Hierarchical structures with LAR *

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February 28, 2015

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1 Affine transformations

1.1 Design decision

First we state the general rules that will be satisfied by the matrices used in this module, mainly devoted to apply affine transformations to vertices of models in structure environments:

1. assume the scipy `ndarray` as the type of vertices, stored in row-major order;

2. use the last coordinate as the homogeneous coordinate of vertices, but do not store it explicitly;

3. store explicitly the homogeneous coordinate of transformation matrices.

4. use labels 'verts' and 'mat' to distinguish between vertices and transformation matrices.

5. transformation matrices are dimension-independent, and their dimension is computed as the length of the parameter vector passed to the generating function.

1.2 Affine mapping

⟨ Apply an affine transformation to a LAR model 1 ⟩ ≡

```
def larApply(affineMatrix):
    def larApply0(model):
        if isinstance(model,Model):
            # V = scipy.dot([v.tolist()+[1.0] for v in model.verts], affineMatrix.T).tolist()
            V = scipy.dot(array([v+[1.0] for v in model.verts]), affineMatrix.T).tolist()
            V = [v[:-1] for v in V]
            CV = copy.copy(model.cells)
            return Model((V,CV))
        elif isinstance(model,tuple) or isinstance(model,list):
            if len(model)==2: V,CV = model
            elif len(model)==3: V,CV,FV = model
            V = scipy.dot([list(v)+[1.0] for v in V], affineMatrix.T).tolist()
            if len(model)==2: return [v[:-1] for v in V],CV
            elif len(model)==3: return [v[:-1] for v in V],CV,FV
    return larApply0
```

◇

Macro referenced in 15.

1.3 Elementary matrices

Elementary matrices for affine transformation of vectors in any dimensional vector space are defined here. They include translation, scaling, rotation and shearing.

Translation

⟨ Translation matrices 2a ⟩ ≡

```
def t(*args):
    d = len(args)
    mat = scipy.identity(d+1)
    for k in range(d):
        mat[k,d] = args[k]
    return mat.view(Mat)
```
◇

Macro referenced in 15.

Scaling

⟨ Scaling matrices 2b ⟩ ≡

```
def s(*args):
    d = len(args)
    mat = scipy.identity(d+1)
    for k in range(d):
        mat[k,k] = args[k]
    return mat.view(Mat)
```
◇

Macro referenced in 15.

Rotation

⟨ Rotation matrices 3a ⟩ ≡

```
def r(*args):
    args = list(args)
    n = len(args)
    ⟨ plane rotation (in 2D) 3b ⟩
    ⟨ space rotation (in 3D) 3c ⟩
    return mat.view(Mat)
```
◇

Macro referenced in 15.

⟨ plane rotation (in 2D) 3b ⟩ ≡

```
if n == 1: # rotation in 2D
    angle = args[0]; cos = COS(angle); sin = SIN(angle)
    mat = scipy.identity(3)
    mat[0,0] = cos;    mat[0,1] = -sin;
    mat[1,0] = sin;    mat[1,1] = cos;
```
◇

Macro referenced in 3a.

⟨ space rotation (in 3D) 3c ⟩ ≡

```python
if n == 3: # rotation in 3D
    mat = scipy.identity(4)
    angle = VECTNORM(args); axis = UNITVECT(args)
    cos = COS(angle); sin = SIN(angle)
```
    ⟨ elementary rotations (in 3D) 3d ⟩
    ⟨ general rotations (in 3D) 3e ⟩
◇

Macro referenced in 3a.

⟨ elementary rotations (in 3D) 3d ⟩ ≡

```python
if axis[1]==axis[2]==0.0:    # rotation about x
    mat[1,1] = cos;    mat[1,2] = -sin;
    mat[2,1] = sin;    mat[2,2] = cos;
elif axis[0]==axis[2]==0.0:    # rotation about y
    mat[0,0] = cos;    mat[0,2] = sin;
    mat[2,0] = -sin;   mat[2,2] = cos;
elif axis[0]==axis[1]==0.0:    # rotation about z
    mat[0,0] = cos;    mat[0,1] = -sin;
    mat[1,0] = sin;    mat[1,1] = cos;
```
◇

Macro referenced in 3c.

