Module Lar2psm *

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Abstract

This software module contains all the functions needed to interface the LAR data structure and/or the geometric objects defined by it with the Plasm environment. In particular, it will include the interfaces towards the visualization primitives provided by the language.

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1 Introduction

The standard definition of vectors and matrices in plasm is the list of vector coordinates and the list of matrix rows, respectively.

2 Implementation

Since the present `lar2psm` module is an interface between the `larcc` library and the PLaSM language, and its various incarnations, it should allow to import the language itself (in Python, the `pyplasm` module).

⟨Import the pyplasm module 2a⟩ ≡
```
from pyplasm import *
```
◇

Macro never referenced.

An useful utility will allow for the creation of a subdirectory from a `dirpath` *string*.

⟨Create directory from path 2b⟩ ≡
```
import os
def createDir(dirpath):
    if not os.path.exists(dirpath):
        os.makedirs(dirpath)
```
◇

Macro referenced in 2c, 6d.

It may be useful to define the repository(ies) for the unit tests associated to the module:

`"test/py/lar2psm-tests.py"` 2c ≡
```
⟨Create directory from path 2b⟩
createDir('test/py/lar2psm/')
```
◇

2.1 Convex combination

Next we define the `CCOMB` function that accepts as input a `vectors` list (i.e., a matrix) and returns *the* point their convex combination.

⟨Compute the convex combination of a list of vectors 2d⟩ ≡
```
import scipy as sp
from pyplasm import *
def CCOMB(vectors):
    return (sp.array(VECTSUM(vectors)) / float(len(vectors))).tolist()
```
◇

Macro referenced in 6c.

Unit tests   First we test `CCOMB` with some special data, then with some random vectors.

`"test/py/lar2psm/test-ccomb.py"` 3a ≡
⟨ Import the module (3b `lar2psm`) 5b ⟩
`from lar2psm import *`
⟨ CCOMB unit tests 7b ⟩
◇

2.2   LAR model of a cell complex

A very important concept introduced by the LAR package is the definition of the *model* of a cell complex, as a pair made by a list of vertices, given as lists of coordinates, and a topological relation.

Definition 1 (LAR model). *A LAR model is a pair, e.g. a Python tuple* (V, FV), *where:*

1. `V` *is the list of vertices, given as lists of coordinates;*

2. `FV` *is a* cell-vertex *relation, in this case the face-vertex relation, given as a list of cells, where each cell is given as a list of vertex indices.*

Examples   Some very simple examples of 0D, 1D, and 2D models follows. They are displayed in Figure 1.

⟨ 2D model examples 3c ⟩ ≡
```
V = [[0.,0.],[1.,0.],[0.,1.],[1.,1.],[0.5,0.5]]
VV = [[0],[1],[2],[3],[4]]
EV = [[0,1],[0,2],[0,4],[1,3],[1,4],[2,3],[2,4],[3,4]]
FV = [[0,1,4],[1,3,4],[2,3,4],[0,2,4]]

model0d, model1d, model2d = (V,VV), (V,EV), (V,FV)
```
◇

Macro referenced in 7a.

2.3   Function `MKPOLS`

The function `MKPOLS` returns a list of HPC objects, i.e. the geometric type of the PLaSM language. This list is generated to be displayed, possibly exploded, by the `pyplasm` viewer.

   Each cell `f` in the model (i.e. each vertex list in the `FV` array of the previous example) is mapped into a polyhedral cell by the `pyplasm` operator `MKPOL`. The vertex indices are mapped from base 0 (the Python and C standard) to base 1 (the Plasm, Matlab, and FORTRAN standard).

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⟨ MaKe a list of HPC objects from a LAR model 4a ⟩ ≡
    ⟨ LAR model decomposition 4b ⟩

```
def MKPOLS (model):
   V,FV = larModelBreak(model)
   pols = [MKPOL([[V[v] for v in f],[range(1,len(f)+1)], None]) for f in FV]
   return pols
```
    ◇

Macro referenced in 6c.

⟨ LAR model decomposition 4b ⟩ ≡

```
def larModelBreak(model):
    if isinstance(model,Model):
        # V, FV = model.verts.tolist(), model.cells
        V, FV = model.verts, model.cells
    elif isinstance(model,tuple) or isinstance(model,list):
        V, FV = model
    return V,FV
```
    ◇

Macro referenced in 4a.

Unit tests   Some simple 3D, 2D, 1D and 0D models are generated and visualised exploded by the file

"test/py/lar2psm/test-models.py" 4c ≡
    ⟨ Import the module (4d lar2psm) 5b ⟩
    ⟨ View model examples 7a ⟩
    ◇

2.4   "Explosion" of the scene

A function EXPLODE used to "explode" an HPC scene defined as a *list* of HPC values, given three real scaling parameters, sx,sy,sz, that are used to transform the position of the centroid of each HPC cell. HPC stands for *HierarchicaL Polyhedral Complex*, the type of plasm geometric values. Of course the assertion

$$sx, sy, sz \geq 1.0$$

must be true, otherways the function would induce some compenetration of the cells of the scene.

