LAR-ABC, a representation of architectural geometry
From concept of spaces, to design of building fabric, to construction simulation *

Alberto Paoluzzi   Enrico Marino   Federico Spini

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Abstract

This paper discusses the application of LAR (Linear Algebraic Representation) scheme [DPS14] to the whole architectural design process, from initial concept of spaces, to the additive manufacturing of design models, to the meshing for CAE analysis, to the detailed design of components of building fabric, to the BIM processing of quantities and costs. LAR (see, e.g. [1]) is a novel general and simple representation scheme for geometric design of curves, surfaces and solids, using simple, general and well founded concepts from algebraic topology. LAR supports all topological incidence structures, including enumerative (images), decompositive (meshes) and boundary (CAD) representations. It is dimension-independent, and not restricted to regular complexes. Furthermore, LAR enjoys a neat mathematical format, being based on chains, the domains of discrete integration, and cochains, the discrete prototype of differential forms, so naturally integrating the geometric shape with the supported physical properties. The LAR representation find his roots in the design language Plasm [Pao03], and is currently embedded in python and javascript, providing the designer with powerful and simple tools for a geometric calculus of shapes. In this paper we introduce the motivation of this approach, discussing how it compares to other mixed-dimensionality representations of geometry and is supported by open-source software projects. We also discuss simple examples of use, with reference to various stages of the design process.

Contents

1 Introduction

Looking for simplicity. Form and function. Who comes first? CAD is evolving with the net. Algebraic geometry on graphics processors.

2 Linear Algebraic Representation

2.1 Representation scheme

A foundational concept. Mapping from mathematical models to computer representations. Taxonomy: decompositive, enumerative, boundary, procedural representations. The defacto standard of PLM systems: non-manifold data structures + NURBS. Old, expensive, and inflexible. Towards big geometric data. The need for rethinking the foundations. Algebraic geometry is here to stay. Sparse matrices and GPGPU.

2.2 Topological operations

Space decompositions. Chains as subsets of spaces. Cochains as fields over chains. Geometric integration: pairing of chains and cochains. Homology and cohomology. Boundary and coboundary operators. A single SpMV multiplication to compute the boundary of any chain of spaces. Transposition and coboundary. Coboundary and operators of vector analysis: gradient, curl, divergenze, and Laplacian. Integration of geometry and physics through topological structures. Topological queries. The d-star of every cell. Decomposition of big structures and distributed computing.

2.3 Models and structures

Model = Topology + Geometry. Model as embedded topology. Topology as the list of higher-dimensional cells of a space decomposition. The classical representation of cells via the list of their vertices. Composition of linear operators as the product of their matrices. Fast transposition and product operations via GPGPU and OpenCL. Structures as hierarchical aggregation of space-instanced models and/or other structures. The representation of structures as ordered sequences of strictres, models and operators. Data Base of structures. The traversal of structures at run-time.

3 LAR for Architecture, Building and Construction

3.1 Architectural structures: the organisation of spaces

Organic or rational architecture? Form from function or vice-versa? In either case, space units produce organised assemblies of spaces with more or less specialised functions. In set-theoretical terms, they provide either a partitioning or a covering of the building space.

At the very end, an architectural design defines a topology of the space, as a collection of subsets (of space), closed with respect to finite intersection and union.

In practical terms, the design concept will result in a cellular decomposition of the space, where elementary space units, either open or closed or partially open, establish pairwise adjacency relations; even before of any concrete embedding, i.e. even before that a global shape is envisioned by the architect.

In the majority of cases, the geometric embedding of the design topology will produce a partitioning of space with plane or curved surfaces, and some horizontal or vertical composition of use patterns. In common building and construction, most of the separating surfaces will be either horizontal or vertical, but different arrangements of space cells are possible.

LAR-ABC requires that the topology is first defined hierarchically, producing finally a space plan subdivided by layers, where the junctions of at least three separating surfaces are identified and numbered. The simplest data definition is, of course, via the production of planar architectural drawings embedded in a common reference system.

3.2 Models, structures, assemblies

In LAR-ABC we make a distinction between geometric *models*, *structures*, and *assemblies*. Some terminology and definitions are given below.

