

# **THE URBAN ECONOMY IN GENERAL EQUILIBRIUM**

**Urban Economics**

**GABRIEL M AHLFELDT**

# I COURSE COMPONENTS

the idea

- Block 1

- Introduction to Urban and Regional Economics and Course Overview
- Topic I: Regional and urban concentration forces
- Topic II: The empirics of agglomeration
- Topic III: Costs and benefits of agglomeration

- Block 2

- Topic IV: Monocentric city I (household location choice)
- Topic V: Monocentric city II (household location choice)
- Topic VI: Firm location choice
- **Topic VII: The urban economy in general equilibrium**

- Block 3

- Topic VIII: The vertical dimension of cities
- Topic IX: Suburbanization and gentrification
- Topic X: Hedonic analysis

# I INTRODUCTION

roadmap

- Last time: *Firm location choice*
  - 1) Firms in the monocentric city model
    - Firm bid-rent
    - Land-use segregation
  - 2) Agglomeration and decentralization
    - Endogenous agglomeration
    - Multiple equilibria
  - 3) Emergence of new clusters
    - Sub-centres
    - Edge cities
    - Historic anchoring

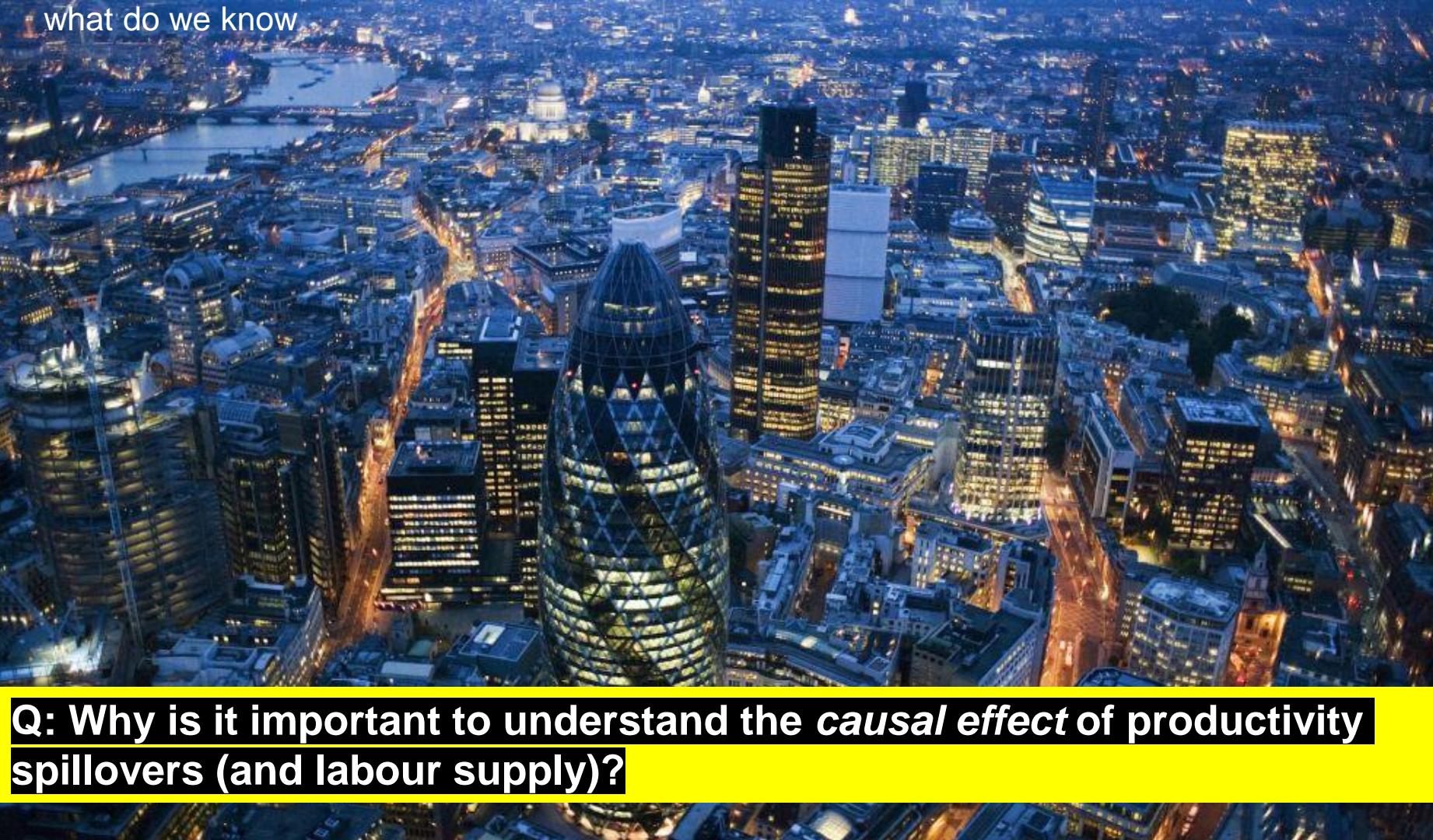
# I INTRODUCTION

roadmap

- This time: *The urban economy in general equilibrium*
  - 1) Recap
    - Compensating differentials, location choice, supply side
  - 2) The Ahlfeldt-Redding-Sturm-Wolf model
    - Model setup
  - 3) Separating spillovers from location fundamentals
    - Reduced-form evidence
    - Difference-in-difference analysis
  - 4) Structural estimation and simulation
    - Identifying structural parameters
    - Simulating the effect of a new metro line

## II RECAP

what do we know



**Q: Why is it important to understand the *causal effect* of productivity spillovers (and labour supply)?**

# I RECAP

roadmap

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# I HOUSEHOLD LOCATION CHOICE

recall

- Households maximize utility subject to budget constraint
  - Dislike longer commutes
  - Like higher wages
  - Like residential amenities
- Spatial equilibrium:
  - Households must be indifferent across locations
  - Rents offset for differences in utility across location
    - Reflect access to firms and amenities

**Household location choice conditional on firm location**

# I FIRM LOCATION COICE

recall

- **Firms maximize profits**

- Like agglomeration / clustering
- Like production amenities
- Like access to workers and lower wages (ignored so far)

- **Spatial equilibrium:**

- Firm profits must be equalized across locations
- Rents (and wages) offset for differences in productivity across location
  - Reflect production amenities and agglomeration

**Firm location choice should also depend on household location (wages)**

# I DEVELOPERS

recall

- **Profit-maximizing developers provide floor space**
  - Convex production cost (building denser more expensive)
  - Use more capital when floor space rents are higher
- **Spatial equilibrium:**
  - Developer profits must be equalized across locations
  - Building density higher when floor space prices are higher
  - Greater construction costs compensate for greater revenues
    - Land rents higher where floor space rents are higher

**Supply side links floor space rent to land rent**

# I OPEN CITY MODEL AND ROSEN-ROBACK

recall

- **Residents are mobile across cities**
  - Attractive features attract residents from other cities
  - Densification increases cost of living in a city
- **In equilibrium:**
  - Reservation utility level constant across locations
- **Rosen-Roback framework**
  - Residential amenities increase rents and decrease wages
  - Production amenities increase wages and rents

**There is a world outside the city**

# II RECAP

roadmap

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## II UNIFYING THE FRAMEWORKS

the ARSW model

- **Can we have a model with the following features?**

- Endogenous household location choice
- Endogenous firm location choice
- Dispersed commuting
- Profit-maximizing developers
- Fundamental production and residential amenities
- Agglomeration effects on production and consumption side
- A region with which the city interacts

