# Topic 5 Preference heterogeneity

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Quantitative Spatial Economics

Humboldt University & Berlin School of Economics Summer term 2024

#### Motivation

Introduction

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- ► So far, individuals have been homogenous
  - ► All workers value place-specific amenities the same
  - ▶ Infinite supply of workers to any location for a given combination of
    - ▶ Wages
    - ► Prices (including rents)
    - ► Place attributes
- ► In QSMs, we (usually) add idiosyncratic tastes for location
  - ► Drawn from extreme value distributions

What do idiosyncratic tastes capture and why do they matter?

## Roadmap

Introduction

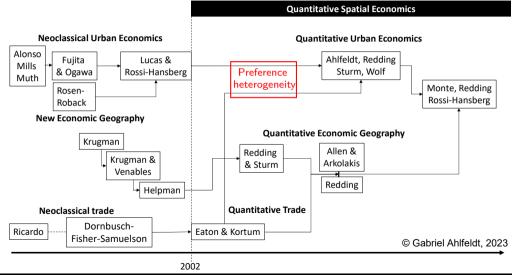
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- ► Review extreme-value distributions
  - ► Fréchet and Gumble
- ► Derive location choice probabilities
  - ▶ Binary case
  - ► Multiple locations
- ► Role of preference heterogeneity in the spatial general equilibrium
  - Dispersion of idiosyncratic tastes affects how
    - differences in fundamentals lead to
    - ▶ differences in prices and quantities on labour and land markets

## History of thought

Introduction

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Extreme value distributions

Introduction

Conclusion

Literature

## Extreme value type I (Gumbel)

$$g(a) = \frac{1}{\beta} \exp\left(-\left[\frac{a-A}{\beta} + \exp\left(-\frac{a-A}{\beta}\right)\right]\right)$$

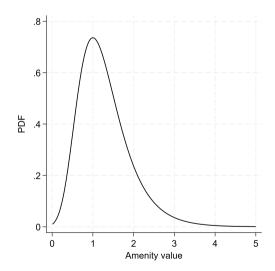
- ► We draw the value of the idiosyncratic amenity a from a distribution g(a)
  - First moment:

$$E(a) = A + \beta \Gamma = A + \left(\frac{1}{\varepsilon}\right) \Gamma$$

Second moment: 
$$\sigma_a^2 = \frac{\pi^2}{6}\beta^2 = \frac{\pi^2}{6}\left(\frac{1}{\varepsilon}\right)^2$$

▶ where ε ≡ 1/β and Γ is the Fuler-Mascheroni constant

What happens if we increase A or  $\varepsilon$ ? What does this mean intuitively?



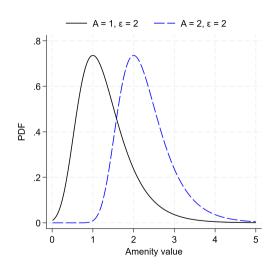
Role in general equilibrium

## Extreme value type I (Gumbel)

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$$g(a) = \frac{1}{\beta} \exp\left(-\left[\frac{a-A}{\beta} + \exp\left(-\frac{a-A}{\beta}\right)\right]\right)$$

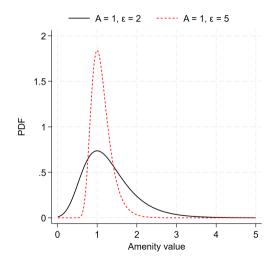
- ► A governs the first moment
  - ► E.g. the average idiosyncratic amenity at a location
- Increasing A implies a higher amenity, on average



## Extreme value type I (Gumbel)

$$g(a) = \frac{1}{\beta} \exp\left(-\left[\frac{a-A}{\beta} + \exp\left(-\frac{a-A}{\beta}\right)\right]\right)$$

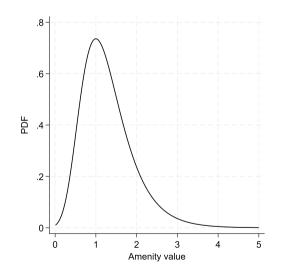
- $\blacktriangleright$   $\varepsilon$  affects first and second moments
  - ► the average idiosyncratic amenity
  - ► the dispersion
- Increasing ε makes workers more similar in tastes
  - ► less dispersion in tastes



