Structured input to HIJSON Towards indoor mapping and IoT modeling *

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June 12, 2015

Abstract

This module aims to prototype the process of entering geometric data representing a complex building, to provide them explicit semantic and a hierarchical model. The generated LAR structures [DPS14, PDFJ15] are finally output to HIJSON format, an experimental data format extending GEOJSON for applications of indoor mapping and the Internet-of-Things. In HIJSON a strongly simplied building model, yet sufficient for useful purposes, accommodates the knowledge concerning the use models of the building and the set of interior devices and their connection.

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^{*}This document is part of the Linear Algebraic Representation with CoChains (LAR-CC) framework [CL13]. June 12, 2015

1 Introduction

2 Implementation

2.1 Input of geometry from external drawings

File input and computation of cellular complex The modeling process starts with the input of a .svg file, the W3C standard for 2D vector graphics on the web. The file must only contain (by now) <rect> and and property primitives. The geometric data generate the partition of the plane induced by an arrangement of intersecting lines. The arrangement of (fragmented) lines is finally transformed into a 2D *LAR model*, made by the triple V,FV,EV of vertices, faces and edges. We notice the the LAR input is normalized by the larFromLines function: all vertices in V are transformed in the standard plane interval [0, 1]².

```
⟨SVG file input and computation of cellular complex 2a⟩ ≡
    """ File input and computation of cellular complex """
    def svg2lar(filename):
        lines = svg2lines(filename)
        larModel = larFromLines(lines)
        V,FV,EV = larModel
        return larModel

if __name__ == "__main__":
        filename = "test/py/inters/plan.svg"
        larModel = svg2lar(filename)
        V,FV,EV = larModel
        FV,EV = larModel
        FV[2] += FV[71] # for now :o)
```

Macro referenced in 6b.

2.2 Emulation of interactive graphics input

In this section two functions are given to emulate two graphics input primitives, respectively.

Emulation of input from "selection box" The function accepts as input the LAR model V, FV, EV and a queryBox given in normalized coordinates. It returns V vertexSubset V, faceSubset V, faceSubset V vertexSubset V vertexSubset

```
\langle Emulation of input from "selection box" 2b \rangle \equiv
```

[&]quot;"" Emulation of input from ''selection box'' over a LAR normalized representation """ from scipy import spatial

```
from bool import crossRelation,pointInPolygonClassification
def subComplexInBox(V,FV,EV,queryBox):
    (xmin,ymin),(xmax,ymax) = queryBox
   if xmin > xmax: xmin,xmax = xmax,xmin
   if ymin > ymax: ymin,ymax = ymax,ymin
   vdict = dict([(vcode(vert),k) for k,vert in enumerate(V)])
   vertexSubset = [vdict[vcode((x,y))] for x,y in V if xmin<=x<=xmax and ymin<=y<=ymax]
   edgeSubset = [e for e,edge in enumerate(EV) if all([v in vertexSubset for v in edge])]
   faceSubset = [f for f,face in enumerate(FV) if all([v in vertexSubset for v in face])]
   return vertexSubset,faceSubset,edgeSubset
if __name__=="__main__":
   selectBox = ((0.45, 0.45), (0.65, 0.75))
   vertexSubset,faceSubset,edgeSubset = subComplexInBox(V,FV,EV,selectBox)
   VIEW(EXPLODE(1.2,1.2,1.2)(MKPOLS((V,[EV[e] for e in edgeSubset])) + [
      COLOR(RED)(MK(selectBox[0])), COLOR(RED)(MK(selectBox[1]))]))
   VIEW(EXPLODE(1.2,1.2,1.2)(MKPOLS((V,[FV[f] for f in faceSubset])) + [
     COLOR(RED)(MK(selectBox[0])), COLOR(RED)(MK(selectBox[1]))]))
```

Macro referenced in 6b.