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⟨ Explode the scene using `sx,sy,sz` scaling parameters 5a ⟩ ≡

```
def EXPLODE (sx,sy,sz):
    def explode0 (scene):
        centers = [CCOMB(S1(UKPOL(obj))) for obj in scene]
        scalings = len(centers) * [S([1,2,3])([sx,sy,sz])]
        scaledCenters = [UK(APPLY(pair)) for pair in
                          zip(scalings, [MK(p) for p in centers])]
        translVectors = [ VECTDIFF((p,q)) for (p,q) in zip(scaledCenters, centers) ]
        translations = [ T([1,2,3])(v) for v in translVectors ]
        return STRUCT([ t(obj) for (t,obj) in zip(translations,scene) ])
    return explode0
```
◇

Macro referenced in 6c.

The `EXPLODE` function is second order: it first application (to the scaling parameters) returns a partial function to be applied to the `scene`, given as a *list* of HPC (Hierarchical Polyhedral Complex) objects. `EXPLODE` is dimension-independent, since it can be applied to points, edges, faces, 3D cells, and even to geometric values of mixed dimensionality (see Figure 1).

It works by computing the centroid of each object, and by applying to each of them a translation equal to the difference betwwen the scaled and the initial positions of its centroid. `EXPLODE` returns a single HPC object (the assembly of input objects, properly translated)

3 Source Output: `lar2psm` module

3.1 Importing a generic module

First we define a parametric macro to allow the importing of `larcc` modules from the project repository `lib/py/`. When the user needs to import some project's module, she may call this macro as done in Section 3.2.

⟨ Import the module 5b ⟩ ≡

```
import sys; sys.path.insert(0, 'lib/py/')
import @1
```
◇

Macro referenced in 3a, 4c, 6a.

Importing a module A function used to import a generic `lacccc` module within the current environment is also useful.

⟨ Function to import a generic module 6a ⟩ ≡

```
    def importModule(moduleName):
        ⟨ Import the module (6b moduleName ) 5b ⟩
    ◇
```

Macro referenced in 6c.

3.2 Lar2psm exporting

Here we assemble top-down the `lar2psm` module, by orderly listing the functional parts it is composed of. Of course, this one is the module version corresponding to the current state of the system, i.e. to a very initial state. Other functions will be added when needed.

`"lib/py/lar2psm.py" 6c ≡`

```
    """Module with functions needed to interface LAR with pyplasm"""
    ⟨ Function to import a generic module 6a ⟩
    ⟨ Compute the convex combination of a list of vectors 2d ⟩
    from pyplasm import *
    import simplexn
    from simplexn import *
    ⟨ Symbolic utility to represent points as strings 9b ⟩
    ⟨ types Mat and Verts 8a ⟩
    ⟨ Model class 8b ⟩
    ⟨ Struct class 8c ⟩
    ⟨ Structure to pair (Vertices,Cells) conversion 9a ⟩
    ⟨ MaKe a list of HPC objects from a LAR model 4a ⟩
    ⟨ Explode the scene using sx,sy,sz scaling parameters 5a ⟩
    ◇
```

4 Unit tests

4.1 Creation of repository of unit tests

A possible unit test strategy is to create a directory for unit tests associated to each source file in `nuweb`. Therefore we create here a directory in `test/py/` with the same name of the present document. Of course other

⟨ create directory and echo of creation 6d ⟩ ≡

```
    ⟨ Create directory from path 2b ⟩
    createDir('@1')
    print "'@1' repository created"
    ◇
```

Macro never referenced.

`"test/py/lar2psm/test01.py" 6e ≡`

```
    ⟨ create directory and echo of creation: (6f test/py/lar2psm/ ) ? ⟩
    ◇
```

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4.2 Viewing some simplicial complexes

Let we start producing some images, displayed in Figure 1, os a small simplicial complex and of its skeletons. Notice that the + character operates the join of lists (of HPC values).

