

# JSPEC v. 2.0.0 User Manual

---

## Using the text-based user interface

---

### Run JSPEC with the input file

Put the input file in the same directory with the JSPEC program and run JSPEC as :

```
jspec.exe inputfile
```

### Format of the input file

The input file is a plain text file and it will be parsed by the program line by line. Each command or expression should occupy a separate line. Comments start with "#". Everything behind the "#" in the line will be ignored by the program. Blank lines, white spaces and tabs are also ignored. The input file is NOT case-sensitive. From version 2.0, it is allowed to break a long line into several lines. Any line ending with "&&" is considered unfinished and will be combined with the following line before processing. All white spaces at the both ends of the two lines and the "&&" will be trimmed before combining them.

The input file is organized by various sections. All the sections fall into three different categories: (1) scratch section, (2) definition sections and (3) operation section. All the sections with the respective categories and usages are listed in the following table.

Section name	Category	Usage
section_scratch	scratch	Define variables and do calculations with the variables. The variables defined in this section can be used in definition sections.
section_ion	definition	Set parameters for the ion beam
section_ring	definition	Set parameters for the ion ring
section_e_beam	definition	Set parameters for the cooling electron beam
section_cooler	definition	Set parameters for the cooler
section_ibs	definition	Set parameters for IBS rate calculation
section_ecool	definition	Set parameters for electron cooling rate calculation
section_luminosity	definition	Set parameters for luminosity calculation
section_run	operation	Create the objectives (ion beam, ion ring, electron beam, cooler) and perform the calculation and/or the simulation.

The input file starts with a section by calling the section name. Once a section name is called, the respective section is created, and this section ends when another section name is called or when the input file ends. Sections can be repeated called and the latter one overwrite the previous ones. But if a parameters is not set again in the latter one, its value remains.

The following example includes three different sections in three different categories.

```

section_scratch #scratch section
  m = 938.272
  ke = 8000
  gamma = ke/m + 1
  print gamma
  list_const
section_e_beam #definition section, define the parameters for electron beam
  gamma = gamma
  tmp_tr = 0.1
  tmp_l = 0.1
  shape = dc_uniform
  radius = 0.004
  current = 2
section_run #operation function
  create_e_beam

```

The first section is a scratch section. In this section, three variables, m, ke, and gamma, are defined. The values of m and ke are assigned, and gamma is calculated from ke and m. The calculation is supported by the math parser, muParser. Fundamental calculations and functions are supported, including summation, subtraction, multiplication, division, square root, exponential function, etc. For more details about the muParser, please refer to <http://beltoforion.de/article.php?a=muparser>. The command "print gamma" will print the value of gamma to the screen. The following command will show a list of all the constant variables supported by the scratch section on the screen. All the constant variables and their values are listed in the following table.

Constant	Value	Meaning
k_c	299792458.0	speed of light, in m/s
k_e	1.602176565E-19;	Elementary charge, in C
k_pi	3.1415926535897932384626	$\pi$
k_u	931.49406121	Atomic mass unit, in MeV/c <sup>2</sup>
k_me	0.510998928	Electron mass, in MeV/c <sup>2</sup>
k_ke	8.9875517873681764E+9	Coulomb's constant, in N*m <sup>2</sup> /C <sup>2</sup>

The second section is a definition section, which sets the parameters for the cooling electron beam. In all the expressions in this section, the left side of the "=" sign is a keyword in section\_e\_beam, which corresponds to a parameter of the electron beam, and the right side is the valued assign to the keyword (the parameter). The first expression in this section is "gamma = gamma".<sup>1</sup> The left gamma is a keyword, which represents the Lorentz factor of the electron beam. The right gamma is the variable defined in the above scratch section. This expression assigns the value of the scratch variable gamma to the keyword gamma. Please note that a scratch variable can be used in other sections to set the value for a keyword, but a keyword cannot be used in the same way. A keyword should always be on the left side of the "=" sign. This is the most important difference between a scratch variable and a keyword. The following expressions assign values for other parameters of the electron beam, which are the transverse temperature, the longitudinal temperature, the shape, the radius and the current of the electron beam respectively. Depending on the shape of the electron, various parameters need to be set. In this example, one needs to set the radius and the current for a uniform DC electron beam. Other supported shapes and the related parameters (keywords) can be found in the lists in the next chapter.

