offspring[i] = alpha * p1 + (1 - alpha) * p2
            offspring[i+1] = alpha * p2 + (1 - alpha) * p1
        else:
            offspring[i], offspring[i+1] = p1, p2
```

```

    return offspring

# Mutation (Random Perturbation)
def mutate(offspring):
    for i in range(POPULATION_SIZE):
        if np.random.rand() < MUTATION_RATE:
            mutation_point = np.random.randint(0, GENE_LENGTH)
            offspring[i][mutation_point] += np.random.uniform(-1, 1)
            # Keep within search space
            offspring[i][mutation_point] =
np.clip(offspring[i][mutation_point], SEARCH_SPACE[0], SEARCH_SPACE[1])
    return offspring

# Gene Expression (Translate Genetic Code into Solutions)
def gene_expression(genes):
    # In this simple example, the genes directly represent the solution
    return genes

# Main Algorithm
def gene_expression_algorithm():
    # Initialize population
    population = initialize_population()
    best_solution = None
    best_fitness = float('inf')

    # Iterate through generations
    for generation in range(GENERATIONS):
        # Evaluate fitness
        fitness = evaluate_fitness(population)

        # Track the best solution
        current_best_idx = np.argmin(fitness)
        if fitness[current_best_idx] < best_fitness:
            best_fitness = fitness[current_best_idx]
            best_solution = population[current_best_idx]

    print(f"Generation {generation+1}: Best Fitness = {best_fitness}")

    # Selection
    parents = select_parents(population, fitness)

    # Crossover
    offspring = crossover(parents)

    # Mutation
    offspring = mutate(offspring)

```

```

        # Gene Expression (not needed explicitly as genes represent
solutions)
        population = gene_expression(offspring)

        print("\nOptimal Solution Found:")
        print("Best Solution:", best_solution)
        print("Best Fitness:", best_fitness)

# Run the algorithm
if __name__ == "__main__":
    gene_expression_algorithm()

```

Output :

```
Generation 1: Best Fitness = 16.545885126119284
```

```
Generation 2: Best Fitness = 11.641082640808637
```

```
...
```

```
Generation 99: Best Fitness = 0.02233046748484963
```

```
Generation 100: Best Fitness = 0.02233046748484963
```

```
Optimal Solution Found:
```

```
Best Solution: [ 0.07226226 -0.11854791  0.03245473 -0.01236219  0.04299877]
```

```
Best Fitness: 0.02233046748484963
```