⟨ general rotations (in 3D) 3e ⟩ ≡

```python
else:        # general 3D rotation (Rodrigues' rotation formula)
    I = scipy.identity(3) ; u = axis
    Ux = scipy.array([
        [0,          -u[2],       u[1]],
        [u[2],          0,      -u[0]],
        [-u[1],      u[0],          0]])
    UU = scipy.array([
        [u[0]*u[0],    u[0]*u[1],    u[0]*u[2]],
        [u[1]*u[0],    u[1]*u[1],    u[1]*u[2]],
        [u[2]*u[0],    u[2]*u[1],    u[2]*u[2]]])
    mat[:3,:3] = cos*I + sin*Ux + (1.0-cos)*UU
```
◇

Macro referenced in 3c.

2 Structure types handling

In order to implement a structure as a list of models and transformations, we need to be able to distinguish between two different types of scipy arrays. The first type is the one of arrays of vertices, the second one is the matrix array used to represent the fine transformations.

2.1 `Mat` and `Verts` classes

⟨ types Mat and Verts 4a ⟩ ≡

```
""" class definitions for LAR """
import scipy
class Mat(scipy.ndarray): pass
class Verts(scipy.ndarray): pass
```
◇

Macro referenced in 15.

2.2 `Model` class

⟨ Model class 4b ⟩ ≡

```
class Model:
    """ A pair (geometry, topology) of the LAR package """
    def __init__(self,(verts,cells)):
        self.n = len(verts[0])
        # self.verts = scipy.array(verts).view(Verts)
        self.verts = verts
        self.cells = cells
    def __getitem__(self,i):
        return list((self.verts,self.cells))[i]
```
◇

Macro referenced in 15.

2.3 `Struct` iterable class

⟨ Struct class 5 ⟩ ≡

```
from myfont import *
class Struct:
    """ The assembly type of the LAR package """
    def __init__(self,data=None,name=None):
        if data==None or data==[]:
            self.body = []
        else:
            self.body = data
            self.box = box(self)
        if name != None:
            self.name = str(name)
        else:
            self.name = str(id(self))
    def __name__(self):
        return self.name
    def __iter__(self):
        return iter(self.body)
    def __len__(self):
```

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```
                return len(list(self.body))
        def __getitem__(self,i):
            return list(self.body)[i]
        def __setitem__(self,i,value):
            self.body[i] = value
        def __print__(self):
            return "<Struct name: %s>" % self.__name__()
        def __repr__(self):
            return "<Struct name: %s>" % self.__name__()
            #return "'Struct(%s,%s)'" % (str(self.body),str(str(self.__name__())))
        def draw(self,color=WHITE,scaling=1,metric=ID):
            vmin,vmax = self.box
            delta = VECTDIFF([vmax,vmin])
            point = CCOMB(self.box)
            scalingFactor = scaling*delta[0]/20.
            text = TEXTWITHATTRIBUTES (TEXTALIGNMENT='centre', TEXTANGLE=0,
                        TEXTWIDTH=0.1*scalingFactor,
                        TEXTHEIGHT=0.2*scalingFactor,
                        TEXTSPACING=0.025*scalingFactor)
            point = metric([point])[0]
            return T([1,2,3])(point)(COLOR(color)(text(self.name)))
    ◇
```

Macro referenced in 15.

2.4 Struct containment box

⟨Computation of the containment box of a Lar Struct or Model 6a⟩ ≡

```
    """ Computation of the containment box of a Lar Struct or Model """
    import copy
    def box(model):
        if isinstance(model,Mat): return []
        elif isinstance(model,Struct):
            dummyModel = copy.deepcopy(model)
            dummyModel.body = [term if (not isinstance(term,Struct)) else [term.box,[[0,1]]]  for
            listOfModels = evalStruct( dummyModel )
            #dim = checkStruct(listOfModels)
            theMin,theMax = box(listOfModels[0])
            for theModel in listOfModels[1:]:
                modelMin, modelMax = box(theModel)
                theMin = [val if val<theMin[k] else theMin[k] for k,val in enumerate(modelMin)]
                theMax = [val if val>theMax[k] else theMax[k] for k,val in enumerate(modelMax)]
            return [theMin,theMax]
        elif isinstance(model,Model):
            V = model.verts
        elif (isinstance(model,tuple) or isinstance(model,list)) and (len(model)==2 or len(model)==
            V = model[0]
```