The third section is the operation section. In the operation section, one can create the objects of the elements, calculate the expansion rate and perform the simulation. In this example, we create an object of the electron beam that has been defined in the above definition section. Please note that the definition section only records the values of the parameters, an element will not be created until the respective command is called in the operation section. For more commands supported in the operation section, please check out the list in the next chapter.

## IBS Expansion Rate Calculation

To calculate the IBS expansion rate, one needs to define the ion beam and the ring. Then set the parameters for IBS rate calculation. Finally, in the operation section create the ion beam and the ring, and call the command to calculate the IBS expansion rate.

```

section_ion      # Define the ion beam
.....
section_ring    # Define the ring
.....
section_ibs     # Set parameters for IBS rate calculation
.....
section_run
  create_ion_beam  # Create the ion beam
  create_ring      # Create the ring
  calculate_ibs    # Calculate the IBS rate

```

To calculate the total expansion rate, which is the summation of the IBS expansion rate and the electron cooling rate, one can call the command "total\_expansion\_rate" in section\_run.

## Cooling Rate Calculation

To calculate the cooling rate, one needs to define the ion beam, the ring, the electron beam and the cooler. Then set the parameters for cooling rate calculation. Finally, in the operation section create all the related elements aforementioned and call the command to calculate the cooling rate.

```
section_ion      # Define the ion beam
.....
section_ring     # Define the ring
.....
section_e_beam   # Define the electron beam
.....
sectoin_cooler   # Define the cooler
.....
section_ecool    # Set the parameters for the electron cooling rate calculation
.....
section_run
  create_ion_beam    # Create the ion beam
  create_ring        # Create the ring
  create_e_beam      # Create the electron beam
  create_cooler      # Create the cooler
  calculate_ecool    # Calculate the electron cooling rate
```

## Simulation

One can simulate the evolution of the ion beam under the IBS effect and/or electron cooling effect during a predetermined time. The emittances, momentum spread, bunch length (for bunched ion beam), and the total expansion rate in all the three dimensions will be outputted into a text file. If desired, the coordinates of all the ion samples can also be saved into files. These parameters are set in section\_simulation, and the simulation starts when the command "run\_simulation" is called in section\_run.

```
section_simulation # Set the parameters for the simulation
.....
section_run
  run_simulation   # Start simulation
```

## Luminosity calculation

To calculate the luminosity, one needs to define the particle number and the rms size of the two colliding particles, the center-to-center distance between the two beams, and the colliding frequency. Instead of giving the rms size of the beams, one can define the geometrical emittance and the beta function at the collision point of them, which may be convenient in many cases. An example is given as follows.

```
section_luminosity
  distance_x = 1e-3
  distance_y = 1e-6
```

```

particle_number_1 = 1e7
particle_number_2 = 1e10
frequency = 1000
bet_x_1 = 0.01
bet_y_1 = 0.01
bet_x_2 = 0.01
bet_y_2 = 0.01
geo_emit_x_1 = 1e-6
geo_emit_x_2 = 4e-7
geo_emit_y_1 = 1e-6
geo_emit_y_2 = 4e-7
use_ion_emittance = false

section_run
    calculate_luminosity

```

If one wants to use the ion beam defined in the cooling simulation in the luminosity calculation, the parameter `use_ion_emittance` should be set to `true`. ( The default value of it is `true`.) Then the program will use the geometrical emittance of the ion beam to set up the first colliding beam. Please note one has to create the ion beam before the luminosity calculation.

```

section_ion #define the ion beam
    ...

section_luminosity
    distance_x = 0
    distance_y = 0
    particle_number_1 = 1e7
    particle_number_2 = 1e10
    frequency = 1000
    bet_x_1 = 0.01
    bet_y_1 = 0.01
    bet_x_2 = 0.01
    bet_y_2 = 0.01
    geo_emit_x_2 = 4e-7
    geo_emit_y_2 = 4e-7
    use_ion_emittance = true

section_run
    create_ion_beam
    calculate_luminosity

```

If one wants to calculate the instant luminosity during the simulation, one should set the `calc_luminosity` parameter in `section_simulation` to be `true`.

```

section_luminosity
    ...

section_simulation
    calc_luminosity = true
    ...

section_run
    run_simulation

```

# List of sections, keywords, and commands

## section\_scratch

Keywords	Meaning
list_var	list all the variables that has been defined.
list_const	list all the constants.
list_exp	list all the expression.
print	Use this command in format "print x" and it will print the value of the variable x in the screen.
printstr	Use this command in format "printstr string" and it will pring the "string" in the screen.

