Hierarchical structures with LAR *

Alberto Paoluzzi

July 23, 2015

Contents

1			
	1.1	Design decision	2
	1.2	Affine mapping	
	1.3	Elementary matrices	2
2	Structure types handling		
	2.1	Mat and Verts classes	5
	2.2	Model class	5
	2.3	Struct iterable class	5
	2.4	Struct containment box	7
3	Structure to LAR conversion		
	3.1	Remove duplicate faces	7
	3.2	Structure to pair (Vertices, Cells) conversion	8
	3.3	Embedding or projecting LAR models	6
4	Hierarchical complexes		
	4.1	Traversal of hierarchical structures	10
		4.1.1 Traversal of nested lists	11
5	Lars	struct exporting	16
6	Examples		
	.1	Importing a generic module	20

^{*}This document is part of the Linear Algebraic Representation with CoChains (LAR-CC) framework [CL13]. July 23, 2015

1 Affine transformations

1.1 Design decision

First we state the general rules that will be satisfied by the matrices used in this module, mainly devoted to apply affine transformations to vertices of models in structure environments:

- 1. assume the scipy ndarray as the type of vertices, stored in row-major order;
- 2. use the last coordinate as the homogeneous coordinate of vertices, but do not store it explicitly;
- 3. store explicitly the homogeneous coordinate of transformation matrices.
- 4. use labels 'verts' and 'mat' to distinguish between vertices and transformation matrices.
- 5. transformation matrices are dimension-independent, and their dimension is computed as the length of the parameter vector passed to the generating function.

1.2 Affine mapping

```
⟨ Apply an affine transformation to a LAR model 1⟩ ≡

def larApply(affineMatrix):
    def larApply0(model):
        if isinstance(model,Model):
            V = scipy.dot(array([v+[1.0] for v in model.verts]), affineMatrix.T).tolist()
            V = [v[:-1] for v in V]
            CV = copy.copy(model.cells)
            return Model((V,CV))
        elif isinstance(model,tuple) or isinstance(model,list):
            if len(model)==2: V,CV = model
            elif len(model)==3: V,CV,FV = model
            V = scipy.dot([list(v)+[1.0] for v in V], affineMatrix.T).tolist()
            if len(model)==2: return [v[:-1] for v in V],CV
            elif len(model)==3: return [v[:-1] for v in V],CV,FV
            return larApply0
```

Macro referenced in 16.

1.3 Elementary matrices

Elementary matrices for affine transformation of vectors in any dimensional vector space are defined here. They include translation, scaling, rotation and shearing.

