

# Modeling Geometry with Assemblies in SysML \*

May 15, 2014

## Abstract

In this module a preliminary concept implementation is provided for the possible introduction of a novel kind of 3D diagram in SysML. Such “Assembly” Diagram is used to specify an operable description of the 3D geometry of a system part.

## Contents

### 1 Introduction

#### 1.1 bbbbbbbb

### 2 Implementation

#### 2.1 Diagram initialization

**Uniform cell sizing** A cuboidal 3-complex is generated by the script below, where the cells have uniform dimension on each coordinate direction.

```
@D Diagram initialization @""" Diagram initialization """ def assemblyDiagramInit(shape):
print "shape =",shape  shape must be 3D, i.e.  a python array with 3 indices assert
len(shape) == 3 diagram = larCuboids(shape) return diagram @
```

**Non-uniform cell sizing** The parameter `quoteList` is used here to generate the new vertices of the `diagram`, previously generated with uniform spacing between the cell vertices in every coordinate direction. Each `pattern` in `quoteList` is a list of positive numbers, each corresponding to the size of the corresponding “coordinate stripe”.

```
@D Diagram initialization (non-uniform sizing) @""" Diagram initialization """ def
assemblyDiagramInit (shape): def assemblyDiagram (quoteList): print "shape =",shape
```

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\*This document is part of the *Linear Algebraic Representation with CoChains* (LAR-CC) framework [?].  
May 15, 2014

shape and quoteList must be 3D, i.e. a python array with 3 indices assert (len(shape) == 3) and (len(quoteList) == 3) coordList = [list(cumsum([0]+pattern)) for pattern in quoteList] verts = CART(coordList), CV = *larCuboids(shape)returnverts, CVreturnassemblyDiagram@*

**Diagram scaling to cuboid of given size** The **size** parameter is the array of lateral dimensions to which to scale the **diagram** parameter. **size** must be an array of 3 numbers; **diagram** is a LAR model

```
@D Diagram scaling to sized cuboid @""" Diagram scaling to given size """ def unit-
Diagram(diagram, size=[1,1,1]): V,CV = diagram print "shape =",shape size must be a
python array with 3 numbers assert (len(size) == 3) and (AND(AA(ISNUM)(size)) ==
True) V=array(V)/AA(float)(max(V))V = (V*size).tolist()diagram = V,CVreturndiagram@
```

## 2.2 Cell numbering

**Drawing numbers of cells** @D Drawing numbers of cells @""" Drawing numbers of cells  
""" def cellNumbering (larModel,hpcModel): V,CV = larModel def cellNumbering0 (cell-
Subset,color=WHITE,scalingFactor=1): text = TEXTWITHATTRIBUTES (TEXTAL-
IGNMENT='centre', TEXTANGLE=0, TEXTWIDTH=0.1\*scalingFactor, TEXTHEIGHT=0.2\*scalingFactor,
TEXTSPACING=0.025\*scalingFactor) hpcList = [hpcModel] for cell in cellSubset: point
= CCOMB([V[v] for v in CV[cell]]) hpcList.append(T([1,2,3])(point)(COLOR(color)(text(str(cell)))))
return STRUCT(hpcList) return cellNumbering0 @

## 2.3 Diagram segmentation

**Boundary cells ( $3D \rightarrow 2D$ ) computation** The computations of boundary cells is executed by calling the **boundaryCells** from the **larcc** module.

```
@D Boundary cells ( $3D \rightarrow 2D$ ) computation @def lar2boundaryFaces(CV,FV): """
Boundary cells computation """ return boundaryCells(CV,FV) @
```

**Interior partitions ( $3D \rightarrow 2D$ ) computation** The indices of the boundary 2-cells are returned in **boundarychain2D**, and subtracted from the set  $\{0, 1, \dots, |E| - 1\}$  in order to return the indices of the **interiorCells**. @D Interior partitions ( $3D \rightarrow 2D$ ) computation  
@def lar2InteriorFaces(CV,FV): """ Boundary cells computation """ boundarychain2D =
boundaryCells(CV,FV) totalChain2D = range(len(FV)) interiorCells = set(totalChain2D).difference(boundarychain2D)
return interiorCells @

## 2.4 Subdiagram mapping

The aim of this section is to allow for separate development of subdiagrams of a geometric diagram. When satisfied with the current design situation, the developer may map a whole diagram into a single 3D cell of the upper-level diagram — in the following called

the *master* diagram. Of course, such nesting may happen several times within a (father) master, producing a hierarchical decomposition (of any depth) of the geometry diagrams.

