# Structured input to HIJSON Towards indoor mapping and IoT modeling \*

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#### March 11, 2016

#### Abstract

This module aims to prototype the process of entering geometric data representing a complex building, to provide them explicit semantic and a hierarchical model. The generated LAR structures [DPS14, PDFJ15] are finally output to HIJSON format, an experimental data format extending GEOJSON for applications of indoor mapping and the Internet-of-Things. In HIJSON a strongly simplied building model, yet sufficient for useful purposes, accommodates the knowledge concerning the use models of the building and the set of interior devices and their connection.

## Contents

1	Introduction	2
2	Implementation	2
	2.1 Input of geometry from external drawings	4
	2.2 Emulation of interactive graphics input	2
	2.3 Structural operations	
3	Exporting the library	Ę
4	Test examples	Ę
	4.1 Example of a complex building model: part definition	ļ
	4.2 Example of a complex building model: integration	

<sup>\*</sup>This document is part of the Linear Algebraic Representation with CoChains (LAR-CC) framework [CL13]. March 11, 2016

## 1 Introduction

Macro referenced in 4b.

# 2 Implementation

## 2.1 Input of geometry from external drawings

File input and computation of cellular complex The modeling process starts with the input of a .svg file, the W3C standard for 2D vector graphics on the web. The file must only contain (by now) <rect> and and property graphics primitives. The geometric data generate the partition of the plane induced by an arrangement of intersecting lines. The arrangement of (fragmented) lines is finally transformed into a 2D LAR model, made by the triple V,FV,EV of vertices, faces and edges. We notice the the LAR input is normalized by the larFromLines function: all vertices in V are transformed in the standard plane interval [0, 1]<sup>2</sup>.

## 2.2 Emulation of interactive graphics input

In this section two functions are given to emulate two graphics input primitives, respectively.

Emulation of input from "selection box" The function accepts as input the LAR model V, FV, EV and a queryBox given in normalized coordinates. It returns V vertexSubset V, faceSubset V, edgeSubset V

```
\( \text{Emulation of input from "selection box" 2b } \) =

\( \text{""" Emulation of input from 'selection box'' over a LAR normalized representation """ from scipy import spatial \)

\( \text{def subComplexInBox(V,FV,EV,queryBox):} \)
\( (\text{xmin,ymin}), (\text{xmax,ymax}) = \text{queryBox} \)
\( if \text{xmin} > \text{xmax: xmin,xmax} = \text{xmax,xmin} \)
\( if \text{ymin} > \text{ymax: ymin,ymax} = \text{ymax,ymin} \)
\( \text{vdict} = \text{dict([(vcode(vert),k) for k,vert in enumerate(V)])} \)
\( \text{} \)
\( \text{Tormalized representation """ over a LAR normalized representation """ ov
```

Macro referenced in 4b.

Emulation of "pick" input over a LAR normalized representation The function accepts as input the LAR model V, FV, EV, the incidence relation FE, that provides for each face the list of incident edges, and a queryPoint given in normalized coordinates. It returns vertexSubset  $\subseteq$  V, faceSubset  $\subseteq$  FV, edgeSubset  $\subseteq$  EV.

```
\langle \text{ Emulation of "pick" input 3a} \rangle \equiv
     """ Emulation of ''pick'' input over a LAR normalized representation """
     def subComplexAroundPoint(V,FV,EV,FE,queryPoint):
         tree = spatial.cKDTree(V)
         pts = np.array([queryPoint])
         dist,closestVertex = tree.query(pts)
         VF = invertRelation(FV)
         closestFaces = VF[closestVertex]
         for face in closestFaces:
             faceEdges = [EV[e] for e in FE[face]]
             classify = pointInPolygonClassification((V,faceEdges))
             if classify(queryPoint) == "p_in":
                  break
         vertexSubset = FV[face]
         edgeSubset = [EV[e] for e in FE[face]]
         faceSubset = [face]
         return vertexSubset,faceSubset,edgeSubset
     if __name__=="__main__":
         VV = AA(LIST)(range(len(V)))
         FE = crossRelation(FV,EV,VV)
         queryPoint = (0.6,0.58)
         vertexSubset,faceSubset,edgeSubset = subComplexAroundPoint(V,FV,EV,FE,queryPoint)
         \#\#VIEW(EXPLODE(1.2,1.2,1.2)(MKPOLS((V,[EV[e] for e in FE[faceSubset[0]]])) + [
```

```
#COLOR(RED)(MK(queryPoint))] ))
```

Macro referenced in 4b.

