

2.4 Construct the prime field  $GF(11)$  with modulo-11 addition and multiplication. Find all the primitive elements, and determine the orders of other elements.

2.14 Construct a table for  $GF(2^5)$  based on the primitive polynomial  $p(X) = 1 + X^2 + X^5$ . Let  $\alpha$  be a primitive element of  $GF(2^5)$ . Find the minimal polynomials of  $\alpha^3$  and  $\alpha^7$ .

2.17 Let  $\alpha$  be a primitive element in  $GF(2^4)$ . Use Table 2.8 to find the roots of  $f(X) = X^3 + \alpha^6 X^2 + \alpha^9 X + \alpha^9$ .

2.19 Let  $\alpha$  be a primitive element in  $GF(2^4)$ . Use Table 2.8 to solve the following simultaneous equations for  $X$ ,  $Y$ , and  $Z$ :

$$\begin{aligned}X + \alpha^5 Y + Z &= \alpha^7, \\X + \alpha Y + \alpha^7 Z &= \alpha^9, \\ \alpha^2 X + Y + \alpha^6 Z &= \alpha.\end{aligned}$$