Geometric model   A geometric *model* is a pair (*geometry*,*topology*) in a given coordinate system, where *topology* is the LAR specification of highest dimensional cells of a cellular decomposition of the model space, and *geometry* is specified by the coordinates of *vertices*, the spatial embedding of 0-cells of the cellular decomposition of space. From a coding viewpoint, a model is either an instance of the `Model` class, or simply a pair (`vertices`, `cells`), where `vertices` is a two-dimensional array of floats arranged by rows, and where the number of columns (i.e. of *coordinates*) equals the dimension n of the embedding Euclidean space $\mathbb{E}^n$. Similarly, `cells` is a list of lists of vertex indices, where every list of indices corresponds to one of d-dimensional *cells* of the space partition, with $d \leq n$.

Structure   A *structure* is the LAR representation of a hierarchical organisation of spaces into substructures, that may be organised into lower-level substructures, and so on, where each part *may* be specified in a *local coordinate system*. Therefore, a structure is given as an *(ordered) list of substructures and transformations* of coordinates, that apply to all the substructures following in the same list. A structure actually represents a *graph of the scene*, since a substructure may be given a name, and referenced more than one time within one or more other structures. The *structure network*, including references, can be seen as an acyclic directed multigraph. In coding term, a structure is an instance of the *Struct* class, whose parameter is a list of either other structures, or models, or transformations of coordinates, or references to structures or models.

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Assembly An assembly is an *(unordered) list of models* all *embedded in the same coordinate space*, i.e. all using the same coordinate system (the *world coordinate system*). A assembly may be either defined by the user as a list of models, or automatically generated by the *traversal* of a structure network. At traversal time, all the traversed structures and models are transformed from their local coordinate system to the world coordinates, that correspond to the coordinate frame of the root of the traversed network, i.e. to the first model of the structure passed as argument to the `evalStruct` function, that implements the traversal algorithm. In few words, we can say that an assembly is the linearised version of the traversed structure network, where all the models are using the world coordinate system.

4 The design of LAR-ABC

LAR-ABC is a python library for geometric design of building objects with the Linear Algebraic Representation (LAR) specialised for Architecture, Building and Construction (ABC). In the present first prototype implementation of the library, we concentrate on the first two letters of this specification, namely the organisation of spaces (architecture) and the specification of physical, concrete components (building).

4.1 Concept design and project plan

The client needs and wishes are initially specified by some initial set of requirements, traduced by the architect firm into a design concept, better specified by an initial project plan. When the project plan is accepted by the client, giving a definite shape to the first architectural concept, the model of construction is usually a 2.5D model, made by opaque or transparent 2D surfaces embedded in 3D space.

In this stage, LAR-ABC allows for the computation of every topological or geometrical property of interest, including the evaluation of the surface of the building envelope and its partitioning into subsets with different thermal requirements, as well as the computation of the internal volume, and its partitioning into any classes of internal space, and will grant any other geometric computation or simulation (for example of the thermal behaviour) of possible interest for the architect or the client.

4.2 Building objects: components and assemblies

The LAR description of the topology and its geometric embedding, defined by the position vectors of vertices or control points of the surfaces, makes possible to (mostly) automatically generate a first 3D model of the physical construction, i.e. of the concrete instances of building components.

This (semi-)automatic transformation from a 2.5D model formed by surfaces to a 3D model formed by assemblies of solid objects, is obtained using the boundary operator, that

allow to discriminate between the various subsystems of the building fabric, i.e. between the horizontal and vertical enclosures, the horizontal and vertical partitions of the interior, the elements of horizontal and vertical communications, and so on, as we show in Section 5.

4.2.1 Some operators for assemblies

Remember that an assembly is a *list* of geometric models, i.e.is a list of pairs made by vertices and cells. Therefore, few specialised higher-level functions are needed to apply the typical operations of models to assemblies. Some higher-order general utilities for handling geometric assemblies are given below.

Some operators for assemblies The function `larCells` is used to apply a given `fun` to the *cells* of every LAR model contained in `assembly`. Conversely, `larVerts` is used to apply a given `fun` to the *vertices* of every model in the `assembly`. Also, `larBinOps` allows to apply a binary `op`aeration to every argument pair generated by right distribution of the `arg` argument over the models contained in `assembly`.

⟨Some operators for assemblies 6⟩ ≡

```
def larCells(fun):
   def larCells0(assembly):
      return TRANS(CONS([S1,COMP([AA(fun),S2])])(TRANS(assembly)))
   return larCells0

def larVerts(fun):
   def larCells0(assembly):
      return TRANS(CONS([ COMP([AA(fun),S1]),S2 ])(TRANS(assembly)))
   return larCells0

def larBinOps(op):
   def larCells0(assembly):
      def larCells1(arg):
         return AA(op)(DISTR([assembly,arg]))
      return larCells1
   return larCells0
◇
```

Macro referenced in 16b.

