

$$Y = d \times e$$

$$Y = (a+b) \times (b-c)$$

$$Y = -(a+b) - (a+2)$$

$$d = a + b$$

$$e = b - c$$

a

b

c

1

2

3

$$\frac{\partial Y}{\partial a} = \frac{\partial Y}{\partial d} \cdot \frac{\partial d}{\partial a} =$$

$$\nabla Y = \begin{bmatrix} \frac{\partial Y}{\partial d} & \frac{\partial Y}{\partial e} \end{bmatrix}$$

$$\nabla Y = \begin{bmatrix} \frac{\partial Y}{\partial d} \\ \frac{\partial Y}{\partial e} \end{bmatrix} = \begin{bmatrix} \frac{\partial d}{\partial a} \\ \frac{\partial d}{\partial b} \end{bmatrix}$$

$$= \begin{bmatrix} \frac{\partial d}{\partial a} & \frac{\partial d}{\partial b} \\ \frac{\partial e}{\partial a} & \frac{\partial e}{\partial b} \end{bmatrix}$$

$$\begin{bmatrix} \frac{\partial Y}{\partial a} \\ \frac{\partial Y}{\partial b} \\ \frac{\partial Y}{\partial c} \end{bmatrix} = \begin{bmatrix} \frac{\partial d}{\partial a} \times \frac{\partial Y}{\partial d} = 1 \times e = e \\ \frac{\partial Y}{\partial b} = \frac{\partial Y}{\partial d} \cdot \frac{\partial d}{\partial b} + \frac{\partial Y}{\partial e} \cdot \frac{\partial e}{\partial b} = \frac{\partial Y}{\partial d} \cdot \frac{\partial d}{\partial b} + \frac{\partial Y}{\partial e} \cdot \frac{\partial e}{\partial b} = e + d \times 1 = e + d \\ \frac{\partial Y}{\partial c} = \frac{\partial Y}{\partial e} \cdot \frac{\partial e}{\partial c} = d \times -1 = -d \end{bmatrix}$$

$$\nabla Y = \begin{bmatrix} \frac{\partial Y}{\partial d} \\ \frac{\partial Y}{\partial e} \end{bmatrix}$$

$$\lim_{h \rightarrow 0} \frac{-(d+h+3) - 3}{h} = \lim_{h \rightarrow 0} \frac{-h-6}{h} = \frac{-1}{1} = -1$$