

L27

Recursion Basics

*The System Design Course Offer ends tonight.
If interested, check out your whatsapp and
purchase **before midnight**.*

Messages were sent on 17th Feb, around 6:35PM.

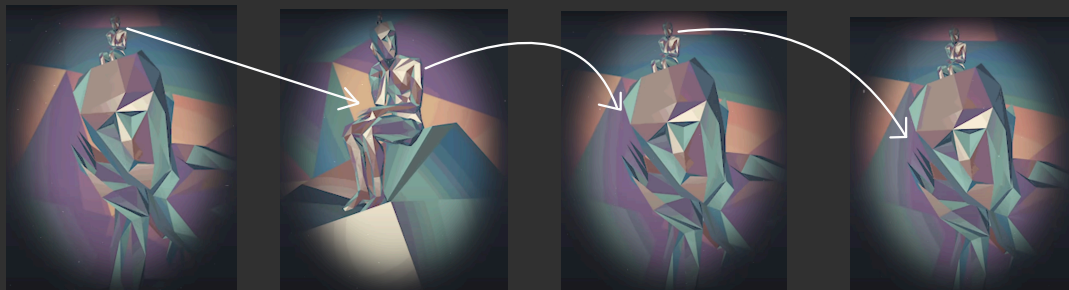
Join Discord - <https://bit.ly/ly-discord>

RECAP

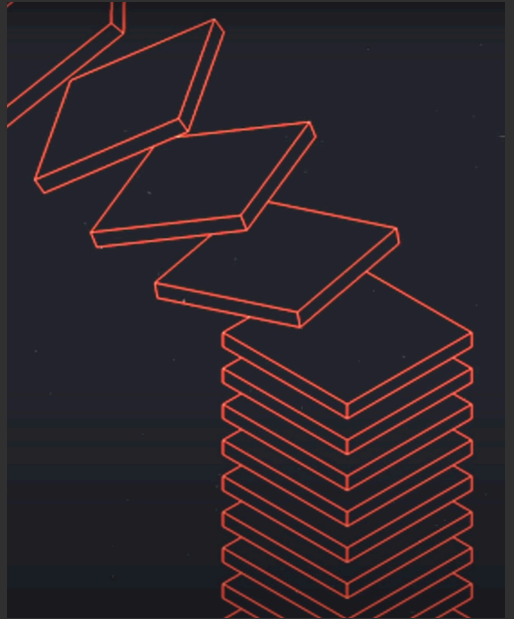
What is Recursion?

It's magic

Imagine having a dream inside of a dream inside of a dream.
Pretty dreamy, right?



```
void dream() {  
  dream()  
}
```



In layman terms, when a function calls itself, it's called recursion.

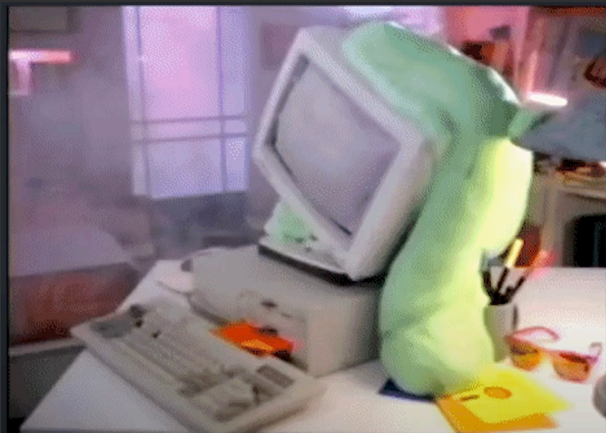
▷ main() -
{
 print ("Faz");

→ main()
}

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But, it just running indefinitely is of no use, right?



So, there needs to be a stopping condition
(AKA Base Condition)

```
void dream() {  
  if(woken_up)  
    return;  
  dream()  
}
```



BASE CASE

short circuits the loop

```

int factorial (int n) (5) (4) (3)
{
    if (n == 0) return 1;
    int partial-ans = factorial(n-1);
    int ans = partial-ans * n;
    return ans;
}

```

Let's try finding the factorial of a number

$$5! = 1 \times 2 \times 3 \times 4 \times 5$$

$$5! = 4! \times 5$$

$$n! = n \times \underline{\underline{(n-1)!}}$$

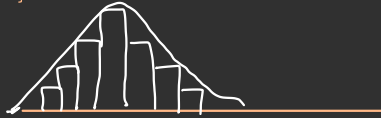
How is it working internally?
AKA Call Stack

```
int factorial(int n) 1
{
    if (n == 0) return 1;
    int partial-ans = factorial(n-1);
    int ans = n * partial-ans;
    return ans;
}
```