From LAR chain to colored HPCs The function cells2hpcs is used to assign a given k color to the cells of a chain (cell subset) of a LAR model V,FV. The function returns a list of HPC (colored) objects.

Macro referenced in 4b.

## 2.3 Structural operations

#### From chains to structures

```
\langle From chains to structures 4a \rangle \equiv
     """ From chains to structures """
     def chain2structs(V,FV,EV,FE):
         def chain2structs0(args):
             if args == ([],[],[]): return
             chain,chainName,classtype = args
             struct = []
             for cell in chain:
                  vs = [V[v] for v in FV[cell]]
                  vdict = dict([[vcode(vert),k] for k,vert in enumerate(vs)])
                  facetEdges = [[V[v] for v in EV[e]] for e in FE[cell]]
                  ev = [(vdict[vcode(v1)], vdict[vcode(v2)]) for v1,v2 in facetEdges]
                  fv = [range(len(vs))]
                  shape = vs,fv,ev
                  struct += [ Struct([ shape ], name=None, category="room" ) ]
             out = Struct( struct, name=chainName, category=classtype )
             return out
         return chain2structs0
```

Macro referenced in 4b.

# 3 Exporting the library

```
"larlib/larlib/hijson.py" 4b ≡

""" Module for Structured input to HIJSON """

from larlib import *

from copy import copy

DEBUG = False

⟨SVG file input and computation of cellular complex 2a⟩

⟨Emulation of input from "selection box" 2b⟩

⟨Emulation of "pick" input 3a⟩

⟨From LAR chain to colored HPCs 3b⟩

⟨From chains to structures 4a⟩

⋄
```

# 4 Test examples

## 4.1 Example of a complex building model: part definition

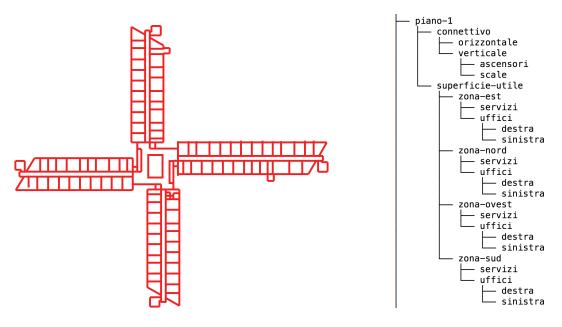


Figure 1: The input SVG drawing of the typical floor layout.

