

Introduction to Probability, Statistics and Data Handling	Basic Definition and Concepts
Tutorial 1	

Subjects for discussion:

1. What is the role of *statistics*?
2. What is meant by the terms: *population, sample*? Give examples.
3. What is a random *experiment, outcome, sample space, event*? Describe.
4. How would like to measure the *probability* of an event?

### Problem Set 1: Basic probability

1. A fair coin is tossed three times.
  - a) define the population and construct a sample space, how many outcomes are possible?
  - b) find a probability that at least one head will appear,
  - c) define:
    - two outcomes that are mutually exclusive,
    - two outcomes and find the sum of them,
    - two outcomes with non-zero intersection;
  - d) calculate the probability that:
    - the coin lands heads more often than tails,
    - the coin lands heads at least twice.
    - the coin lands heads on the last toss.
2. We have 10 students in our group. Four of them learn Spanish (event  $A$ ), two German ( $B$ ), and one German and Spanish. Are  $A$  and  $B$  independent?
3. The table describes the distribution of a random sample  $S$  of 100 individuals, organized by gender and whether they are right- or left-handed. Let's denote the events  $M$  = the subject is male,  $F$  = the subject is female,  $R$  = the subject is right-handed,  $L$  = the subject is left-handed. Compute the following probabilities:

	R	L
Males	43	9
Females	44	4

- a)  $P(M)$
- b)  $P(F)$
- c)  $P(R)$
- d)  $P(L)$
- e)  $P(M \text{ AND } R)$
- f)  $P(F \text{ AND } L)$
- g)  $P(M \text{ OR } F)$
- h)  $P(M \text{ OR } R)$
- i)  $P(F \text{ OR } L)$
- j)  $P(M')$
- k)  $P(R|M)$
- l)  $P(F|L)$
- m)  $P(L|F)$

4. Carlos plays college soccer. He makes a goal 65% of the time he shoots. Carlos is going to attempt two goals in a row in the next game.  $A$  = the event Carlos is successful on his first attempt.  $P(A) = 0.65$ .  $B$  = the event Carlos is successful on his second attempt.  $P(B) = 0.65$ . Carlos tends to shoot in streaks. The probability that he makes the second goal **GIVEN** that he made the first goal is 0.90.
  - a) What is the probability that he makes both goals?
  - b) What is the probability that Carlos makes either the first goal or the second goal?
  - c) Are  $A$  and  $B$  independent?
  - d) Are  $A$  and  $B$  mutually exclusive?