Emulation of "pick" input over a LAR normalized representation The function accepts as input the LAR model V,FV,EV, the incidence relation FE, that provides for each face the list of incident edges, and a queryPoint given in normalized coordinates. It returns vertexSubset \subseteq V, faceSubset \subseteq FV, edgeSubset \subseteq EV.

```
\langle Emulation of "pick" input 3a\rangle \equiv
     """ Emulation of ''pick'' input over a LAR normalized representation """
     def subComplexAroundPoint(V,FV,EV,FE,queryPoint):
         tree = spatial.cKDTree(V)
         pts = np.array([queryPoint])
         dist,closestVertex = tree.query(pts)
         VF = invertRelation(FV)
         closestFaces = VF[closestVertex]
         for face in closestFaces:
             faceEdges = [EV[e] for e in FE[face]]
             if pointInPolygonClassification(queryPoint, (V,faceEdges)) == "p_in":
                 break
         vertexSubset = FV[face]
         edgeSubset = [EV[e] for e in FE[face]]
         faceSubset = [face]
         return vertexSubset,faceSubset,edgeSubset
     if __name__=="__main__":
```

Macro referenced in 6b.

Macro referenced in 6b.

From LAR chain to colored HPCs The function cells2hpcs is used to assign a given k color to the cells of a chain (cell subset) of a LAR model V,FV. The function returns a list of HPC (colored) objects.

2.3 Structural operations

From 2D chains to boundary chains

Macro referenced in 6b.

From chains to structures

```
\langle From chains to structures 4b\rangle \equiv
     """ From chains to structures """
     def chain2structs(V,FV,EV,FE):
         def chain2structs0(args):
             if args == ([],[],[]): return
             chain,chainName,classtype = args
             #chain = eval(chainName)
             boundaryFacets = chain2BoundaryChain(FV,EV)(chain)
             #VIEW(EXPLODE(1.2,1.2,1.2)(MKPOLS((V,[EV[e] for e in boundaryFacets]))))
             chainFacets = sorted(set(CAT([FE[cell] for cell in chain])))
             struct = []
             chainVerts = list(set(CAT([FV[cell] for cell in chain])))
             localOrigin = min([V[v] for v in chainVerts])
             for cell in chain:
                 vs = (array([V[v] for v in FV[cell]]) - localOrigin).tolist()
                 vdict = dict([[vcode(vert),k] for k,vert in enumerate(vs)])
                 facetEdges = [ (array([V[v] for v in EV[e]]) - localOrigin).tolist() for e in FE[c] \\
                 ev = [(vdict[vcode(v1)], vdict[vcode(v2)]) for v1,v2 in facetEdges]
                 fv = [range(len(vs))]
                 tvect = eval(min(vdict))
                 shape = (array(vs)-tvect).tolist(),fv,ev
                 struct += [ Struct([ t(*tvect), shape],name=None,category="room" ) ]
                 out = Struct([t(*localOrigin)]+struct,name=chainName,category=classtype)
             return out
         return chain2structs0
```

Macro referenced in 6b.

From Struct object to LAR boundary model

```
\(\text{From Struct object to LAR boundary model 5a} \) \(\text{=} \)
\(\text{""" From Struct object to LAR boundary model """}
\(\text{def structBoundaryModel(struct):} \)
\(\text{V,FV,EV} = \text{struct2lar(struct)} \)
\(\text{edgeBoundary} = \text{boundaryCells(FV,EV)} \)
\(\text{cycles} = \text{boundaryCycles(edgeBoundary,EV)} \)
\(\text{edges} = [\text{signedEdge for cycle in cycles for signedEdge in cycle]} \)
\(\text{orientedBoundary} = [\text{AA(SIGN)(edges), AA(ABS)(edges)}] \)
\(\text{cells} = [\text{EV[e] if sign==1 else REVERSE(EV[e]) for (sign,e) in zip(*orientedBoundary)]} \)
\(\text{return V,cells} \)
\(\text{A} \)
\(\text{orientedBoundary} = [\text{AA(SIGN)(edges), AA(ABS)(edges)}] \)
\(\text{return V,cells} = (\text{orientedBoundary}) \)
\(\text{orientedBoundary} = (\text{orientedBoundary}) \)
\(\text{orientedBound
```

Macro referenced in 6b.

From LAR oriented boundary model to polylines

```
\langle From LAR boundary model to polylines 5b\rangle \equiv
     """ From LAR oriented boundary model to polylines """
     def boundaryModel2polylines(model):
         V,EV = model
         polylines = []
         succDict = dict(EV)
         visited = [False for k in range(len(V))]
         nonVisited = [k for k in succDict.keys() if not visited[k]]
         while nonVisited != []:
             first = nonVisited[0]; v = first; polyline = []
             while visited[v] == False:
                  visited[v] = True;
                  polyline += V[v],
                  v = succDict[v]
             polyline += [V[first]]
             polylines += [polyline]
             nonVisited = [k for k in succDict.keys() if not visited[k]]
         return polylines
```

Macro referenced in 6b.