The following keywords records the results from the previous computation. They can be used to set up the value for the following computation or to display the results onto the screen.

Keywords	Meaning
vl_emit_nx	horizontal normalized emittance.
vl_emit_ny	vertical normalized emittance.
vl_momentum_spread	The momentum spread.
vl_bunch_length	The rms bunch length for a bunched ion beam. The value is zero for a coasting ion beam.
vl_rate_ibs_x	horizontal ibs expansion rate.
vl_rate_ibs_y	vertical ibs expansion rate.
vl_rate_ibs_s	longitudinal ibs expansion rate.
vl_rate_ecool_x	horizontal electron cooling rate.
vl_rate_ecool_y	vertical electron cooling rate.
vl_rate_ecool_s	longitudinal electron cooling rate.
vl_rate_total_x	total expansion rate in the horizontal direction.
vl_rate_total_y	total expansion rate in the vertical direction.
vl_rate_total_s	total expansion rate in the longitudinal direction
vl_t	time

## section\_ion

Keywords	Meaning
charge_number	Number of the charges of the ion
mass	Mass in [MeV/c <sup>2</sup> ] of the ion
kinetic_energy	Kinetic energy in [MeV] of the ion
norm_emit_x	Normalized horizontal emittance in [m*rad] of the ion beam
norm_emit_y	Normalized vertical emittance in [m*rad] of the ion beam
momentum_spread	Momentum spread of the ion beam
particle_number	Total particle number for coasting ion beam or the particle number of one bunch for bunched ion beam.
rms_bunch_length	RMS bunch length for bunched ion beam in [m]

### section\_ring

Keywords	Meaning
lattice	The name of the file that saves the lattice. This file should be in the MAD X output format (.tfs).
qx	Transverse betatron tune
qy	Vertical betatron tune
qs	Synchrotron tune
gamma_tr	Transition gamma
rf_v	Voltage of the RF cavity in [V]
rf_h	Harmonic number
rf_phi	RF phase in [2\$\\pi\$]

### section\_cooler

Keywords	Meaning
length	Length of the cooler in [m]
section_number	Number of the coolers
magnetic_field	Magnetic field in [T]
bet_x	Beta function in horizontal direction in [m]
bet_y	Beta function in vertical direction in [m]
disp_x	Dispersion in horizontal direction in [m]
disp_y	Dispersion in vertical direction in [m]
alpha_x	Alpha in horizontal direction
alpha_y	Alpha in in vertical direction
disp_dx	Derivative of the dispersion in horizontal direction
disp_dy	Derivative of the dispersion in vertical direction

### section\_e\_beam

Keywords	Meaning
gamma	Lorentz factor gamma for the cooling electron beam
tmp_tr	Transverse temperature in [eV]
tmp_l	Longitudinal temperature in [eV] for the cooling electron beam
shape	Electron beam shape. Choose from dc_uniform, bunched_gaussian, bunched_uniform, bunched_uniform_elliptic, dc_uniform_hollow, bunched_uniform_hollow, bunched_user_defined.
radius	Radius of dc_uniform or bunched_uniform electron beam in [m].
current	Current of dc_uniform or bunched_uniform electron beam. For bunched_uniform beam, set the current as if it is a dc_uniform beam in [A].
length	Length of the bunched_uniform electron beam in [m].
sigma_x	RMS size in horizontal direction of bunched_gaussian electron beam in [m].