Translation

Macro referenced in 3a.

```
\langle \text{Translation matrices } 2a \rangle \equiv
      def t(*args):
           d = len(args)
           mat = scipy.identity(d+1)
           for k in range(d):
                mat[k,d] = args[k]
           return mat.view(Mat)
Macro referenced in 16.
Scaling
\langle\, {\rm Scaling\ matrices\ 2b}\, \rangle \equiv
      def s(*args):
           d = len(args)
           mat = scipy.identity(d+1)
           for k in range(d):
                mat[k,k] = args[k]
           return mat.view(Mat)
Macro referenced in 16.
Rotation
\langle Rotation matrices 3a\rangle \equiv
      def r(*args):
           args = list(args)
           n = len(args)
           ⟨ plane rotation (in 2D) 3b⟩
           \langle \text{ space rotation (in 3D) } 3c \rangle
           return mat.view(Mat)
Macro referenced in 16.
\langle \text{ plane rotation (in 2D) 3b} \rangle \equiv
      if n == 1: # rotation in 2D
           angle = args[0]; cos = COS(angle); sin = SIN(angle)
           mat = scipy.identity(3)
           mat[0,0] = cos;
                                  mat[0,1] = -sin;
           mat[1,0] = sin;
                                  mat[1,1] = cos;
```

```
\langle \text{ space rotation (in 3D) 3c} \rangle \equiv
      if n == 3: # rotation in 3D
          mat = scipy.identity(4)
          angle = VECTNORM(args); axis = UNITVECT(args)
          cos = COS(angle); sin = SIN(angle)
           ⟨ elementary rotations (in 3D) 3d ⟩
           \langle \text{ general rotations (in 3D) } 3e \rangle
Macro referenced in 3a.
\langle elementary rotations (in 3D) 3d\rangle \equiv
      if axis[1] == axis[2] == 0.0:
                                        # rotation about x
          mat[1,1] = cos;
                                mat[1,2] = -sin;
          mat[2,1] = sin;
                                mat[2,2] = cos;
      elif axis[0] == axis[2] == 0.0:
                                          # rotation about y
          mat[0,0] = cos;
                                mat[0,2] = sin;
          mat[2,0] = -sin;
                                  mat[2,2] = cos;
      elif axis[0] == axis[1] == 0.0:
                                          # rotation about z
          mat[0,0] = cos;
                                mat[0,1] = -sin;
          mat[1,0] = sin;
                                mat[1,1] = cos;
Macro referenced in 3c.
\langle \text{ general rotations (in 3D) 3e} \rangle \equiv
      else:
                     # general 3D rotation (Rodrigues' rotation formula)
          I = scipy.identity(3) ; u = axis
          Ux = scipy.array([
               [0,
                            -u[2],
                                          u[1]],
               [u[2],
                                        -u[0]],
                               Ο,
                                             0]])
               [-u[1],
                             u[0],
          UU = scipy.array([
               [u[0]*u[0],
                                u[0]*u[1],
                                                 u[0]*u[2]],
                                u[1]*u[1],
               [u[1]*u[0],
                                                 u[1]*u[2]],
               [u[2]*u[0],
                                u[2]*u[1],
                                                 u[2]*u[2]])
          mat[:3,:3] = cos*I + sin*Ux + (1.0-cos)*UU
```

Macro referenced in 3c.

2 Structure types handling

In order to implement a structure as a list of models and transformations, we need to be able to distinguish between two different types of scipy arrays. The first type is the one of arrays of vertices, the second one is the matrix array used to represent the fine transformations.

2.1 Mat and Verts classes

```
\langle \text{ types Mat and Verts 4a} \rangle \equiv
     """ class definitions for LAR """
     import scipy
     class Mat(scipy.ndarray): pass
     class Verts(scipy.ndarray): pass
Macro referenced in 16.
2.2
    Model class
\langle \text{ Model class 4b} \rangle \equiv
     class Model:
          """ A pair (geometry, topology) of the LAR package """
          def __init__(self,(verts,cells)):
              self.n = len(verts[0])
              # self.verts = scipy.array(verts).view(Verts)
              self.verts = verts
              self.cells = cells
          def __getitem__(self,i):
              return list((self.verts,self.cells))[i]
Macro referenced in 16.
2.3
      Struct iterable class
\langle Struct class 5\rangle \equiv
     from myfont import *
     class Struct:
          """ The assembly type of the LAR package """
          def __init__(self,data=None,name=None,category=None):
              if data==None or data==[]:
                   self.body = []
              else:
                   self.body = [item for item in data if item != None]
                   self.box = box(self)
                   self.dim = len(self.box[0])
              if name != None:
                   self.name = str(name)
              else:
                   self.name = str(id(self))
              if category != None:
```

self.category = str(category)

self.category = "feature"