From structures to boundary polylines

Macro referenced in 6b.

3 Exporting the library

```
"lib/py/hijson.py" 6b =
    """ Module for Structured input to HIJSON """
    from pyplasm import *
    """ import modules from larcc/lib """
    import sys
    sys.path.insert(0, 'lib/py/')
    from inters import *
    from iot3d import *
    from larcc import *
```

```
from bool import *
from copy import copy
DEBUG = False

\( \text{SVG file input and computation of cellular complex 2a} \)
\( \text{Emulation of input from "selection box" 2b} \)
\( \text{Emulation of "pick" input 3a} \)
\( \text{From LAR chain to colored HPCs 3b} \)
\( \text{From 2D chains to boundary chains 4a} \)
\( \text{From chains to structures 4b} \)
\( \text{From Struct object to LAR boundary model 5a} \)
\( \text{From LAR boundary model to polylines 5b} \)
\( \text{From structures to boundary polylines 6a} \)
```

4 Test examples

4.1 Example of a complex building model: part definition

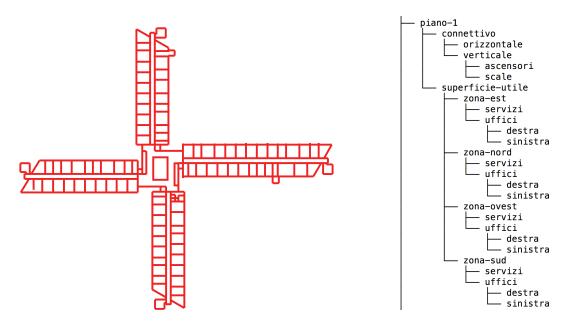


Figure 1: The input SVG drawing of the typical floor layout.