**Task decomposition** The procedure to map a subdiagram to a diagram is described below in a top-down manner, decomposing the task into an ordered set of subtasks. @D Subdiagram to diagram mapping @ @; 3D window to viewport transformation @;

```
def diagram2cell(diagram, master, cell): mat = diagram2cellMatrix(diagram)(master, 7)
diagram = larApply(mat)(diagram) V, CV1, CV2, n12 = vertexSieve(master, diagram)
yet to finish coding masterBoundaryFaces = boundaryOfChain(CV, FV)([7]) diagram-
BoundaryFaces = lar2boundaryFaces(CV, FV)
master = V, CV1+CV2 return master @
```

**3D window to viewport transformation** @D 3D window to viewport transformation @; 3D window to viewport transformation @;

```
def diagram2cellMatrix(diagram): def diagramToCellMatrix0(master, cell): wdw = min(diagram[0])
+ max(diagram[0]) window3D cV = [master[0][v] for v in master[1][cell]] vpt = min(cV)
+ max(cV) viewport3D print "window3D =", wdw print "viewport3D =", vpt
mat = zeros((4,4)) mat[0,0] = (vpt[3]-vpt[0])/(wdw[3]-wdw[0]) mat[0,3] = vpt[0] -
mat[0,0]*wdw[0] mat[1,1] = (vpt[4]-vpt[1])/(wdw[4]-wdw[1]) mat[1,3] = vpt[1] - mat[1,1]*wdw[1]
mat[2,2] = (vpt[5]-vpt[2])/(wdw[5]-wdw[2]) mat[2,3] = vpt[2] - mat[2,2]*wdw[2] mat[3,3]
= 1 print "mat =", mat return mat return diagramToCellMatrix0 @
```

## 3 Library export

### 3.1 Exporting the library

```
@O lib/py/sysml.py @; Initial import of modules @; @; To compute the boundary (d-1)-
chain of a given d-chain @; @; Diagram initialization (non-uniform sizing) @; @; Boundary
cells (3D → 2D) computation @; @; Interior partitions (3D → 2D) computation @; @;
Diagram scaling to sized cuboid @; from myfont import * @; Drawing numbers of cells @;
@; Subdiagram to diagram mapping @; @
```

## 4 Tests

### 4.1 Diagram initialization

```
@O test/py/sysml/test01.py @; testing initial steps of Assembly Diagram construction
@; Initial import of modules @; from sysml import *
shape = [1,2,2] sizePatterns = [[1],[2,1],[0.8,0.2]] diagram = assemblyDiagramInit(shape)(sizePatterns)
print "diagram =", diagram VIEW(SKEL1(STRUCT(MKPOLS(diagram))))
```

```

VV,EV,FV,CV = gridSkeletons(shape) boundaryFaces = lar2boundaryFaces(CV,FV)
interiorFaces = list(set(range(len(FV)).difference(boundaryFaces)) print "boundary faces
=" ,boundaryFaces print "interior faces =" ,interiorFaces diagram1 = unitDiagram(diagram)
VIEW(SKEL1(STRUCT(MKPOLS(diagram1))))
hpc = SKEL1(STRUCT(MKPOLS(diagram1)))V = diagram1[0]hpc = cellNumbering((V,FV),hpc)(in
cellNumbering((V,EV),hpc)(range(len(EV)),GREEN,.4)VIEW(hpc)hpc = cellNumbering((V,VV),hpc)
@

```

## 4.2 Diagram merging

```

@O test/py/sysml/test02.py @""" definition and merging of two diagrams into a single
diagram """ @; Initial import of modules @; from sysml import *
master = assemblyDiagramInit([2,2,2])([.4,.6],[.4,.6],[.4,.6]) diagram = assemblyDia-
gramInit([3,3,3])([.4,.2,.4],[.4,.2,.4],[.4,.2,.4]) VIEW(SKEL1(STRUCT(STRUCT(MKPOLS(master)),T(2
hpc = SKEL1(STRUCT(MKPOLS(master)))hpc = cellNumbering(master,hpc)(range(len(master[1]),
master = diagram2cell(diagram,master,7) VIEW(SKEL1(STRUCT(MKPOLS(master))))
@