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$$f(a) = \frac{\varepsilon}{A} \left(\frac{a}{A}\right)^{-1-\varepsilon} \exp\left(-\left(\frac{a}{A}\right)^{-\varepsilon}\right)$$

- ► We draw the value of the idiosyncratic amenity a from a distribution f(a)
  - First moment:  $E(a) = A\Gamma(1-\frac{1}{a})$
  - Second moment:  $\sigma_{a} = A^{2}\Gamma\left(1 - \frac{2}{3}\right) - \left(\Gamma\left(1 - \frac{1}{3}\right)\right)^{2}$ 
    - ▶ where Γ is the Euler–Mascheroni constant
- Comparative statics similar to Gumbel
  - ▶ Larger  $A \Rightarrow$  greater E(a)
  - ▶ Larger  $\varepsilon \Rightarrow$  smaller  $\sigma_a$
  - ▶ Though A and  $\varepsilon$  affect E(a) and  $\sigma_a$



## Lessons for inversion

#### ▶ Recall

Introduction

- ► QSM has parameters and fundamentals
- For given parameters we invert first moment of fundamental (e.g. average amenity)

#### ▶ Notice

- ightharpoonup First moment depends on structural paramater  $\varepsilon$
- ► Under Gumbel and Fréchet

#### ► Remember

- lacktriangle Fundamental amenity recovered is always specific to the chosen value of  $\epsilon$
- ightharpoonup Therefore, cannot change  $\epsilon$  without changing A

Can do counterfactuals under different values of  $\varepsilon$ . But predicting what happens when  $\varepsilon$  changes is not straightforward

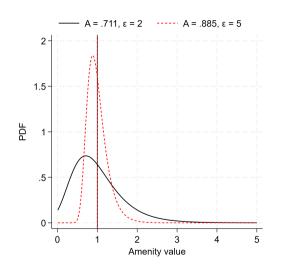
# Inverting A (Gumbel)

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$$A = E(a) - \frac{1}{\epsilon}\Gamma$$

- ► We re-arrange first moment to find A
  - ightharpoonup Can rationalize any given E(a)
- ightharpoonup Say, we want E(a)=1
  - $\blacktriangleright$  We set A=0.711 if  $\varepsilon=2$
  - $\blacktriangleright$  We set A=0.885 if  $\varepsilon=3$
- ► Principle is the same with Fréchet
  - ► Just with a different formula

$$A = \frac{E(a)}{\Gamma(1-\frac{1}{a})}$$



# Location choice probabilities

## Discrete choice

Introduction

- ► We want to move **beyond perfect mobility** 
  - infinite supply of homogeneous workers
- ► Preference heterogeneity generates well-behaved location choice probabilities
  - ► Some people will always choose a location, even if real wage and amenity are low
    - ▶ But it could be a very small fraction of the population (with extreme preferences)
  - ightharpoonup A better location attracts a greater share of the worker endowment,  $\bar{L}$ 
    - ▶ Better in terms of higher wages, lower rents, lower prices, higher amenities
- ► Application of McFadden's (1974) seminal work
  - ► Nobel Prize winner in 2000

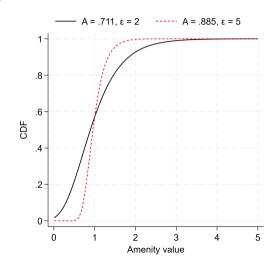
Let's develop the intuition in a simple binary choice setting: City vs. RoW

## Cumulative density function (Gumbel)

$$G(a) = \exp(-\exp(-(a-A)\varepsilon))$$

- ► CDF tells us the probability that *a* is equal or smaller than a certain value
  - ► Let a be idiosyncratic urban utility
  - About 60% chance that  $a \le 1$
- lacktriangle Outside option offering utility  $ar{U}=1$ 
  - Probability of **not choosing city**:  $Pr(a > \bar{U}) = G(\bar{U}) \approx 60\%$
  - Probability of **choosing city**:  $Pr(a > \bar{U}) = 1 G(\bar{U}) \approx 40\%$

CDF gives us choice probabilities!