else:

```
def __name__(self):
    return self.name
def __category__(self):
   return self.category
def __iter__(self):
    return iter(self.body)
def __len__(self):
    return len(list(self.body))
def __getitem__(self,i):
    return list(self.body)[i]
def __setitem__(self,i,value):
    self.body[i] = value
def __print__(self):
    return "<Struct name: %s>" % self.__name__()
def __repr__(self):
    return "<Struct name: %s>" % self.__name__()
    #return "'Struct(%s,%s)'" % (str(self.body),str(str(self.__name__())))
def set_name(self,name):
    self.name = str(name)
def clone(self,i=0):
    from copy import deepcopy
    newObj = deepcopy(self)
    if i != 0: newObj.name = self.name + "_" + str(i)
    return newObj
def set_category(self,category):
    self.category = str(category)
def boundary(self):
    data = struct2lar(self)
    if len(data) == 3:
        V,FV,EV = data
        #import pdb; pdb.set_trace()
        return V,FV,EV
    else:
        return "<Struct name: %s> boundary non computable" % self.__name__()
def draw(self,color=WHITE,scaling=1,metric=ID):
    vmin,vmax = self.box
    delta = VECTDIFF([vmax,vmin])
    point = CCOMB(self.box)
    scalingFactor = scaling*delta[0]/20.
    text = TEXTWITHATTRIBUTES (TEXTALIGNMENT='centre', TEXTANGLE=0,
                TEXTWIDTH=0.1*scalingFactor,
                TEXTHEIGHT=0.2*scalingFactor,
                TEXTSPACING=0.025*scalingFactor)
    point = metric([point])[0]
    return T([1,2,3])(point)(COLOR(color)(text(self.name)))
```

 \Diamond

2.4 Struct containment box

```
\langle Computation of the containment box of a Lar Struct or Model 6\rangle \equiv
     """ Computation of the containment box of a Lar Struct or Model """
     import copy
     def box(model):
         if isinstance(model,Mat): return []
         elif isinstance(model,Struct):
             dummyModel = copy.deepcopy(model)
             dummyModel.body = [term if (not isinstance(term,Struct)) else [term.box,[[0,1]]] for
             listOfModels = evalStruct( dummyModel )
             #dim = checkStruct(listOfModels)
             theMin,theMax = box(listOfModels[0])
             for theModel in listOfModels[1:]:
                 modelMin, modelMax = box(theModel)
                 theMin = [val if val<theMin[k] else theMin[k] for k,val in enumerate(modelMin)]
                 theMax = [val if val>theMax[k] else theMax[k] for k,val in enumerate(modelMax)]
             return [theMin,theMax]
         elif isinstance(model, Model):
             V = model.verts
         elif (isinstance(model,tuple) or isinstance(model,list)) and (len(model)==2 or len(model)=
             V = model[0]
         coords = TRANS(V)
         theMin = [min(coord) for coord in coords]
         theMax = [max(coord) for coord in coords]
         return [theMin,theMax]
```

Macro referenced in 16.

3 Structure to LAR conversion

3.1 Remove duplicate faces

```
⟨Remove duplicate faces 7a⟩ ≡

""" Remove duplicate faces """

from collections import defaultdict
def removeDups (CW):

    CW = list(set(AA(tuple)(CW)))

    CWs = list(set(AA(tuple) (AA(sorted)(CW)) ))

    no_duplicates = defaultdict(list)
    for f in CWs: no_duplicates[f] = []

    for f in CW:

        no_duplicates[tuple(sorted(f))] += [f]
```

```
CW = [f[0] for f in no_duplicates.values()]
return CW
```

Macro referenced in 16.

3.2 Structure to pair (Vertices, Cells) conversion

```
\langle Structure to pair (Vertices, Cells) conversion 7b\rangle \equiv
     """ Structure to pair (Vertices, Cells) conversion """
     def struct2lar(structure,metric=ID):
         listOfModels = evalStruct(structure)
         vertDict = dict()
         index, defaultValue, CW, W, FW = -1, -1, [], [], []
         for model in listOfModels:
              if isinstance(model, Model):
                  V,FV = model.verts,model.cells
             elif (isinstance(model,tuple) or isinstance(model,list)):
                  if len(model) == 2: V, FV = model
                  elif len(model)==3: V,FV,EV = model
             for k,incell in enumerate(FV):
                  outcell = []
                  for v in incell:
                      key = vcode(V[v])
                      if vertDict.get(key,defaultValue) == defaultValue:
                          index += 1
                          vertDict[key] = index
                          outcell += [index]
                          W += [eval(key)]
                          outcell += [vertDict[key]]
                  CW += [outcell]
              if len(model) == 3:
                  for k,incell in enumerate(EV):
                      outcell = []
                      for v in incell:
                          key = vcode(V[v])
                          if vertDict.get(key,defaultValue) == defaultValue:
                               index += 1
                               vertDict[key] = index
                               outcell += [index]
                               W += [eval(key)]
                           else:
                               outcell += [vertDict[key]]
                      FW += [outcell]
```

```
if len(model)==2:
    if len(CW[0])==2:
        CW = list(set(AA(tuple)(AA(sorted)(CW))))
    else: CW = removeDups(CW)
    return metric(W),CW

if len(model)==3:
    FW = list(set(AA(tuple)(AA(sorted)(FW))))
    CW = removeDups(CW)
    return metric(W),CW,FW
```

Macro referenced in 16.