**Yes, we can!**

## II THE ARSW MODEL

the ARSW model

- **Ahlfeldt, Redding, Sturm, Wolf (2015)**

- Combines features of various urban models
- No “awkward” geography
  - City consists of a series of “blocks”
  - Can take any form observed in real world
- Empirically **tractable GE model**
- First urban economics paper to win “Frisch medal”
  - Best paper of last five years in 2018 (Econometric Society)



Gabriel Ahlfeldt



Steve Redding



Daniel Sturm



Niklaus Wolf

## II THE ARSW MODEL

the ARSW model

### ■ Ressources

- User-friendly VOXEU column
  - <https://voxeu.org/article/economics-density-evidence-berlin-wall>
- Macroeconomic insights
  - <http://microeconomicinsights.org/economics-density-evidence-berlin-wall/>
- Video: Gabriel explaining the impact of the model
  - <https://www.youtube.com/watch?v=feZPzB29oU8>
- Video: Gabriel explaining what winning the Frisch Medal means for urban economics
  - <https://www.youtube.com/watch?v=tDHw07csblo>



Gabriel Ahlfeldt



Steve Redding



Daniel Sturm



Niklaus Wolf

## II THE GENERAL SETUP

the ARSW model

### ▪ ARSW (2015)

- City embedded in larger economy – *reservation utility*  $\bar{U}$
- A single final good which is freely traded
- All markets are perfectly competitive
- Households and firms make optimal choices
- Discrete city blocks  $i$
- Effective land is optimally allocated between residential and commercial use
- Construction sector producing floor space using land and capital

### ▪ Within-city characteristics

- Fundamental production and consumption amenities
- Consumption spillovers **lead to concentration of residents**
- Production spillovers **lead to concentration of firms**
- Commuting costs **lead to co-location of firms and residents**

## II RESIDENTS I

the ARSW model

Utility for worker  $o$  residing in block  $i$  and working in block  $j$ :

$$U_{ijo} = \frac{B_i z_{ijo}}{d_{ij}} \left( \frac{c_{ij}}{\beta} \right)^\beta \left( \frac{\ell_{ij}}{1-\beta} \right)^{1-\beta}, \quad 0 < \beta < 1,$$

- Consumption of the final good ( $c_{ij}$ ), chosen as numeraire ( $p_i = 1$ )
- Residential floor space ( $\ell_{ij}$ )
- Residential amenity  $B_i$
- Commuting costs  $d_{ij} = e^{\kappa \tau_{ij}}$
- Idiosyncratic shock  $z_{ijo}$  that captures idiosyncratic reasons for a worker living in block  $i$  and working in block  $j$

**Standard Cobb-Douglas utility function with consumption of housing and other goods**

**Making use of first-order conditions and budget constrain**

Indirect utility

$$U_{ijo} = \frac{z_{ijo} B_i w_j Q_i^{\beta-1}}{d_{ij}},$$

**Decreases in rent  $Q$**   
**Decreases in commuting cost  $d$**   
**Increases in residential amenities  $B$**   
**Depends on “idiosyncratic” tastes  $z$**

The idiosyncratic shock to worker productivity is drawn from a Fréchet distribution:

$$F(z_{ijo}) = e^{-T_i E_j z_{ijo}^{-\epsilon}}, \quad T_i, E_j > 0, \epsilon > 1,$$

## II RESIDENTS II

the ARSW model

Probability worker chooses to live in block  $i$  and work in block  $j$  is:

$$\pi_{ij} = \frac{T_i E_j \left( d_{ij} Q_i^{1-\beta} \right)^{-\epsilon} (B_i w_j)^\epsilon}{\sum_{r=1}^S \sum_{s=1}^S T_r E_s \left( d_{rs} Q_r^{1-\beta} \right)^{-\epsilon} (B_r w_s)^\epsilon} \equiv \frac{\Phi_{ij}}{\Phi}.$$

Residential and workplace choice probabilities

$$\pi_{Ri} = \sum_{j=1}^S \pi_{ij} = \frac{\sum_{j=1}^S \Phi_{ij}}{\Phi}, \quad \pi_{Mj} = \sum_{i=1}^S \pi_{ij} = \frac{\sum_{i=1}^S \Phi_{ij}}{\Phi}.$$

Commuting market clearing

$$H_{Mj} = \sum_{i=1}^S \frac{E_j (w_j / d_{ij})^\epsilon}{\sum_{s=1}^S E_s (w_s / d_{is})^\epsilon} H_{Ri}, \quad d_{ij} = e^{\kappa \tau_{ij}}.$$

Workers working at  $j$

Workers living at  $i$

**More labour supplied to locations  $j$  where/if: wages  $w$  are higher and/or there are more workers with within a short commuting range**

## II SPATIAL EQUILIBRIUM IN OPEN CITY

the ARSW model

Expected utility of moving to the city

$$\mathbb{E}[u] = \gamma \left[ \sum_{r=1}^S \sum_{s=1}^S T_r E_s \left( d_{rs} Q_r^{1-\beta} \right)^{-\epsilon} (B_r w_s)^\epsilon \right]^{1/\epsilon} = \bar{U}.$$

**Spatial equilibrium in an open city framework implies that expected utility at all locations within the city is fixed to a reservation utility level**

Solve for adjusted residential amenities ( $\tilde{B}_i$ ):

$$\ln \left( \frac{\tilde{B}_i}{\bar{B}} \right) = \frac{1}{\epsilon} \ln \left( \frac{H_{Ri}}{\bar{H}_R} \right) + (1 - \beta) \ln \left( \frac{Q_i}{\bar{Q}} \right) - \ln \left( \frac{W_i}{\bar{W}} \right),$$

**Positive residential amenities  $B$  compensated for by higher rents  $Q$  and/or lower wages (net of commuting)  $W$**

**Rosen-Roback equivalent within cities!**

## II FIRMS

the ARSW model

A single final good (numeraire) is produced under conditions of perfect competition, constant returns to scale and zero trade costs with a larger economy:

$$X_j = A_j H_{Mj}^\alpha L_{Mj}^{1-\alpha}, \quad 0 < \alpha < 1,$$

Profit maximization and zero profits:

**Very similar to Ahlfeldt & Wendland (2013), except firms use floor space not land**

$$q_j = (1 - \alpha) \left( \frac{\alpha}{w_j} \right)^{\frac{\alpha}{1-\alpha}} A_j^{\frac{1}{1-\alpha}}.$$

Solve for adjusted productivity ( $\tilde{A}_i$ ):

$$\ln \left( \frac{\tilde{A}_{it}}{\tilde{A}_t} \right) = (1 - \alpha) \ln \left( \frac{Q_{it}}{\bar{Q}_t} \right) + \alpha \ln \left( \frac{\tilde{w}_{it}}{\bar{w}_t} \right)$$

**Positive production amenities  
A compensated for by higher rents  $Q$  and/or higher wages  $w$**

**Rosen-Roback equivalent within cities!**

## II FUNDAMENTALS AND SPILLOVERS

the ARSW model

- Productivity depends on

- Exogenous production fundamentals
- Endogenous production externalities (spillovers)

$$A_j = [a_j] Y_j^\lambda, \quad Y_j \equiv \sum_{s=1}^S e^{-\delta \tau_{js}} \left( \frac{H_{Ms}}{K_s} \right)$$

**Production *a* and residential *b* fundamentals are exogenously given, e.g. view on river or lake, location on top of a hill, etc.**

**Production spillovers depend on the surrounding workers at workplace, weighted by distance, e.g. due to knowledge spillovers**

