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http://www.ais.uni-bonn.de/WS2223/4204\_L\_NN.html

# Exercises for module Technical Neural Networks (MA-INF 4204), WS22/23

#### Assignments Sheet 2, due: Monday 31.10.2022

24.10.2022

Group	Name	8	9	10	11	12	13	$\sum$ Sheet 2

#### Assignment 8 (3 Points)

For some reason, a special computer is not capable of calculating the exponential function, the hyperbolic tangent or the trigonometric functions (sin, cos, ...) in acceptable time. Your task is to develop an alternative transferfunction g(z) which shape is almost like the hyperbolic tangent tanh(z), (maximal deviation below 0.05) but uses less computing power.

Write down your formula for g(z) and draw it together with tanh(z).

## Assignment 9 (2 Point)

Show by calculation that the transfer function tanh(z) is identical to the shifted and rescaled Fermi-function (also called logistic function)  $f_{\log}(z) = \frac{1}{1+e^{-z}}.$ 

#### Assignment 10 (3 Points)

A N-H1-M MLP with tanh as transferfunction, in hidden-layer and output-layer is given, the input values are  $x_n = -1.0$ , all weights are  $w_{i,j} = -10.0$ .

How is the result  $y_m$  for this network changing, if you include a second hidden layer H2 with transferfunction tanh and all new weights  $w_{h,k} = -10.0$ ? (with N, H1, H2, M > 4).

#### Assignment 11 (2 Points)

Develop and describe an algorithm that shuffles a fixed, given set of training patterns into a new random sequence (as necessary for BP training).

The algorithm shall be efficient with respect to memory and time consumption.

## Assignment 12 (3 Points)

Explain the training algorithm Backpropagation-of-Error in your own words.

Please describe how BP is used to make a neural network learn a desired task.

You are not intended to describe the mathematical derivation of the algorithm, but describe how this algorithm is structured into different phases (five to seven) with respect to a programmer who wants to implement it.

#### Assignment 13 (4 Points)

Derive a new learning rule \*\* for a Multi-Layer-Perceptron.

Start from the new objective function (cost function, error function)  $E^{**}$  and derive the new learning rule in analogy to Backpropagation of Error. The new cost function has been extended by a term that depends on all weights  $w_{ij}$ .

Write down all calculation steps, and give the formulas for calculating the  $\delta^{**}$  in output- and hidden layer.

$${}^{p}E^{**} = \frac{1}{2} \sum_{m=1}^{M} ({}^{p}\hat{y}_{m} - {}^{p}y_{m})^{2} + \beta \frac{1}{2} \sum_{i,j} (w_{ij})^{2}$$

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Implement in Python a Multi-Layer-Perzeptron including the learning rule Backpropagation of Error and test your program. Do not use libraries that have pre-implemented neural network structures.

#### Implement a Multi Layer Perzeptron

Your program must be capable of setting the structure of the network, number of layers (maximum 4), number of neurons per layer (maximum 1000), transferfunction separately for each layer (tanh or logistic or identity). It is O.K. to set these parameters directly within the source-code, please do not implement a user interface for that.

Initialize the weights to random values between -2.0 and +2.0, make sure, that the random number generator is under your control, and that you can reproduce your results. Set/initialize the random number generator explicitly (random seed).

#### Implement Backpropagation of Error

Implement the 7 steps of the Backpropagation of Error Algorithm (from the lecture). Your program shall read training patterns (input  $p_{x_n}$ , teacher  $p_{\hat{y}_m}$ ) from a file training\_data.txt with up to P = 1000 patterns. Use the sum over quadratic differences as error function. Allow to set different learning rates  $\eta$  for the different layers.

Calculate the error in every training step, and print it during the training process as a learning curve into a file learning\_curve.txt and visualize it.

End the training if a predefined number of training steps has been performed, and then test the performance of the network (no further weight changes) with respect to a second set of data, the test set test\_data.txt (same file format as the training data). Choose resonable test data on your own.

The training\_data.txt file starts with two lines of header, followed by P lines of data. Each header line starts with a # character followed by some characters and strings that you can ignore (if you want to).

Each of the P data lines contains the data for one pattern p: N-input values  ${}^{p}x_{1}, \ldots, {}^{p}x_{N}$ , separated by one or more blanks, M-teacher values  ${}^{p}\hat{y}_{1}, \ldots, {}^{p}\hat{y}_{M}$ , separated by blanks.

Extra: (no extra points) If you are experienced with neural networks and MLPs, you can implement and train an MLP with Rectified Linear Units (ReLUs) using the ramp function.