

Topic 8

ARSW (2015): Counterfactuals

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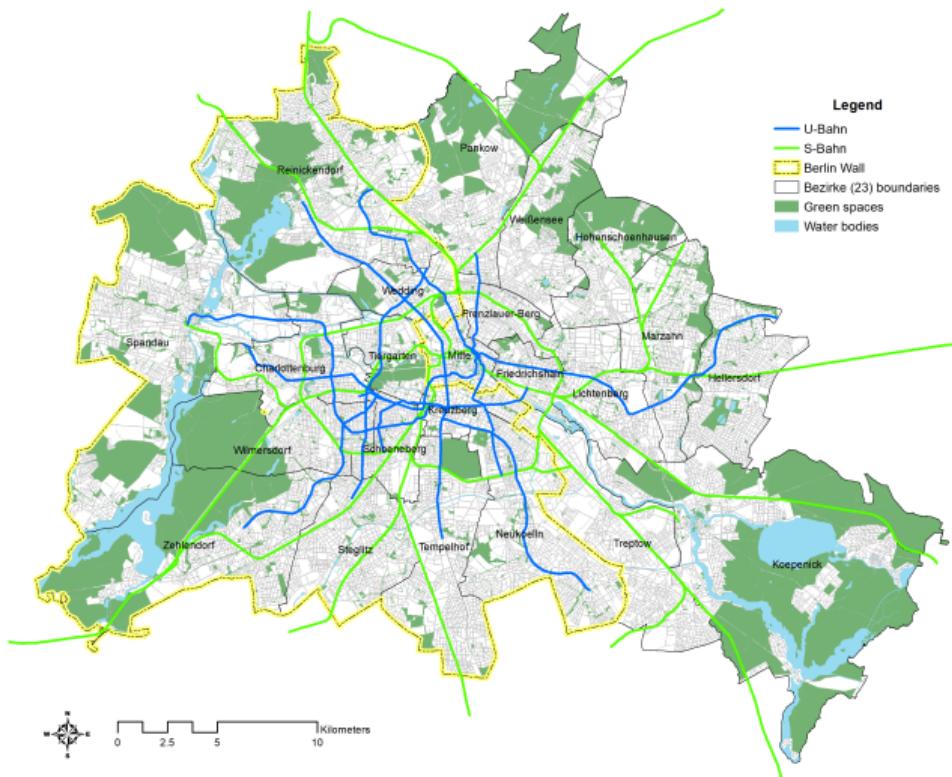
Introduction

Counterfactuals

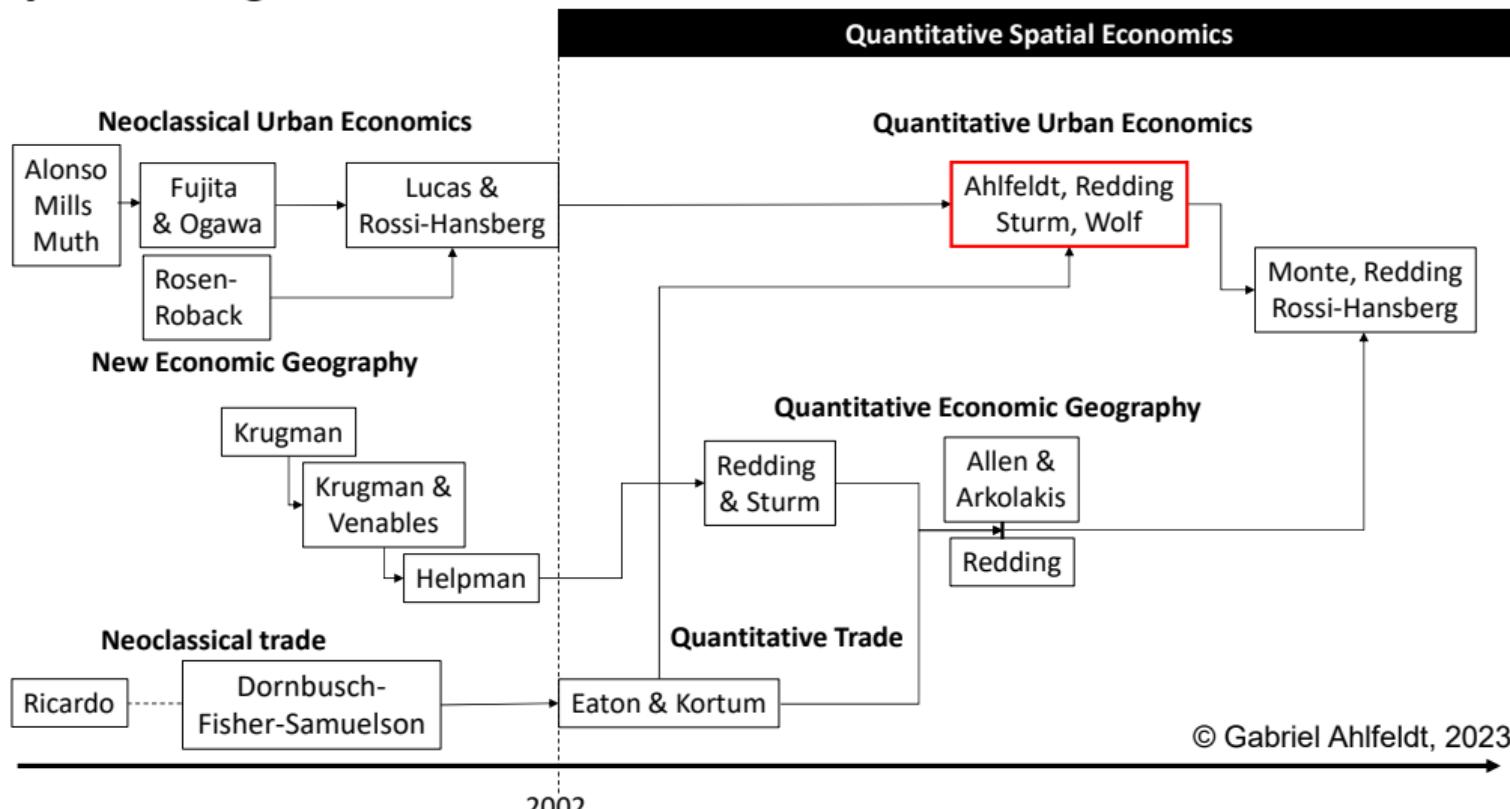
- ▶ **Reduced-form** models provide transparent evidence, but there are **limitations**
 - ▶ If a spatial policy attracts workers, these must come from somewhere
 - ▶ Hard to establish where they come from and what happens at those locations
 - ▶ Are there aggregate welfare effects?
- ▶ Key **strength of QSMs** is the ability to perform counterfactuals
 - ▶ in **general equilibrium**
 - ▶ accounting for **relocation** effects
 - ▶ Identify spatial winners and losers
 - ▶ Establishing **welfare** effects

Counterfactual

What will happen to the spatial structure if we ban cars?



History of thought



Roadmap

- ▶ **Topic 6**
 - ▶ Building blocks of the model
 - ▶ Reduced-form evidence
 - ▶ **Topic 7**
 - ▶ Estimation
 - ▶ Inversion
 - ▶ **Topic 8 (today)**
 - ▶ Counterfactuals with exogenous fundamentals
 - ▶ Counterfactuals with agglomeration forces

Variants of the model

- ▶ **Exogenous fundamentals**
 - ▶ Unique equilibrium
- ▶ **Endogenous agglomeration forces**
 - ▶ $\{A_i, B_i\}$ depend on fundamentals and surrounding (endogenous) density
 - ▶ Multiple equilibria are theoretically possible
 - ▶ More likely if agglomeration forces are stronger
- ▶ **Closed city**
 - ▶ Total employment H is exogenous, utility \bar{U} is endogenous
- ▶ **Open city**
 - ▶ Total employment H is endogenous, utility \bar{U} is exogenous
- ▶ This lecture is closely connected to the ARSW **toolkit**, use it! [ARSW2015-toolkit](#)