Low-dimensional constructors: 1D and 0D The `larQuote1D` function replicates the behaviour of the PLaSM `QUOTE` operator, where `pattern` is a list of either positive or negative numbers, respectively used to fill solid or empty intervals on the real line, producing as output a 1D LAR model. The `larQuote0D` function is used to embed several instances of a d-dimensional model in $\mathbb{E}^d$, i.e. to compte a Cartesian product of models

without increasing neither the embedding nor the intrinsic dimensions. A typical case use is to compute the d-skeleton (needed for the ∂_{d+1} operator) in a $(d+1)$-dimesional extrausion.

⟨ Low-dimensional constructors: 1D and 0D 7a ⟩ ≡

```
def larQuote1D(pattern):
   return larExtrude1( VOID, pattern )

def larQuote0D(pattern):
   V,CV = larQuote1D(pattern)
   return V,[[k] for k in range(len(V))]
◇
```

Macro referenced in 16b.

4.3 Construction process: computer simulation

Some general information about the technologies to be used in the construction allows to visualise as a computer animation the construction process embedded in time. Starting to the specification of the hierarchical assemblies and from some additional information about the precedence relation between the construction activities, a construction PERT, giving the time schedule of the building erection. Of course, a preliminary but informed guess of quantities and costs ban be also produced from the 3D solid model.

5   Example: apartment block design

A simple example of housing design is discussed in this section. The concept of the dwelling produced by using a vectorial drawing program, is shown in Figure 1. The input file is parsed, producing the LAR `model` given in the script below, as a pair `V,FV` of vertices `V` and 2-cells `FV`.

5.1   LAR model input

Input of the dwelling concept   The vertices list `V` contains pairs of coordinates within a local reference frame. The 2-cell list `FV` of references to vertices is given counterclockwise, in order to automatically get a complete LAR representation of topology, i.e. the pair `FV,` `EV` of 2-cells and 1-cells.

⟨ Input of LAR architectural plan 7b ⟩ ≡

```
V = [[3,-3],
[9,-3],[0,0],[3,0],[9,0],[15,0],
[3,3],[6,3],[9,3],[15,3],[21,3],
```
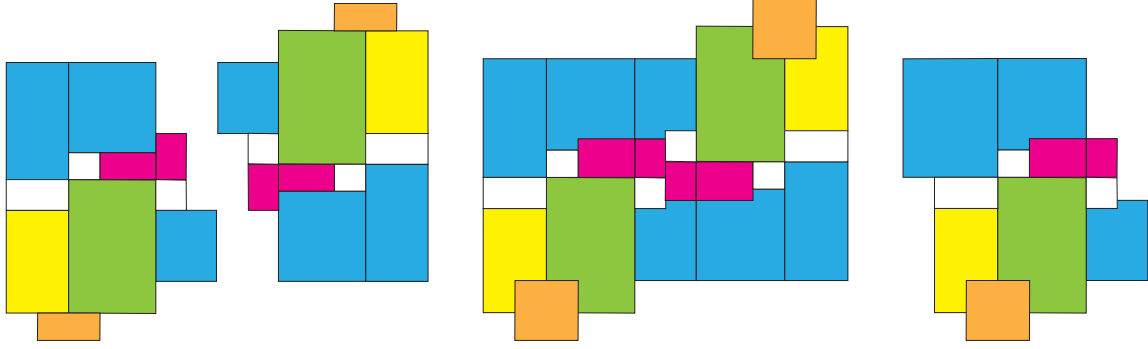
Figure 1: Concept design. living/eating area (green/yellow); bedrooms (cyan), lavatories (magenta); entrance (white).

```
[0,9],[6,9],[15,9],[18,9],[0,13],
[6,13],[9,13],[15,13],[18,10],[21,10],
[18,13],[6,16],[9,16],[9,17],[15,17],
[18,17],[-3,24],[6,24],[15,24],[-3,13]]
FV = [
[22,23,24,25,29,28], [15,16,22,28,27,30], [18,21,26,25],
[13,14,19,21,18], [16,17,23,22], [11,12,16,15],
[9,10,20,19,14,13], [2,3,6,7,12,11], [0,1,4,8,7,6,3],
[4,5,9,13,18,17,16,12,7,8],[17,18,25,24,23]]
dwelling = [V,FV]
◇
```

Macro referenced in 9, 11bc, 17b, 18a.