```
        coords = TRANS(V)
        theMin = [min(coord) for coord in coords]
        theMax = [max(coord) for coord in coords]
        return [theMin,theMax]
    ◇
```

Macro referenced in 15.

3   Structure to LAR conversion

3.1   Remove duplicate faces

⟨ Remove duplicate faces 6b ⟩ ≡
```
    """ Remove duplicate faces  """
    from collections import defaultdict
    def removeDups (CW):
        CW = list(set(AA(tuple)(CW)))
        CWs = list(set(AA(tuple)  (AA(sorted)(CW))  ))
        no_duplicates = defaultdict(list)
        for f in CWs: no_duplicates[f] = []
        for f in CW:
          no_duplicates[tuple(sorted(f))] += [f]
        CW = [f[0] for f in no_duplicates.values()]
        return CW
    ◇
```

Macro referenced in 15.

3.2   Structure to pair (Vertices,Cells) conversion

⟨ Structure to pair (Vertices,Cells) conversion 7 ⟩ ≡
```
    """ Structure to pair (Vertices,Cells) conversion """

    def struct2lar(structure,metric=ID):
        listOfModels = evalStruct(structure)
        vertDict = dict()
        index,defaultValue,CW,W,FW = -1,-1,[],[],[]

        for model in listOfModels:
            if isinstance(model,Model):
                V,FV = model.verts,model.cells
            elif (isinstance(model,tuple) or isinstance(model,list)):
                if len(model)==2: V,FV = model
                elif len(model)==3: V,FV,EV = model
            for k,incell in enumerate(FV):
                outcell = []
                for v in incell:
```

```
                    key = vcode(V[v])
                    if vertDict.get(key,defaultValue) == defaultValue:
                        index += 1
                        vertDict[key] = index
                        outcell += [index]
                        W += [eval(key)]
                    else:
                        outcell += [vertDict[key]]
                CW += [outcell]
            if len(model)==3:
                for k,incell in enumerate(EV):
                    outcell = []
                    for v in incell:
                        key = vcode(V[v])
                        if vertDict.get(key,defaultValue) == defaultValue:
                            index += 1
                            vertDict[key] = index
                            outcell += [index]
                            W += [eval(key)]
                        else:
                            outcell += [vertDict[key]]
                    FW += [outcell]


        if len(model)==2:
          if len(CW[0])==2:
            CW = list(set(AA(tuple)(AA(sorted)(CW))))
          else: CW = removeDups(CW)
          return metric(W),CW
        if len(model)==3:
          FW = list(set(AA(tuple)(AA(sorted)(FW))))
          CW = removeDups(CW)
          return metric(W),CW,FW
    ◇
```

Macro referenced in 15.

3.3   Embedding or projecting LAR models

In order to apply 3D transformations to a two-dimensional LAR model, we must embed it in 3D space, by adding one more coordinate to its vertices.

Embedding or projecting a geometric model   This task is performed by the function `larEmbed` with parameter k, that inserts its d-dimensional geometric argument in the $x_{d+1}, \ldots, x_{d+k} = 0$ subspace of $\mathbb{E}^{d+k}$. A projection transformation, that removes the last k

coordinate of vertices, without changing the object topology, is performed by the function `larEmbed` with *negative* integer parameter.

⟨Embedding and projecting a geometric model 8⟩ ≡