Keywords	Meaning
sigma_y	RMS size in vertical direction of bunched_gaussian electron beam in [m].
sigma_z	RMS bunch length of bunched_gaussian electron beam in [m].
rh	Length of the semi-axis in horizontal direction in [m].
rv	Length of the semi-axis in vertical direction in [m].
r_inner	Inner radius of a hollow beam in [m]
r_outter	Outter radius of a hollow beam in [m]
particle_file	Name of the file that saves the particles if the beam shape is defined as "bunched_user_defined"
total_particle_number	Total number of particles to load from the user-provided file
box_particle_number	Maximum number of particles in each childless box when constructing the tree structure. Default is 200.
line_skip	Number of lines to skip when loading particles from the user-provided text file.
vel_pos_corr	Whether to consider the correlation between the velocity and the position. Default is false.
binary_file	Whether the user-provided file is in binary format. Default is false, which means a text file.
buffer_size	Buffer size when loading particles from the user-provided binary file.
multi_bunches	If true, use multiple electron bunches to cool one ion beam. The electron bunches are assumed to be the same except that their positions are different. One should set at least one of list_cx, list_cy, and list_cz for the centers of the electron bunches.
list_cx	When multi_bunches to be true, use list_cx to set the horizontal coordinates of the electron bunches. The format should be integer,double,double, ... The first number should be an integer, which tells how many horizontal coordinates (the double flouting numbers) follows it. All the numbers are seperated by coma.
list_cy	When multi_bunches to be true, use list_cy to set the vertical coordinates of the electron bunches. The format is the same as that of list_cx.
list_cz	When multi_bunches to be true, use list_cz to set the longitudinal coordinates of the electron bunches. The format is the same as that of list_cx.

## section\_ibs

Keywords	Meaning
nu	Set the grid number in horizontal direction for the 3D integration.
nv	Set the grid number in vertical direction for the 3D integration.
nz	Set the grid number in longitudinal direction for the 3D integration.
log_c	Coulomb logarithm. If log_c is set, then the integration in the longitudinal direction is replaced by the Coulomb logarithm. Thus the parameter nz is ignored.
coupling	Transverse coupling rate, ranging from 0 to 1.
model	Model for IBS expansion rate calculation: Martini or BM.

### section\_ecool

Keywords	Meaning
sample_number	Number of the sample ions.
force_formula	Choose the formula for friction force calculation. Now only support the Parkhomchuk formul, using force_formula = PARKHOMCHUK.

### section\_luminosity

Keywords	Meaning
distance_x	Horizontal distance between the centers of the two colliding beam, in [m].
distance_y	Vertical distance between the centers of the two colliding beam, in [m].
particle_number_1	Particle number of the first colliding beam.
particle_number_2	Particle number of the 2nd colliding beam.
frequency	Colliding frequency, in [1/s].
bet_x_1	Horizontal beta function of the first colliding beam at the colliding point, in [m].
bet_y_1	Vertical beta function of the first colliding beam at the colliding point, in [m].
bet_x_2	Horizontal beta function of the second colliding beam at the colliding point, in [m].
bet_y_2	Vertical beta function of the second colliding beam at the colliding point, in [m].
beam_size_x_1	Horizontal rms size of the first colliding beam, in [m].
beam_size_y_1	Vertical rms size of the first colliding beam, in [m].
beam_size_x_2	Horizontal rms size of the second colliding beam, in [m].
beam_size_y_2	Vertical rms size of the second colliding beam, in [m].
geo_emit_x_1	Geometrical horizontal emittance of the first colliding beam, in [m*rad]. If the beam size is given, this parameter is ignored.
geo_emit_y_1	Geometrical vertical emittance of the first colliding beam, in [m*rad].If the beam size is given, this parameter is ignored.
geo_emit_x_2	Geometrical horizontal emittance of the second colliding beam, in [m*rad].If the beam size is given, this parameter is ignored.
geo_emit_y_2	Geometrical vertical emittance of the second colliding beam, in [m*rad].If the beam size is given, this parameter is ignored.
use_ion_emittance	Whether to use the ion beam emittance to set up the first colliding beam: yes (true) or no (false). The default value is true. When the value is true, parameters of the beam size and the emittance of the first colliding beam is ignored and the ion beam should be defined and created before the luminosity calculation.

## section\_simulation

Keywords	Meaning
time	Total time to simulate, in [s].
step_number	Total number of steps. The time interval of each step is time/step_number.
sample_number	Number of the sample ions. The parameter must be set when using the Particle model to simulate the IBS expansion process without cooling. When setting this parameter with cooling effect, the "sample_number" parameter in the "section_ecool" will be overwritten by this value.
ibs	Choose to simulate the IBS effect or not by setting the value as "true" or "false".
e_cool	Choose to simulate the electron cooling effect or not by setting the value as "true" or "false".
model	"RMS" or "Particle" model to choose for the simulation.
output_file	Output file name
output_interval	The interval of steps to write into the output file. Default is one.
save_particle_interval	The interval of steps to save the 6D coordinates of the ions. No saving if the value is less than zero. Default is -1. This is only useful when using the Particle model in simulations.
ref_bet_x	TWISS parameters for the reference point. Only needed when the "model beam" method is selected and the electron cooling effect is not included in the simulation.
ref_bet_y	Same as above.
ref_alf_x	Same as above.
ref_alf_y	Same as above.
ref_disp_x	Same as above.
ref_disp_y	Same as above.
ref_disp_dx	Same as above.
ref_disp_dy	Same as above.
fixed_bunch_length	Maintain a constant ion bunch length. Default is false.
reset_time	Whether to reset the starting time to zero (value: true) or use the final time from the previous simulation (value: false).
overwrite	Whether overwrite the output file is it exists. The default value is true. If the value is false, a new output file will be generated. The name of the new file is created by adding a number before the specific file name.
calc_luminosity	Whether to calculate the luminosity during the simulation: yes (true) or no (false). The default value is false.