Exogenous fundamentals

General equilibrium

- ▶ Given
 - ▶ Given the model's exogenous parameters $\{\alpha, \beta, \mu, \varepsilon, \kappa\}$
 - ▶ the exogenous reservation utility level \bar{U} (or exogenous total employment H)
 - ▶ exogenous location characteristics $\{T_i, E_i, A_i, B_i, \varphi_i, K_i, \xi_i, \tau_{ij}\}$
 - ▶ the **unique general equilibrium** of the model is referenced by
 - ▶ the endogenous objects $\{\pi_{Mi}, \pi_{Ri}, Q_i, q_i, w_i, \theta_i, H\}$ (or H instead of \bar{U})
 - ▶ If we have them, we can compute all other objects

Need seven equations to bin down seven endogenous objects

Referencing the equilibrium

- The general equilibrium is referenced by the following seven equations

1. Population mobility (9): $\mathbb{E}[u] = \gamma \left[\sum_{r=1}^S \sum_{s=1}^S T_{r,s} E_s (d_{rs} Q_r^{-\beta})^{-\varepsilon} (B_r, w_s)^\varepsilon \right]^{1/\varepsilon} = \bar{U}$

2. Residential choice probability (5): $\pi_{R_i} = \sum_{j=1}^S \pi_{ij} = \frac{\sum_{j=1}^S \Phi_{ij}}{\Phi}$

3. Workplace choice probability (5): $\pi_{M_j} = \sum_{i=1}^S \pi_{ij} = \frac{\sum_{i=1}^S \Phi_{ij}}{\Phi}$

4. Commercial land market clearing (18): $\left(\frac{(1-\alpha)A_j}{q_j}\right)^{1/\alpha} H_{M_j} = \theta_j L_j$

5. Residential land market clearing (19): $\left(\frac{(1-\alpha)A_j}{q_i}\right)^{1/\alpha} H_{Rj} = \theta_j L_j$

6. Profit maximization and zero profits (12): $q_j = (1 - \alpha) \left(\frac{\alpha}{w_j} \right)^{\alpha/(1-\alpha)} A_j^{1/(1-\alpha)}$.

7. No-Arbitrage between alternative uses of land (13): $\theta_i = \begin{cases} 1 & \text{if } q_i > \xi_i Q_i, \\ [0, 1] & \text{if } q_i = \xi_i Q_i, \\ 0 & \text{if } q_i < \xi_i Q_i. \end{cases}$

Target variables

- ▶ System of equations that reference equilibrium solve for:
 - ▶ $\{\pi_{Mi}, \pi_{Ri}, Q_i, q_i, w_i, \theta_i, H\}$ (or H instead of \bar{U})
 - ▶ Need to solve the following target variables numerically
 - ▶ $\{q_i, Q_i, w_i, \theta_i\}$
 - ▶ Use **recursive structure** to solve for the remaining non-target objects
 - ▶ Get H (or \bar{U}) from 1.
 - ▶ Notice that $H = \Phi$ corresponds to the term in brackets, see p. 18 in the supplement
 - ▶ Get π_{Ri} from 2.
 - ▶ Notice that $\Phi_{ij} = T_i E_j (d_{ij} Q_i^{1-\beta})^{-\varepsilon} (B_i w_j)^\varepsilon$, hence, we have all we need
 - ▶ Get π_{Mi} from 3.
 - ▶ Again, we have all we need since $\Phi_{ij} = T_i E_j (d_{ij} Q_i^{1-\beta})^{-\varepsilon} (B_i w_j)^\varepsilon$

Fixed-point solver (closed-city case)

- ▶ Treat the solution for $\{\pi_{Mi}, \pi_{Ri}, Q_i, q_i, \tilde{w}_i, \theta_i, \bar{U}\}$ as a **fixed-point problem**
 - ▶ Notice that we solve for adjusted (for workplace amenities) wages \tilde{w}_i
 - ▶ Basic idea is as follows:
 - ▶ Start with **guessed values of the target objects** $\{Q_i^0, q_i^0, \tilde{w}_i^0, \theta_i^0\}$
 - ▶ **Solve for non-target objects** that reference the equilibrium $\{\pi_{Mi}, \pi_{Hi}, \bar{U}\}$
 - ▶ Use non-target objects to **predict target objects** $\{Q_i^1, q_i^1, \tilde{w}_i^1, \theta_i^1\}$
 - ▶ **Update guesses** to weighted combinations of old guesses '⁰' and predicted values '¹'
 - ▶ Iterate until guesses no longer change

Cookbook for fixed-point solver

Algorithm 1: Solving for the equilibrium for given primitives: smodexog.m

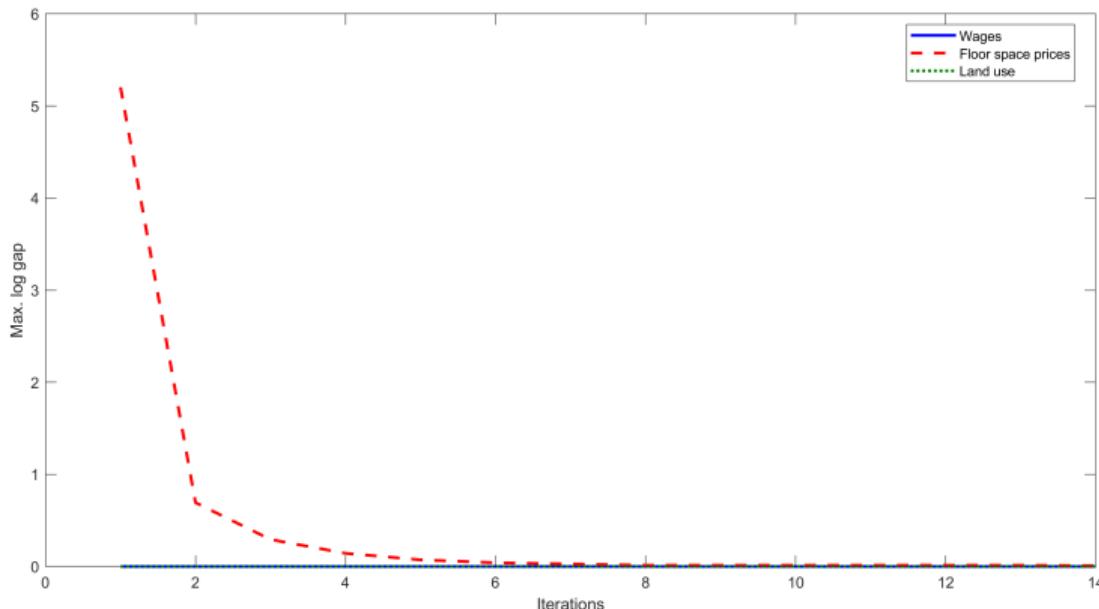
Data: Given values of structural parameters $\{\alpha, \beta, \kappa, \varepsilon\}$, bilateral travel times τ_{ij} , inverted adjusted productivity, adjusted amenity, and floor space stock $\{\tilde{A}_j, \tilde{B}_i, L_i\}$; guesses of the target variables adjusted wages, commercial and residential floor space prices, commercial floor space shares $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$; total employment H .

- 1 while guesses of target variables $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ change do
 - 2 Compute location choice probabilities π_{ij} using guesses of $\{\tilde{w}_i^0, q_i^0, Q_i^0\}$ and $\{\tilde{A}_j, \tilde{B}_i\}$ in Eq. (4)
 - 3 Compute residence and workplace employment $\{\hat{H}_{Mi}, \hat{H}_{Ri}\}$ using π_{ij} , H and residence and Eq. (5).
 - 4 Compute output \hat{Y}_i using the production function in Eq. (10), workplace employment \hat{H}_{Mi} , inverted total floor space L_i , and guesses of θ_i^0 .
 - 5 Compute predicted adjusted wage $\tilde{w}_i^1 = \alpha \frac{\hat{Y}_i}{\hat{H}_{Mi}}$ using the input demand function derived from F.O.C. of Eq. (10) and $\{\hat{Y}_i, \hat{H}_{Mi}\}$
 - 6 Compute total income $\mathbb{E}(\hat{w}_i \times \hat{H}_{Mi})$ using Eq. (S.20), predicted \tilde{w}_i^1 , \hat{H}_{Mi} , and conditional commuting probabilities $\pi_{ij|i} = \pi_{ij} / \sum_j \pi_{ij}$
 - 7 Compute predicted commercial and residential floor space prices $\{q_i^1, Q_i^1\}$ using \hat{Y}_i , guesses of θ_i^0 , and Marshallian demand and input demand based on Eqs. (1) and (10)
 - 8 Compute predicted values of θ_i^0 using commercial floor space input $L_{Mi} = (1 - \alpha)\hat{Y}_i/q_i^1$ recovered from input demand function based on Eq. (10) and L_i in Eq. (S.53)
 - 9 Update guesses of target variables $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ to weighted average of old guesses $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ and predicted values $\{w_i^1, q_i^1, Q_i^1, \theta_i^1\}$

Result: Predicted values of adjusted wage, total income, commercial floor space shares, output, commercial and residential floor space prices, workplace employment and residence, total employment, unconditional commuting probabilities
 $\{\hat{w}_j, \mathbb{E}(\hat{w}_j \times \hat{H}_{Mi}), \theta_j, Y_i, q_i, Q_i, H_{Mi}, H_{Ri}, \pi_{ij}\}$

Matlab code

Covergence path



Track the value of the objective function and check for bouncing...