- Residential amenities depend on

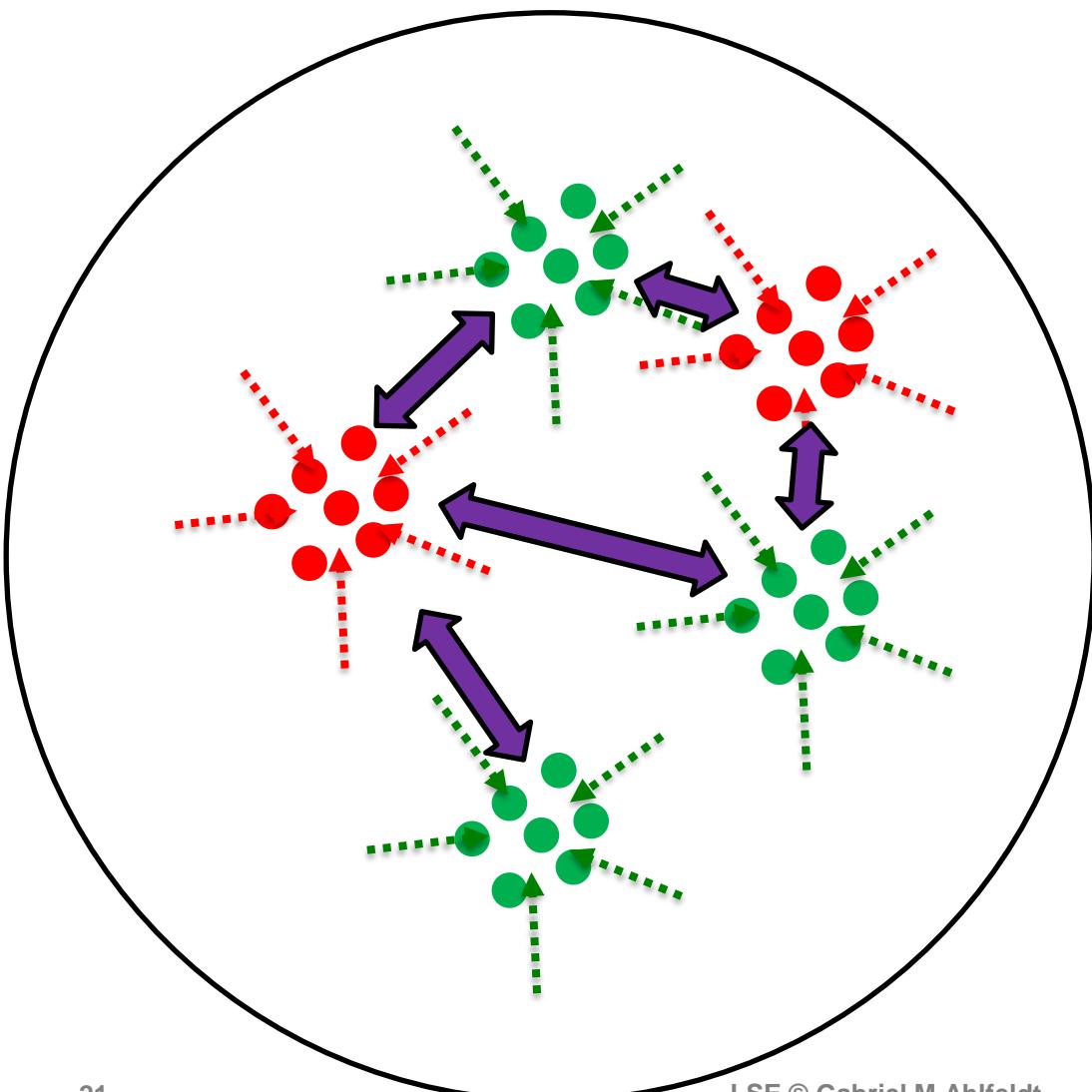
- Exogenous residential fundamentals
- Endogenous residential externalities (spillovers)

$$B_i = [b_i] \Omega_i^\eta, \quad \Omega_i \equiv \sum_{s=1}^S e^{-\rho \tau_{is}} \left( \frac{H_{Rs}}{K_s} \right)$$

**Residential spillovers depend on the surrounding workers at residence, weighted by distance, e.g. attract endogenous amenities such as restaurants**

## II CONCENTRATION FORCES

the ARSW model



**1) Production spillovers lead to concentration of firms**

**2) Residential spillovers lead to concentration of residents**

**3) Commuting cost lead to co-location of firms and residents**

**Q) Why does the city not collapse into a single “hyper-concentrated” point?**

## II PRODUCTION OF FLOOR SPACE

the ARSW model

- Land is limited and inelastically supplied
- Floor space is produced by a construction sector with a concave production function, using land and capital
- *In perfect analogy to topic IV*
  - More space can only be provided at higher floor space rents
  - Higher floor space price translates to higher land rents

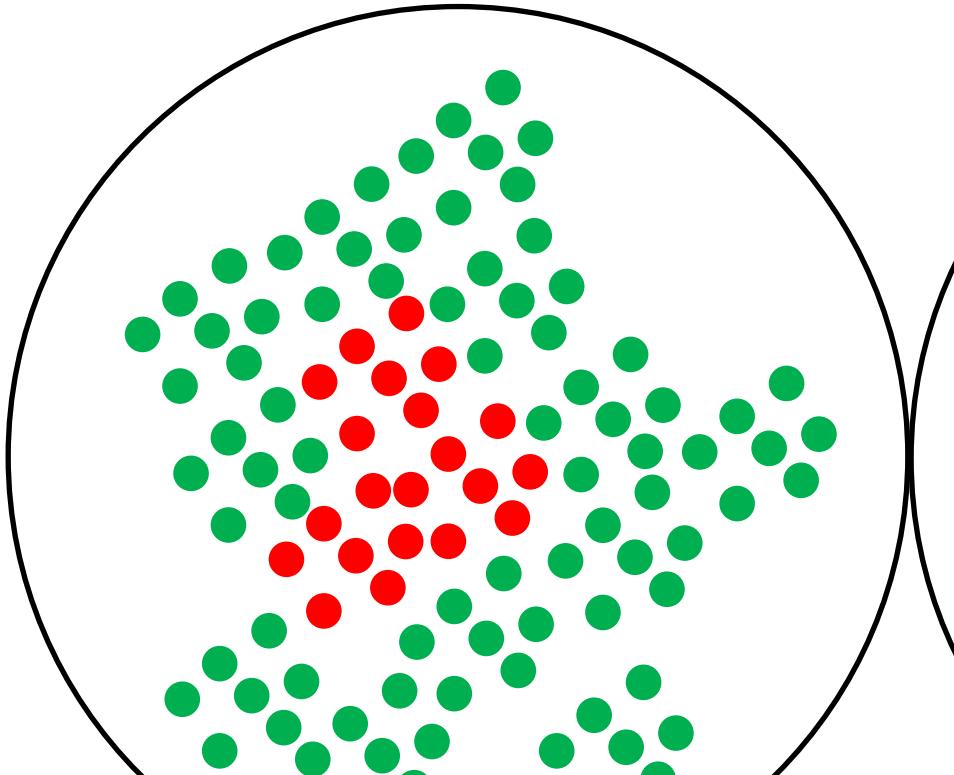
**Cost of building dense and tall creates a dispersion force that prevents hyper-concentration**

**End up with clusters of commercial activity, residential areas and mixed-use zones. City can have different configurations (multiple equilibria, see topic VI)**