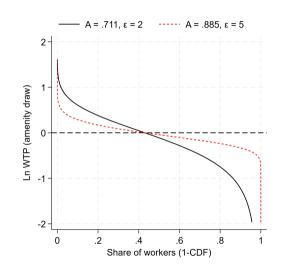


## Demand for residence

Introduction

- ► CDF implies downward-sloping demand for residence
  - Number of workers in the city is  $L = \mu \bar{L}$ , where  $\mu = 1 G(\bar{U})$

Valuation of the marginal resident falls the more workers enter the city!

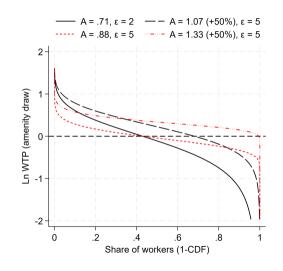


## Role of $\varepsilon$

Introduction

- ► If we **increase** *A*, the residence demand curve shifts outwards
  - ► Average utility increases
  - City attracts workers who enjoy urban life less relative to others
- ▶ 50% increase in A leads to an increase in urbanization rate from  $\approx$  to 40%
  - ▶ to  $\approx 70\%$  if  $\epsilon = 2$
  - ightharpoonup close to 100% if  $\epsilon=5$

 $\epsilon$  governs population response in counterfactuals!



## Multi-location setting I

Extreme value distributions

- ► The logic extends to the setting with many locations (maths more involved)
  - ► You will need to go through the intermediate steps at your own pace (tutorial)
- Let's now assume workers indexed by o
  - ► can choose among many locations i
  - receive idiosyncratic utility according to Fréchet CDF  $F(a_0) = \exp(-a_0^{-\epsilon})$
  - ▶ obtain indirect utility  $U = A_i a_{io} \frac{w_i}{p^{1-\alpha}}$
- ightharpoonup The share of workers getting a utility of up to u at i is

- ▶ Using the CDF and the indirect utility function, we get

## Multi-location setting II

- ightharpoonup Want to know the **probability that workers choose** i,  $\pi_i = Pr(u_i \geq \max\{u_r\} \forall i)$ 
  - Intuitively, this is the probability that workers achieve a utility u at i,  $g_i(u)$ , multiplied by the probability that the maximum utility in any other location is **less than or equal** to u,  $\prod_{r\neq i} G_r(u)$ , evaluated over all u:
  - $\blacktriangleright \pi_i = \int_0^\infty g_i(u) \left(\prod_{r\neq i} G_r(u)\right) du$
- ightharpoonup Several steps later (using G(u) from which we also derive g(u)...
  - ▶ Location choice probability  $\mu_i = \frac{L_i}{L} = \frac{\left(\frac{A_i w_i}{p_i^{1-\alpha}}\right)^{\epsilon}}{\left(\sum_s \left(\frac{A_s w_s}{p_i^{1-\alpha}}\right)^{\epsilon}\right)}$

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Eureka!  $\varepsilon$  is the labour supply elasticity to the city! (Moretti, 2010)

# Role in general equilibrium

Introduction

## Implications for quality of life

- ► Recall quality of life in Rosen-Roback framework (Glaeser & Gottlieb, 2009)
  - $lackbox{lack} A_i = c rac{p_i^lpha}{w_i} ext{ (in GG2009 notations } \log(B_c) = \Omega_3 + \sigma \log(P_c) \log(W_c))$
- ightharpoonup Solving the **location choice probability** equation for  $A_i$ , we get

$$\blacktriangleright \ \ \textit{A}_{\textit{i}} = \underbrace{c \frac{p_{\textit{i}}^{\alpha}}{w_{\textit{i}}}}_{\mathsf{RR-OoL}} \textit{L}^{\frac{1}{\varepsilon}} \ \mathsf{Notice} \ \mathsf{that} \ \mathsf{if} \ \varepsilon \to \infty \Rightarrow \textit{L}^{\frac{1}{\varepsilon}} \to 1$$

- ▶ QSM nests Rosen-Roback as special case with  $\varepsilon \to \infty$ 
  - lacktriangle By implication: If  $\varepsilon < \infty$  and QSM is right, Rosen-Roback must give wrong QoL

Does RR over- or underestimate the urban QoL premium?