Matlab code

Counterfactuals

- ▶ QSM recovers observed values of endogenous variables by construction
 - ▶ **Fundamentals** have been inverted to **rationalize data as an equilibrium of the model**
- ▶ Solve for **counterfactual equilibria**
 - ▶ **Update** any of the model's **primitives**
 - ▶ Run the equilibrium solver
- ▶ Compare counterfactual equilibrium values to initial equilibrium
 - ▶ Initial equilibrium corresponds data where observed
 - ▶ Usually use relative differences, e.g. percentage changes or log differences

Ban cars by changing τ_{ij} to public transit travel times

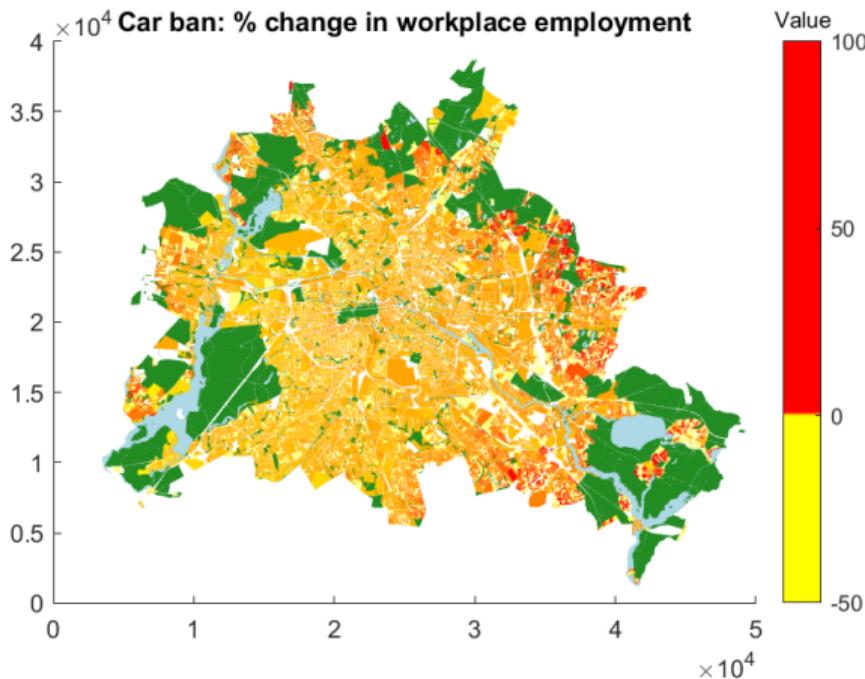
Car ban: Impact on residence employment

- ▶ More costly to reach jobs from suburbs
- ▶ Workers relocate to central areas



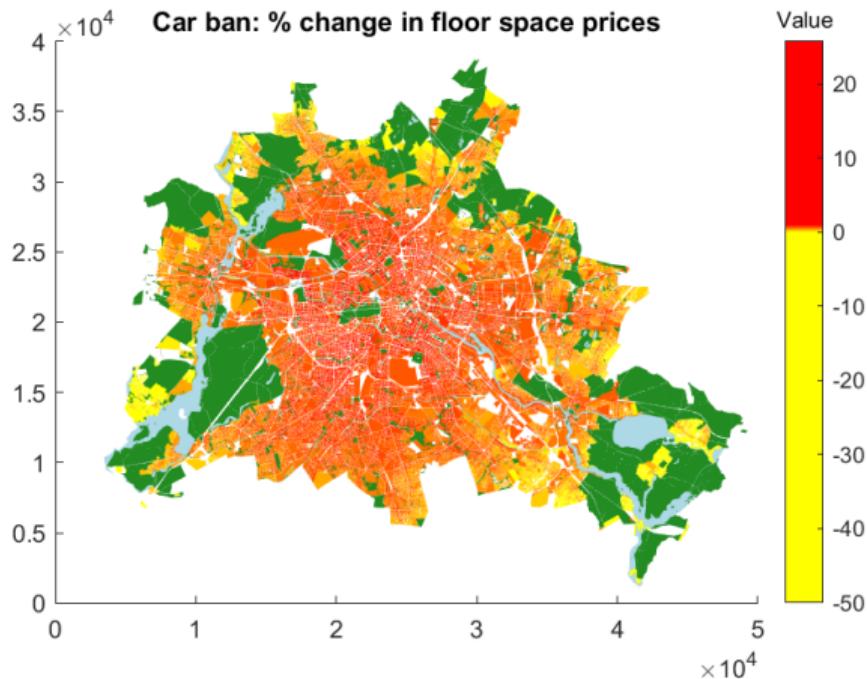
Car ban: Impact on workplace employment

- ▶ **Commuting cost higher ⇒ Mixed use more widespread**
 - ▶ Residents leaving suburbs free up space for firms
 - ▶ Workplace employment increases in suburbs



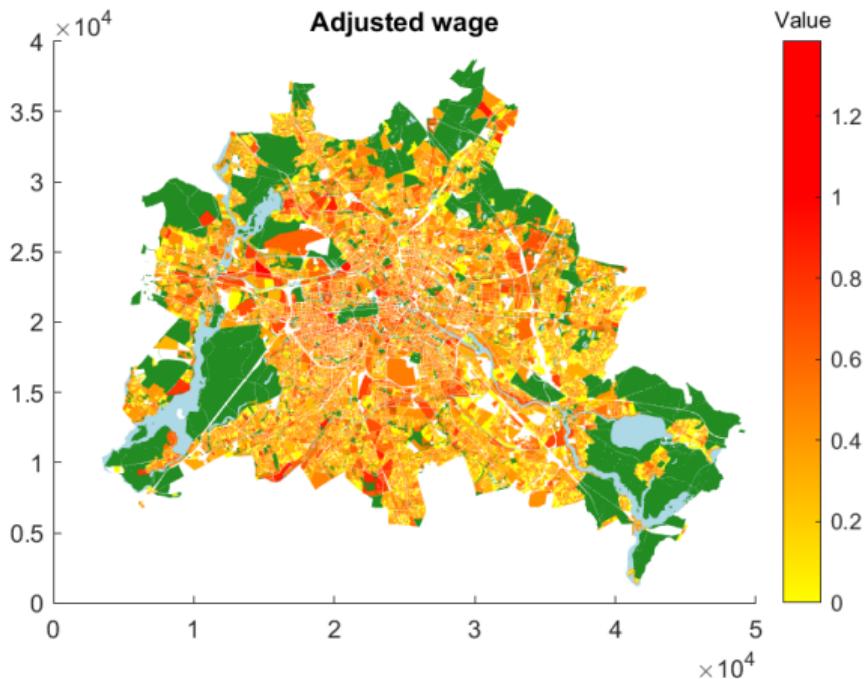
Car ban: Impact on floor space prices

- ▶ **Accessibility comes at a premium ⇒ cost savings increasingly capitalize in floor space prices**
 - ▶ Floor space prices increase in places well-connected by public transit
 - ▶ Floor space prices in remote areas fall due to worse accessibility



Car ban: Impact on wages

- ▶ Firms need to compensate for higher commuting costs ⇒ Wages generally increase
- ▶ Commuting cost increase dominates
- ▶ Utility falls by 5.8%