## section\_run

Keywords	Meaning
create_ion_beam	Create the ion beam.
create_ring	Create the ring. Must create the ion beam before calling this command.
create_e_beam	Create the electron beam
create_cooler	Create the cooler.
calculate_ibs	Calculate the IBS rate and output to the screen. Must create the ion beam and the ring before calling this command.
calculate_ecool	Calculate the electron cooling rate and output to the screen. Must create the ion beam, the ring, the electron beam, and the cooler before calling this command.
calculate_luminosity	Calculate the luminosity, in $[1/s * 1/cm^2]$
total_expansion_rate	Calculate the total expansion rate (summation of the ibs rate and electron cooling rate) and output to the screen. Must create the ion beam, the ring, the electron beam, and the cooler before calling this command.
run_simulation	Simulate the evolution of the ion beam under IBS and/or electron cooling effect(s).
srand	Seed the random number. It is used as "srand expression". The expression will be processed by the math parser and the simplest choice is an integer. Seed the random number with the same value will generate the same sequence of random numbers. This may be useful in debugging, testing, or verifying some results.

## Example

In the following example, a DC electron cooler and a bunched proton beam is defined. The IBS rate and the electron cooling rate are calculated. Then the evolution of the proton beam under both the IBS effect and the electron cooling effect is simulated for 600 seconds.

```
section_ion          # Define the ion (proton) beam
  charge_number = 1   # Charge number
  mass = 938.272      # Mass of the ion
  kinetic_energy = 8000 # Kinetic energy
  norm_emit_x = 2.2e-6 # Normalized emittance in horizontal direction
  norm_emit_y = 2.2e-6 # Normalized emittance in vertical direction
  momentum_spread = 0.0006 # Momentum spread
  particle_number = 6.58e11 # Total ion number (per bunch)
  rms_bunch_length = 7      # Rms bunch length of the bunched ion beam
```

```

section_ring                                # Define the ring
    lattice = MEICColliderRedesign1IP.tfs  # file that saves the lattice of the
ring
section_ibs #define the arguments for IBS calculation
    nu = 100          # Grid number in horizontal direction for IBS integration
    nv = 100          # Grid number in vertical direction for IBS integration
    nz = 40           # Grid number in longitudinal direction for IBS integration
    log_c = 20.6       # Define Coulomb logarithm. nz is ignored after log_c is
defined.
    coupling = 0       # No coupling
section_cooler                             # Define the cooler
    length = 3.4       # Cooler length
    section_number = 1  # Number of coolers
    magnetic_field = 0.039 # Magnetic field
    bet_x = 10          # Twiss parameter at the cooler
    bet_y = 10
    #disp_x = 0          # If the values are zero, the command can be
omitted.
    #disp_y = 0
    #alpha_x = 0
    #alpha_y = 0
    #disp_dx = 0
    #disp_dy = 0
section_scratch                             # A scratch section
    m = 938.272        # Define variable m and assign a value.
    ke = 8000           # Define variable ke and assign a value.
    gamma = ke/m + 1    # Define variable gamma and calculate its value.
section_e_beam                             # Define the electron beam
    gamma = gamma       # Lorentz factor, the right "gamma" is the variable
define above.
    tmp_tr = 0.1        # Transverse temperature
    tmp_l = 0.01        # Longitudinal temperature
    shape = dc_uniform  # Shape of the electron beam, DC beam with uniform
charge density
    radius = 0.004      # Radius of the DC electron beam
    current = 2          # Current is 2 A
section_ecool                             # Set parameters for electron cooling rate
calculation
    sample_number = 10000          # Number of ion samples
    force_formula = PARKHOMCHUK    # Formula for friction force calculation
section_run                             # Operation section
    create_ion_beam
    create_ring
    calculate_ibs                    # Calculate the IBS rate
    create_e_beam
    create_cooler
    calculate_ecool                  # Calculate the electron cooling rate
    total_expansion_rate             # Calculate the total rate = IBS rate + electron
cooling rate
section_simulation                       # Set parameters for simulation
    ibs = on                         # Simulate IBS effect
    e_cool = on                     # Simulate electron cooling effect
    time = 600                      # Time to simulate
    step_number = 600               # Number of steps
    sample_number = 100000          # Number of ion samples
    #save_particle_interval = 100    # Save the coordinates of the ions
every 100 steps