⟨ View model examples 7a ⟩ ≡

```
from lar2psm import *
⟨2D model examples 3c⟩
explode = EXPLODE(1.5,1.5,1.5)
VIEW(explode(MKPOLS(model0d)))
VIEW(explode(MKPOLS(model1d)))
VIEW(explode(MKPOLS(model2d)))
VIEW(explode(MKPOLS(model2d) + MKPOLS(model1d) + MKPOLS(model0d)))
◇
```
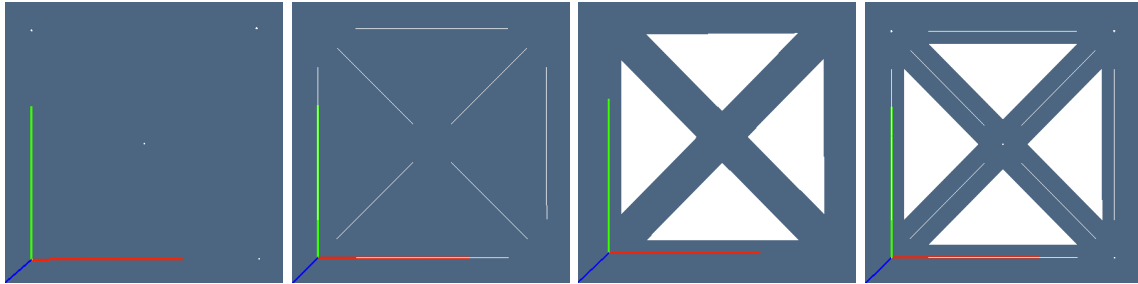
Macro referenced in 4c.

Figure 1: Images of the skeletons of a small simplicial complex.

4.3 Testing convex combination of vectors

⟨ CCOMB unit tests 7b ⟩ ≡

```
assert( CCOMB([]) == [] )
assert( CCOMB([[0,1]]) == [0.0, 1.0] )
assert( CCOMB([[0,1],[1,0]]) == [0.5, 0.5] )
assert( CCOMB([[1,0,0],[0,1,0],[0,0,1]]) == [1./3,1./3,1./3])

import random
vects = [[random.random() for i in range(3)] for k in range(4)]
assert( CCOMB([VECTSUM(vects)]) == \
        (sp.array(CCOMB(vects)) * len(vects)).tolist() )
◇
```

Macro referenced in 3a.

References

[CL13] CVD-Lab, *Linear algebraic representation*, Tech. Report 13-00, Roma Tre University, October 2013.

4.4   Structure types handling

In order to implement a structure as a list of models and transformations, we need to be able to distinguish between two different types of scipy arrays. The first type is the one of arrays of vertices, the second one is the matrix array used to represent the fine transformations.

`Mat` and `Verts` classes

⟨ types Mat and Verts 8a ⟩ ≡
```
""" class definitions for LAR """
import scipy
class Mat(scipy.ndarray): pass
class Verts(scipy.ndarray): pass
```
◇

Macro referenced in 6c.

`Model` class

⟨ Model class 8b ⟩ ≡
```
class Model:
   """ A pair (geometry, topology) of the LAR package """
   def __init__(self,(verts,cells)):
      self.n = len(verts[0])
      # self.verts = scipy.array(verts).view(Verts)
      self.verts = verts
      self.cells = cells
```
◇

Macro referenced in 6c.

`Struct` iterable class

⟨ Struct class 8c ⟩ ≡
```
class Struct:
   """ The assembly type of the LAR package """
   def __init__(self,data):
      self.body = data
   def __iter__(self):
      return iter(self.body)
```

```
        def __len__(self):
            return len(list(self.body))
        def __getitem__(self,i):
            return list(self.body)[i]
    ◇
```

Macro referenced in 6c.

4.5   Structure to LAR conversion

Structure to pair (Vertices,Cells) conversion

⟨ Structure to pair (Vertices,Cells) conversion 9a ⟩ ≡

```
    """ Structure to pair (Vertices,Cells) conversion """

    from mapper import evalStruct

    def struct2lar(structure):
        listOfModels = evalStruct(structure)
        vertDict = dict()
        index,defaultValue,CW,W = -1,-1,[],[]

        for model in listOfModels:
            V,FV = larModelBreak(model)
            for k,incell in enumerate(FV):
                outcell = []
                for v in incell:
                    key = vcode(V[v])
                    if vertDict.get(key,defaultValue) == defaultValue:
                        index += 1
                        vertDict[key] = index
                        outcell += [index]
                        W += [eval(key)]
                    else:
                        outcell += [vertDict[key]]
                CW += [outcell]

        return W,CW
    ◇
```

Macro referenced in 6c.

4.6   Numeric utilities

A small set of utility functions is used to transform a *point* representation, given as array of coordinates, into a string of fixed format to be used as point key into python dictionaries.

⟨ Symbolic utility to represent points as strings 9b ⟩ ≡

```
""" TODO: use package Decimal (http://docs.python.org/2/library/decimal.html) """
global PRECISION
PRECISION = 4.

def verySmall(number): return abs(number) < 10**-(PRECISION)

def prepKey (args): return "["+", ".join(args)+"]"

def fixedPrec(value):
    out = round(value*10**(PRECISION))/10**(PRECISION)
    if out == -0.0: out = 0.0
    return str(out)

def vcode (vect):
    """
    To generate a string representation of a number array.
    Used to generate the vertex keys in PointSet dictionary, and other similar operations.
    """
    return prepKey(AA(fixedPrec)(vect))
```
◇

Macro referenced in 6c.