5.2   Partitioning the 1-cells

The subdivision of 1-cells of the complex between boundary cells and interior cells is executed by computing the boundary operator ∂_2, and multiplying it by the coordinate representation **1** of the 2D basis of cells.

Subdivide the 1-cells of the concept plan   The input to `bUnit_to_eEiP`, to compute the 1D external envelope and interior partitions starting from 2D from building units, is given below.

⟨ Subdivide the 1-cells 8 ⟩ ≡

```
def bUnit_to_eEiP(FV,EV):
    """ Subdivide the 1-cells.
    Return external envelope and interior partitions """
    eE = lar2boundaryEdges(FV,EV)
    iP = lar2InteriorEdges(FV,EV)
```
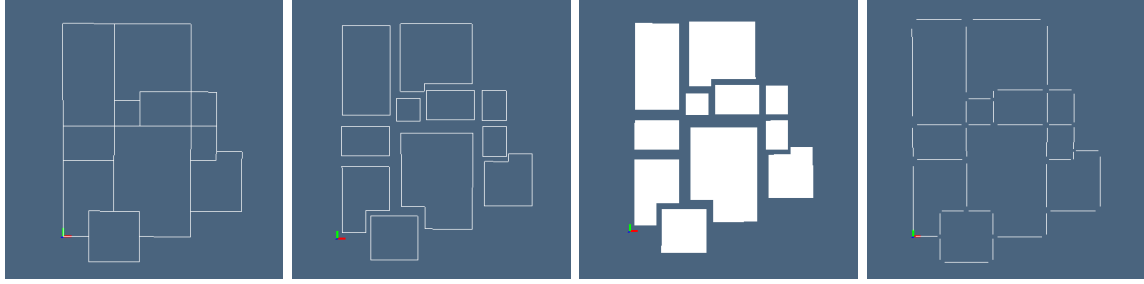
Figure 2: (a) LAR drawing as close polylines: (b) exploded polylines: (c) exploded 2-cells: (d) exploded 1-cells.

```
        return eE,iP
    ◇
```
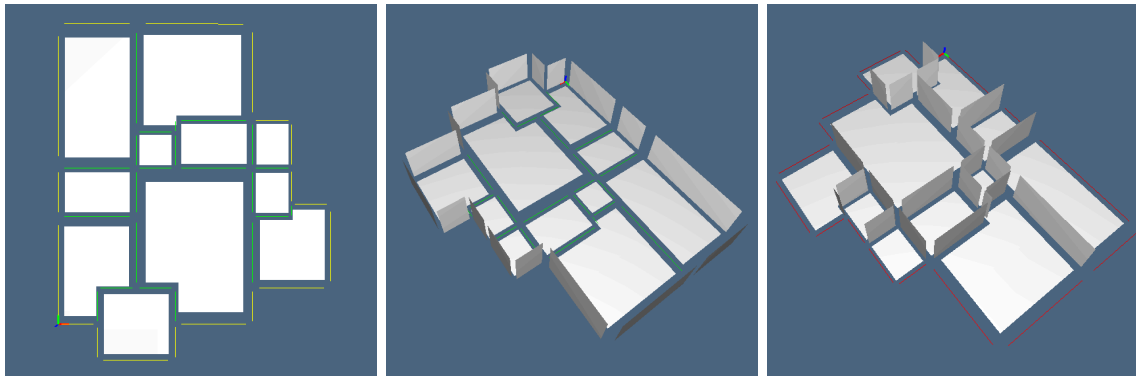Macro referenced in 16b.

Figure 3: (a) 2-cells, interior 1-chain (green), boundary 1-chain (red): (b) boundary 2-chain: (c) interior 2-chain.