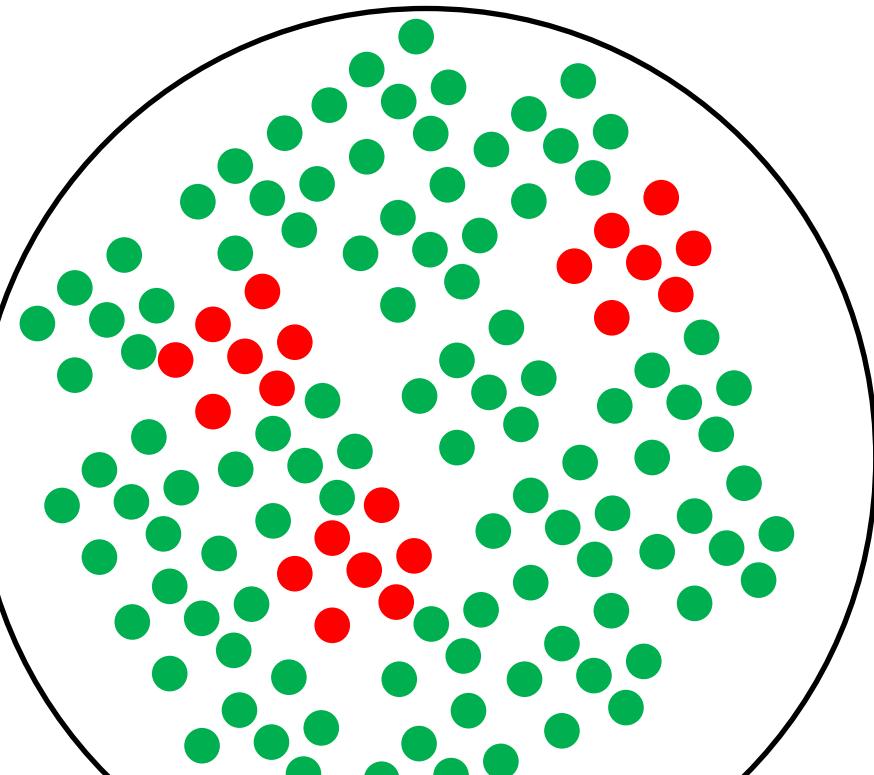
## II CONCENTRATION FORCES

the ARSW model

Monocentric city



Polycentric city



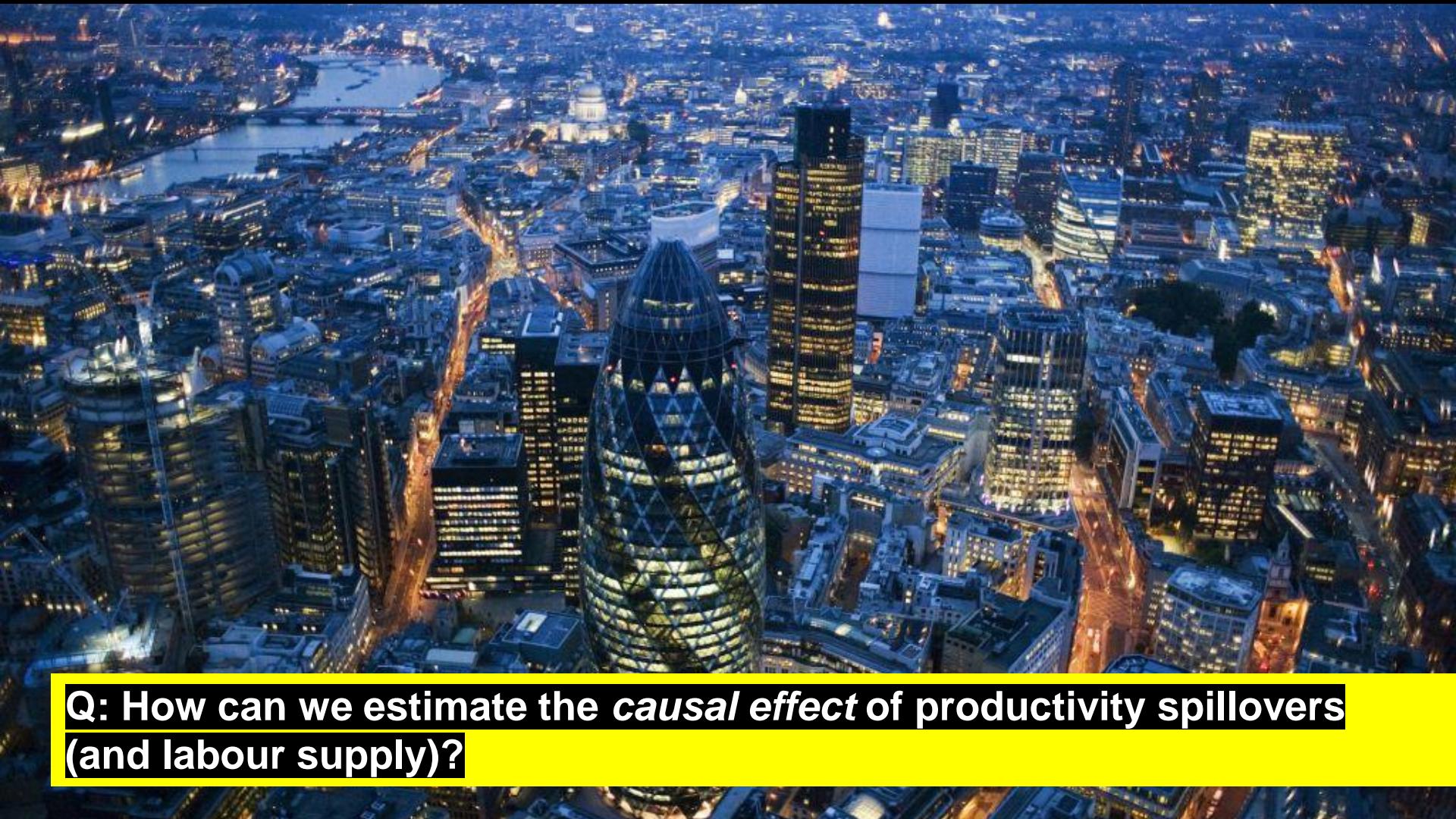
**Recall Topic VI:** Can transform cities IFF external returns to scale matter!

**Recall Topic II:** Estimating agglomeration effects is challenging due to endogeneity

# III SEPARATING SPILLOVERS FROM FUNDAMENTALS

roadmap

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**Q: How can we estimate the *causal effect* of productivity spillovers  
(and labour supply)?**