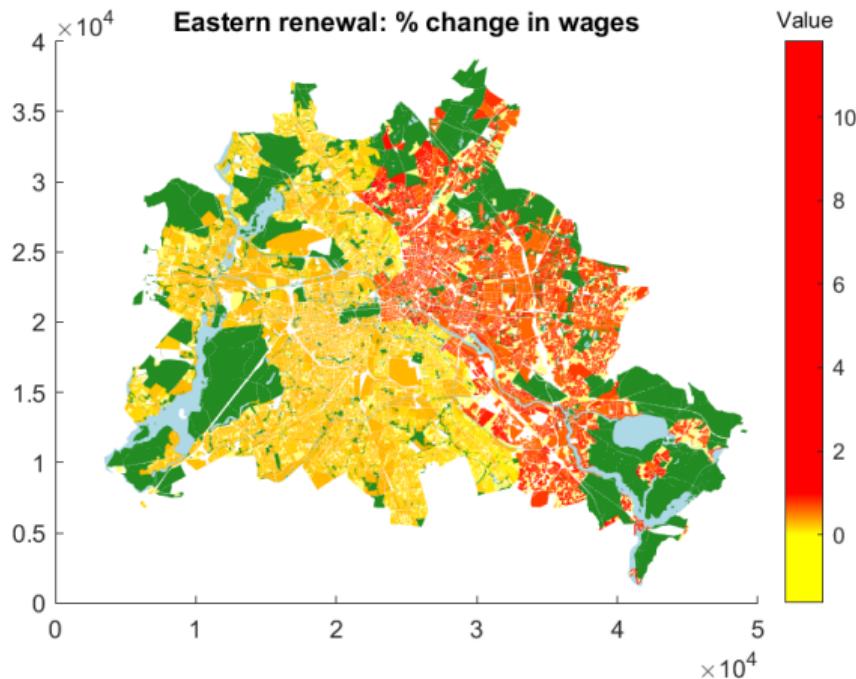
Counterfactuals (again)

- ▶ Transport policies are just one of many applications for counterfactuals
 - ▶ Albeit a particularly popular one (see list of studies in Topic 6)
- ▶ But we can think of many others
 - ▶ New parks, better urban design affect **amenity** \Rightarrow change B_i
 - ▶ Change effective land supply, more **floor space** \Rightarrow change φ_i
 - ▶ Improvements that affect **productivity** \Rightarrow change A_i

**What happens if productivity in former East Berlin increases by 10%
(e.g. due to an upgrade of capital stock)?**

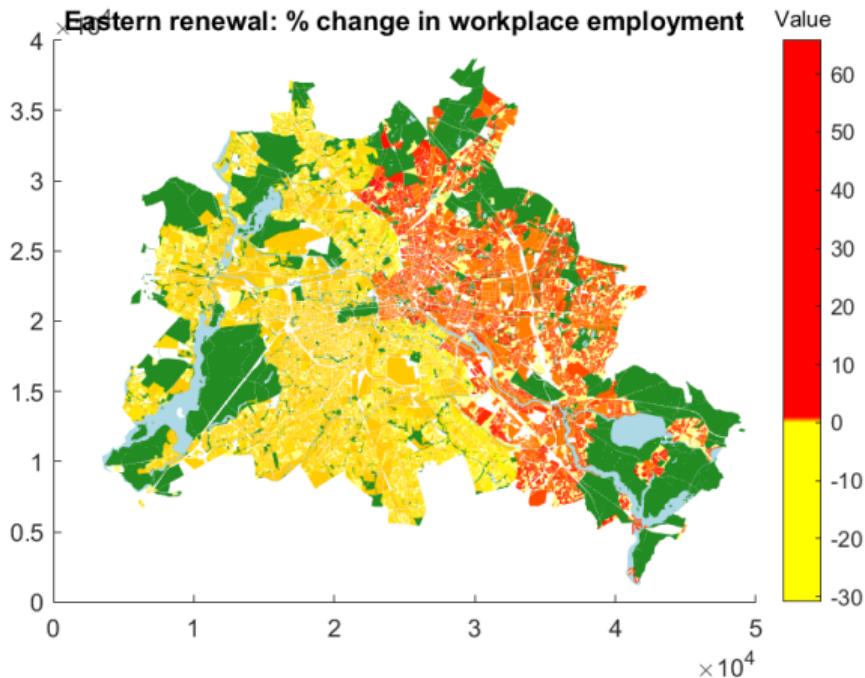
East Berlin productivity increase: Impact on wages

- ▶ **Greater productivity**
 - ⇒ greater labour demand
 - ⇒ higher wages



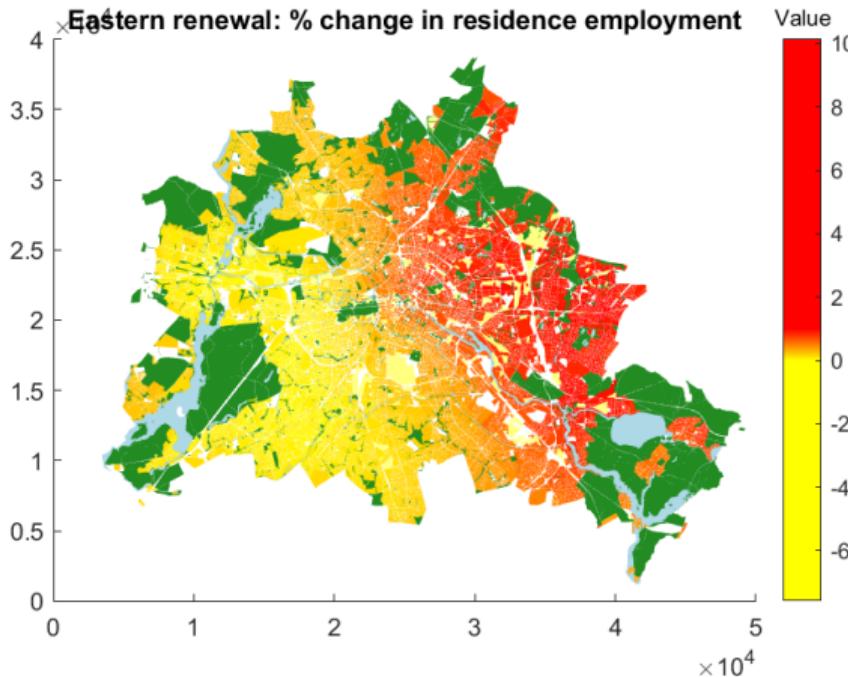
East Berlin productivity increase: Impact on workplace employment

- ▶ **Greater productivity**
 - ⇒ greater labour demand
 - ⇒ more workplace employment



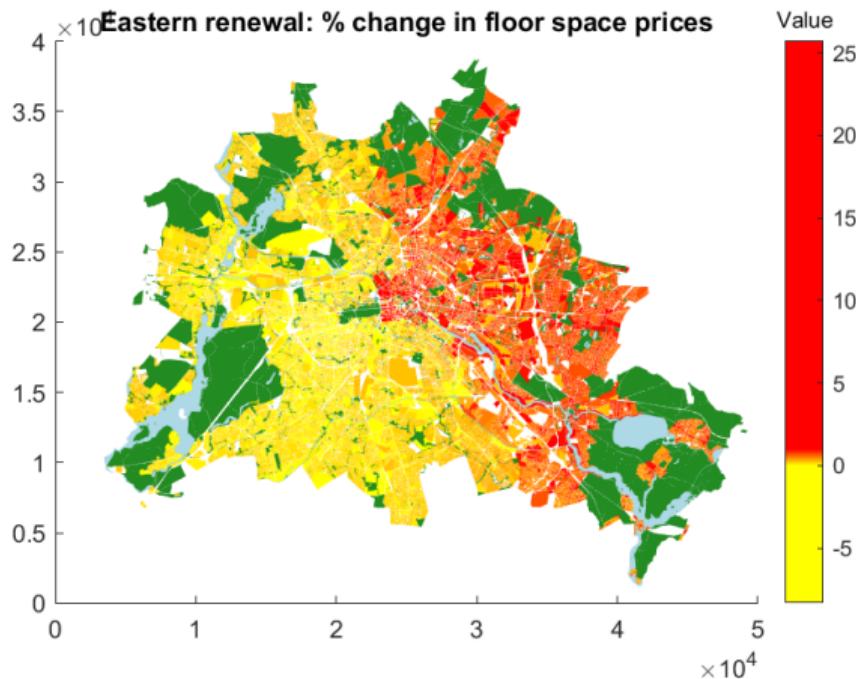
East Berlin productivity increase: Impact on residence employment