```
def larEmbed(k):
    def larEmbed0(model):
        if len(model)==2: V,CV = model
        elif len(model)==3: V,CV,FV = model
        if k>0:
            V = [v+[0.]*k for v in V]
        elif k<0:
            V = [v[:-k] for v in V]
        if len(model)==2: return V,CV
        elif len(model)==3: return V,CV,FV
    return larEmbed0
```
◇

Macro referenced in 15.

4 Hierarchical complexes

Hierarchical models of complex assemblies are generated by an aggregation of subassemblies, each one defined in a local coordinate system, and relocated by affine transformations of coordinates. This operation may be repeated hierarchically, with some subassemblies defined by aggregation of simpler parts, and so on, until one obtains a set of elementary components, which cannot be further decomposed.

Two main advantages can be found in a hierarchical modeling approach. Each elementary part and each assembly, at every hierarchical level, are defined independently from each other, using a local coordinate frame, suitably chosen to make its definition easier. Furthermore, only one copy of each component is stored in the memory, and may be instanced in different locations and orientations how many times it is needed.

4.1 Traversal of hierarchical structures

Of course, the main algorithm with hierarchical structures is the *traversal* of the structure network, whose aim is to transform every encountered object from local to global coordinates, where the global coordinates are those of the network root (the only node with indegree zero).

A structure network can be modelled using a directed acyclic multigraph, i.e. a triple (N, A, f) made by a set N of nodes, a set A of arcs, and a function $f : A \to N^2$ from arcs to ordered pairs of nodes. Conversely that in standard oriented graphs, in this kind of structure more than one oriented arc is allowed between the same pair on nodes.

A simple modification of a DFS (Depth First Search) visit of a graph can be used to traverse the structure network This algorithm is given in Figure 1 from [Pao03].

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Script 8.3.1 (Traversal of a multigraph)
algorithm TRAVERSAL $((N, A, f) : multigraph)$ {
    $CTM :=$ identity matrix;
    TraverseNode $(root)$
}

proc TRAVERSENODE $(n : node)$ {
    foreach $a \in A$ outgoing from n **do** TraverseArc (a);
    ProcessNode (n)
}

proc TRAVERSEARC $(a = (n, m) : arc)$ {
    Stack.push (CTM);
    $CTM := CTM$ * a.mat;
    TraverseNode (m);
    $CTM :=$ Stack.pop()
}

proc PROCESSNODE $(n : node)$ {
    foreach object $\in n$ **do** Process(CTM * object)
}

Figure 1: Traversal algorithm of an acyclic multigraph.

4.1.1 Traversal of nested lists

The representation chosen for structure networks with LAR is the serialised one, consisting in ordered sequences (lists) of either (a) LAR models, or (b) affine transformations, or (c) references to other structures, either directly nested within some given structure, or called by reference (name) from within the list.

The aim of a structure network traversal is, of course, to transform every component structure, usually defined in a local coordinate system, into the reference frame of the structure as a whole, normally corresponding with the reference system of the structure's root, called the *world coordinate* system.

The pattern of calls and returned values In order to better understand the behaviour of the traversal algorithm, where every transformation is applied to all the following models, — but only if included in the same structure (i.e. list) — it may be very useful to start with an *algorithm emulation*. In particular, the recursive script below discriminates between three different cases (number, string, or sequence), whereas the actual traversal must do with (a) Models, (b) Matrices, and (c) Structures, respectively.

⟨Emulation of scene multigraph traversal 10a⟩ ≡

```
from pyplasm import *
def __traverse(CTM, stack, o):
    for i in range(len(o)):
        if ISNUM(o[i]): print o[i], REVERSE(CTM)
        elif ISSTRING(o[i]):
            CTM.append(o[i])
        elif ISSEQ(o[i]):
            stack.append(o[i])                # push the stack
            __traverse(CTM, stack, o[i])
            CTM = CTM[:-len(stack)]        # pop the stack

def algorithm(data):
    CTM,stack = ["I"],[]
    __traverse(CTM, stack, data)
◇
```
Macro never referenced.

Some use example of the above algorithm are provided below. The printout produced at run time is shown from the `emulation of traversal algorithm` macro.

⟨Examples of multigraph traversal 10b⟩ ≡