5.3   Floor assembly of apartment building

Typical floor assembly of apartment block

```
"test/py/architectural/test04.py" 9 ≡
    """ D LAR model input and handling """
    ⟨ Initial import of modules 17a ⟩
    from architectural import *
    ⟨ Input of LAR architectural plan 7b ⟩
    ⟨ Generation of the typical flat of apartment block 11a ⟩
    ◇
```
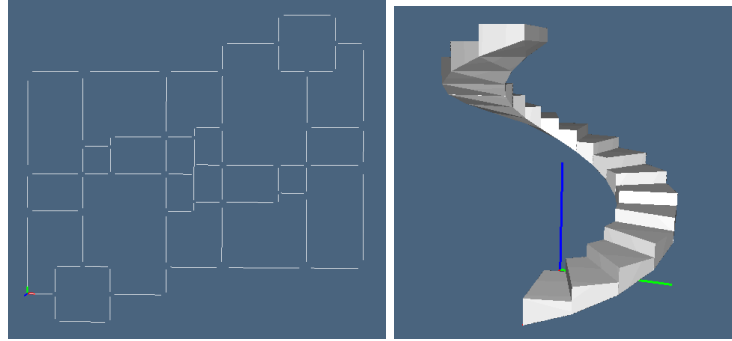
Figure 4: Concept design: (a) aggregation of two building units; (b) fully parametric spiral stair.
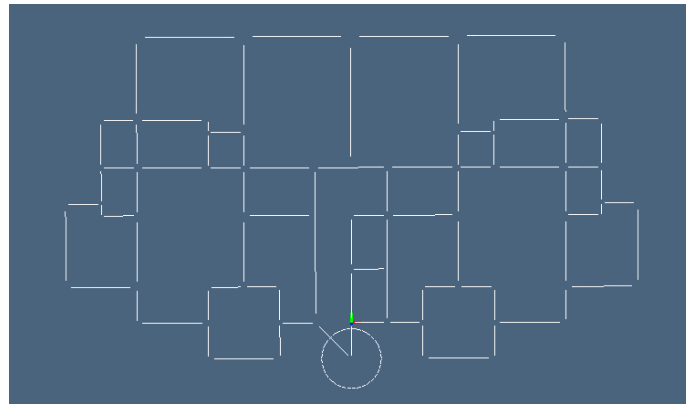
Figure 5: Concept design: (a) aggregation of two building units; (b) fully parametric spiral stair.

⟨ Generation of the typical flat of apartment block 11a ⟩ ≡

```
    V,FV = larApply(t(3,0))(dwelling)
    print "\n V,FV =",V,FV
    VIEW(EXPLODE(1.2,1.2,1)(MKPOLS(dwelling)))
    dwelling = Struct([ t(3,0), dwelling ])
    V1 = [[0,0],[3,0],[3,4.5],[0,4.5],[3,9],[0,9],[3,13],[-3,13],[-3,0],[0,-3]]
    FV1 = [[0,1,2,3],[3,2,4,5],[0,3,5,4,6,7,8,9]]
    landing = V1,FV1
    plan = Struct([landing,dwelling,s(-1,1),dwelling])
    assembly2D = evalStruct(plan)
    assembly1D = larCells(face2edge)(assembly2D)
    VIEW(EXPLODE(1.2,1.2,1)(CAT(AA(MKPOLS)(assembly1D))))
    ◇
```

Macro referenced in 9, 11b.

Initial 3D assembly of apartment block

"test/py/architectural/test05.py" 11b ≡

```
    """ 3D mock-up of apartment block """
    ⟨ Initial import of modules 17a ⟩
    from architectural import *
    ⟨ Input of LAR architectural plan 7b ⟩
    ⟨ Generation of the typical flat of apartment block 11a ⟩
    stair = spiralStair(width=0.2,R=3,r=0.25,riser=0.1,pitch=4.4,nturns=1.75,steps=36)
    stair = larApply(r(0,0,3*PI/4))(stair)
    stair = larApply(t(0,-3,0))(stair)
    stairColumn = larApply(t(0,-3,0))(larRod(0.25,4.2)())
    mod_1 = larQuote1D( 6*[0.2,-3.8] )
    assembly3D = larBinOps(larModelProduct)(assembly2D)(mod_1)
    VIEW(EXPLODE(1.2,1.2,1)(CAT(AA(MKPOLS)(assembly3D))))

    horClosures = horizontalClosures([0.2,-3.8]*12 +[0.2])(assembly2D)
    VIEW(STRUCT(horClosures))

    wire = SKEL_1(INSR(PROD)(AA(QUOTE)([[6,9,9,9,9,6],[-3,10,11],[4]*12])))
    VIEW(wire)
    frame3D = T(1)(-24)(OFFSET([.2,.6,.2])(wire))
    VIEW(frame3D)

    assembly3D = evalStruct(Struct([stairColumn,stair,t(0,0,4)]*12))
    VIEW(STRUCT(CAT(AA(MKPOLS)(assembly3D)) + horClosures + [frame3D]))
    ◇
```