Visualization of cell numbering in a 2D complex

 \langle Visualization of cell numbering in a 2D complex 7a \rangle \equiv

```
""" Visualization of cell numbering in a 2D complex """
     VV = AA(LIST)(range(len(V)))
     submodel = STRUCT(MKPOLS((V,EV)))
     VIEW(larModelNumbering(1,1,1)(V,[VV,EV,FV[:-1]],submodel,0.025))
Macro referenced in 12b.
Ala nord (HPCs)
\langle Ala nord 7b \rangle \equiv
     FE = crossRelation(FV,EV)
     chainsToStruct = chain2structs(V,FV,EV,FE)
     """ Ala nord """
     boxes = [0 for k in range(64)]
     point = [0 for k in range(64)]
     boxes[0] = [[0.431, 0.607], [0.474, 0.91]] #[V[k] for k in [39,208]]
     boxes[1] = [[0.416, 0.657], [0.372, 0.953]] #[V[k] for k in [162,39]]
     boxes[2] = [[0.416, 0.627], [0.431, 0.986]] #[V[k] for k in [206,247]]
     boxes[3] = [[0.431, 0.607], [0.448, 0.627]] #[V[k] for k in [39,7]]
     boxes[4] = [[0.431, 0.91], [0.494, 0.929]] #[V[k] for k in [213,234]]
     boxes[5] = [[0.431, 0.97], [0.466, 1.0]] #[V[k] for k in [58,88]]
     boxes[27] = [[0.416, 0.627], [0.372, 0.657]] #[V[k] for k in [110,82]]
     point[0] = [0.394, 0.9625] \#CCOMB([V[k] for k in [190,197]])
     point[1] = [0.4525, 0.9325] \#CCOMB([V[k] for k in [166,159]])
     piano1_superficieUtile_zonaNord_uffici_destra = subComplexInBox(V,FV,EV,boxes[0])[1]
     piano1_superficieUtile_zonaNord_uffici_sinistra = subComplexInBox(V,FV,EV,boxes[1])[1]
     piano1_connettivo_orizzontale_zonaNord = subComplexInBox(V,FV,EV,boxes[2])[1]
     piano1_connettivo_verticale_zonaNord_ascensore = subComplexInBox(V,FV,EV,boxes[3])[1]
     piano1_connettivo_verticale_zonaNord_ascensore += subComplexInBox(V,FV,EV,boxes[4])[1]
     piano1_connettivo_verticale_zonaNord_scale = subComplexInBox(V,FV,EV,boxes[5])[1]
     piano1_superficieUtile_zonaNord_servizi = subComplexAroundPoint(V,FV,EV,FE,point[0])[1]
     piano1_superficieUtile_zonaNord_servizi += subComplexAroundPoint(V,FV,EV,FE,point[1])[1]
     piano1_superficieUtile_zonaNord_servizi += subComplexInBox(V,FV,EV,boxes[27])[1]
     piano1N = [piano1_superficieUtile_zonaNord_uffici_destra, piano1_superficieUtile_zonaNord_uffi
Macro defined by 7b, 8a.
Macro referenced in 12b.
\langle \text{ Ala nord 8a} \rangle \equiv
     """ Ala nord """
     piano1N_nomi = ["piano1_superficieUtile_zonaNord_uffici_destra", "piano1_superficieUtile_zonaN
     piano1N_categorie = ["uffici","uffici","corridoi","ascensori","scale","servizi"]
```

```
p1N = zip(piano1N,piano1N_nomi,piano1N_categorie)
     piano1_zonaNord = Struct(AA(chainsToStruct)(p1N), "piano1_zonaNord", "ala")
     VIEW(SKEL_1(STRUCT(MKPOLS(struct2lar(piano1_zonaNord)))))
     nord = CAT([cells2hpcs(V,FV,chain,k) for k,chain in enumerate(piano1N)])
     VIEW(EXPLODE(1.2,1.2,1.2)(nord))
Macro defined by 7b, 8a.
Macro referenced in 12b.
Ala est (HPCs)
\langle Ala \text{ est } 8b \rangle \equiv
     """ Ala est """
     boxes[6] = [[0.019, 0.533], [0.376, 0.577]] #[V[k] for k in [241,29]]
     boxes[7] = [[0.07, 0.474], [0.343, 0.518]] #[V[k] for k in [264,148]]
     boxes[8] = [[0.013, 0.518], [0.376, 0.533]] #[V[k] for k in [22,63]]
     boxes[9] = [[0.376, 0.533], [0.39, 0.549]] #[V[k] for k in [63,92]]
     boxes[10] = [[0.001, 0.474], [0.07, 0.518]] #[V[k] for k in [263,265]]
     boxes[11] = [[0.343, 0.474], [0.376, 0.518]] #[V[k] for k in [84,149]]
     point[2] = [0.015, 0.5535] \#CCOMB([V[k] for k in [228,14]])
     piano1_superficieUtile_zonaEst_uffici_destra = subComplexInBox(V,FV,EV,boxes[6])[1]
     piano1_superficieUtile_zonaEst_uffici_sinistra = subComplexInBox(V,FV,EV,boxes[7])[1]
     piano1_connettivo_orizzontale_zonaEst = subComplexInBox(V,FV,EV,boxes[8])[1]
     piano1_connettivo_verticale_zonaEst_ascensore = subComplexInBox(V,FV,EV,boxes[9])[1]
     piano1_connettivo_verticale_zonaEst_scale = subComplexAroundPoint(V,FV,EV,FE,point[2])[1]
     piano1_superficieUtile_zonaEst_servizi = subComplexInBox(V,FV,EV,boxes[10])[1]
     piano1_superficieUtile_zonaEst_servizi += subComplexInBox(V,FV,EV,boxes[11])[1]
     piano1E = [piano1_superficieUtile_zonaEst_uffici_destra, piano1_superficieUtile_zonaEst_uffici
Macro defined by 8b, 9a.
Macro referenced in 12b.
\langle \text{Ala est } 9a \rangle \equiv
     """ Ala est """
     piano1E_nomi = ["piano1_superficieUtile_zonaEst_uffici_destra", "piano1_superficieUtile_zonaEs
     piano1E_categorie = ["uffici","uffici","corridoi","ascensori","scale","servizi"]
     p1E = zip(piano1E,piano1E_nomi, piano1E_categorie)
     piano1_zonaEst = Struct(AA(chainsToStruct)(p1E), "piano1_zonaEst", "ala")
     VIEW(SKEL_1(STRUCT(MKPOLS(struct2lar(piano1_zonaEst)))))
     est = CAT([cells2hpcs(V,FV,chain,k) for k,chain in enumerate(piano1E)])
     VIEW(EXPLODE(1.2,1.2,1.2)(est + nord))
```

```
Macro defined by 8b, 9a. Macro referenced in 12b.
```