- ▶ Labour supply adjusts, subject to commuting friction
- ▶ East-West gradient in residence employment



East Berlin productivity increase: Impact on floor space prices

- Demand for floor space by firms and residents increases ⇒ higher floor space prices
- Impact on wages dominates floor space price effect ⇒ \bar{U} increases by 3.8%



Endogenous agglomeration forces

Endogenous agglomeration forces



Q: How do the effects of a productivity upgrade in East Berlin **differ under endogenous agglomeration forces?**

General equilibrium

- ▶ With endogenous agglomeration forces, we have
 - ▶ four more parameters, i.e. $\{\alpha, \beta, \mu, \varepsilon, \kappa, \lambda, \delta, \eta\rho\}$
 - ▶ two more endogenous objects, $\{\pi_{Mi}, \pi_{Ri}, Q_i, q_i, w_i, \theta_i, H, A_i, B_i\}$ (or H instead of \bar{U})
 - ▶ $\{a, b_i\}$ replace $\{A_i, B_i\}$ as exogenous characteristics $\{T_i, E_i, a_i, b_i, \varphi_i, K_i, \xi_i, \tau_{ij}\}$
 - ▶ two more equations that determine the equilibrium
 8. Productivity spillovers (20): $A_j = a_j \times \Upsilon_j^\lambda, \quad \Upsilon_j = \left[\sum_{s=1}^S e^{-\delta\tau_{is}} \left(\frac{H_{Ms}}{K_s} \right) \right]$
 9. Residential spillovers (21): $B_i = b_i \times \Omega_i^\eta, \quad \Omega_i = \left[\sum_{s=1}^S e^{-\rho\tau_{is}} \left(\frac{H_{Rs}}{K_s} \right) \right]$
- ▶ the same objects still reference the **general equilibrium**
 - ▶ the endogenous objects $\{\pi_{Mi}, \pi_{Ri}, Q_i, q_i, w_i, \theta_i, H\}$ (or H instead of \bar{U})

Two more variables, two more equations, **can still solve for the equilibrium ✓**

Algorithm 2: Solving for the equilibrium with endogenous agglomeration forces and exogenous total employment H : `smodendog.m`

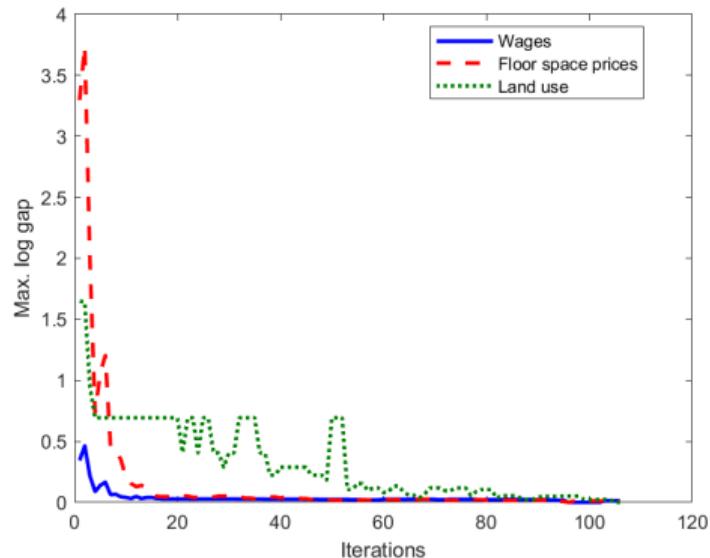
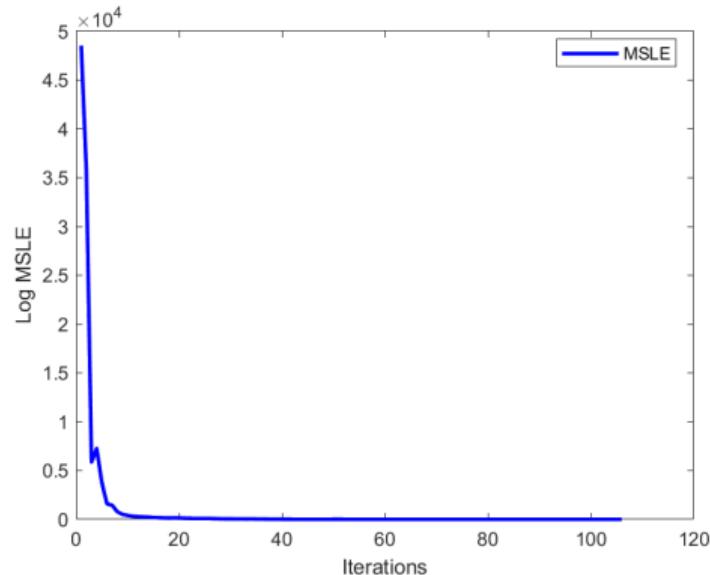
Data: Given values of structural parameters $\{\alpha, \beta, \kappa, \varepsilon, \mu\}$, bilateral travel times τ_{ij} , land area K_i ; inverted fundamental productivity and amenity $\{a_i, b_i\}$, adjusted density of development $\tilde{\varphi}_i$; guesses of the target variables: adjusted wages, commercial and residential floor space prices, commercial floor space shares $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ and initial values of workplace and residence employment $\{H_{Mi}, H_{Ri}\}$; total employment H

- 1 Compute floor space L_i using $\tilde{\varphi}_i$ and K_i in Eq. (S.52)
 - 2 Compute adjusted productivity \tilde{A}_i using τ_{ij} and initial values of H_{Mi} and Eq. (20)
 - 3 Compute adjusted amenity \tilde{B}_i using τ_{ij} and initial values of H_{Ri} and Eq. (21)
 - 4 Compute total employment $H = \sum H_{Mi}$
 - 5 while guesses of target variables $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ change do
 - 6 Compute choice probabilities π_{ij}^0 using guesses of $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ and $\{\tilde{A}_i, \tilde{B}_i\}$ in Eq. (4)
 - 7 Compute residence and workplace employment $\{\hat{H}_{Mi}, \hat{H}_{Ri}\}$ using $\hat{\pi}_{ij}^0, H$ and Eq. (5)
 - 8 Compute utility \hat{U} using guesses of $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ and $\{\tilde{A}_i, \tilde{B}_i\}$ in Eq. (9)
 - 9 Compute \tilde{A}_i using τ_{ij} and \hat{H}_{Mi} in Eq. (20)
 - 10 Compute \tilde{B}_i using τ_{ij} and \hat{H}_{Ri} in Eq. (21)
 - 11 Compute output \hat{Y}_i using the production function in Eq. (10), \hat{H}_{Mi} , total floor space L_i , and guesses of θ_i^0
 - 12 Compute predicted adjusted wage $\tilde{w}_i^1 = \alpha \hat{Y}_i / \hat{H}_{Mi}$ using the input demand function derived from F.O.C. of Eq. (10), and $\{\hat{Y}_i, \hat{H}_{Mi}\}$
 - 13 Compute total income $\mathbb{E}(\tilde{w}_i \times \hat{H}_{Ri})$ using Eq. (S.20), $\{\tilde{w}_i^1, \hat{H}_{Mi}\}$, and conditional commuting probabilities $\pi_{ij|i} = \Phi_{ij} / \sum_j \Phi_{ij}$
 - 14 Compute predicted commercial and residential floor space prices $\{q_i^1, Q_i^1\}$ using \hat{Y} , guesses of θ_i^0 , and Marshallian demand functions and input demand functions based on Eqs. (1) and (10)
 - 15 Compute predicted values of commercial floor space θ_i^1 using commercial floor space input $L_{Mi} = (1 - \alpha) \hat{Y}_i / q_i^1$ recovered from input demand function based on Eqs. (10) and (S.53)
 - 16 Update guesses of target variables $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ to weighted average of old guesses $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ and predicted values $\{w_i^1, q_i^1, Q_i^1, \theta_i^1\}$