# III TESTING FOR SPILLOVERS

separating spillovers from location fundamentals

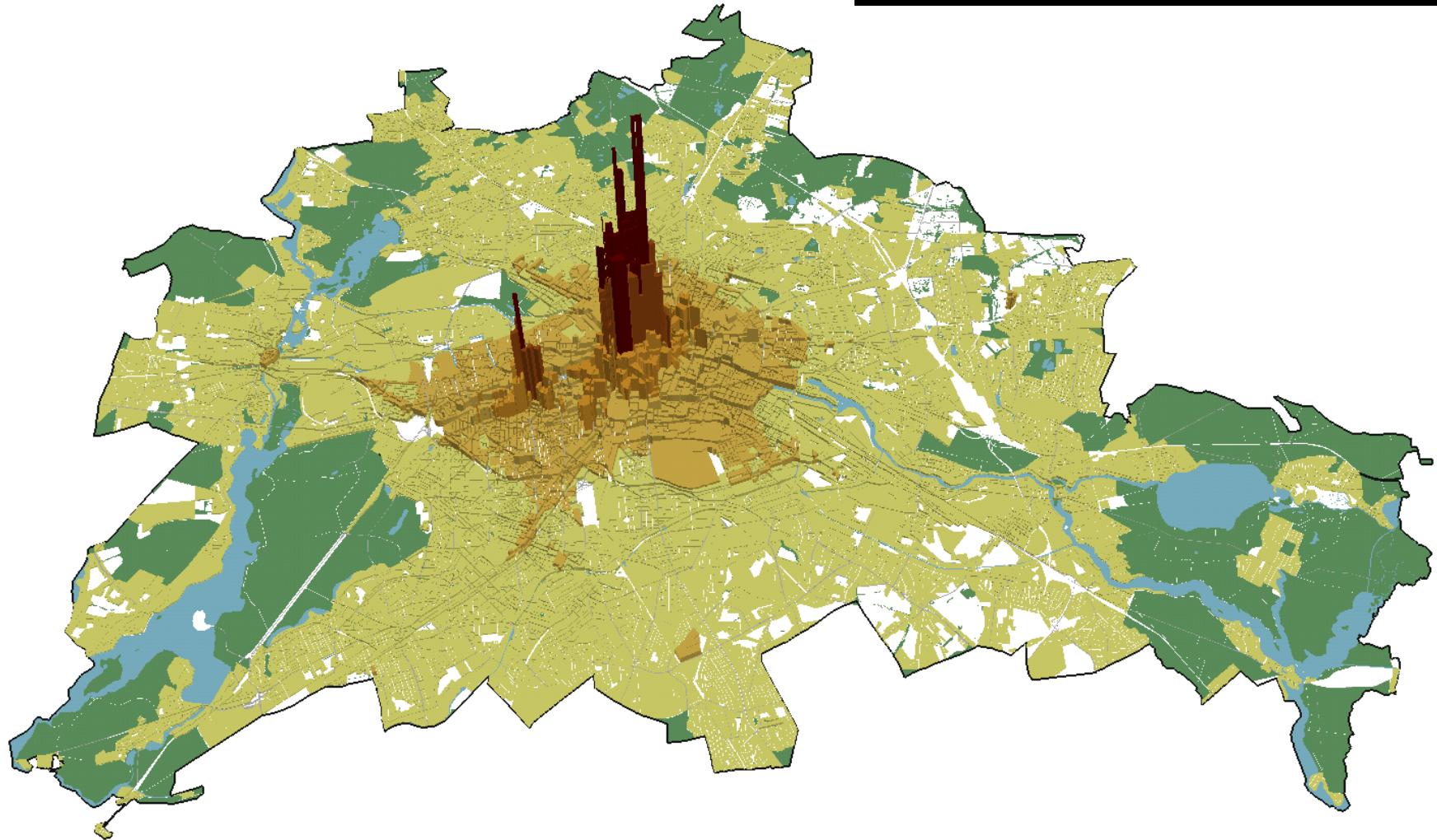
- To separate spillovers from location fundamentals, we need
  - plausibly exogenous variation in exposure to spillovers
  - over time
- Variation over time allows for a before-after comparison
  - Can rule out local fundamentals which are time-invariant
- Need a shock that increases or decreases some location's exposure to spillovers from other locations and affects
  - Shared inputs
  - Labour market pooling
  - Knowledge spillovers

**Q: Why type of events induce changes in exposure to spillovers?**

# III LAND PRICES IN BERLIN 1936

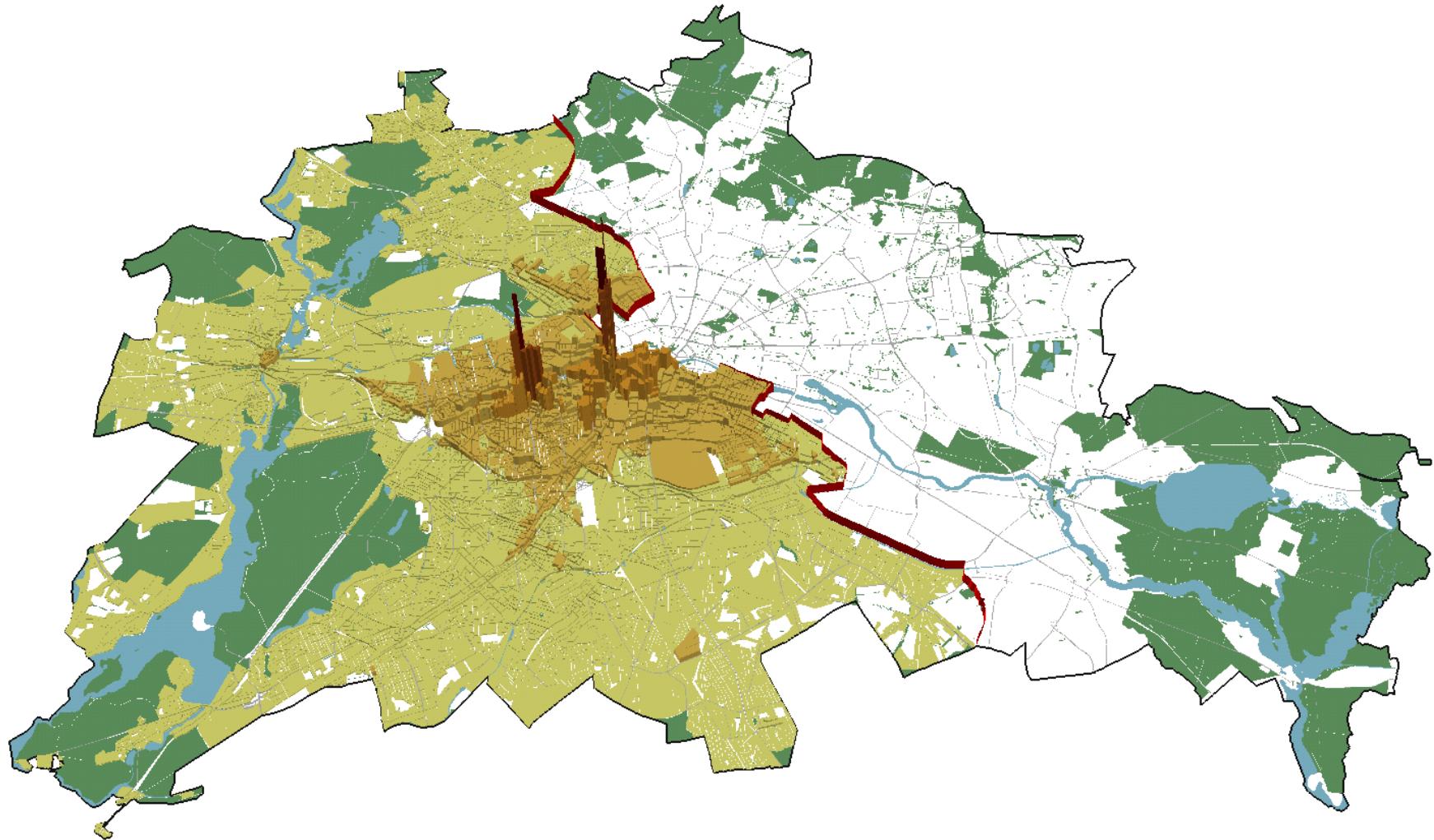
separating spillovers from location fundamentals

