

Homework 52

The **due date** for this homework is **Tue 7 May 2013 12:00 AM EDT -0400**.

This homework is a bit different. There are very few problems, but each one is an amalgam of many problems. It may take a long time to do these, but the practice will be very good for you!

Question 1

For which of the following series does the *root test* ensure **convergence**? Select all that apply.

- ☐ $\sum_{n=1}^{\infty} \left(\frac{2n^2 + 4n + 1}{3n^2 + 1} \right)^n$
- ☐ $\sum_{n=1}^{\infty} \left(\frac{2 \arctan n}{\pi} \right)^n$
- ☐ $\sum_{n=1}^{\infty} \left(\frac{3n - 1}{3n} \right)^{n^2}$
- ☐ $\sum_{n=1}^{\infty} \left(\frac{n^4 \ln^2 \left(\cos \frac{1}{n} \right)}{n + 1} \right)^n$
- ☐ $\sum_{n=1}^{\infty} \left(\frac{2n}{2n + 1} \right)^{2n}$
- ☐ $\sum_{n=1}^{\infty} \left(\frac{n}{\ln n} \right)^{n/2}$
- ☐ $\sum_{n=1}^{\infty} \left(\frac{n + 1}{2n - 1} \right)^n$

☐ $\sum_{n=1}^{\infty} \left(\frac{\pi}{2 \arctan n} \right)^n$

☐ $\sum_{n=1}^{\infty} \left(\frac{3n}{3n-1} \right)^{n^2}$

☐ $\sum_{n=1}^{\infty} \left(\frac{\ln(3n+1)}{n} \right)^{2n}$

Question 2

For which of the following series does the *ratio test* ensure **divergence**? Select all that apply.

☐ $\sum_{n=1}^{\infty} \frac{(n^2)!}{(2n)!}$

☐ $\frac{1}{2} + \frac{1 \cdot 5}{2 \cdot 5} + \frac{1 \cdot 5 \cdot 9}{2 \cdot 5 \cdot 8} + \cdots + \frac{1 \cdot 5 \cdot 9 \cdots (4n-3)}{2 \cdot 5 \cdot 8 \cdots (3n-1)} + \cdots$

☐ $\frac{2}{1} + \frac{2 \cdot 5}{1 \cdot 5} + \frac{2 \cdot 5 \cdot 8}{1 \cdot 5 \cdot 9} + \cdots + \frac{2 \cdot 5 \cdot 8 \cdots (3n-1)}{1 \cdot 5 \cdot 9 \cdots (4n-3)} + \cdots$

☐ $\sum_{n=1}^{\infty} \frac{(n!)^2}{(2n)!}$

☐ $\sum_{n=1}^{\infty} \frac{n!}{2^{n!}}$

☐ $\frac{1}{3} + \frac{1 \cdot 3}{3 \cdot 5} + \frac{1 \cdot 3 \cdot 5}{3 \cdot 5 \cdot 7} + \cdots + \frac{1 \cdot 3 \cdot 5 \cdots (2n-1)}{3 \cdot 5 \cdot 7 \cdots (2n+1)} + \cdots$

☐ $\sum_{n=1}^{\infty} \frac{(n+1)^{2n}}{(n+1)!}$

☐ $\sum_{n=1}^{\infty} \frac{e^n}{n^2}$

☐ $\sum_{n=1}^{\infty} \frac{n!}{2^n + 3}$

$$\square \quad \frac{3}{1} + \frac{3 \cdot 5}{1 \cdot 3} + \frac{3 \cdot 5 \cdot 7}{1 \cdot 3 \cdot 5} + \cdots + \frac{3 \cdot 5 \cdot 7 \cdots (2n+1)}{1 \cdot 3 \cdot 5 \cdots (2n-1)} + \cdots$$

Question 3

Using *any* of the convergence tests covered in this chapter, determine which of the following sequences **converge**. Select all that converge.

$$\square \quad \sum_{n=1}^{\infty} \frac{1 + (-1)^n}{2 + (-1)^n}$$

$$\square \quad \frac{2}{2} + \frac{2 \cdot 5}{2 \cdot 9} + \frac{2 \cdot 5 \cdot 10}{2 \cdot 9 \cdot 28} + \cdots + \frac{2 \cdot 5 \cdot 10 \cdots (n^2 + 1)}{2 \cdot 9 \cdot 28 \cdots (n^3 + 1)}$$

$$\square \quad \sum_{n=1}^{\infty} \frac{3^n}{n^3}$$

$$\square \quad \sum_{n=1}^{\infty} \left(\frac{n-1}{n+1} \right)^{n^2+n}$$

$$\square \quad \sum_{n=1}^{\infty} \frac{n^2 - 1}{n^3 + n^2 + 1}$$

$$\square \quad \sum_{n=1}^{\infty} \arcsin \frac{1}{2} \arcsin \frac{2}{3} \cdots \arcsin \frac{n}{n+1}$$

$$\square \quad \sum_{n=1}^{\infty} \frac{n!}{(2n)!}$$

$$\square \quad \sum_{n=1}^{\infty} \left(1 + \frac{1}{n^2} \right)^{n^3}$$

$$\square \quad \sum_{n=1}^{\infty} \frac{n(n^2 + 1)^2}{n^8 + 2n^2 + 4n + 1}$$

$$\square \quad \sum_{n=1}^{\infty} \ln \frac{n^2 + 1}{n^2}$$

☐
$$\sum_{n=1}^{\infty} \frac{1 \cdot 3 \cdot 5 \cdots (2n-1)}{n!}$$

☐
$$\sum_{n=1}^{\infty} \frac{\cos^2 n}{n^2}$$

☐
$$\sum_{n=1}^{\infty} \frac{n^3 + 1}{\sqrt[3]{n^{10} + n}}$$

☐
$$\sum_{n=1}^{\infty} \frac{1}{2^n + n^2}$$

☐
$$\sum_{n=1}^{\infty} \left(\frac{n^2}{2n+1} \right)^n$$

☐
$$\sum_{n=1}^{\infty} \left(\frac{2n}{3n+1} \right)^n$$

☐ In accordance with the Honor Code, I certify that my answers here are my own work.

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