```

## 4.3 Diagram visualization

```

@O test/py/sysml/test03.py @""" definition and merging of two diagrams into a single
diagram """ @; Initial import of modules @; from sysml import *
master = assemblyDiagramInit([2,2,2])([.4,.6],[.4,.6],[.4,.6]) diagram = assemblyDia-
gramInit([3,3,3])([.4,.2,.4],[.4,.2,.4],[.4,.2,.4])
VV,EV,FV,CV = gridSkeletons([2,2,2]) V,CV = master hpc = SKEL1(STRUCT(MKPOLS(master)))hpc
cellNumbering(master,hpc)(range(len(CV)),CYAN,.5)VIEW(hpc)
master = diagram2cell(diagram,master,7) VIEW(SKEL1(STRUCT(MKPOLS(master))))
VIEW(EXPLODE(1.5,1.5,1.5)(MKPOLS(larFacets(master))))
masterBoundaryFaces = boundaryOfChain(CV,FV)([7]) diagramBoundaryFaces = lar2boundaryFaces(CV
@

```

## A Utilities

```

@D To compute the boundary (d-1)-chain of a given d-chain @ def boundaryOfChain(cells,facets):
csrBoundaryMat = boundary(cells,facets) csrChain = zeros((len(cells),1)) def boundary-
OfChain0(chain): for cell in chain: csrChain[cell,0]=1.0 csrBoundaryChain = matrixProd-
uct(csrBoundaryMat, csrChain) boundaryCells = [k for k,val in enumerate(csrBoundaryChain.tolist())
if val == [1.0]] return boundaryCells return boundaryOfChain0 @

```

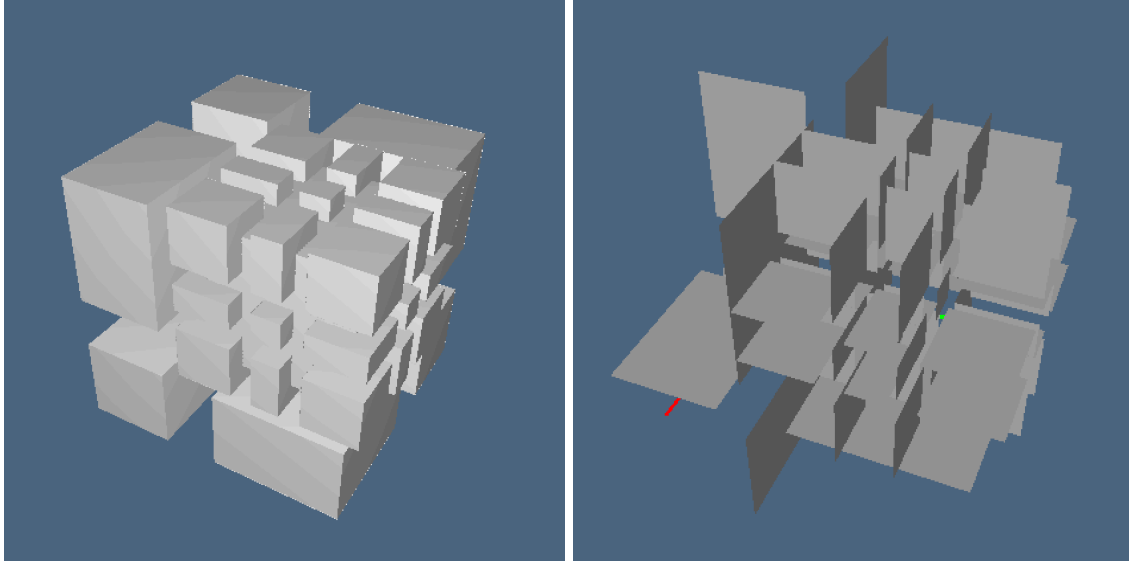


Figure 1: Example of a geometry diagram merged in a master diagram

### A.1 Initial import of modules

**Initial import of modules** @D Initial import of modules @from pyplasm import \*  
from scipy import \* import os,sys """ import modules from larcc/lib """ sys.path.insert(0,  
'lib/py/') from lar2psm import \* from simplexn import \* from larcc import \* from largrid  
import \* from mapper import \* from boolean import \* @