#### Visualization of cell numbering in a 2D complex

 $\langle$  Visualization of cell numbering in a 2D complex  $5a\rangle \equiv$ 

```
""" Visualization of cell numbering in a 2D complex """
     VV = AA(LIST)(range(len(V)))
     submodel = STRUCT(MKPOLS((V,EV)))
     #VIEW(larModelNumbering(1,1,1)(V,[VV,EV,FV[:-1]],submodel,2.5))
Macro referenced in 10b.
Ala nord (HPCs)
\langle \text{ Ala nord 5b} \rangle \equiv
     VV = AA(LIST)(range(len(V)))
     FE = crossRelation(FV,EV,VV)
     chainsToStruct = chain2structs(V,FV,EV,FE)
     """ Ala nord """
     boxes = [0 \text{ for } k \text{ in range}(64)]
     point = [0 for k in range(64)]
     boxes[0] = array([[0.431, 0.607], [0.474, 0.91]])*scaleFactor #[V[k] for k in [39,208]]
     boxes[1] = array([[0.416, 0.657], [0.372, 0.953]])*scaleFactor #[V[k] for k in [162,39]]
     boxes[2] = array([[0.416, 0.627], [0.431, 0.986]])*scaleFactor #[V[k] for k in [206,247]]
     boxes[3] = array([[0.431, 0.607], [0.448, 0.627]])*scaleFactor #[V[k] for k in [39,7]]
     boxes[4] = array([[0.431, 0.91], [0.494, 0.929]])*scaleFactor #[V[k] for k in [213,234]]
     boxes[5] = array([[0.431, 0.97], [0.466, 1.0]])*scaleFactor #[V[k] for k in [58,88]]
     boxes[27] = array([[0.416, 0.627], [0.372, 0.657]])*scaleFactor #[V[k] for k in [110,82]]
     point[0] = array([0.394, 0.9625])*scaleFactor #CCOMB([V[k] for k in [190,197]])
     point[1] = array([0.4525, 0.9325])*scaleFactor #CCOMB([V[k] for k in [166,159]])
     piano1_superficieUtile_zonaNord_uffici_destra = subComplexInBox(V,FV,EV,boxes[0])[1]
     piano1_superficieUtile_zonaNord_uffici_sinistra = subComplexInBox(V,FV,EV,boxes[1])[1]
     piano1_connettivo_orizzontale_zonaNord = subComplexInBox(V,FV,EV,boxes[2])[1]
     piano1_connettivo_verticale_zonaNord_ascensore = subComplexInBox(V,FV,EV,boxes[3])[1]
     piano1_connettivo_verticale_zonaNord_ascensore += subComplexInBox(V,FV,EV,boxes[4])[1]
     piano1_connettivo_verticale_zonaNord_scale = subComplexInBox(V,FV,EV,boxes[5])[1]
     piano1_superficieUtile_zonaNord_servizi = subComplexAroundPoint(V,FV,EV,FE,point[0])[1]
     piano1_superficieUtile_zonaNord_servizi += subComplexAroundPoint(V,FV,EV,FE,point[1])[1]
     piano1_superficieUtile_zonaNord_servizi += subComplexInBox(V,FV,EV,boxes[27])[1]
     piano1N = [piano1_superficieUtile_zonaNord_uffici_destra, piano1_superficieUtile_zonaNord_uffi
Macro defined by 5b, 6a.
Macro referenced in 10b.
\langle \text{ Ala nord 6a} \rangle \equiv
```

```
""" Ala nord """
     piano1N_nomi = ["piano1_superficieUtile_zonaNord_uffici_destra", "piano1_superficieUtile_zonaN
     piano1N_categorie = ["uffici","uffici","corridoi","ascensori","scale","servizi"]
     p1N = zip(piano1N,piano1N_nomi,piano1N_categorie)
     piano1_zonaNord = Struct(AA(chainsToStruct)(p1N), "piano1_zonaNord", "ala")
     #VIEW(SKEL_1(STRUCT(MKPOLS(struct2lar(piano1_zonaNord)))))
     nord = CAT([cells2hpcs(V,FV,chain,k) for k,chain in enumerate(piano1N)])
     #VIEW(EXPLODE(1.2,1.2,1.2)(nord))
Macro defined by 5b, 6a.
Macro referenced in 10b.
Ala est (HPCs)
\langle \text{Ala est 6b} \rangle \equiv
     """ Ala est """
     boxes[6] = array([[0.019, 0.533], [0.376, 0.577]])*scaleFactor #[V[k] for k in [241,29]]
     boxes[7] = array([[0.07, 0.474], [0.343, 0.518]])*scaleFactor #[V[k] for k in [264,148]]
     boxes[8] = array([[0.013, 0.518], [0.376, 0.533]])*scaleFactor #[V[k] for k in [22,63]]
     boxes[9] = array([[0.376, 0.533], [0.39, 0.549]])*scaleFactor #[V[k] for k in [63,92]]
     boxes[10] = array([[0.001, 0.474], [0.07, 0.518]])*scaleFactor #[V[k] for k in [263,265]]