A descriptive version of ARSW, 2015



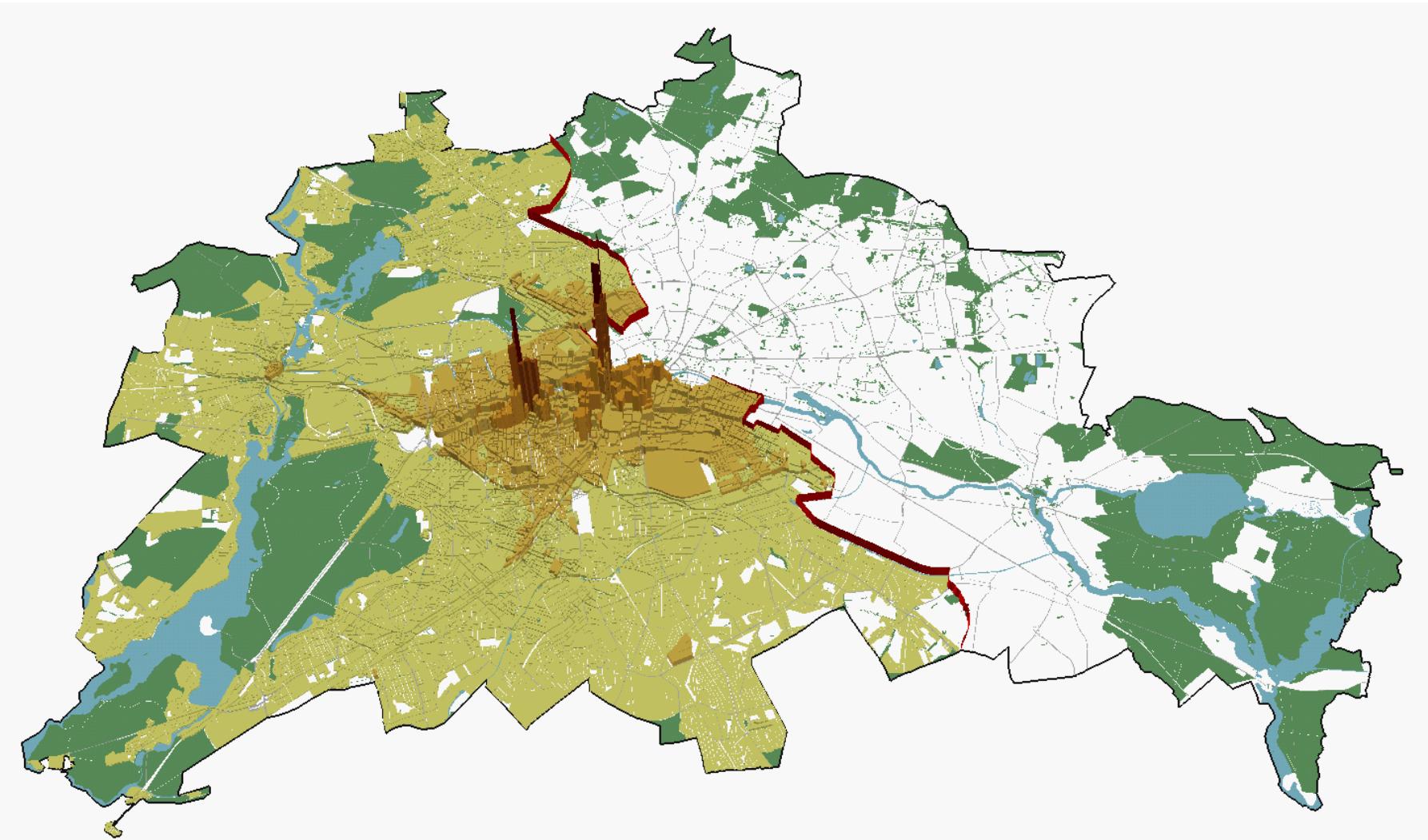
# III LAND PRICES IN WEST BERLIN 1936

separating spillovers from location fundamentals



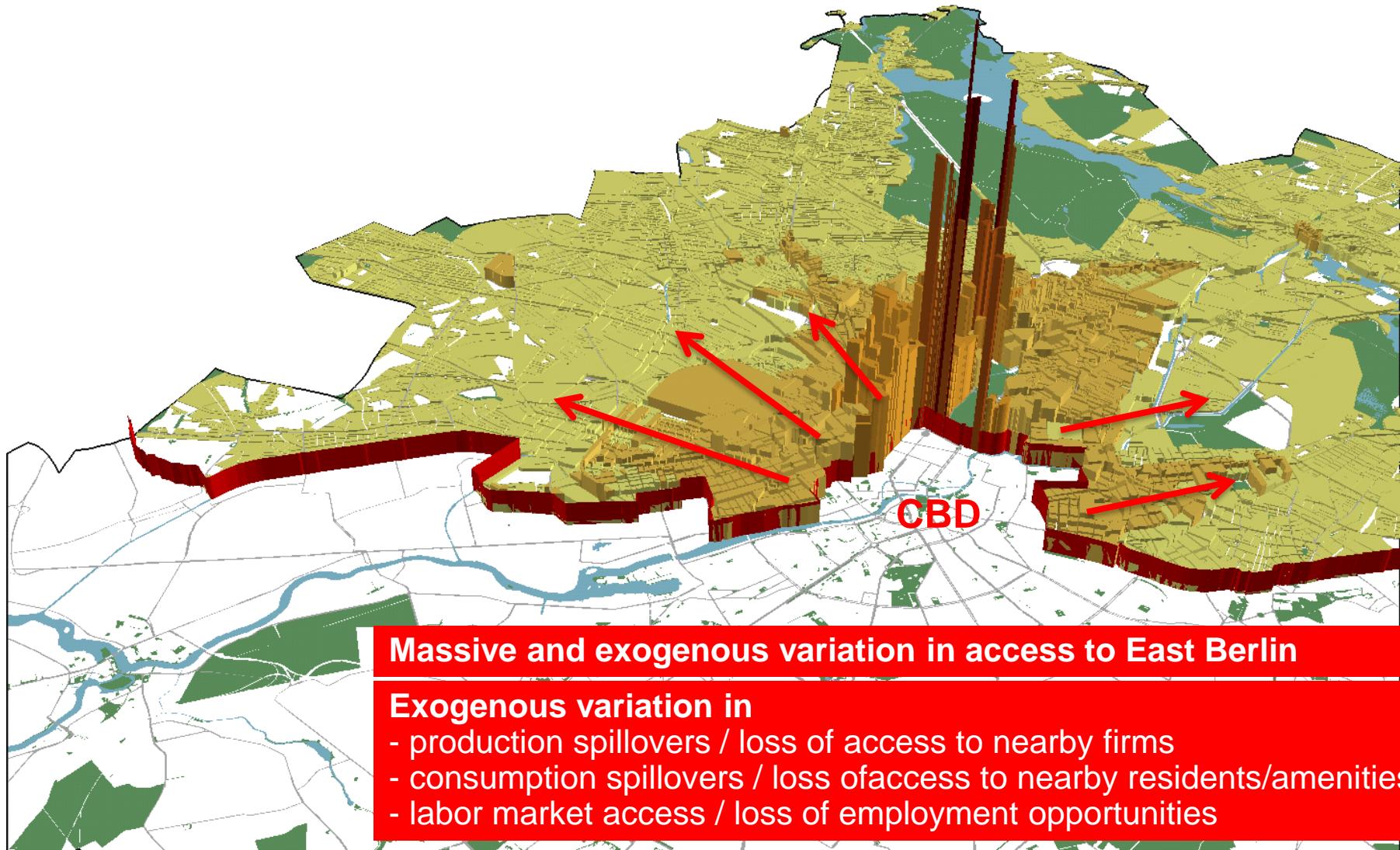
# III LAND PRICES IN WEST BERLIN 1936

separating