

Design context-free grammar (CFG) for the following languages:

1. $\{x^{2n} \# y^{3n} \mid n \geq 1\}$ Here, $\Sigma = \{x, y, \#\}$
2. $L = \{a^m b^n c^{3n} d^{2m} \mid \text{where } m, n \geq 1\}$
3. $L = \{x^i y^j z^k \mid \text{where } i=k \text{ or } j=k \text{ and } i, j, k \geq 0\}$
4. $L = \{w \text{ is consisted of } \{0,1\} \mid w \text{ is odd and mid symbol is } 0\}$
5. $L = \{w \text{ is considered of } \{0,1\} \mid w \text{ is of even length \& } w \text{ starts and ends with different symbol}\}$
6. $L = \{a^i b^j c^k \mid \text{where } i \neq j \text{ and } k \geq 1\}$
7. $L = \{a^i b^j c^k \mid 2i + 3j \geq 6 \text{ and } 4i - 8j \geq -16 \text{ and } k \geq 1\}$
8. $L = \{a^{m+n} c^{3n} d^{2m} \mid n, m \geq 2\}$
9. $L = \{c^p \# d^q g^r h \mid q=4p, p, q \geq 0 \text{ and } r \geq 2\}$
10. $L = \{a^m b^n c^u d^v \mid m = \frac{n}{2}, v = \frac{u}{4}, m, n, u, v > 0\}$

Consider the following Context-free grammars(CFG) and answer according to it:

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| 1. | $S \rightarrow S + S \mid S * S \mid A \mid B$ $A \rightarrow aA \mid 1$ $B \rightarrow bB \mid 2$ | With the help of Top-Down Parse Trees, find-out if the grammar is Ambiguous or not for the string “bbb2 + aa1 + b2” |
| 2. | $S \rightarrow S + S \mid S - S \mid (S) \mid T$ $T \rightarrow X * X \mid X \% X \mid X$ $X \rightarrow x \mid y \mid z \mid Y$ $Y \rightarrow 0 \mid 1 \mid 2 \mid 3$ | With the help of Leftmost derivation, derive the following string “(x + 2*y) - (3*z + 1)” |

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| 3. | $E \rightarrow E + E \mid E - E \mid E = E$ $E \rightarrow MNV \mid MN$ $M \rightarrow - \mid \varepsilon$ $N \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \mid NN$ $V \rightarrow x \parallel y \mid z$ | <p>a. With the help of Top-Down Parse Trees, figure out if the grammar is Ambiguous or not for the string “x + y + z = 2”</p> <p>b. Show the Right Most Derivation for the string “-26x + 3y - 8z = -83”</p> |
| 4. | $S \rightarrow AS \mid BAC$ $A \rightarrow A1 \mid 0A1 \mid 0B1 \mid B$ $B \rightarrow 0B \mid 0 \mid \epsilon$ $C \rightarrow 1 \mid \epsilon$ | With the help of Top-Down Parse Trees, find-out if the grammar is Ambiguous or not for the string 00011111 |
| 5. | $E \rightarrow E+E \mid E-E \mid (E) \mid V$ $V \rightarrow p \mid q \mid r \mid X$ $X \rightarrow X*X \mid X\%X \mid Y$ $Y \rightarrow 0 \mid 1$ | With the help of Leftmost derivation, find-out if the grammar is Ambiguous or not for the string p+(0*1%0)-r |
| 6. | $S \rightarrow 2BA \mid 1S \mid 2A$ $B \rightarrow 1B3 \mid 1S3 \mid \varepsilon$ $A \rightarrow A11 \mid 12AS3 \mid B \mid \varepsilon$ | <p>Consider the following context-free grammars (CFG). With the help of Top-Down Parse Tree decide whether the grammars are ambiguous or not:</p> <p style="text-align: center;">211211313</p> |
| 7. | $B \rightarrow 11BS \mid 0S0B \mid \varepsilon$ $S \rightarrow AC01 \mid 0S \mid 1S \mid A1$ $A \rightarrow 1 \mid B \mid CA \mid \varepsilon$ $C \rightarrow x \mid y \mid A$ | <p>Consider the following context-free grammars (CFG). With the help of Top-Down Parse Tree decide whether the grammars are ambiguous or not:</p> <p style="text-align: center;">011010</p> |