3.3 Embedding or projecting LAR models

In order to apply 3D transformations to a two-dimensional LAR model, we must embed it in 3D space, by adding one more coordinate to its vertices.

Embedding or projecting a geometric model This task is performed by the function larEmbed with parameter k, that inserts its d-dimensional geometric argument in the $x_{d+1}, \ldots, x_{d+k} = 0$ subspace of \mathbb{E}^{d+k} . A projection transformation, that removes the last k coordinate of vertices, without changing the object topology, is performed by the function larEmbed with negative integer parameter.

```
⟨ Embedding and projecting a geometric model 9⟩ ≡
  def larEmbed(k):
    def larEmbed0(model):
        if len(model)==2: V,CV = model
        elif len(model)==3: V,CV,FV = model
        if k>0:
            V = [v+[0.]*k for v in V]
        elif k<0:
            V = [v[:-k] for v in V]
        if len(model)==2: return V,CV
        elif len(model)==3: return V,CV,FV
        return larEmbed0</pre>
```

Macro referenced in 16.

4 Hierarchical complexes

Hierarchical models of complex assemblies are generated by an aggregation of subassemblies, each one defined in a local coordinate system, and relocated by affine transformations

of coordinates. This operation may be repeated hierarchically, with some subassemblies defined by aggregation of simpler parts, and so on, until one obtains a set of elementary components, which cannot be further decomposed.

Two main advantages can be found in a hierarchical modeling approach. Each elementary part and each assembly, at every hierarchical level, are defined independently from each other, using a local coordinate frame, suitably chosen to make its definition easier. Furthermore, only one copy of each component is stored in the memory, and may be instanced in different locations and orientations how many times it is needed.

4.1 Traversal of hierarchical structures

Of course, the main algorithm with hierarchical structures is the *traversal* of the structure network, whose aim is to transform every encountered object from local to global coordinates, where the global coordinates are those of the network root (the only node with indegree zero).

A structure network can be modelled using a directed acyclic multigraph, i.e. a triple (N, A, f) made by a set N of nodes, a set A of arcs, and a function $f: A \to N^2$ from arcs to ordered pairs of nodes. Conversely that in standard oriented graphs, in this kind of structure more than one oriented arc is allowed between the same pair on nodes.

```
Script 8.3.1 (Traversal of a multigraph)
algorithm Traversal ((N, A, f) : multigraph) {
    CTM := identity \ matrix;
    TraverseNode (root)
}

proc TraverseNode (n : node) {
    foreach a \in A outgoing from n do TraverseArc (a);
    ProcessNode (n)
}

proc TraverseArc (a = (n, m) : arc) {
    Stack.push (CTM);
    CTM := CTM * a.mat;
    TraverseNode (m);
    CTM := Stack.pop()
}

proc ProcessNode (n : node) {
    foreach object \in n do Process( CTM * object)
}
```

Figure 1: Traversal algorithm of an acyclic multigraph.

A simple modification of a DFS (Depth First Search) visit of a graph can be used to traverse the structure network This algorithm is given in Figure 1 from [Pao03].

4.1.1 Traversal of nested lists

The representation chosen for structure networks with LAR is the serialised one, consisting in ordered sequences (lists) of either (a) LAR models, or (b) affine transformations, or (c) references to other structures, either directly nested within some given structure, or called by reference (name) from within the list.

The aim of a structure network traversal is, of course, to transform every component structure, usually defined in a local coordinate system, into the reference frame of the structure as a whole, normally corresponding with the reference system of the structure's root, called the *world coordinate* system.