```

```

output_file = simulation_test.txt      # File to save the simulation
results
model = particle                      # Select the model used in the
simulation
section_run                          # Operation section
run_simulation                        # Start simulation

```

## Extended Topics

### Keep a constant bunch length of the ion beam in simulation

The momentum spread of the ion beam changes due to the intrabeam scattering effect and the electron cooling effect during the simulation, hence the bunch length changes if the RF voltage is constant. However, if the RF voltage changes accordingly with the momentum spread, it is possible to maintain a constant bunch length. JSPEC allows the user to choose whether to keep the bunch length constant in the simulation. When the bunch length is maintained constant, the RF voltage is calculated and saved in the output file.

To use this feature, one needs to set the parameter "fixed\_bunch\_length" in section\_simulation to be **true**. One also needs to set the parameters, rf\_h (harmonic number), rf\_phi (RF phase), and gamma\_tr (transition gamma) in section\_ring.

```

section_ring #define the ring
...
rf_h = 3584
rf_phi = 0
gamma_tr = 12.46

...

section_simulation
...
fixed_bunch_length = true

```

### Use of the scratch section

In the scratch section, one can define variables and perform some simple calculations using the variables. These variables are accessible in the following sections. In the following example, one puts many parameters in the scratch section and use them to define the ion beam, electron beam and the cooler in the following sections. This is convenient to adjust the parameters in simulations since all the parameters are defined on top of the input file.

```

section_scratch
#Ion beam parameters:
ex = 0.75e-6    # normalized horizontal emittance
ey = 0.15e-6    # normalized vertical emittance
dp = 0.0006    # momentum spread
np = 0.98e10    # proton number
ds = 0.02      # proton bunch length
ke = 100000    # proton kinetic energy
me = 938.272   # proton mass
gamma = ke/me+1

```

```

beta = (1-gamma^(-2))^(1/2)
dx = 0.9      # horizontal dispersion at the cooler
dy = 0.4      # vertical dispersion at the cooler
cpl = 0.5     # transverse coupling
twiss_beta = 100 # beta function at the cooler
sigma_x = (twiss_beta*ex/beta/gamma)^(1/2) # rms horizontal bunch size
sigma_y = (twiss_beta*ey/beta/gamma)^(1/2) # rms vertical bunch size

#Electron beam parameters:
q_e = 3.2E-9   # electron number
l_e = 0.03     # electron bunch length
k_c = 299792458.0 # speed of light
I_e = q_e*beta*k_c/l_e # peak current of the electron beam

section_ion #define the ion beam
  charge_number = 1
  mass = 938.272
  kinetic_energy = ke
  norm_emit_x = ex
  norm_emit_y = ey
  momentum_spread = dp
  particle_number = np
  rms_bunch_length = ds

section_ring #define the ring
  lattice = MEIColliderRedesign1IP.tfs

section_ibs #define the arguments for IBS calculation
  model = bm
  log_c = 20
  coupling = cpl

section_cooler
  length = 60
  section_number = 1
  magnetic_field = 1
  bet_x = twiss_beta
  bet_y = twiss_beta
  disp_x = dx
  disp_y = dy

section_e_beam
  gamma = gamma
  shape = bunched_uniform_elliptic
  rh = sigma_x
  rv = sigma_y
  current = I_e
  length = l_e
  tmp_tr = 0.246
  tmp_l = 0.184
...

```

---

1. The author intended to write this expression in this way in order to emphasize the difference between a scratch variable and a keyword. However, this expression may be confusing. So it is not recommended to use scratch variables with the same name of a keyword. [↩](#)