## Ahlfeldt, Bald, Roth, Seidel toolkit

- ► Toy version of the full quantitative spatial model
  - ► Abstracts from trade costs and non-tradable sector
  - But offers analytical solutions!
- ► Get toolkit

- - ► Contains the description of the toy model and intuition, worth reading
- ► Install Stata ado file: ssc install ABRS
  - Creates the four-quadrant diagram
  - ► For the syntax, type: help ABRS
- - ► Only bar chart showing effects on equilibrium outcomes

## Preferences

Introduction

 $\blacktriangleright$  Worker living in location i derives utility from the consumption of goods ( $Q_{i\omega}$ ) and floor space  $(h_{i\omega})$  according to

$$U_{i\omega} = \left(\frac{Q_{i\omega}}{\alpha}\right)^{\alpha} \left(\frac{h_{i\omega}}{1-\alpha}\right)^{1-\alpha} \exp[a_{i\omega}],\tag{1}$$

- $\triangleright$  where  $Q_{i\omega}$  represents a final good (Armington, 1969)
  - ► locally assembled from tradable intermediate goods  $a_{ii\omega}$
  - according to the CES-aggregator
  - at zero cost under perfect competition
  - ► shipped from origin *i* to destination *i*,

$$Q_{i\omega} = \left[\sum_{j \in J} (q_{ji\omega})^{\frac{\sigma-1}{\sigma}}\right]^{\frac{\sigma}{\sigma-1}} \tag{2}$$

## Mobility frictions

Introduction

▶ Idiosyncratic preference for location  $\exp[a_{i\omega}^{\theta}]$  (Gumbel)

$$F_i^{\theta}(a) = \exp\left(-(A_i)^{\gamma^{\theta}} \exp\left\{-\left[\gamma a + \Gamma\right]\right\}\right) \text{ with } \gamma > 0,$$
 (3)

- $\triangleright$   $A_i$  (average preference) serves as an exogenous measure of local quality of life
  - ▶ Notice that **Gumbel CDF** has been engineered to give  $A_i = \mathbb{E}(a|i)$
- $ightharpoonup \gamma$  governs the dispersion of individual amenity shocks
  - ► Introduces imperfect spatial arbitrage ⇒
  - ► inverse measure of mobility frictions

Literature

## Technology: Housing

Introduction

 Supplied under perfect competition combining a share of the globally available capital stock,  $K_i$  (available at unit prices), with **fixed land supply**.  $\bar{T}_i$ :

$$H_i^{\mathcal{S}} = \eta_i \left(\frac{\overline{T}_i}{\delta}\right)^{\delta} \left(\frac{K_i}{1-\delta}\right)^{1-\delta}.$$
 (4)

- ► Total factor productivity n<sub>i</sub>
  - captures the role of regulatory (e.g. height regulations) and physical (e.g. a rugged surface) constraints (Saiz 2010)
- ▶  $\delta$  governs the housing supply elasticity  $\frac{\partial \ln H_i^S}{\partial \ln p_i^H} = \frac{1-\delta}{\delta}$  (inverse relationship)
  - ► Use first-order conditions in profit function

## Technology: Non-housing goods

- ► Each location produces a unique variety of a tradable intermediate good
  - ightharpoonup using labour  $L_i$  as the only production input
  - under perfect competition according to
- $ightharpoonup q_i = \varphi_i L_i$

- Endogenous labour productivity  $\varphi_i = \bar{\varphi}_i L_i^{\zeta}$ 
  - $\triangleright$  increases in local employment according to the agglomeration elasticity  $\zeta$ .
- ▶ We get price  $p_{ji} = w_j/\varphi_j$  and trade share  $\chi_{ji} = \frac{(w_j/\varphi_j)^{1-\sigma}}{\sum_j (w_j/\varphi_j)^{1-\sigma}}$ 
  - ► Trade in intermediate goods is free
  - ► Perfect competition equates prices to marginal costs

## Location choice

Introduction

▶ Probability  $\lambda_i^{\theta}$  that a worker lives in location *i*:

$$\lambda_{i} = \frac{\left(A_{i} w_{i} / \mathcal{P}_{i}\right)^{\gamma}}{\sum_{j \in J} \left(A_{j} w_{j}^{\theta} / \mathcal{P}_{j}\right)^{\gamma}},\tag{5}$$

- where  $\mathcal{P}_i \equiv (P_i)^{\alpha} (p_i^H)^{1-\alpha}$  is the aggregate consumer price index.
- ► Mobility of workers equalizes expected utility in equilibrium

This is what we have derived before...