spillovers from location fundamentals



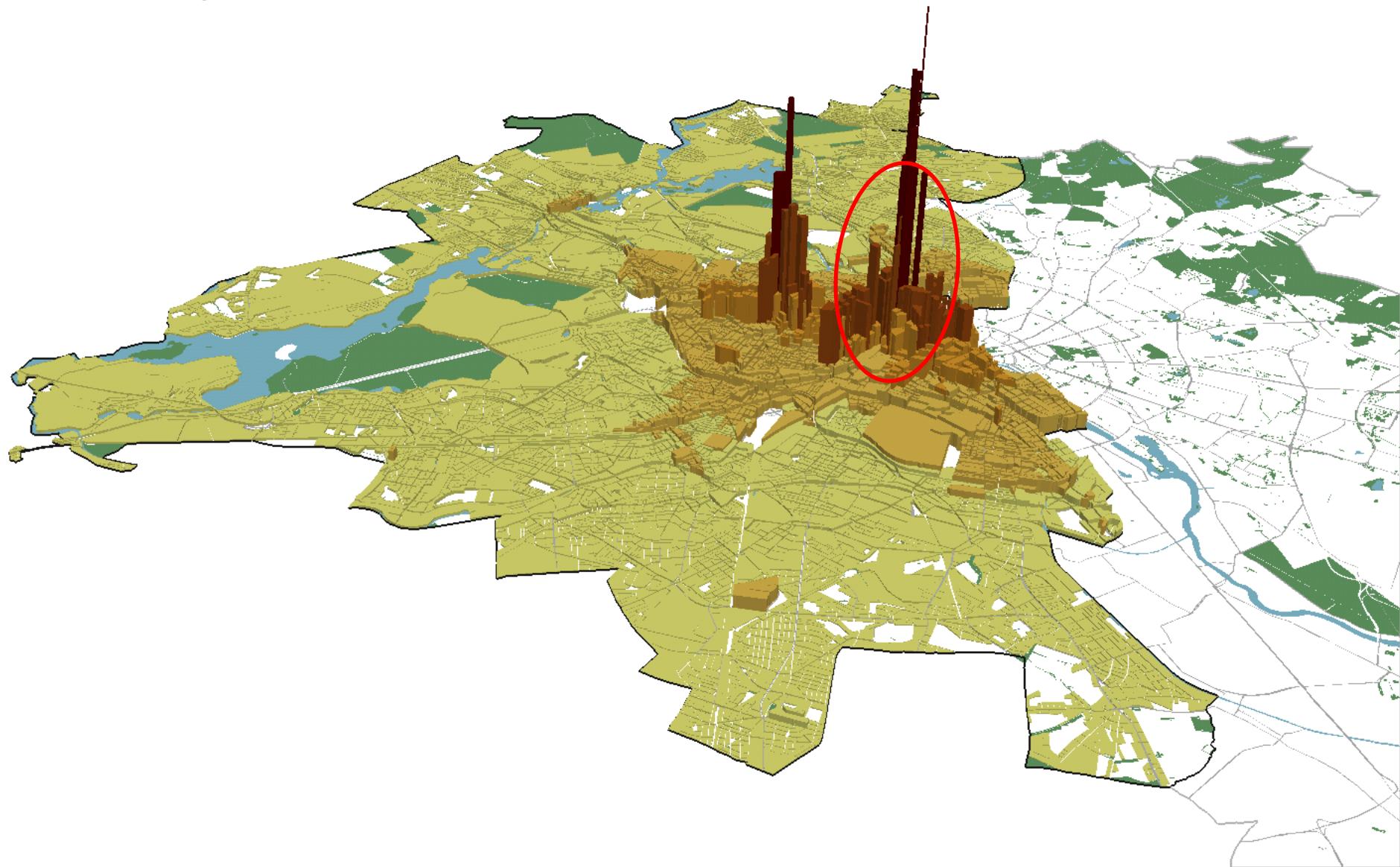
# III LAND PRICES IN WEST BERLIN 1936

separating spillovers from location fundamentals



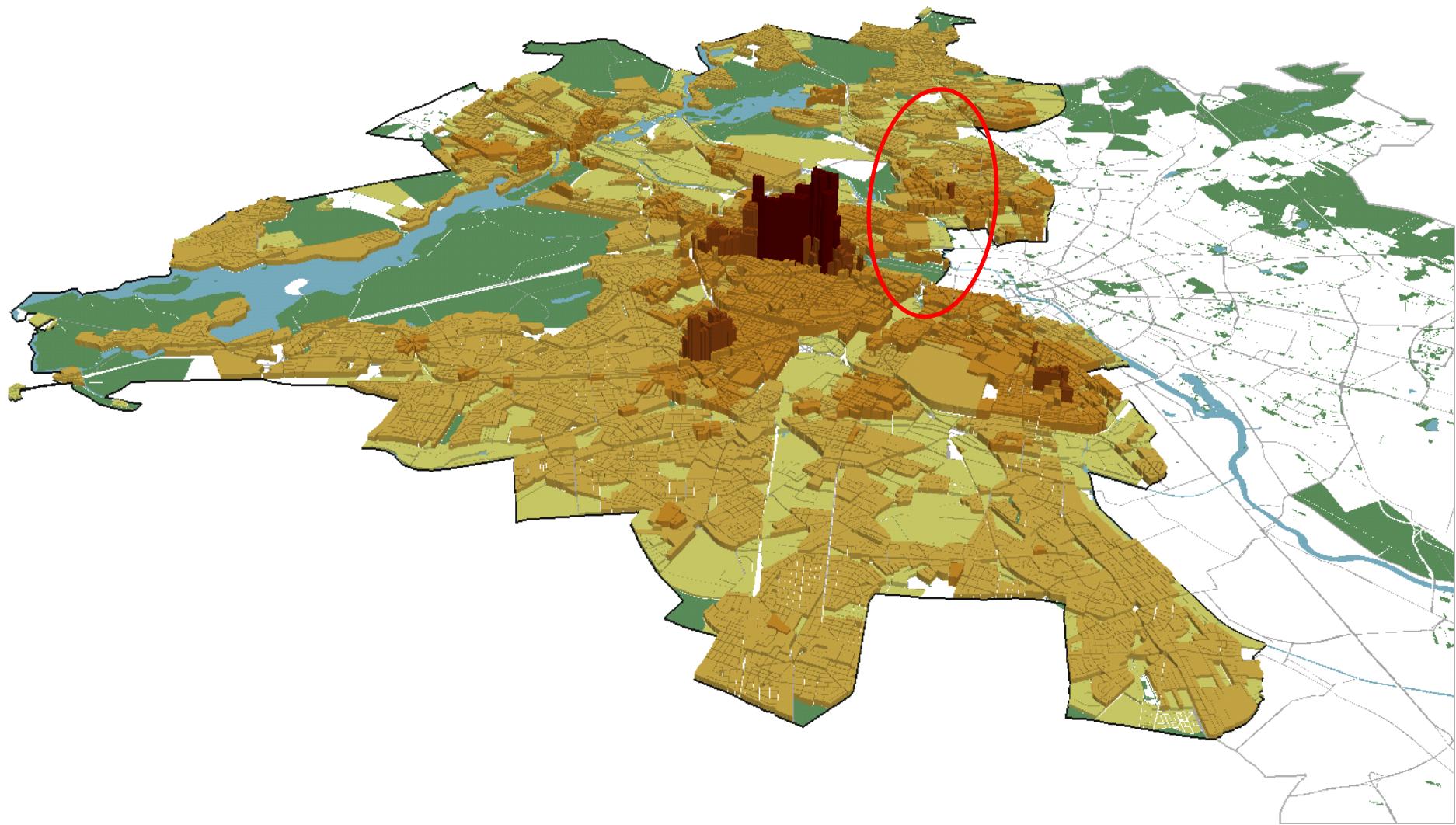
### III LAND PRICES IN 1936 (PRE-DIVISION)