The pattern of calls and returned values — In order to better understand the behaviour of the traversal algorithm, where every transformation is applied to all the following models, — but only if included in the same structure (i.e. list) — it may be very useful to start with an algorithm emulation. In particular, the recursive script below discriminates between three different cases (number, string, or sequence), whereas the actual traversal must do with (a) Models, (b) Matrices, and (c) Structures, respectively.

```
\langle Emulation of scene multigraph traversal 11a\rangle \equiv
     from pyplasm import *
     def __traverse(CTM, stack, o):
         for i in range(len(o)):
              if ISNUM(o[i]): print o[i], REVERSE(CTM)
              elif ISSTRING(o[i]):
                  CTM.append(o[i])
              elif ISSEQ(o[i]):
                  stack.append(o[i])
                                                        # push the stack
                   __traverse(CTM, stack, o[i])
                  CTM = CTM[:-len(stack)]
                                                     # pop the stack
     def algorithm(data):
         CTM, stack = ["I"],[]
          __traverse(CTM, stack, data)
```

Macro never referenced.

Some use example of the above algorithm are provided below. The printout produced at run time is shown from the emulation of traversal algorithm macro.

```
\langle Examples of multigraph traversal 11b\rangle \equiv
```

```
data = [1,"A", 2, 3, "B", [4, "C", 5], [6,"D", "E", 7, 8], 9]
     print algorithm(data)
     >>> 1 ['I']
         2 ['A', 'I']
         3 ['A', 'I']
         4 ['B', 'A', 'I']
         5 ['C', 'B', 'A', 'I']
         6 ['B', 'A', 'I']
         7 ['E', 'D', 'B', 'A', 'I']
         8 ['E', 'D', 'B', 'A', 'I']
         9 ['B', 'A', 'I']
     data = [1,"A", [2, 3, "B", 4, "C", 5, 6,"D"], "E", 7, 8, 9]
     print algorithm(data)
     >>> 1 ['I']
         2 ['A', 'I']
         3 ['A', 'I']
         4 ['B', 'A', 'I']
         5 ['C', 'B', 'A', 'I']
         6 ['C', 'B', 'A', 'I']
         7 ['E', 'A', 'I']
         8 ['E', 'A', 'I']
         9 ['E', 'A', 'I']
Macro never referenced.
\langle Emulation of traversal algorithm 12\rangle \equiv
     dat = [2, 3, "B", 4, "C", 5, 6, "D"]
     print algorithm(dat)
     >>> 2 ['I']
         3 ['I']
         4 ['B', 'I']
         5 ['C', 'B', 'I']
         6 ['C', 'B', 'I']
     data = [1, "A", dat, "E", 7, 8, 9]
     print algorithm(data)
     >>> 1 ['I']
         2 ['A', 'I']
         3 ['A', 'I']
         4 ['B', 'A', 'I']
         5 ['C', 'B', 'A', 'I']
         6 ['C', 'B', 'A', 'I']
         7 ['E', 'A', 'I']
         8 ['E', 'A', 'I']
         9 ['E', 'A', 'I']
     \Diamond
Macro never referenced.
```

Traversal of a scene multigraph The previous traversal algorithm is here customised for scene multigraph, where the objects are LAR models, i.e. pairs of vertices of type 'Verts and cells, and where the transformations are matrix transformations of type 'Mat'.

Check models for common dimension The input list of a call to larStruct primitive is preliminary checked for uniform dimensionality of the enclosed LAR models and transformations. The common dimension dim of models and matrices is returned by the function checkStruct, within the class definition Struct in the module lar2psm. Otherwise, an exception is generated (TODO).

```
⟨Check for dimension of a structure element (Verts or V) 13a) ≡
⟨Flatten a list 13b⟩
def checkStruct(lst):
    """ Return the common dimension of structure elements.

    TODO: aggiungere test sulla dimensione minima delle celle (legata a quella di immersione)
    """
    obj = lst[0]
    if (isinstance(obj,tuple) or isinstance(obj,list)):
        dim = len(obj[0][0])
    elif isinstance(obj,Model):
        dim = obj.n
    elif isinstance(obj,Mat):
        dim = obj.shape[0]-1
    elif isinstance(obj,Struct):
        dim = len(obj.box[0])
    return dim
```

Macro referenced in 16.