## General equilibrium I

Introduction

- Goods market clearing (GMC):  $w_i L_i = \sum_{j \in J} \frac{(w_i/\varphi_i)^{1-\sigma}}{\sum_i (w_i/\varphi_i)^{1-\sigma}} \left(\alpha w_j L_j + r_j \bar{T}_j\right)$ 
  - ▶ Wage bill at i must equate to the revenues from all locations i
- ▶ Labor market clearing (LMC):  $L_i = \lambda_i \bar{L}$ 
  - Labour input  $L_i$  must equate labour supply
    - ightharpoonup product of the share of workers living in i,  $\lambda_i$ , and the national labour endowment  $\bar{L}$ .
- Floor-space market clearing (FMC):  $p_i^H = \left(\frac{\tilde{\alpha}\delta w_i L_i}{\frac{1}{\sigma}\delta \tilde{\tau}}\right)^{\delta}$ ,
  - where  $\tilde{\alpha} \equiv (1 \alpha) + \alpha(1 \beta)(1 \delta)$  is a constant.
  - ightharpoonup Set simply set  $H_i^S = H_i^D$ 
    - $ightharpoonup H^D$  is Marshallian housing demand
    - $H_i^S = n^{\frac{1}{\delta}} \bar{T}_i(p_i^H)^{\frac{1-\delta}{\delta}}/\delta$  from first-order conditions in profit function

## General equilibrium II

- ► For the toolkit, we consider relative differences in a two-region case
  - $\hat{\mathbf{x}} = \frac{\mathbf{x}_i}{\mathbf{x}_i}$
- System of equations simplifies to
  - $\blacktriangleright$  GMC:  $\hat{L} = \hat{\varpi}^{\frac{\sigma-1}{\Lambda}} \hat{w}^{-\frac{\sigma}{\Lambda}}$
  - ► LMC:  $\hat{L} = (\hat{A}\hat{w}(\hat{p}^H)^{\alpha-1})^{\gamma}$
  - FMC:  $\hat{p}^H = \hat{k} (\hat{w} \hat{L})^{\delta}$ 
    - lacktriangle where  $\Lambda\equiv 1-\zeta(\sigma-1)$  and  $k_i\equiv \frac{1}{\eta_i}\left(\frac{\tilde{lpha}\delta}{\tilde{T}_i}\right)^{\delta}$  collect various primitives
  - 3 log-linear equations with 3 unkonwns  $\{\hat{L}, \hat{w}, \hat{p}^H\} \Rightarrow$  closed-form solution  $\checkmark$

# Mapping

Introduction

▶ We have direct mapping from primitives to endogenous objects

$$\hat{L} = \hat{k}^{-\frac{(1-\alpha)\sigma}{\Delta}} \hat{\varphi}^{\frac{(\sigma-1)(1-(1-\alpha)\delta)}{\Delta}} \hat{A}^{\frac{\sigma}{\Delta}}$$

$$\hat{w} = \hat{k}^{\frac{(1-\alpha)\Lambda}{\Delta}} \hat{\varphi}^{\frac{(\sigma-1)(1/\gamma+(1-\alpha)\delta)}{\Delta}} \hat{A}^{-\frac{\Lambda}{\Delta}}$$

$$\hat{p}^{H} = \hat{k}^{\frac{\Lambda+\sigma/\gamma}{\Delta}} \hat{\varphi}^{\frac{(\sigma-1)(1+1/\gamma)\delta}{\Delta}} \hat{A}^{\frac{\delta(\sigma-\Lambda)}{\Delta}}$$