Ala sud (HPCs)

```
\langle \text{ Ala sud 9b} \rangle \equiv
     """ Ala sud """
     boxes[12] = [[0.467, 0.138], [0.423, 0.476]] #[V[k] for k in [252,47]]
     boxes[13] = [[0.482, 0.145], [0.525, 0.445]] #[V[k] for k in [241,126]]
     boxes[14] = [[0.482, 0.476], [0.467, 0.116]] #[V[k] for k in [254,232]]
     boxes[15] = [[0.449, 0.476], [0.467, 0.493]] #[V[k] for k in [40,237]]
     boxes[16] = [[0.431, 0.101], [0.467, 0.131]] #[V[k] for k in [259,2]]
     boxes[17] = [[0.482, 0.445], [0.525, 0.476]] #[V[k] for k in [155,248]]
     boxes[18] = [[0.525, 0.104], [0.482, 0.145]] #[V[k] for k in [111,241]]
     piano1_superficieUtile_zonaSud_uffici_destra = subComplexInBox(V,FV,EV,boxes[12])[1]
     piano1_superficieUtile_zonaSud_uffici_sinistra = subComplexInBox(V,FV,EV,boxes[13])[1]
     piano1_connettivo_orizzontale_zonaSud = subComplexInBox(V,FV,EV,boxes[14])[1]
     piano1_connettivo_verticale_zonaSud_ascensore = subComplexInBox(V,FV,EV,boxes[15])[1]
     piano1_connettivo_verticale_zonaSud_scale = subComplexInBox(V,FV,EV,boxes[16])[1]
     piano1_superficieUtile_zonaSud_servizi = subComplexInBox(V,FV,EV,boxes[17])[1]
     piano1_superficieUtile_zonaSud_servizi += subComplexInBox(V,FV,EV,boxes[18])[1]
     piano1S = [piano1_superficieUtile_zonaSud_uffici_destra, piano1_superficieUtile_zonaSud_uffici
Macro defined by 9b, 10a.
Macro referenced in 12b.
\langle \text{Ala sud } 10a \rangle \equiv
     """ Ala sud """
     piano1S_nomi = ["piano1_superficieUtile_zonaSud_uffici_destra", "piano1_superficieUtile_zonaSu
     piano1S_categorie = ["uffici","uffici","corridoi","ascensori","scale","servizi"]
     p1S = zip(piano1S,piano1S_nomi, piano1S_categorie)
     piano1_zonaSud = Struct(AA(chainsToStruct)(p1S), "piano1_zonaSud", "ala")
     VIEW(SKEL_1(STRUCT(MKPOLS(struct2lar(piano1_zonaSud)))))
     sud = CAT([cells2hpcs(V,FV,chain,k) for k,chain in enumerate(piano1S)])
     VIEW(EXPLODE(1.2,1.2,1.2)(est + nord + sud))
Macro defined by 9b, 10a.
Macro referenced in 12b.
Ala ovest (HPCs)
\langle \text{ Ala ovest 10b} \rangle \equiv
```

```
""" Ala ovest """
     boxes[19] = [[0.521, 0.526], [0.963, 0.568]] #[V[k] for k in [169,202]]
     boxes[20] = [[0.555, 0.584], [0.955, 0.627]] #[V[k] for k in [12,23]]
     boxes[21] = [[0.521, 0.568], [0.985, 0.584]] #[V[k] for k in [209,204]]
     boxes[22] = [[0.506, 0.551], [0.521, 0.568]] #[V[k] for k in [89,209]]
     boxes[23] = [[0.808, 0.504], [0.828, 0.526]] #[V[k] for k in [270,77]]
     boxes[24] = [[0.955, 0.584], [0.997, 0.627]] \#[V[k]] for k in [220,24]]
     boxes[25] = [[0.521, 0.584], [0.555, 0.627]] #[V[k] for k in [11,144]]
     boxes[26] = [[1.0, 0.533], [0.97, 0.568]] #[V[k] for k in [233,201]]
     piano1_superficieUtile_zonaOvest_uffici_destra = subComplexInBox(V,FV,EV,boxes[19])[1]
     piano1_superficieUtile_zonaOvest_uffici_sinistra = subComplexInBox(V,FV,EV,boxes[20])[1]
     piano1_connettivo_orizzontale_zonaOvest = subComplexInBox(V,FV,EV,boxes[21])[1]