```
data = [1,"A", 2, 3, "B", [4, "C", 5], [6,"D", "E", 7, 8], 9]
print algorithm(data)
>>> 1 ['I']
    2 ['A', 'I']
```

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```
        3 ['A', 'I']
        4 ['B', 'A', 'I']
        5 ['C', 'B', 'A', 'I']
        6 ['B', 'A', 'I']
        7 ['E', 'D', 'B', 'A', 'I']
        8 ['E', 'D', 'B', 'A', 'I']
        9 ['B', 'A', 'I']

    data = [1,"A", [2, 3, "B", 4, "C", 5, 6,"D"], "E", 7, 8, 9]
    print algorithm(data)
    >>> 1 ['I']
        2 ['A', 'I']
        3 ['A', 'I']
        4 ['B', 'A', 'I']
        5 ['C', 'B', 'A', 'I']
        6 ['C', 'B', 'A', 'I']
        7 ['E', 'A', 'I']
        8 ['E', 'A', 'I']
        9 ['E', 'A', 'I']
    ◇
```
Macro never referenced.

⟨ Emulation of traversal algorithm 11 ⟩ ≡
```
    dat = [2, 3, "B", 4, "C", 5, 6,"D"]
    print algorithm(dat)
    >>> 2 ['I']
        3 ['I']
        4 ['B', 'I']
        5 ['C', 'B', 'I']
        6 ['C', 'B', 'I']
    data = [1,"A", dat, "E", 7, 8, 9]
    print algorithm(data)
    >>> 1 ['I']
        2 ['A', 'I']
        3 ['A', 'I']
        4 ['B', 'A', 'I']
        5 ['C', 'B', 'A', 'I']
        6 ['C', 'B', 'A', 'I']
        7 ['E', 'A', 'I']
        8 ['E', 'A', 'I']
        9 ['E', 'A', 'I']
    ◇
```
Macro never referenced.

Traversal of a scene multigraph   The previous traversal algorithm is here customised for scene multigraph, where the objects are LAR models, i.e. pairs of vertices of type 'Verts and cells, and where the transformations are matrix transformations of type 'Mat'.

Check models for common dimension   The input list of a call to `larStruct` primitive is preliminary checked for uniform dimensionality of the enclosed LAR models and transformations. The common dimension `dim` of models and matrices is returned by the function `checkStruct`, within the class definition `Struct` in the module `lar2psm`. Otherwise, an exception is generated (TODO).

⟨ Check for dimension of a structure element (Verts or V) 12a ⟩ ≡
```
    ⟨ Flatten a list 12b ⟩
    def checkStruct(lst):
        """ Return the common dimension of structure elements.

            TODO: aggiungere test sulla dimensione minima delle celle (legata a quella di immersion
        """
        obj = lst[0]
        if (isinstance(obj,tuple) or isinstance(obj,list)):
            dim = len(obj[0][0])
        elif isinstance(obj,Mat):
            dim = obj.shape[0]-1
        elif isinstance(obj,Struct):
            dim = len(obj.box[0])
        return dim
    ◇
```
Macro referenced in 15.

Flatten a list using Python generators   The `flatten` is a generator that yields the non-list values of its input in order. In the example, the generator is converted back to a list before printing. Modified from *Rosetta code* project. It is used here to flatten a structure in order to check for common dimensionality of elements.

⟨ Flatten a list 12b ⟩ ≡
```
    """ Flatten a list using Python generators """
    def flatten(lst):
        for x in lst:
            if (isinstance(x,tuple) or isinstance(x,list)) and len(x)==2:
                yield x
            elif (isinstance(x,tuple) or isinstance(x,list)):
                for x in flatten(x):
                    yield x
            elif isinstance(x, Struct):
                for x in flatten(x.body):
```

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```
                yield x
            else:
                yield x