Result: Predicted values of adjusted wage, total income, commercial floor space shares, output, commercial and residential floor space prices, workplace employment and residence, total employment, unconditional commuting probabilities $\{ \tilde{w}_i, \mathbb{E}(\hat{w}_i \times \hat{H}_{Mi}), \theta_i, Y_i, q_i, Q_i, H_{Mi}, H_{Ri}, \tilde{A}_i, \tilde{B}_i, \tilde{U}_i, \pi_{ii} \}$

- Program similar to `smodexog.m`, except that we need to compute endogenous productivity and amenity $\{\tilde{A}_i, \tilde{B}_i\}$ using the model-based predictions of $\{H_{Mi}, H_{Ri}\}$ Matlab code

Convergence path



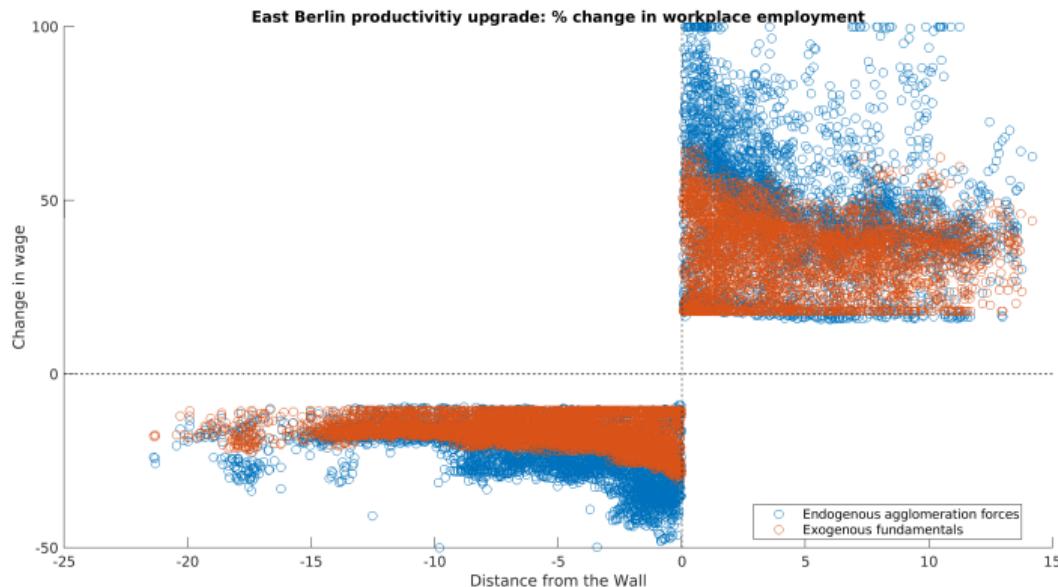
- Overall smooth path, except for θ which seems a bit bumpy
 - But there we expect changes at the extensive margin, so naturally less smooth

Uniqueness

- ▶ With agglomeration spillovers, the equilibrium is **not necessarily unique**
 - ▶ Typical feature of models with agglomeration forces
 - ▶ If you shift a sufficiently large mass of economic activity to a different location
 - ▶ Density at that location generates productivity or amenity
 - ▶ Firms or workers will have an incentive to remain at that location
 - ▶ **Temporary policies could have permanent effects**

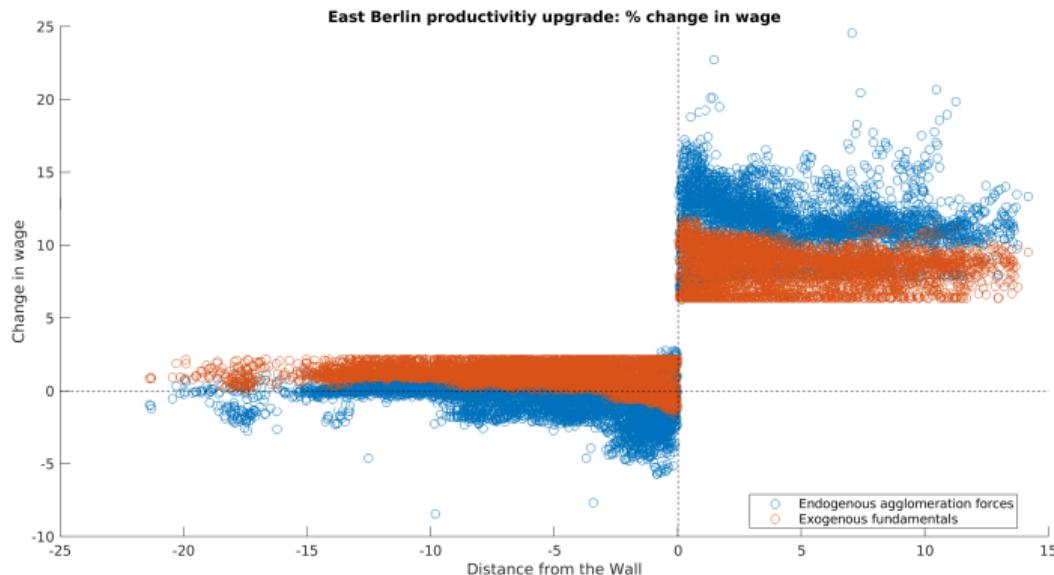
In practice, not particularly relevant as long as the **congestion force is strong enough** and there is **enough heterogeneity in location fundamentals**

East Berlin productivity increase: Workplace employment



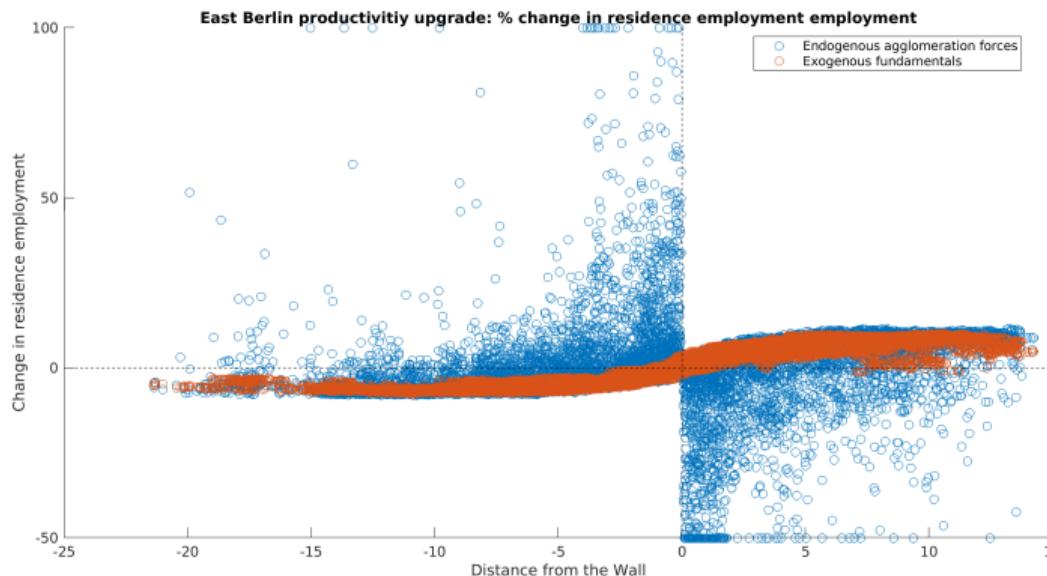
- Agglomeration spillovers amplify direct productivity effect
- More pronounced relocation of workplace employment to East Berlin