Flatten a list using Python generators The flatten is a generator that yields the non-list values of its input in order. In the example, the generator is converted back to a list before printing. Modified from *Rosetta code* project. It is used here to flatten a structure in order to check for common dimensionality of elements.

Macro referenced in 13a.

Initialization and call of the algorithm The function evalStruct is used to evaluate a structure network, i.e. to return a scene list of objects of type Model, all referenced in the world coordinate system. The input variable struct must contain an object of class Struct, i.e. a reference to an unevaluated structure network. The variable dim contains the embedding dimension of the structure, i.e. the number of coordinates of its vertices (normally either 2 or 3), the CTM (Current Transformation Matrix) is initialised to the (homogeneous) identity matrix, and the scene is returned by calling the traverse algorithm.

```
⟨Traversal of a scene multigraph 14⟩ ≡
    """ Traversal of a scene multigraph """
    ⟨Structure traversal algorithm 15a⟩
    def evalStruct(struct):
        dim = checkStruct(struct.body)
        CTM, stack = scipy.identity(dim+1), []
        scene = traversal(CTM, stack, struct, [])
        return scene
```

Macro referenced in 16.

Structure traversal algorithm The traversal algorithm decides between three different cases, depending on the type of the currently inspected object. If the object is a Model instance, then applies to it the CTM matrix; else if the object is a Mat instance, then the CTM matrix is updated by (right) product with it; else if the object is a Struct instance, then the CTM is pushed on the stack, initially empty, then the traversal is called (recursion), and finally, at (each) return from recursion, the CTM is recovered by popping the stack.

```
\langle Structure traversal algorithm 15a\rangle \equiv
     def traversal(CTM, stack, obj, scene=[]):
         for i in range(len(obj)):
              if isinstance(obj[i],Model):
                  scene += [larApply(CTM)(obj[i])]
              elif (isinstance(obj[i],tuple) or isinstance(obj[i],list)) and (
                       len(obj[i])==2 or len(obj[i])==3):
                  scene += [larApply(CTM)(obj[i])]
              elif isinstance(obj[i],Mat):
                  CTM = scipy.dot(CTM, obj[i])
              elif isinstance(obj[i],Struct):
                  stack.append(CTM)
                  traversal(CTM, stack, obj[i], scene)
                  CTM = stack.pop()
         return scene
Macro referenced in 14.
Structure embedding algorithm
\langle \text{ Embed a struct object 15b} \rangle \equiv
     """ embed a struct object """
     ⟨Structure embedding algorithm 15c⟩
     def embedStruct(n):
         def embedStructO(struct,suffix="New"):
              if n==0:
                  return struct, len(struct.box[0])
              cloned = Struct()
              cloned.box = hstack((struct.box, [n*[0],n*[0]])).tolist()
              cloned.name = str(id(cloned)) #struct.name+suffix
              cloned.category = struct.category
              cloned.dim = struct.dim + n
              cloned = embedTraversal(cloned, struct, n, suffix)
              return cloned
         return embedStruct0
Macro referenced in 16.
Structure embedding algorithm
\langle Structure embedding algorithm 15c\rangle \equiv
     """ Structure embedding algorithm """
     def embedTraversal(cloned, obj,n,suffix):
         for i in range(len(obj)):
```

```
if isinstance(obj[i],Model):
        cloned.body += [obj[i]]
    elif (isinstance(obj[i],tuple) or isinstance(obj[i],list)) and (
            len(obj[i])==2):
        V,EV = obj[i]
        V = [v+n*[0.0] \text{ for } v \text{ in } V]
        cloned.body += [(V,EV)]
    elif (isinstance(obj[i],tuple) or isinstance(obj[i],list)) and (
            len(obj[i])==3):
        V,FV,EV = obj[i]
        V = [v+n*[0.0] \text{ for } v \text{ in } V]
        cloned.body += [(V,FV,EV)]
    elif isinstance(obj[i],Mat):
        mat = obj[i]
        d,d = mat.shape
        newMat = scipy.identity(d+n*1)
        for h in range(d-1):
            for k in range(d-1):
                newMat[h,k] = mat[h,k]
            newMat[h,d-1+n*1] = mat[h,d-1]
        cloned.body += [newMat.view(Mat)]
    elif isinstance(obj[i],Struct):
        newObj = Struct()
        newObj.box = hstack((obj[i].box, [n*[0],n*[0]]))
        newObj.name = obj[i].name+suffix
        newObj.category = obj[i].category
        cloned.body += [embedTraversal(newObj, obj[i], n, suffix)]
return cloned
```