     boxes[11] = array([[0.343, 0.474], [0.376, 0.518]])*scaleFactor #[V[k] for k in [84,149]]
     point[2] = array([0.015, 0.5535])*scaleFactor #CCOMB([V[k] for k in [228,14]])
     piano1_superficieUtile_zonaEst_uffici_destra = subComplexInBox(V,FV,EV,boxes[6])[1]
     piano1_superficieUtile_zonaEst_uffici_sinistra = subComplexInBox(V,FV,EV,boxes[7])[1]
     piano1_connettivo_orizzontale_zonaEst = subComplexInBox(V,FV,EV,boxes[8])[1]
     piano1_connettivo_verticale_zonaEst_ascensore = subComplexInBox(V,FV,EV,boxes[9])[1]
     piano1_connettivo_verticale_zonaEst_scale = subComplexAroundPoint(V,FV,EV,FE,point[2])[1]
     piano1_superficieUtile_zonaEst_servizi = subComplexInBox(V,FV,EV,boxes[10])[1]
     piano1_superficieUtile_zonaEst_servizi += subComplexInBox(V,FV,EV,boxes[11])[1]
     piano1E = [piano1_superficieUtile_zonaEst_uffici_destra, piano1_superficieUtile_zonaEst_uffici
Macro defined by 6b, 7a.
Macro referenced in 10b.
\langle \text{Ala est 7a} \rangle \equiv
     """ Ala est """
     piano1E_nomi = ["piano1_superficieUtile_zonaEst_uffici_destra", "piano1_superficieUtile_zonaEs
     piano1E_categorie = ["uffici","uffici","corridoi","ascensori","scale","servizi"]
     p1E = zip(piano1E,piano1E_nomi, piano1E_categorie)
     piano1_zonaEst = Struct(AA(chainsToStruct)(p1E), "piano1_zonaEst", "ala")
     #VIEW(SKEL_1(STRUCT(MKPOLS(struct2lar(piano1_zonaEst)))))
```

```
#VIEW(EXPLODE(1.2,1.2,1.2)(est + nord))
Macro defined by 6b, 7a.
Macro referenced in 10b.
Ala sud (HPCs)
\langle \text{Ala sud 7b} \rangle \equiv
     """ Ala sud """
     boxes[12] = array([[0.467, 0.138], [0.423, 0.476]])*scaleFactor #[V[k] for k in [252,47]]
     boxes[13] = array([[0.482, 0.145], [0.525, 0.445]])*scaleFactor #[V[k] for k in [241,126]]
     boxes[14] = array([[0.482, 0.476], [0.467, 0.116]])*scaleFactor #[V[k] for k in [254,232]]
     boxes[15] = array([[0.449, 0.476], [0.467, 0.493]])*scaleFactor #[V[k] for k in [40,237]]
     boxes[16] = array([[0.431, 0.101], [0.467, 0.131]])*scaleFactor #[V[k] for k in [259,2]]
     boxes[17] = array([[0.482, 0.445], [0.525, 0.476]])*scaleFactor #[V[k] for k in [155,248]]
     boxes[18] = array([[0.525, 0.104], [0.482, 0.145]])*scaleFactor #[V[k] for k in [111,241]]
     piano1_superficieUtile_zonaSud_uffici_destra = subComplexInBox(V,FV,EV,boxes[12])[1]
     piano1_superficieUtile_zonaSud_uffici_sinistra = subComplexInBox(V,FV,EV,boxes[13])[1]
     piano1_connettivo_orizzontale_zonaSud = subComplexInBox(V,FV,EV,boxes[14])[1]
     piano1_connettivo_verticale_zonaSud_ascensore = subComplexInBox(V,FV,EV,boxes[15])[1]
     piano1_connettivo_verticale_zonaSud_scale = subComplexInBox(V,FV,EV,boxes[16])[1]
     piano1_superficieUtile_zonaSud_servizi = subComplexInBox(V,FV,EV,boxes[17])[1]
     piano1_superficieUtile_zonaSud_servizi += subComplexInBox(V,FV,EV,boxes[18])[1]
     piano1S = [piano1_superficieUtile_zonaSud_uffici_destra, piano1_superficieUtile_zonaSud_uffici
Macro defined by 7b, 8a.
Macro referenced in 10b.
\langle \text{Ala sud 8a} \rangle \equiv
     piano1S_nomi = ["piano1_superficieUtile_zonaSud_uffici_destra", "piano1_superficieUtile_zonaSu
     piano1S_categorie = ["uffici","uffici","corridoi","ascensori","scale","servizi"]
     p1S = zip(piano1S,piano1S_nomi, piano1S_categorie)
     piano1_zonaSud = Struct(AA(chainsToStruct)(p1S), "piano1_zonaSud", "ala")
     #VIEW(SKEL_1(STRUCT(MKPOLS(struct2lar(piano1_zonaSud)))))
     sud = CAT([cells2hpcs(V,FV,chain,k) for k,chain in enumerate(piano1S)])
     #VIEW(EXPLODE(1.2,1.2,1.2)(est + nord + sud))
Macro defined by 7b, 8a.
Macro referenced in 10b.
```