"test/py/architectural/test01.py" 11c ≡

```
    ⟨ Initial import of modules 17a ⟩
    from architectural import *
```

⟨ Input of LAR architectural plan 7b ⟩
```
bU = AA(SOLIDIFY)(AA(POLYLINE)(lar2polylines (dwelling)))
EV = face2edge(FV)
VIEW(EXPLODE(1.2,1.2,1)(MKPOLS((V,EV))))

eE,iP = bUnit_to_eEiP(FV,EV)
modEe1D = V, [EV[e] for e in eE]
modIp1D = V, [EV[e] for e in iP]
eE1D = AA(COLOR(RED))(MKPOLS(modEe1D))
iP1D = AA(COLOR(GREEN))(MKPOLS(modIp1D))

VIEW(EXPLODE(1.2,1.2,1)(eE1D))
VIEW(EXPLODE(1.2,1.2,1)(iP1D))
VIEW(STRUCT(bU + iP1D + eE1D))
VIEW(EXPLODE(1.2,1.2,1)(bU + iP1D + eE1D))

floorHeight = larIntervals([1])([4])
modIp2D = larModelProduct([ modIp1D, floorHeight ])
modEe2D = larModelProduct([ modEe1D, floorHeight ])

VIEW(EXPLODE(1.2,1.2,1)(bU + MKPOLS(modIp2D) + eE1D))
VIEW(EXPLODE(1.2,1.2,1)(bU + iP1D + MKPOLS(modEe2D)))
VIEW(EXPLODE(1.2,1.2,1)(bU + MKPOLS(modIp2D) + MKPOLS(modEe2D)))
```
◇

File defined by 11c, 17b.

Horizontal closures generator   The function `horizontalClosures` is applied to a 2D assembly and to a 1D pattern of positive (full) or negative (empty) measures, in order to generate a 3D model of vertical closures of a building block.

⟨ Horizontal closures generator 12 ⟩ ≡
```
def horizontalClosures(pattern):
    vertical1D = larQuote1D(pattern)
    vertical0D = larQuote0D(pattern)
    def horizontalClosures0(assembly2D):
        out = []
        for flat2D in assembly2D:
            V,FV = flat2D
            EV = face2edge(FV)
            dwellH3D = larModelProduct([flat2D,vertical0D])
            dwellV3D = larModelProduct([(V,EV),vertical1D])
            poly3D = AA(POLYLINE)(lar2polylines(dwellH3D))
            floors3D = AA(solidify)(poly3D)
            out += floors3D+MKPOLS(dwellV3D)
        return out
```

```
            return horizontalClosures0
    ◇
```
Macro referenced in 16b.

Spatial beams and frames

⟨ Spatial beams and frames 13 ⟩ ≡
```
    from myfont import *
    columns0D = V,[[k] for k in range(len(V))]
    columns = larModelProduct([columns0D,larQuote1D([4])])
    indices = [T([1,2])(v)(S([1,2])([.1,.1])(TEXT(str(k)))) for k,v in enumerate(V)]
    VIEW(STRUCT(MKPOLS(columns)+indices))


    wire = SKEL_1(INSR(PROD)(AA(QUOTE)([[6,9,9,9,9,6],[-3,10,11],[4.2]*5])))
    VIEW(wire)
    frame3D = T(1)(-24)(OFFSET([.2,.4,.4])(wire))
    VIEW(frame3D)


    ◇
```
Macro never referenced.

6   The ABC computational framework

6.1   ABC: a set of classes

We have already specified some geometric and topological conchps as a set of basic ABC classes: vertices and cells, models, structures and assemblies. Such basis classes are further specialized by a hierarchy of subclasses adding detailed semantics relative to the particular class of buildings under consideration and/or the considered construction technology and process.

6.2   Some specialised methods

2 column

6.3   Zero install: working in the browser

0.5 column

7 Software module contents

7.1 From faces to list of edges

Some transformations of 2D data are given In this section.

From faces FV to list of edges EV   The `face2edge` operator takes every consecutive pair of vertex indices from each face and return such list of pairs (i.e. the EV relation), filtered from double instances.

⟨ From faces FV to list of edges EV 14a ⟩ ≡

```
def face2edge(FV):
    """ From faces to list of edges """
    edges = AA(sorted)(CAT([TRANS([face, face[1:]+[face[0]]]) for face in FV]))
    return AA(eval)(set(AA(str)(edges)))
◇
```

Macro defined by 14ab.
Macro referenced in 16b.