Macro referenced in 15b.

5 Larstruct exporting

Here we assemble top-down the lar2psm module, by orderly listing the functional parts it is composed of. Of course, this one is the module version corresponding to the current state of the system, i.e. to a very initial state. Other functions will be added when needed.

```
"lib/py/larstruct.py" 16 =
    """Module with functions needed to interface LAR with pyplasm"""
    import sys; sys.path.insert(0, 'lib/py/')
    from lar2psm import *
    from larcc import *
    ⟨Translation matrices 2a⟩
```

```
⟨Scaling matrices 2b⟩
⟨Rotation matrices 3a⟩
⟨Embedding and projecting a geometric model 9⟩
⟨Apply an affine transformation to a LAR model 1⟩
⟨Check for dimension of a structure element (Verts or V) 13a⟩
⟨Remove duplicate faces 7a⟩
⟨Traversal of a scene multigraph 14⟩
⟨types Mat and Verts 4a⟩
⟨Model class 4b⟩
⟨Struct class 5⟩
⟨Structure to pair (Vertices,Cells) conversion 7b⟩
⟨Embedding and projecting a geometric model 9⟩
⟨Embed a struct object 15b⟩
⟨Computation of the containment box of a Lar Struct or Model 6⟩
```

6 Examples

Some examples of structures as combinations of LAR models and affine transformations are given in this section.

Global coordinates We start with a simple 2D example of a non-nested list of translated 2D object instances and rotation about the origin.

Local coordinates A different composition of transformations, from local to global coordinate frames, is used in the following example.

[&]quot;test/py/larstruct/test05.py" $17b \equiv$

```
""" Example of non-nested structure with translation and rotations """
import sys; sys.path.insert(0, 'lib/py/')
from largrid import *
from larstruct import *
square = larCuboids([1,1])
#square = Model(square)
table = larApply( t(-.5,-.5) )(square)
chair = larApply( s(.35,.35) )(table)
chair = larApply( t(.75, 0) )(chair)
struct = Struct([table] + 4*[chair, r(PI/2)])
scene = evalStruct(struct)
VIEW(SKEL_1(STRUCT(CAT(AA(MKPOLS)(scene)))))
```