- where  $\Delta \equiv \Lambda[1 (1 \alpha)\delta] + \sigma[1/\gamma + (1 \alpha)\delta]$
- ► This mapping is all we need to do counterfactuals Open ABRS-toolkit (web-version)
  - ightharpoonup change fundamentals  $\{A, \varphi, \eta\}$

## GE in four quadrants

Introduction

For didactic purposes it is useful to combine GMC, LMC, FMC to give

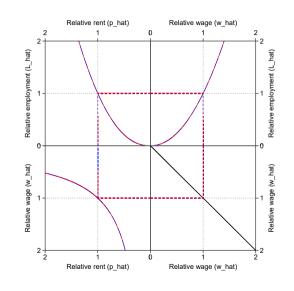
$$\hat{L} = \hat{k}^{-rac{1-lpha}{rac{1}{\gamma}+(1-lpha)\delta}} \cdot \hat{A}_{1}^{rac{1}{\gamma}+\delta(1-lpha)} \cdot \hat{w}^{rac{1-\delta(1-lpha)}{rac{1}{\gamma}+\delta(1-lpha)}} 
onumber \ \hat{p}^{H} = \hat{k}^{rac{1}{1-(1-lpha)\delta}} \cdot \hat{A}_{1}^{-rac{\delta}{1-\delta(1-lpha)}} \cdot \hat{L}^{rac{\delta\left(rac{1}{\gamma}+1
ight)}{1-(1-lpha)\delta}} 
onumber \ \hat{w} = \left(rac{\hat{p}^{H}}{\hat{k}}
ight)^{rac{\zeta(\sigma-1)-1}{\delta(\sigma-1)(\zeta+1)}} \cdot \hat{arphi}^{rac{1}{\zeta+1}}$$

- Notice that we map  $\hat{w}$  into  $\hat{L}$ .  $\hat{L}$  into  $\hat{p}^H$ , and then  $\hat{p}^H$  back into  $\hat{w}$
- A  $\hat{w}$  that gets us back to the same  $\hat{w}$  satisfies all equilibrium conditions

## ABRS "A\_hat\_1=0"

▶ Quadrant 1

- ► Higher worker wage ⇒ greater employment due to upward-sloping labour supply
- ▶ Quadrant 2
  - Greater employment ⇒ higher rent due to greater housing demand & imperfectly elastic supply
- ► Quadrant 3
  - ► Higher rent implies larger employment ⇒ Firm wage must be lower given downward-sloping labour demand
- Quadrant 4
  - ► Projects firm wage onto worker wage



## Questions I

Introduction

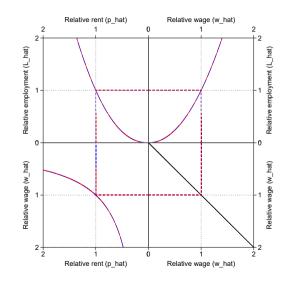
Q1: What happens if we set  $\gamma = 1$  (instead of 3)

ABRS "A\_hat\_1=0" "gamma=1"

Q2: What happens if we set  $\ln \hat{A} = 0.2$ 

ABRS

Q3: What happens if we set  $\ln \hat{A} = 0.2$  and increase  $\gamma$ ? ABRS-toolkit (web)



## Questions II

Introduction

Q4: What happens if we set  $\ln \hat{A} = 0.2$  alone vs.  $\ln \hat{A} = 0.2$  and  $\ln \hat{\eta} = 0.8$  ?

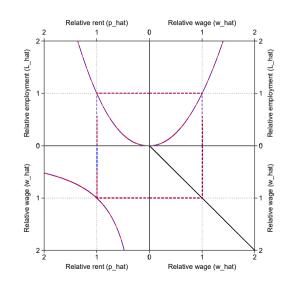
ABRS "A\_hat\_2=0.2" "eta\_hat\_2=0.8"

Q5: What happens if we set  $\ln \hat{A} = 0.2$  alone vs.  $\ln \hat{A} = 0.2$  and  $\ln \hat{\varphi} = 0.8$  ?

ABRS "A\_hat\_2=0.2" "phibar\_hat\_2=0.8" "max\_L\_hat=4"

Q6: What happens if we keep  $\ln \hat{A} = 0$  and set  $\ln \hat{\eta} = 0.8$  and  $\ln \hat{\varphi} = 0.8$  ?