From LAR model to list of polylines   The function `lar2polylines` transform a LAR model into a list of polylines, i.e. of (closed) lists of 2D points, where the last point coincides with the first one.

⟨ From faces FV to list of edges EV 14b ⟩ ≡

```
def lar2polylines (model):
    """ From LAR model to list of polylines """
    V,FV = model
    return [[V[v] for v in cell]+[V[cell[0]]] for cell in FV]
◇
```

Macro defined by 14ab.
Macro referenced in 16b.

Boundary cells $(2D \rightarrow 1D)$ **computation**   The computations of boundary cells is executed by calling the `boundaryCells` from the `larcc` module.

⟨ Boundary cells $(2D \rightarrow 1D)$ computation 14c ⟩ ≡

```
def lar2boundaryEdges(FV,EV):
    """ Boundary cells computation """
    return boundaryCells(FV,EV)
◇
```

Macro referenced in 16b.

14

Interior partitions $(2D \to 1D)$ **computation**   The indices of the boundary 1-cells are returned in `boundarychain1`, and subtracted from the set $\{0, 1, \ldots, |E| - 1\}$ in order to return the indices of the `interiorCells`.

⟨Interior partitions $(2D \to 1D)$ computation 15a⟩ ≡

```
def lar2InteriorEdges(FV,EV):
    """ Boundary cells computation """
    boundarychain1 = boundaryCells(FV,EV)
    totalChain1 = range(len(EV))
    interiorCells = set(totalChain1).difference(boundarychain1)
    return interiorCells
```
    ◇

Macro referenced in 16b.

7.2 Geometric aggregation of building units

Several methods can be used to to aggregate the LAR models `[V,CV]` and `[W,CW]` of two building units into one single structure. The method provided by the `movePoint2point(twoModels)` function aggregates the vertices of two models after having applied a translation `t()` to the second set of vertices (`W`). The translation vector is computed as vector difference of `pointQ` and `pointP`.

Move : $Model \times Model \to Model$ **operator**

⟨Move $(P \to Q)$ operator 15b⟩ ≡

```
def movePoint2point(twoModels):
    """ Move (P -> Q) operator """
    def movePoint2point0(pointP):
        def movePoint2point1(pointQ):
            [V,CV], [W,CW] = twoModels
            mat = t( *DIFF([pointP,pointQ]) )
            [W,CW] = larApply(mat)([W,CW])
            print "\n W =",W
            print "\n CW =",CW
            n = len(V)
            return [ V+W, CV+[[w+n for w in REVERSE(cell)] for cell in CW] ]
        return movePoint2point1
    return movePoint2point0
```
    ◇

Macro referenced in 16b.

Parametric spiral stair A fully parametric `spiralStair` functions is given below, where the major and minor radiuses `R` and `r`, the step `riser`, the spiral `pitch`, i.e. the distance between two turns, the real number of turns `nturns` and the number of `steps` for every 2π angle can be user-specified.

⟨Trasform a solid helicoid into a spiral stair 16a⟩ ≡

```
def spiralStair(width=0.2,R=1.,r=0.5,riser=0.1,pitch=2.,nturns=2.,steps=18):
    V,CV = larSolidHelicoid(width,R,r,pitch,nturns,steps)()
    W = CAT([[V[k],V[k+1],V[k+2],V[k+3]]+
        [SUM([V[k+1],[0,0,-riser]]),SUM([V[k+3],[0,0,-riser]])]
        for k,v in enumerate(V[:-4]) if k%4==0])
    for k,w in enumerate(W[:-12]):
        if k%6==0: W[k+1][2] = W[k+10][2]; W[k+3][2] = W[k+11][2]
    nsteps = len(W)/12
    CW =[SUM([[0,1,2,3,6,8,10,11],[6*k]*8]) for k in range(nsteps)]
    return W,CW

if __name__=="__main__":
    VIEW(STRUCT(MKPOLS(spiralStair())))
    VIEW(STRUCT(MKPOLS(spiralStair(0.1))))
```
◇

Macro referenced in 16b.