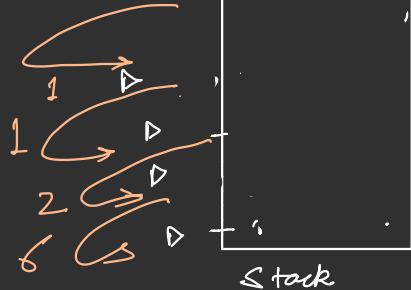
```
int factorial(int n) 2
{
    if (n == 0) return 1;
    int partial-ans = factorial(n-1);
    int ans = n * partial-ans;
    return ans;
}
```

```
int factorial(int n) 3
{
    if (n == 0) return 1;
    int partial-ans = factorial(n-1);
    int ans = n * partial-ans;
    return ans;
}
```

```
int factorial(int n) 0
{
    if (n == 0) return 1;
    int partial-ans = factorial(n-1);
    int ans = n * partial-ans;
    return ans;
}
```



$n!$



Let's do some more practice now.

```

void printN(int n, int i)
{
    if (i == n+1) return;
    print(i);
    printN(n, i+1);
}

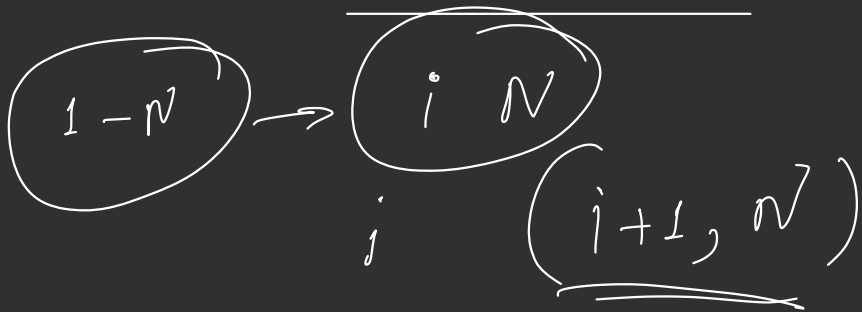
```

```

main()
{
    printN(5, 1);
}

```

Given a value of N, print numbers from 1 to N.



Given a value of N, print numbers from N to 1.

$N=0, 0$
 $N=1, 1$
 $N=2, 1$
 $N=3, 2$

$N=4, 3$
 $N=5, 5$
 $N=6, 8$

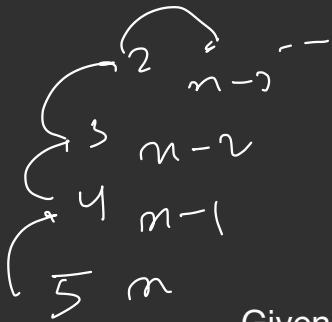
Given a number N , find n th fibonacci number ($f_0 = 0, f_1 = 1$)
 $(F_n = F_{n-1} + F_{n-2})$

```

int fibo(n) {
    if (n == 0 || n == 1) return n;
    int a = fibo(n-1);
    int b = fibo(n-2);
    return a + b;
}

```

$(0 = 0 + 1)$



$$2^{-4} = \frac{1}{2^4}$$

$$2^{-n} = \frac{1}{2^n}$$

Given a number a, n - find $\text{pow}(a, n)$

$$a^n$$

$$x^n \rightarrow x * x^{n-1}$$

$$x^n \rightarrow x^{n/2} * x^{n/2}$$

$$x^6 \rightarrow x^3 * x^3$$

$$\underline{x^7 \rightarrow x^3 * x^3 * x}$$

$$\begin{array}{ll} x^n \rightarrow x^{n/2} * x^{n/2} & n \text{ is even} \\ \emptyset \rightarrow x^{n/2} * x^{n/2} * x & n \text{ is odd} \end{array}$$

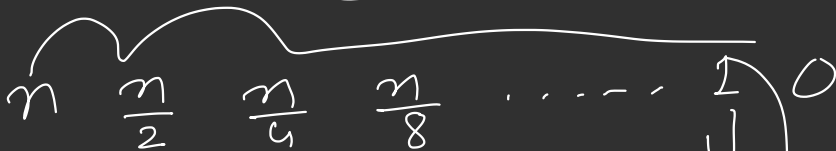
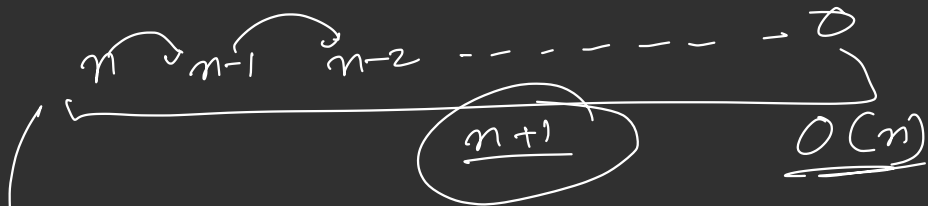


Diagram illustrating a sequence of numbers: $\frac{n}{2^0}, \frac{n}{2^1}, \frac{n}{2^2}, \frac{n}{2^3}, \dots$. A bracket under the sequence is labeled $\log_2 n + 1$.

$$L = \frac{n}{2^k} \quad \frac{2^k = n}{\log_2 n = \log n}$$

$$k \log 2 = \log n$$

Given a number n , check if n is a perfect power of 3.

Thank You!

Reminder: Going to the gym & observing the trainer work out can help you know the right technique, but you'll muscle up only if you lift some weights yourself.

So, PRACTICE, PRACTICE, PRACTICE!