    #  lst = [[1], 2, [[3,4], 5], [[[]]], [[[6]]], 7, 8, []]
    #  print list(flatten(lst))
    #  [1, 2, 3, 4, 5, 6, 7, 8]

    #  import itertools
    #  chain = itertools.chain.from_iterable([[1,2],[3],[5,89],[],[6]])
    #  print(list(chain))
    #  [1, 2, 3, 5, 89, 6]     ###  TODO: Bug coi dati sopra?
    ◇
```

Macro referenced in 12a.

Initialization and call of the algorithm   The function `evalStruct` is used to evaluate a structure network, i.e. to return a `scene` list of objects of type `Model`, all referenced in the world coordinate system. The input variable `struct` must contain an object of class `Struct`, i.e. a reference to an unevaluated structure network. The variable `dim` contains the embedding dimension of the structure, i.e. the number of doordinates of its vertices (normally either 2 or 3), the CTM (Current Transformation Matrix) is initialised to the (homogeneous) identity matrix, and the `scene` is returned by calling the `traverse` algorithm.

⟨Traversal of a scene multigraph 13a⟩ ≡
```
    """ Traversal of a scene multigraph """
    ⟨Structure traversal algorithm 13b⟩
    def evalStruct(struct):
        dim = checkStruct(struct.body)
        CTM, stack = scipy.identity(dim+1), []
        scene = traversal(CTM, stack, struct, [])
        return scene
    ◇
```

Macro referenced in 15.

Structure traversal algorithm   The `traversal` algorithm decides between three different cases, depending on the type of the currently inspected object. If the object is a `Model` instance, then applies to it the `CTM` matrix; else if the object is a `Mat` instance, then the `CTM` matrix is updated by (right) product with it; else if the object is a `Struct` instance, then the `CTM` is pushed on the stack, initially empty, then the `traversal` is called (recursion), and finally, at (each) return from recursion, the `CTM` is recovered by popping the stack.

⟨Structure traversal algorithm 13b⟩ ≡

```
def traversal(CTM, stack, obj, scene=[]):
    for i in range(len(obj)):
        if isinstance(obj[i],Model):
            scene += [larApply(CTM)(obj[i])]
        elif (isinstance(obj[i],tuple) or isinstance(obj[i],list)) and (
                len(obj[i])==2 or len(obj[i])==3):
            scene += [larApply(CTM)(obj[i])]
        elif isinstance(obj[i],Mat):
            CTM = scipy.dot(CTM, obj[i])
        elif isinstance(obj[i],Struct):
            stack.append(CTM)
            traversal(CTM, stack, obj[i], scene)
            CTM = stack.pop()
    return scene
```
◇

Macro referenced in .

Structure embedding algorithm

⟨Embed a struct object 14a⟩ ≡
```
""" embed a struct object """
```
⟨Structure embedding algorithm 14b⟩
```

def embedStruct(n):
    def embedStruct0(struct):
        if n==0:
            return struct, len(struct.box[0])
        cloned = Struct()
        cloned.box = hstack((struct.box, [n*[0],n*[0]])).tolist()
        cloned.name = struct.name+"New"
        cloned = embedTraversal(cloned,struct,n)
        return cloned
    return embedStruct0
```
◇

Macro referenced in .

Structure embedding algorithm

⟨Structure embedding algorithm 14b⟩ ≡
```
""" Structure embedding algorithm """
def embedTraversal(cloned, obj,n):
    for i in range(len(obj)):
        if isinstance(obj[i],Model):
            cloned.body += [obj[i]]
        elif (isinstance(obj[i],tuple) or isinstance(obj[i],list)) and (
```

```
                    len(obj[i])==2 or len(obj[i])==3):
                V,FV,EV = obj[i]
                V = [v+n*[0.0] for v in V]
                cloned.body  += [(V,FV,EV)]
            elif isinstance(obj[i],Mat):
                mat = obj[i]
                d,d = mat.shape

                newMat = scipy.identity(d+n*1)
                for h in range(d-1):
                    for k in range(d-1):
                        newMat[h,k] = mat[h,k]
                    newMat[h,d-1+n*1] = mat[h,d-1]
                cloned.body  +=  [newMat.view(Mat)]

            elif isinstance(obj[i],Struct):
                newObj = Struct()
                newObj.box = hstack((obj[i].box, [n*[0],n*[0]]))
                newObj.name = obj[i].name+"New"
                cloned.body  += [embedTraversal(newObj, obj[i], n)]
        return cloned
    ◇
```

Macro referenced in 14a.

5   Larstruct exporting

Here we assemble top-down the `lar2psm` module, by orderly listing the functional parts
it is composed of. Of course, this one is the module version corresponding to the current
state of the system, i.e. to a very initial state. Other functions will be added when needed.