East Berlin productivity increase: Wages



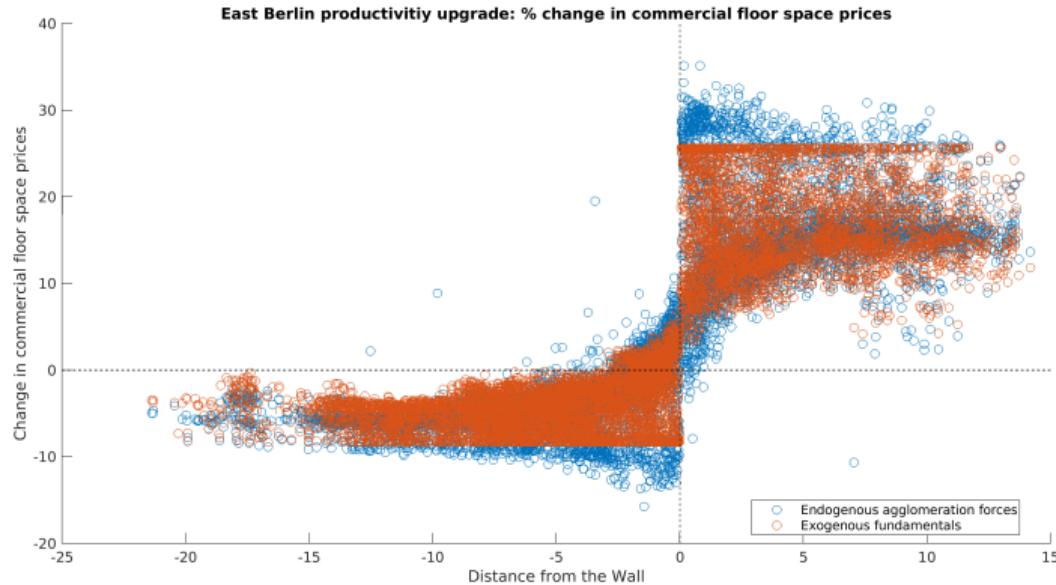
- ▶ Amplification of productivity increases in East \Rightarrow larger wage gains in East
- ▶ Relocation of workplace employment to East \Rightarrow Negative wage spillovers to West

East Berlin productivity increase: Residence employment



- ▶ Shift in workplace employment to East crowds out residence employment
 - ▶ Increase in residence employment in West at border to East

East Berlin productivity increase: Floor space prices



- More pronounced floor space price response
 - Net effect on \bar{U} slightly lower at 3% (instead of 3.8%)
 - Fundamental productivity relatively less important

Open city

Population mobility



Q: How do the effects of a productivity upgrade in East Berlin **differ in an open-city model?**

Open-city model

- In a **closed-city model**, H is a fixed endowment
 - $\{H_{Ri}, H_{Mi}\}$ follow directly from location choice probabilities $\{\pi_{Ri}, \pi_{Mi}\}$ given fixed H
 - We know already from the MCM that utility is endogenous
 - In an **open-city model**, \bar{U} is fixed and H is endogenous
 - We need to find the H that equates $\mathbb{E}[u]$ to the reservation utility \bar{U}
 - This is actually straight forward since the population mobility implies $\mathbb{E}[u] = \gamma [H]^{\frac{1}{\varepsilon}}$
 - Expected utility falls in total employment at an elasticity $-\varepsilon$
 - If expected utility exceeds \bar{U} , we increase the population until we converge
 - Need to invert \bar{U} to have the target value, which is done by [Matlab code](#)

H becomes a target object

Algorithm 3:

Solving for the equilibrium with endogenous agglomeration forces and exogenous reservation utility: ussmodendog.m

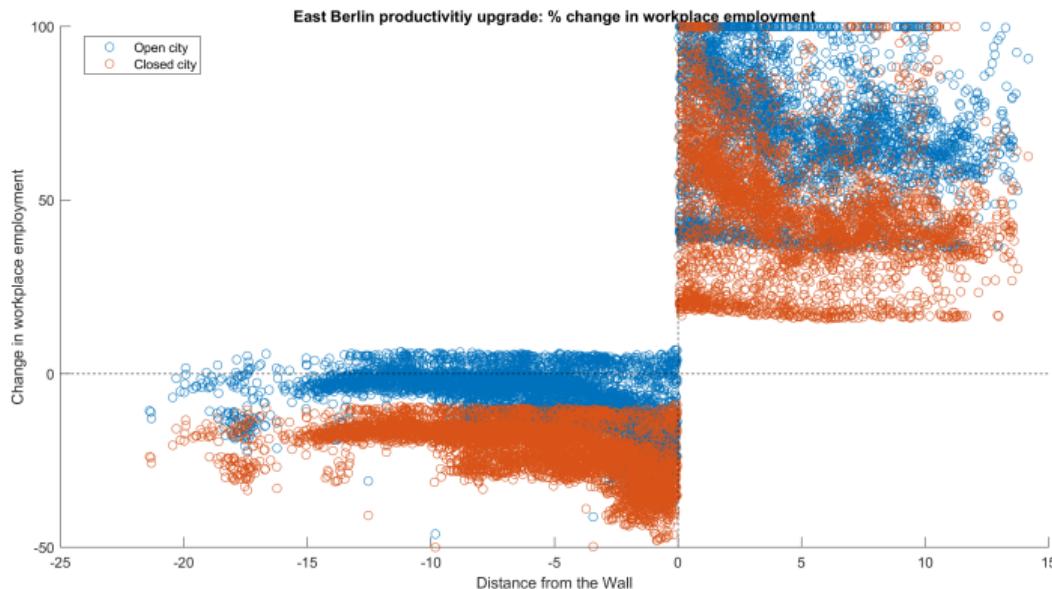
Data: Given values of structural parameters $\{\alpha, \beta, \kappa, \varepsilon, \mu\}$, bilateral travel times τ_{ij} , land area K_i ; inverted fundamental productivity and amenity $\{a_i, b_i\}$, adjusted density of development $\bar{\varphi}_i$; guesses of the target variables: adjusted wages, commercial and residential floor space prices, commercial floor space shares $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ and initial values of workplace and residence employment $\{H_{Mi}, H_{Ri}\}$; calibrated value of exogenous reservation utility level \bar{U}

- 1 Compute floor space L_i using $\bar{\varphi}_i$ and K_i in Eq. (S.52)
- 2 Compute adjusted productivity \tilde{A}_i using τ_{ij} and initial values of H_{Mi} and Eq. (20)
- 3 Compute adjusted amenity \tilde{B}_i using τ_{ij} and initial values of H_{Ri} and Eq. (21)
- 4 Compute total employment $H = \sum H_{Mi}$
- 5 **while** guesses of target variables $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ change or $E(U) \neq \bar{U}$ **do**
- 6 Compute choice probabilities π_{ij} using guesses of $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ and $\{\tilde{A}_i, \tilde{B}_i\}$ in Eq. (4)
- 7 Compute residence and workplace employment $\{\hat{H}_{Mi}, \hat{H}_{Ri}\}$ using $\hat{\pi}_{ij}$, H and Eq. (5)
- 8 Compute utility \hat{U} using guesses of $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ and $\{\tilde{A}_i, \tilde{B}_i\}$ in Eq. (9)
- 9 Compute \tilde{A}_i using τ_{ij} and \hat{H}_{Mi} in Eq. (20)
- 10 Compute \tilde{B}_i using τ_{ij} and \hat{H}_{Ri} in Eq. (21)
- 11 Compute output \hat{Y}_i using the production function in Eq. (10), \hat{H}_{Mi} , total floor space L_i , and guesses of θ_i^0
- 12 Compute predicted adjusted wage $\tilde{w}_i^1 = \alpha \frac{\hat{Y}_i}{H_{Mi}}$ using the input demand function derived from F.O.C. of Eq. (10), and $\{\hat{Y}_i, \hat{H}_{Mi}\}$
- 13 Compute total income $E(\hat{w}_i \times \hat{H}_{Ri})$ using Eq. (S.20), $\{\tilde{w}_i^1, \hat{H}_{Mi}\}$, and conditional commuting probabilities $\pi_{ij|i} = \Phi_{ij} / \sum_j \Phi_{ij}$
- 14 Compute predicted commercial and residential floor space prices $\{q_i^1, Q_i^1\}$ using \hat{Y}_i , guesses of θ_i^0 , and Marshallian demand functions and input demand functions based on Eqs. (1) and (10)
- 15 Compute predicted values of commercial floor space θ_i^1 using commercial floor space input $L_{Mi} = (1 - \alpha)\hat{Y}_i/q_i^1$ recovered from input demand function based on Eqs. (10) and (S.53)
- 16 Update guesses of target variables $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ to weighted average of old guesses $\{\tilde{w}_i^0, q_i^0, Q_i^0, \theta_i^0\}$ and predicted values $\{w_i^1, q_i^1, Q_i^1, \theta_i^1\}$
- 17 **Update H using adjustment factor that depends on $\frac{\bar{U}}{U}$ (we increase total employment if expected utility exceeds reservation utility)**

