## 1) KNAPSACK

```
#include <iostream>
#include <vector>
using namespace std;
int knapsack(int weights[], int values[], int n, int capacity) {
  // Backtracking function to explore all subsets
  if (n == 0 \mid | capacity == 0)
    return 0;
  // If the weight of the nth item is more than the remaining capacity
  if (weights[n - 1] > capacity)
    return knapsack(weights, values, n - 1, capacity);
  // Case 1: Exclude the current item
  int exclude = knapsack(weights, values, n - 1, capacity);
  // Case 2: Include the current item
  int include = values[n - 1] + knapsack(weights, values, n - 1, capacity - weights[n - 1]);
  // Return the maximum of including or excluding the item
  return max(exclude, include);
}
int main() {
  int values[] = {60, 100, 120};
  int weights[] = \{10, 20, 30\};
  int capacity = 50;
  int n = sizeof(values) / sizeof(values[0]);
  cout << "Maximum value that can be carried: " << knapsack(weights, values, n, capacity) <<
endl;
  return 0;
}
```

## 2) TRAVELLING SALESMAN

```
#include <bits/stdc++.h>
using namespace std;
// Function to find the minimum cost using backtracking
void totalCost(vector<vector<int>>& cost, vector<bool>& visited,
        int currPos, int n, int count, int costSoFar, int& ans) {
  // If all nodes are visited and there's an edge to the start node
  if (count == n && cost[currPos][0]) {
    // Update the minimum cost
    ans = min(ans, costSoFar + cost[currPos][0]);
    return;
  }
  // Try visiting each node from the current position
  for (int i = 0; i < n; i++) {
    if (!visited[i] && cost[currPos][i]) {
       // If node is not visited and has an edge
      visited[i] = true;
       totalCost(cost, visited, i, n, count + 1, costSoFar + cost[currPos][i], ans);
      visited[i] = false;
    }
  }
}
// Function to solve the TSP problem
int tsp(vector<vector<int>>& cost) {
  int n = cost.size();
  vector<bool> visited(n, false);
  visited[0] = true; // Start from the first city
  int ans = INT_MAX; // Initialize the answer to a large value
  totalCost(cost, visited, 0, n, 1, 0, ans); // Start the backtracking process
```

```
return ans;
}
int main() {
  // Distance matrix representing the cost between cities
  vector<vector<int>> cost = {
    {0, 10, 15, 20},
    {10, 0, 35, 25},
    {15, 35, 0, 30},
    {20, 25, 30, 0}
  };
  // Call the TSP function and get the result
  int res = tsp(cost);
  // Output the minimum cost of the tour
  cout << "Minimum cost of the tour: " << res << endl;
  return 0;
}
   3) PARTITION INTO K SUBSET OF EQUAL SUM
#include <bits/stdc++.h>
using namespace std;
bool isKPartitionPossible(vector<int> &arr, vector<int> &subsetSum,
              vector<bool> &taken, int target, int k,
               int n, int currldx, int limitIdx) {
  // If the current subset sum matches the target
  if (subsetSum[currIdx] == target) {
    // If all but one subset are filled, the
   // last subset is guaranteed to work
    if (currldx == k - 2)
       return true;
    return isKPartitionPossible(arr, subsetSum, taken,
                    target, k, n, currldx + 1, n - 1);
```

```
}
  // Try including each element in the current subset
  for (int i = limitIdx; i \ge 0; i--) {
    // Skip if the element is already used
    if (taken[i])
       continue;
    int temp = subsetSum[currldx] + arr[i];
    if (temp <= target) {
       // Only proceed if it doesn't exceed the target
       taken[i] = true;
       subsetSum[currldx] += arr[i];
       if (isKPartitionPossible(arr, subsetSum, taken,
                      target, k, n, currldx, i - 1))
         return true;
       // Backtrack
       taken[i] = false;
       subsetSum[currldx] -= arr[i];
    }
  }
  return false;
bool isKPartitionPossible(vector<int> &arr, int k) {
  int n = arr.size(), sum = accumulate(arr.begin(), arr.end(), 0);
  // If only one subset is needed, it's always possible
  if (k == 1)
    return true;
  // Check if partition is impossible
  if (n < k \mid | sum \% k != 0)
    return false;
```

}

```
int target = sum / k;
  vector<int> subsetSum(k, 0);
  vector<bool> taken(n, false);
  // Initialize first subset with the last element
  subsetSum[0] = arr[n - 1];
  taken[n - 1] = true;
  // Recursively check for partitions
  return isKPartitionPossible(arr, subsetSum, taken,
                  target, k, n, 0, n - 1);
}
int main() {
  vector<int> arr = {2, 1, 4, 5, 3, 3};
  int k = 3;
  if (isKPartitionPossible(arr, k))
    cout << "true";
  else
    cout << "false";
  return 0;
    4) PALINDROMIC PARTITION
#include <iostream>
#include <vector>
using namespace std;
bool isPalindrome(string& str, int start, int end) {
  while (start < end) {
    if (str[start] != str[end]) return false;
    start++;
    end--;
  return true;
```

```
}
void palindromicPartitionsHelper(string& str, int index, vector<string>& current) {
  if (index == str.size()) {
    for (string& s : current) {
       cout << s << " ";
    }
    cout << endl;
    return;
  }
  for (int i = index; i < str.size(); ++i) {
    if (isPalindrome(str, index, i)) {
       current.push_back(str.substr(index, i - index + 1));
       palindromicPartitionsHelper(str, i + 1, current);
       current.pop_back();
    }
  }
}
void printPalindromicPartitions(string& str) {
  vector<string> current;
  palindromicPartitionsHelper(str, 0, current);
}
int main() {
  string str = "aab";
  printPalindromicPartitions(str);
  return 0;
}
   aa
```