7.3 Exporting the library

`"lib/py/architectural.py"` 16b ≡

⟨Initial import of modules 17a⟩
⟨From faces FV to list of edges EV 14a, ... ⟩
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⟨Low-dimensional constructors: 1D and 0D 7a⟩
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⟨Horizontal closures generator 12⟩
◇

8 Conclusion

8.1 The state of the art

0.5 column

8.2 What next

0.5 column

References

[CL13]   CVD-Lab, *Linear algebraic representation*, Tech. Report 13-00, Roma Tre University, October 2013.

[DPS14] Antonio Dicarlo, Alberto Paoluzzi, and Vadim Shapiro, *Linear algebraic representation for topological structures*, Comput. Aided Des. **46** (2014), 269–274.

[Pao03] A. Paoluzzi, *Geometric programming for computer aided design*, John Wiley & Sons, Chichester, UK, 2003.

1.5 column = 10 pages

A   Appendix

B   Utility functions

Initial import of modules

⟨Initial import of modules 17a⟩ ≡

```
from pyplasm import *
from scipy import *
import os,sys
""" import modules from larcc/lib """
sys.path.insert(0, 'lib/py/')
from lar2psm import *
from simplexn import *
from larcc import *
from largrid import *
from mapper import *
from boolean import vertexSieve
    ◇
```

Macro referenced in 9, 11bc, 16b, 17b, 18a.

C   Tests

Concept design

"test/py/architectural/test01.py" 17b ≡

⟨Initial import of modules 17a⟩
```
from architectural import *
```
⟨Input of LAR architectural plan 7b⟩
```
# VIEW(STRUCT(AA(POLYLINE)(lar2polylines (model))))
# VIEW(EXPLODE(1.2,1.2,1)(AA(POLYLINE)(lar2polylines (model))))
bU = AA(SOLIDIFY)(AA(POLYLINE)(lar2polylines (dwelling)))
# VIEW(EXPLODE(1.2,1.2,1)(bU))
EV = face2edge(FV)
VIEW(EXPLODE(1.2,1.2,1)(MKPOLS((V,EV))))

eE,iP = bUnit_to_eEiP(FV,EV)
modEe1D = V, [EV[e] for e in eE]
modIp1D = V, [EV[e] for e in iP]
eE1D = AA(COLOR(RED))(MKPOLS(modEe1D))
iP1D = AA(COLOR(GREEN))(MKPOLS(modIp1D))

VIEW(EXPLODE(1.2,1.2,1)(eE1D))
VIEW(EXPLODE(1.2,1.2,1)(iP1D))
VIEW(STRUCT(bU + iP1D + eE1D))
VIEW(EXPLODE(1.2,1.2,1)(bU + iP1D + eE1D))

floorHeight = larIntervals([1])([4])
modIp2D = larModelProduct([ modIp1D, floorHeight ])
modEe2D = larModelProduct([ modEe1D, floorHeight ])

VIEW(EXPLODE(1.2,1.2,1)(bU + MKPOLS(modIp2D) + eE1D))
VIEW(EXPLODE(1.2,1.2,1)(bU + iP1D + MKPOLS(modEe2D)))
VIEW(EXPLODE(1.2,1.2,1)(bU + MKPOLS(modIp2D) + MKPOLS(modEe2D)))
```
⋄

File defined by 11c, 17b.

"test/py/architectural/test02.py" 18a ≡
⟨Initial import of modules 17a⟩
```
from architectural import *
```
⟨Input of LAR architectural plan 7b⟩
```
(W,FW) = larApply(s(-1,-1))(dwelling)
(V,FV) = dwelling
(V,FV) = movePoint2point([ (V,FV),(W,FW) ])(V[20])(W[25])
EV = face2edge(FV)
VIEW(EXPLODE(1.2,1.2,1)(MKPOLS((V,EV))))
```
⋄

⟨Specialized version of solidify operator for horizontal 3D polygons 18b⟩ ≡
```
""" Solidify horizontal polygons in 3D """
def solidify(pol):
    min=MIN([1])(pol)[0]
```

```
max=MAX([1])(pol)[0]
z = MIN([3])(pol)[0]
pol = PROJECT(1)(pol)
siz=max-min
far_point=max+siz*100
def InftyProject(pol):
    verts,cells,pols=UKPOL(pol)
    verts=[[far_point] + v[1:] for v in verts]
    return MKPOL([verts,cells,pols])
ret=SPLITCELLS(pol)
ret=[JOIN([pol,InftyProject(pol)]) for pol in ret]
return T(3)(z)(XOR(ret))
```
◇

Macro referenced in 16b.