Result: Predicted values of adjusted wage, total income, commercial floor space shares, output, commercial and residential floor space prices, workplace employment and residence, total employment, unconditional commuting probabilities $\{\tilde{w}_i, E(\tilde{w}_i) \times \hat{H}_{Mi}, \theta_i, Y_i, q_i, Q_i, H_{Mi}, H_{Ri}, \tilde{A}_i, \tilde{B}_i, H, \pi_{ij}\}$

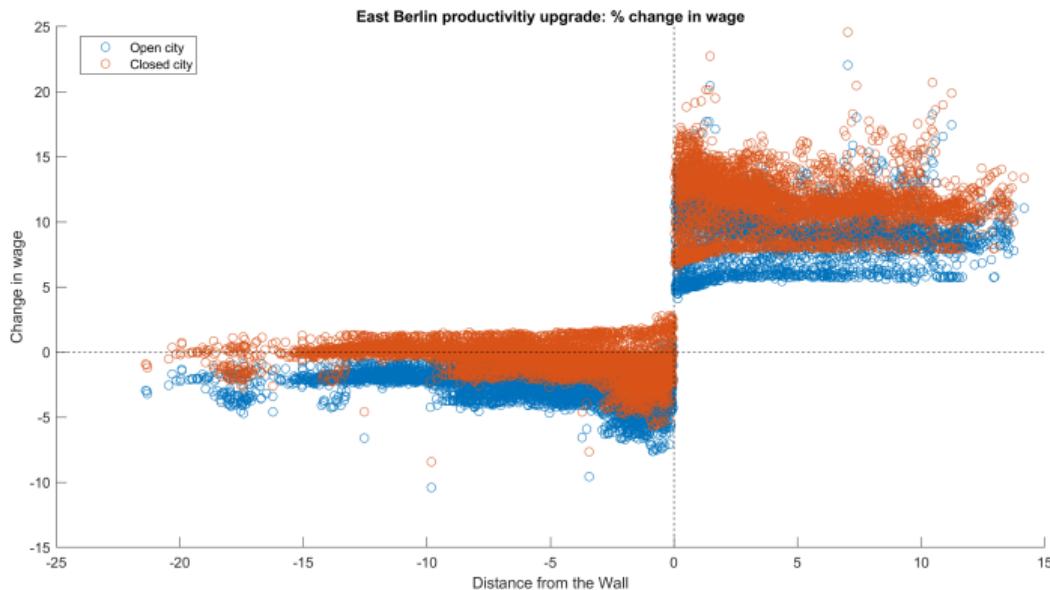
- ▶ Program similar to smodendog.m, except that we update H to that $E(U)$ matches \bar{U}

East Berlin productivity increase: Workplace employment



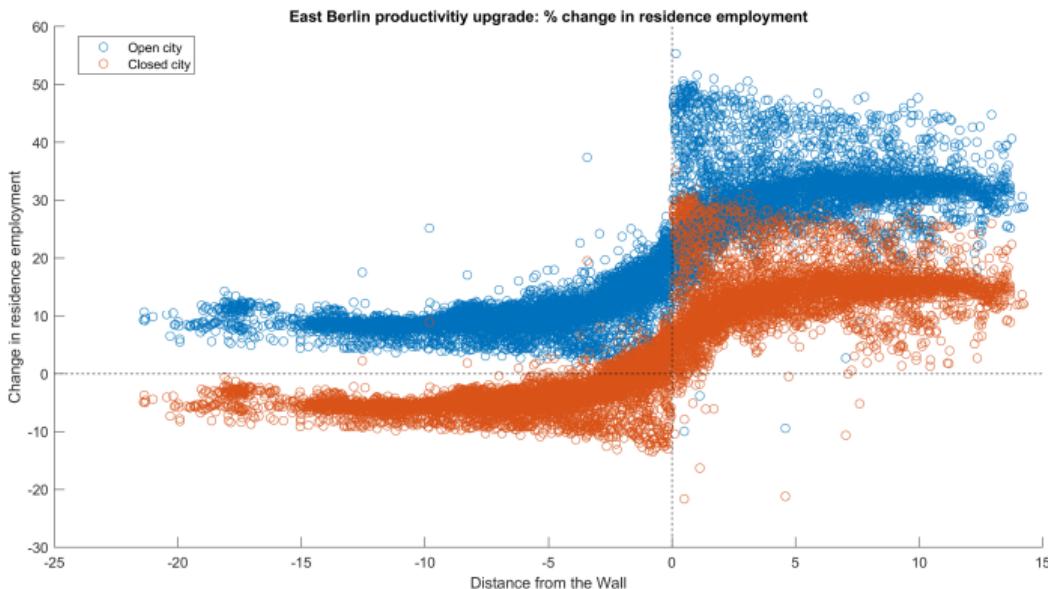
- ▶ Total employment increases by about 300k to restore reservation utility
 - ▶ Some blocks in West turn from losers to winners!

East Berlin productivity increase: Wages



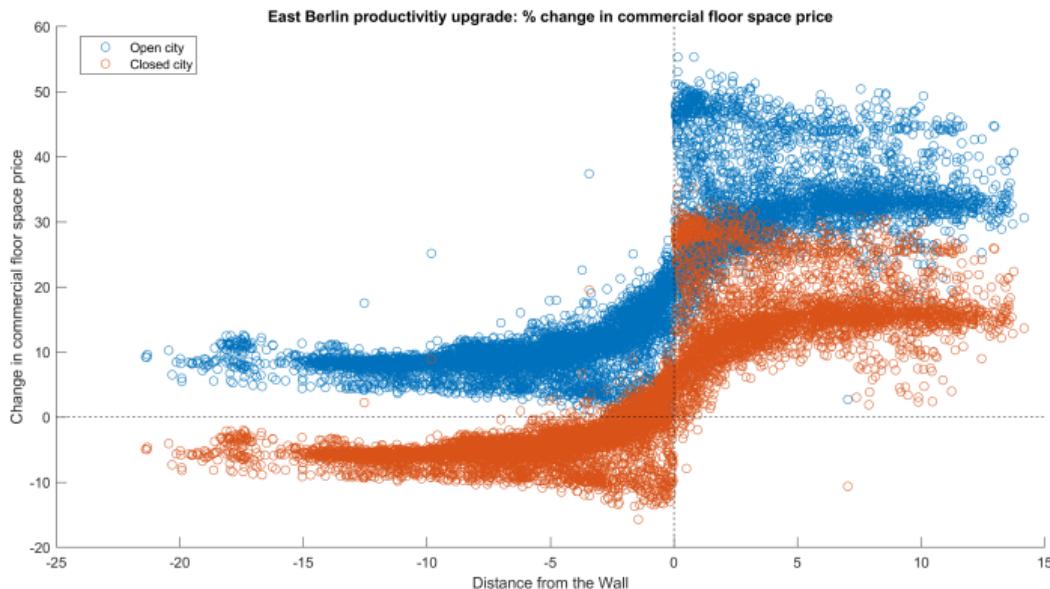
- Wages increase since city generates more agglomeration economies (more workers)
 - Some blocks in West turn from losers to winners!

East Berlin productivity increase: Residence employment



- ▶ Residence employment increases throughout city
 - ▶ Most blocks in West turn from losers into winners!

East Berlin productivity increase: Floor space prices



- ▶ Floro space prices increase throughout city (to restore the reservation utility)
 - ▶ Most blocks in West turn from losers into winners!

Conclusion

Summary

- ▶ QSMs can perform counterfactuals in spatial general equilibrium
 - ▶ Re-solve the model under different primitives that reflect, e.g. a policy change
- ▶ With **endogenous agglomeration forces** spatial adjustments tend to be larger
 - ▶ Model with exogenous fundamentals doesn't fully account for Berlin Wall effects
- ▶ Local shocks tend to generate spatial winners and losers due to relocation effects
 - ▶ Positive shocks produce more losers in **closed city model**
 - ▶ In **open-city** model large inflow of workers mitigates local losses
- ▶ ARSW assumes perfect mobility across the city border
 - ▶ No idiosyncratic tastes for living in a specific city ⇒ akin to RR
 - ▶ One could add idiosyncratic tastes for being in the city maybe more realistic

Next week: **Quantitative Economic Geography**

Literature I

Core readings

- ▶ Ahlfeldt, G., Redding, S., Sturm, D., Wolf, N. (2015): The economics of Density: Evidence From the Berlin Wall. *Econometrica*, 83(6), 2127–2189.

Other readings

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