```
"lib/py/larstruct.py" 15 ≡
    """Module with functions needed to interface LAR with pyplasm"""
    ⟨Function to import a generic module 19b⟩
    from lar2psm import *
    ⟨Translation matrices 2a⟩
    ⟨Scaling matrices 2b⟩
    ⟨Rotation matrices 3a⟩
    ⟨Embedding and projecting a geometric model 8⟩
    ⟨Apply an affine transformation to a LAR model 1⟩
    ⟨Check for dimension of a structure element (Verts or V) 12a⟩
    ⟨Remove duplicate faces 6b⟩
    ⟨Traversal of a scene multigraph 13a⟩
    ⟨types Mat and Verts 4a⟩
    ⟨Model class 4b⟩
    ⟨Struct class 5⟩
```

$\langle$ Structure to pair (Vertices,Cells) conversion 7 $\rangle$
$\langle$ Embedding and projecting a geometric model 8 $\rangle$
$\langle$ Embed a struct object 14a $\rangle$
$\langle$ Computation of the containment box of a Lar Struct or Model 6a $\rangle$
$\diamond$

6 Examples

Some examples of structures as combinations of LAR models and affine transformations
are given in this section.

Global coordinates   We start with a simple 2D example of a non-nested list of translated
2D object instances and rotation about the origin.

```
"test/py/larstruct/test04.py" 16a ≡
    """ Example of non-nested structure with translation and rotations """
    import sys; sys.path.insert(0, 'lib/py/')
    from largrid import *
    from larstruct import *
    square = larCuboids([1,1])
    table = larApply( t(-.5,-.5) )(square)
    chair = larApply( s(.35,.35) )(table)
    chair1 = larApply( t(.75, 0) )(chair)
    chair2 = larApply( r(PI/2) )(chair1)
    chair3 = larApply( r(PI/2) )(chair2)
    chair4 = larApply( r(PI/2) )(chair3)
    VIEW(SKEL_1(STRUCT(MKPOLS(table)+MKPOLS(chair1)+
                       MKPOLS(chair2)+MKPOLS(chair3)+MKPOLS(chair4))))
    ◇
```

Local coordinates   A different composition of transformations, from local to global co-
ordinate frames, is used in the following example.

```
"test/py/larstruct/test05.py" 16b ≡
    """ Example of non-nested structure with translation and rotations """
    import sys; sys.path.insert(0, 'lib/py/')
    from largrid import *
    from larstruct import *
    square = larCuboids([1,1])
    square = Model(square)
    table = larApply( t(-.5,-.5) )(square)
    chair = larApply( s(.35,.35) )(table)
    chair = larApply( t(.75, 0) )(chair)
    struct = Struct([table] + 4*[chair, r(PI/2)])
```