est = CAT([cells2hpcs(V,FV,chain,k) for k,chain in enumerate(piano1E)])

#### Ala ovest (HPCs)

```
\langle \text{ Ala ovest 8b} \rangle \equiv
     """ Ala ovest """
     boxes[19] = array([[0.521, 0.526], [0.963, 0.568]])*scaleFactor #[V[k] for k in [169,202]]
     boxes[20] = array([[0.555, 0.584], [0.955, 0.627]])*scaleFactor #[V[k] for k in [12,23]]
     boxes[21] = array([[0.521, 0.568], [0.985, 0.584]])*scaleFactor #[V[k] for k in [209,204]]
     boxes[22] = array([[0.506, 0.551], [0.521, 0.568]])*scaleFactor #[V[k] for k in [89,209]]
     boxes[23] = array([[0.808, 0.504], [0.828, 0.526]])*scaleFactor #[V[k] for k in [270,77]]
     boxes[24] = array([[0.955, 0.584], [0.997, 0.627]])*scaleFactor #[V[k] for k in [220,24]]
     boxes[25] = array([[0.521, 0.584], [0.555, 0.627]])*scaleFactor #[V[k] for k in [11,144]]
     boxes[26] = array([[1.0, 0.533], [0.97, 0.568]])*scaleFactor #[V[k] for k in [233,201]]
     piano1_superficieUtile_zonaOvest_uffici_destra = subComplexInBox(V,FV,EV,boxes[19])[1]
     piano1_superficieUtile_zonaOvest_uffici_sinistra = subComplexInBox(V,FV,EV,boxes[20])[1]
     piano1_connettivo_orizzontale_zonaOvest = subComplexInBox(V,FV,EV,boxes[21])[1]
     piano1_connettivo_verticale_zonaOvest_ascensore = subComplexInBox(V,FV,EV,boxes[22])[1]
     piano1_connettivo_verticale_zonaOvest_ascensore += subComplexInBox(V,FV,EV,boxes[23])[1]
     piano1_superficieUtile_zonaOvest_servizi = subComplexInBox(V,FV,EV,boxes[24])[1]
     piano1_superficieUtile_zonaOvest_servizi += subComplexInBox(V,FV,EV,boxes[25])[1]
     piano1_connettivo_verticale_zonaOvest_scale = subComplexInBox(V,FV,EV,boxes[26])[1]
     piano10 = [piano1_superficieUtile_zonaOvest_uffici_destra, piano1_superficieUtile_zonaOvest_uf
Macro defined by 8b, 9a.
Macro referenced in 10b.
\langle \text{ Ala ovest 9a} \rangle \equiv
     """ Ala ovest """
     piano10_nomi = ["piano1_superficieUtile_zona0vest_uffici_destra", "piano1_superficieUtile_zona
     piano10_categorie = ["uffici","uffici","corridoi","ascensori","scale","servizi"]
     p10 = zip(piano10, piano10_nomi, piano10_categorie)
     piano1_zonaOvest = Struct(AA(chainsToStruct)(p10), "piano1_zonaOvest", "ala")
     #VIEW(SKEL_1(STRUCT(MKPOLS(struct2lar(piano1_zona0vest)))))
     ovest = CAT([cells2hpcs(V,FV,chain,k) for k,chain in enumerate(piano10)])
     \#VIEW(EXPLODE(1.2,1.2,1.2)(est + nord + sud + ovest))
Macro defined by 8b, 9a.
Macro referenced in 10b.
Centro stella (HPCs)
\langle Centro stella 9b\rangle \equiv
```

```
""" Centro stella """
     piano1_connettivo_orizzontale_centroStella = [2]
     piano1_connettivo_verticale_centroStella_scale = [15,26]
     piano1C = [[],[],piano1_connettivo_orizzontale_centroStella,[], piano1_connettivo_verticale_centroStella,[]
     centro = CAT([cells2hpcs(V,FV,chain,k) for k,chain in enumerate(piano1C)])
Macro defined by 9bc.
Macro referenced in 10b.
\langle Centro stella 9c\rangle \equiv
     """ Centro stella """
     piano1C_nomi = [[],[],"piano1_connettivo_orizzontale_centroStella", [], "piano1_connettivo_ver
     piano1C_categorie = [[],[],"corridoi",[], "ascensori"]
     p1C = zip(piano1C,piano1C_nomi, piano1C_categorie)
     piano1_centroStella = Struct(AA(chainsToStruct)(p1C), "piano1_centroStella", "centro")
     #VIEW(SKEL_1(STRUCT(MKPOLS(struct2lar(piano1_centroStella)))))
     #VIEW(EXPLODE(1.2,1.2,1.2)(est + nord + sud + ovest + centro))
     #VIEW(STRUCT(est + nord + sud + ovest + centro))
Macro defined by 9bc.
Macro referenced in 10b.
```