Call of nested structures by reference Finally, a similar 2D example is given, by nesting one (or more) structures via separate definition and call by reference from the interior. Of course, a cyclic set of calls must be avoided, since it would result in a *non acyclic* multigraph of the structure network.

```
"test/py/larstruct/test06.py" 18a \equiv
     """ Example of nested structures with translation and rotations """
     import sys; sys.path.insert(0, 'lib/py/')
     from largrid import *
     from larstruct import *
     square = larCuboids([1,1])
     #square = Model(square)
     table = larApply(t(-.5,-.5))(square)
     chair = Struct([t(.75, 0), s(.35, .35), table])
     struct = Struct([t(2,1)] + [table] + 4*[r(PI/2), chair])
     struct = Struct(10*[struct,t(0,2.5)])
     struct = Struct(10*[struct,t(3,0)])
     scene = evalStruct(struct)
     VIEW(SKEL_1(STRUCT(CAT(AA(MKPOLS)(scene)))))
"test/py/larstruct/test08.py" 18b \equiv
     """ LAR model input and handling """
     (Input of LAR architectural plan 18c)
     dwelling = larApply(t(3,0))(Model((V,FV)))
     print "\n dwelling =",dwelling
     VIEW(EXPLODE(1.2,1.2,1)(MKPOLS((dwelling.verts,dwelling.cells))))
     plan = Struct([dwelling,s(-1,1),dwelling])
     VIEW(EXPLODE(1.2,1.2,1)(CAT(AA(MKPOLS)(evalStruct(plan)))))
\langle \text{Input of LAR architectural plan } 18c \rangle \equiv
```

```
\langle Initial import of modules ? \rangle
from mapper import *
V = [[3,-3],
[9,-3],[0,0],[3,0],[9,0],[15,0],
[3,3],[6,3],[9,3],[15,3],[21,3],
[0,9],[6,9],[15,9],[18,9],[0,13],
[6,13],[9,13],[15,13],[18,10],[21,10],
[18,13],[6,16],[9,16],[9,17],[15,17],
[18,17],[-3,24],[6,24],[15,24],[-3,13]]
FV = [
[22,23,24,25,29,28], [15,16,22,28,27,30], [18,21,26,25],
[13,14,19,21,18], [16,17,23,22], [11,12,16,15],
[9,10,20,19,14,13], [2,3,6,7,12,11], [0,1,4,8,7,6,3],
[4,5,9,13,18,17,16,12,7,8],[17,18,25,24,23]]
```

Macro referenced in 18b.

Transformation of Struct object to LAR model pair The following test application first generates a grid 3×3 of LAR cubes, extracts its boundary cells as BV, then produces a struct object with 30 translated instances of it, and finally transforms the struct object into a LAR pair W,FW. Let us notice that due to the assembly process, some 2-cells in FW are doubled.

```
"test/py/larstruct/test09.py" 19a \(\text{ 19a}\) =

""" Transformation of Struct object to LAR model pair """

import sys
""" import modules from larcc/lib """

sys.path.insert(0, 'lib/py/')

from larstruct import *

\(\text{ Transform Struct object to LAR model pair 19b}\)

\(\text{ }\)
\(\text{ 19b}\)
\(\text{ }\)
\(\text{ }\)
\(\text{ }\)
\(\text{ }\)
\(\text{ 19b}\)
\(\text{ }\)
\(\text{ 19b}\)
\(\text{ }\)
\(\text{ 19b}\)
\(\text{ 19
```

The actual generation of the structure and its transformation to a LAR model pair is actually performed in the following macro.

```
\langle Transform Struct object to LAR model pair 19b \rangle \in 
""" Generation of Struct object and transform to LAR model pair """
cubes = larCuboids([10,10,10],True)
V = cubes[0]
FV = cubes[1][-2]
CV = cubes[1][-1]
bcells = boundaryCells(CV,FV)
BV = [FV[f] for f in bcells]
VIEW(EXPLODE(1.2,1.2,1.2)(MKPOLS((V,BV))))
```

```
block = Model((V,BV))
struct = Struct(10*[block, t(10,0,0)])
struct = Struct(10*[struct, t(0,10,0)])
struct = Struct(3*[struct, t(0,0,10)])
W,FW = struct2lar(struct)

VIEW(EXPLODE(1.2,1.2,1.2)(MKPOLS((W,FW))))
```

Macro referenced in 19a.

.1 Importing a generic module

First we define a parametric macro to allow the importing of larcc modules from the project repository lib/py/. When the user needs to import some project's module, she may call this macro as done in Section ??.

Macro referenced in 20b.

Importing a module A function used to import a generic lacccc module within the current environment is also useful.

```
\label{eq:function} \begin{split} \langle \, & \text{Function to import a generic module 20b} \, \rangle \equiv \\ & \text{def importModule(moduleName):} \\ & \langle \, & \text{Import the module (20c moduleName ) 20a} \, \rangle \\ & \diamond \end{split}
```

Macro never referenced.

References

- [CL13] CVD-Lab, Linear algebraic representation, Tech. Report 13-00, Roma Tre University, October 2013.
- [Pao03] A. Paoluzzi, Geometric programming for computer aided design, John Wiley & Sons, Chichester, UK, 2003.