ABRS "A\_hat\_1=0" "A\_hat\_2=0" "eta\_hat\_2=0.8" "phibar\_hat\_2=0.8" "max I, hat=4"



Conclusion

## Summary

Introduction

- ► With extreme-value distributed location preferences
  - ► Allows deriving discrete choice probabilities
  - ▶ Upward-sloping labor demand and downward-sloping housing demand
    - ► More preference heterogeneity, less mobility and steeper curves
- ► Important effects on general equilibrium See further comments on Q1-Q6 in Appendix
  - **Real wages no longer reflect QoL differences!** (unless  $\gamma$  is large)
    - ► Housing productivity increases real wages
    - ► Labour productivity increases real wages
  - ► High real wages wrongly attributed to low QoL in RR!

Next week: Idiosyncratic preferences

#### Literature I

Introduction

#### Core readings

- ► Ahlfeldt, G., Bald, F., Roth, D., Seidel, T. (2024): Measuring quality of life under spatial frictions: Toy version of the model. https://github.com/Ahlfeldt/ABRS-toolkit
- ▶ Ahlfedt, G., Redding, S., Sturm, D., Wolf, N. (2015): "Supplement to: The economics of Density: Evidence From the Berlin Wall" (Econometrica, 83(6)), Sections S.2.1, S.2.2, S.2.3.
- ▶ Moretti, E. (2010): Local labour markets. Handbook of Labor Economics, Volume 4b.

#### Other readings

- Armington, P. (1969). A Theory of Demand for Products Distinguished by Place of Production. IMF Staff Papers, 16(1), 159-178.
- McFadden, D. (1974): Conditional Logit Analysis of Qualitative Choice Behavior. In P. Zarembka (Ed.), Frontiers in Econometrics (pp. 105-142). Academic Press
- ► Saiz, A. (2010): The Geographic Determinants of Housing Supply. The Quarterly Journal of Economics, 125(3), 1253–1296

## Comments on Q1-Q6

► Q1

- ► Curve in Quadrant 1 flatter since labor supply is less elastic
  - ▶ Notice that axes are reversed relative to the standard demand-supply diagram
  - ► Flatter curve implies **less** elastic labour supply
- **▶** Q2
  - Curve in Quadrant 1 is steeper since greater labor supply for the same wage
    - Consequentially, wage lower
  - ightharpoonup Curve in Quadrant 2 steeper since for the same employment, wage is lower  $\Rightarrow$ housing demand lower
    - ► Rent higher since the positive employment effect dominates the negative wage effect on housing demand
  - ► Real wage lower by 0.09 log units, less than half of the QoL difference (0.2)
    - ► Rosen-Roback framework delivers wrong measurement of QoL

## Comments on Q1-Q6

**▶** Q3

- $\blacktriangleright$  The larger  $\gamma$ , the closer the inverse real wage difference gets to the QoL difference
  - ▶ At  $\gamma=10$ , real wage is 0.15 lower; at  $\gamma=10$ , real wage is 0.175 lower; at  $\gamma=65$ , real wage is 0.19 lower; at  $\gamma=500$ , real wage is 0.199 lower
- ► Q4
  - Curve in the second Quadrant is steeper since lower rent due to greater housing supply
  - Curve in the first Quadrant is steeper since lower rent implies that workers accept lower wage
    - ► For a given employment level
  - ► Curve in the third Quadrant shifts inwards since at the same rent there are more workers ⇒ lower wage clears the market

## Comments on Q1-Q6

► Q5

- Curve in Quadrant 5 shifts outwards since
  - ► labor demand increases as workers are more productive
  - ▶ at same rent (employment), firms pay higher wages (perfect competition)
- ▶ RR qualitatively wrong since real wage difference positive
  - ► (implying negative QoL differential)
- ► Q6
  - ightharpoonup Effects in first and second Quadrants like in Q4 ( $\hat{\eta}$  effect)
  - ▶ Shift effects of  $\hat{\eta}$  and  $\hat{\varphi}$  cancel out each other in Quadrant 3
    - Curve does not shift
  - ► RR qualitatively wrong since real wage difference positive
    - ► (implying negative QoL differential)