### 4.2 Example of a complex building model: integration

#### Assembly of parts (HPCs)

#### Assembling floor layout generation

```
\langle Assembling floor layout generation 10b\rangle \equiv
      """ Assembling floor layout generation """
      (Visualization of cell numbering in a 2D complex 5a)
      \langle \text{ Ala nord } 5b, \dots \rangle
      \langle \text{ Ala est 6b}, \dots \rangle
      \langle \text{Ala sud } 7b, \dots \rangle
      \langle \text{Ala ovest 8b}, \dots \rangle
      ⟨ Centro stella 9b, ... ⟩
      (Assemblaggio 10a)
Macro referenced in 11ab.
\langle Tower example initialization 10c\rangle \equiv
      """ make the model of a layout floor """
      scaleFactor = 83.333
      filename = "test/svg/inters/plan.svg"
      larModel = svg2lar(filename)
      larModel = larApply(s(scaleFactor, scaleFactor))(larModel[:3])
      V,FV,EV = larModel
      FV[2] += FV[71]
                              # for now :o)
Macro referenced in 11ab.
"test/py/hijson/test01.py" 11a \equiv
      """ make the model of a layout floor """
      from larlib import *
      ⟨ Tower example initialization 10c⟩
      (Assembling floor layout generation 10b)
      primoPiano = AA(list)([CAT(AA(S1)(p1N)),CAT(AA(S1)(p1E)),CAT(AA(S1)(p1S)),
                        CAT(AA(S1)(p10)), CAT(AA(S1)(p1C))])
      primoPiano_nomi = ["piano1_zonaNord", "piano1_zonaEst", "piano1_zonaSud", "piano1_zonaOvest", "pia
      primoPiano_categorie = ["ala","ala","ala","ala","centro"]
      pianoPrimo = zip(primoPiano, primoPiano_nomi, primoPiano_categorie)
      piano_1 = Struct( AA(chainsToStruct)(pianoPrimo), "piano1", "level" )
      piano_1_3D = embedStruct(1)(piano_1,"3D")
      iot3d.printStruct2GeoJson("./",piano_1_3D)
      print "piano_1_3D =",piano_1_3D.category
      print "piano_1_3D.body[0] =",piano_1_3D.body[0].category
      print "piano_1_3D.body[0] .body[0] = ",piano_1_3D.body[0].body[0].category
```

```
"test/py/hijson/test02.py" 11b \equiv
     """ make the 2.5 model of a building tower """
     from larlib import *
     \langle Tower example initialization 10c \rangle
     \langle Assembling floor layout generation 10b\rangle
     pianoNord3D = embedStruct(1)(piano1_zonaNord, "3D")
     pianoEst3D = embedStruct(1)(piano1_zonaEst,"3D")
     pianoSud3D = embedStruct(1)(piano1_zonaSud,"3D")
     pianoOvest3D = embedStruct(1)(piano1_zonaOvest,"3D")
     pianoCentro3D = embedStruct(1)(piano1_centroStella,"3D")
     torreNord = Struct(4*[pianoNord3D,t(0,0,3)], "torreNord", "edificio")
     torreEst = Struct(7*[pianoEst3D,t(0,0,3)], "torreEst", "edificio")
     torreSud = Struct(7*[pianoSud3D,t(0,0,3)], "torreSud", "edificio")
     torreOvest = Struct(7*[pianoOvest3D,t(0,0,3)], "torreOvest", "edificio")
     torreCentro = Struct(7*[pianoCentro3D,t(0,0,3)], "torreCentro", "edificio")
     torre = Struct([torreNord,torreEst,torreSud,torreOvest,torreCentro],"torre", "edificio")
     V,FV,EV = struct2lar(torre)
     #VIEW(EXPLODE(1.2,1.2,1.2)(MKPOLS((V,EV))))
     #VIEW(STRUCT(MKPOLS((V,FV))))
```

# References

- [CL13] CVD-Lab, *Linear algebraic representation*, Tech. Report 13-00, Roma Tre University, October 2013.
- [DPS14] Antonio Dicarlo, Alberto Paoluzzi, and Vadim Shapiro, *Linear algebraic representation for topological structures*, Comput. Aided Des. **46** (2014), 269–274.
- [PDFJ15] Alberto Paoluzzi, Antonio DiCarlo, Francesco Furiani, and Miroslav Jirik, *Cad models from medical images using lar*, Computer-Aided Design and Applications **13** (2015), To appear.