     piano1_connettivo_verticale_zona0vest_ascensore = subComplexInBox(V,FV,EV,boxes[22])[1]
     piano1_connettivo_verticale_zonaOvest_ascensore += subComplexInBox(V,FV,EV,boxes[23])[1]
     piano1_superficieUtile_zonaOvest_servizi = subComplexInBox(V,FV,EV,boxes[24])[1]
     piano1_superficieUtile_zonaOvest_servizi += subComplexInBox(V,FV,EV,boxes[25])[1]
     piano1_connettivo_verticale_zonaOvest_scale = subComplexInBox(V,FV,EV,boxes[26])[1]
     piano10 = [piano1_superficieUtile_zonaOvest_uffici_destra, piano1_superficieUtile_zonaOvest_uf
Macro defined by 10b, 11a.
Macro referenced in 12b.
\langle \text{Ala ovest } 11a \rangle \equiv
     """ Ala ovest """
     piano10_nomi = ["piano1_superficieUtile_zona0vest_uffici_destra", "piano1_superficieUtile_zona
     piano10_categorie = ["uffici","uffici","corridoi","ascensori","scale","servizi"]
     p10 = zip(piano10,piano10_nomi, piano10_categorie)
     piano1_zonaOvest = Struct(AA(chainsToStruct)(p10), "piano1_zonaOvest", "ala")
     VIEW(SKEL_1(STRUCT(MKPOLS(struct2lar(piano1_zonaOvest)))))
     ovest = CAT([cells2hpcs(V,FV,chain,k) for k,chain in enumerate(piano10)])
     VIEW(EXPLODE(1.2,1.2,1.2)(est + nord + sud + ovest))
Macro defined by 10b, 11a.
Macro referenced in 12b.
Centro stella (HPCs)
\langle \text{ Centro stella 11b} \rangle \equiv
     """ Centro stella """
     piano1_connettivo_orizzontale_centroStella = [2]
     piano1_connettivo_verticale_centroStella_scale = [15,26]
     piano1C = [[],[],piano1_connettivo_orizzontale_centroStella,[], piano1_connettivo_verticale_ce
```

```
centro = CAT([cells2hpcs(V,FV,chain,k) for k,chain in enumerate(piano1C)])

Amacro defined by 11bc.
Macro referenced in 12b.

(Centro stella 11c) ==
    """ Centro stella """
    piano1C_nomi = [[],[],"piano1_connettivo_orizzontale_centroStella", [], "piano1_connettivo_ver piano1C_categorie = [[],[],"corridoi",[], "ascensori"]
    p1C = zip(piano1C,piano1C_nomi, piano1C_categorie)
    piano1_centroStella = Struct(AA(chainsToStruct)(p1C), "piano1_centroStella", "centro")
    VIEW(SKEL_1(STRUCT(MKPOLS(struct2lar(piano1_centroStella)))))

VIEW(EXPLODE(1.2,1.2,1.2)(est + nord + sud + ovest + centro))

Amacro defined by 11bc.
Macro referenced in 12b.
```

4.2 Example of a complex building model: integration

Assembly of parts (HPCs)

```
""" make the model of a layout floor """
""" import modules from larcc/lib """
import sys
sys.path.insert(0, 'lib/py/')
from hijson import *
filename = "test/py/inters/plan.svg"
larModel = svg2lar(filename)
V,FV,EV = larModel
FV[2] += FV[71]
                           # for now :o)
⟨ Visualization of cell numbering in a 2D complex 7a⟩
\langle \text{ Ala nord 7b}, \dots \rangle
\langle \text{Ala est 8b}, \dots \rangle
\langle \text{ Ala sud 9b}, \dots \rangle
\langle \text{ Ala ovest } 10b, \dots \rangle
⟨ Centro stella 11b, ... ⟩
⟨Assemblaggio 12a⟩
```

References

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