```
        scene = evalStruct(struct)
        VIEW(SKEL_1(STRUCT(CAT(AA(MKPOLS)(scene)))))
        ◇
```

Call of nested structures by reference   Finally, a similar 2D example is given, by
nesting one (or more) structures via separate definition and call by reference from the
interior. Of course, a cyclic set of calls must be avoided, since it would result in a *non
acyclic* multigraph of the structure network.

"test/py/larstruct/test06.py" 17a ≡
```
        """ Example of nested structures with translation and rotations """
        import sys; sys.path.insert(0, 'lib/py/')
        from largrid import *
        from larstruct import *
        square = larCuboids([1,1])
        square = Model(square)
        table = larApply( t(-.5,-.5) )(square)
        chair = Struct([ t(.75, 0), s(.35,.35), table ])
        struct = Struct( [t(2,1)] + [table] + 4*[r(PI/2), chair])
        struct = Struct(10*[struct,t(0,2.5)])
        struct = Struct(10*[struct,t(3,0)])
        scene = evalStruct(struct)
        VIEW(SKEL_1(STRUCT(CAT(AA(MKPOLS)(scene)))))
        ◇
```

"test/py/larstruct/test08.py" 17b ≡
```
        """ LAR model input and handling """
        ⟨Input of LAR architectural plan 17c⟩
        dwelling = larApply(t(3,0))(Model((V,FV)))
        print "\n dwelling =",dwelling
        VIEW(EXPLODE(1.2,1.2,1)(MKPOLS(dwelling)))
        plan = Struct([dwelling,s(-1,1),dwelling])
        VIEW(EXPLODE(1.2,1.2,1)(CAT(AA(MKPOLS)(evalStruct(plan)))))
        ◇
```

⟨Input of LAR architectural plan 17c⟩ ≡
```
        ⟨Initial import of modules ?⟩
        from mapper import *
        V = [[3,-3],
        [9,-3],[0,0],[3,0],[9,0],[15,0],
        [3,3],[6,3],[9,3],[15,3],[21,3],
        [0,9],[6,9],[15,9],[18,9],[0,13],
        [6,13],[9,13],[15,13],[18,10],[21,10],
        [18,13],[6,16],[9,16],[9,17],[15,17],
        [18,17],[-3,24],[6,24],[15,24],[-3,13]]
        FV = [
```

```
[22,23,24,25,29,28], [15,16,22,28,27,30], [18,21,26,25],
[13,14,19,21,18], [16,17,23,22], [11,12,16,15],
[9,10,20,19,14,13], [2,3,6,7,12,11], [0,1,4,8,7,6,3],
[4,5,9,13,18,17,16,12,7,8],[17,18,25,24,23]]
◇
```

Macro referenced in .

Transformation of Struct object to LAR model pair   The following test application first generates a grid 3×3 of LAR cubes, extracts its boundary cells as BV, then produces a struct object with 30 translated instances of it, and finally transforms the struct object into a LAR pair W,FW. Let us notice that due to the assembly process, some 2-cells in FW are doubled.

`"test/py/larstruct/test09.py"` 18a ≡

```
""" Transformation of Struct object to LAR model pair """
import sys
""" import modules from larcc/lib """
sys.path.insert(0, 'lib/py/')
from larstruct import *

⟨ Transform Struct object to LAR model pair 18b ⟩
◇
```

The actual generation of the structure and its transformation to a LAR model pair is actually performed in the following macro.

⟨ Transform Struct object to LAR model pair 18b ⟩ ≡

```
""" Generation of Struct object and transform to LAR model pair """
cubes = larCuboids([10,10,10],True)
V = cubes[0]
FV = cubes[1][-2]
CV = cubes[1][-1]
bcells = boundaryCells(CV,FV)
BV = [FV[f] for f in bcells]
VIEW(EXPLODE(1.2,1.2,1.2)(MKPOLS((V,BV))))

block = Model((V,BV))
struct = Struct(10*[block, t(10,0,0)])
struct = Struct(10*[struct, t(0,10,0)])
struct = Struct(3*[struct, t(0,0,10)])
W,FW = struct2lar(struct)

VIEW(EXPLODE(1.2,1.2,1.2)(MKPOLS((W,FW))))
◇
```

Macro referenced in .

.1 Importing a generic module

First we define a parametric macro to allow the importing of `larcc` modules from the project repository `lib/py/`. When the user needs to import some project's module, she may call this macro as done in Section **??**.

⟨ Import the module 19a ⟩ ≡
```
import sys; sys.path.insert(0, 'lib/py/')
import @1
```
◇

Macro referenced in 19b.

Importing a module A function used to import a generic `lacccc` module within the current environment is also useful.

⟨ Function to import a generic module 19b ⟩ ≡
```
def importModule(moduleName):
```
    ⟨ Import the module (19c `moduleName`) 19a ⟩
◇

Macro referenced in 15.

References

[CL13]   CVD-Lab, *Linear algebraic representation*, Tech. Report 13-00, Roma Tre University, October 2013.

[Pao03] A. Paoluzzi, *Geometric programming for computer aided design*, John Wiley & Sons, Chichester, UK, 2003.