separating spillovers from location fundamentals



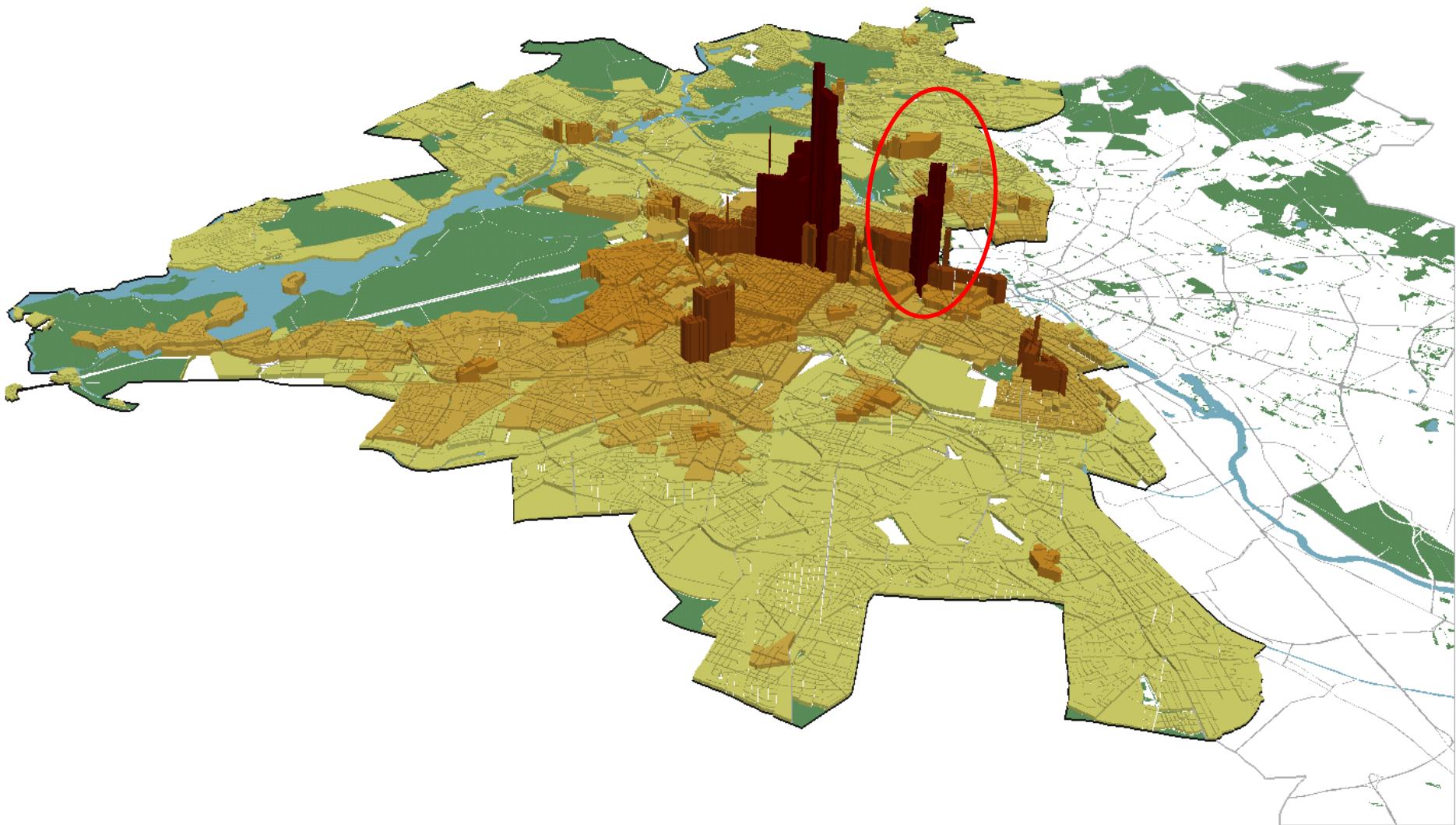
### III LAND PRICES IN 1986 (DIVISION)

separating spillovers from location fundamentals



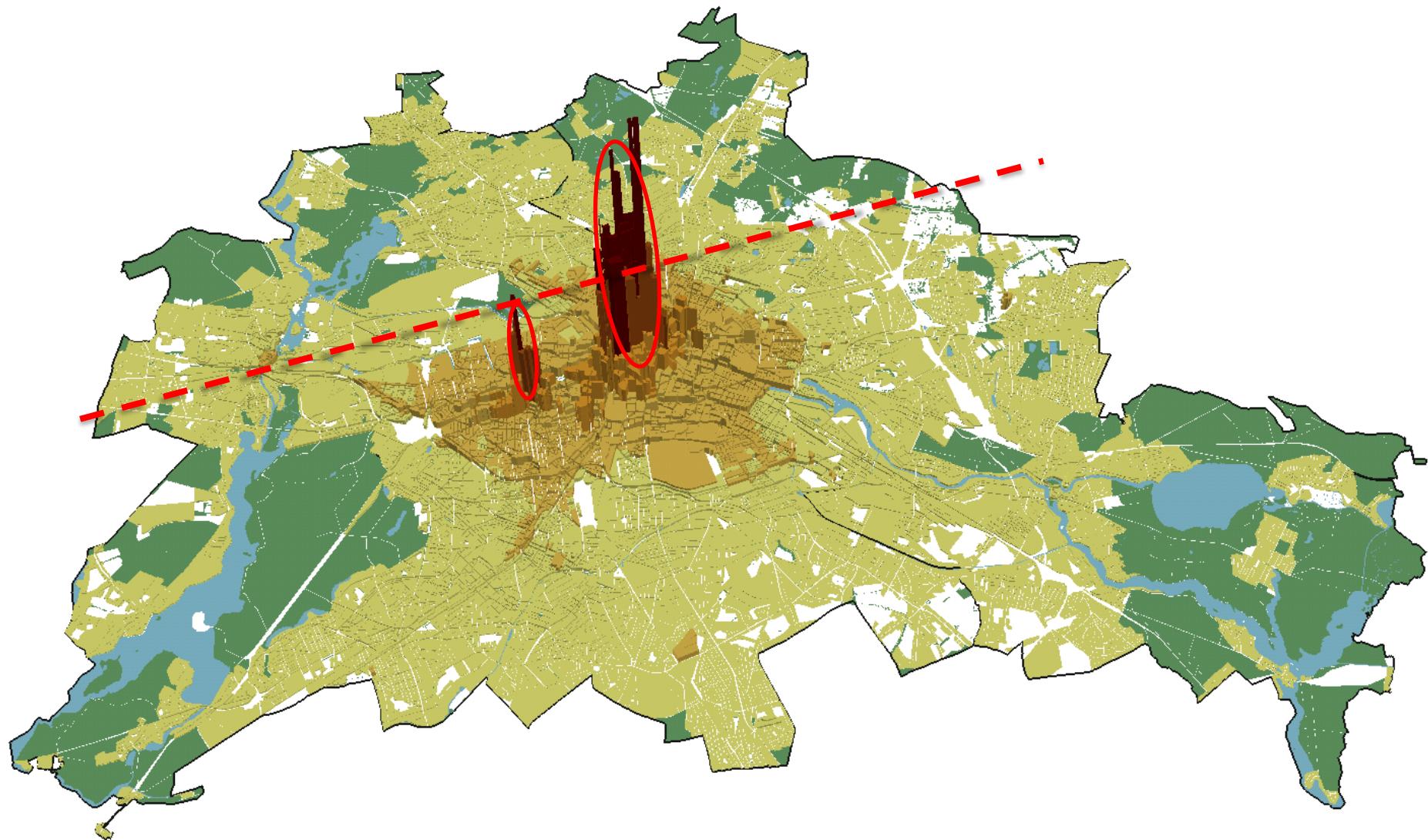
### III LAND PRICES IN 2006 (POST-UNIFICATION)

separating spillovers from location fundamentals



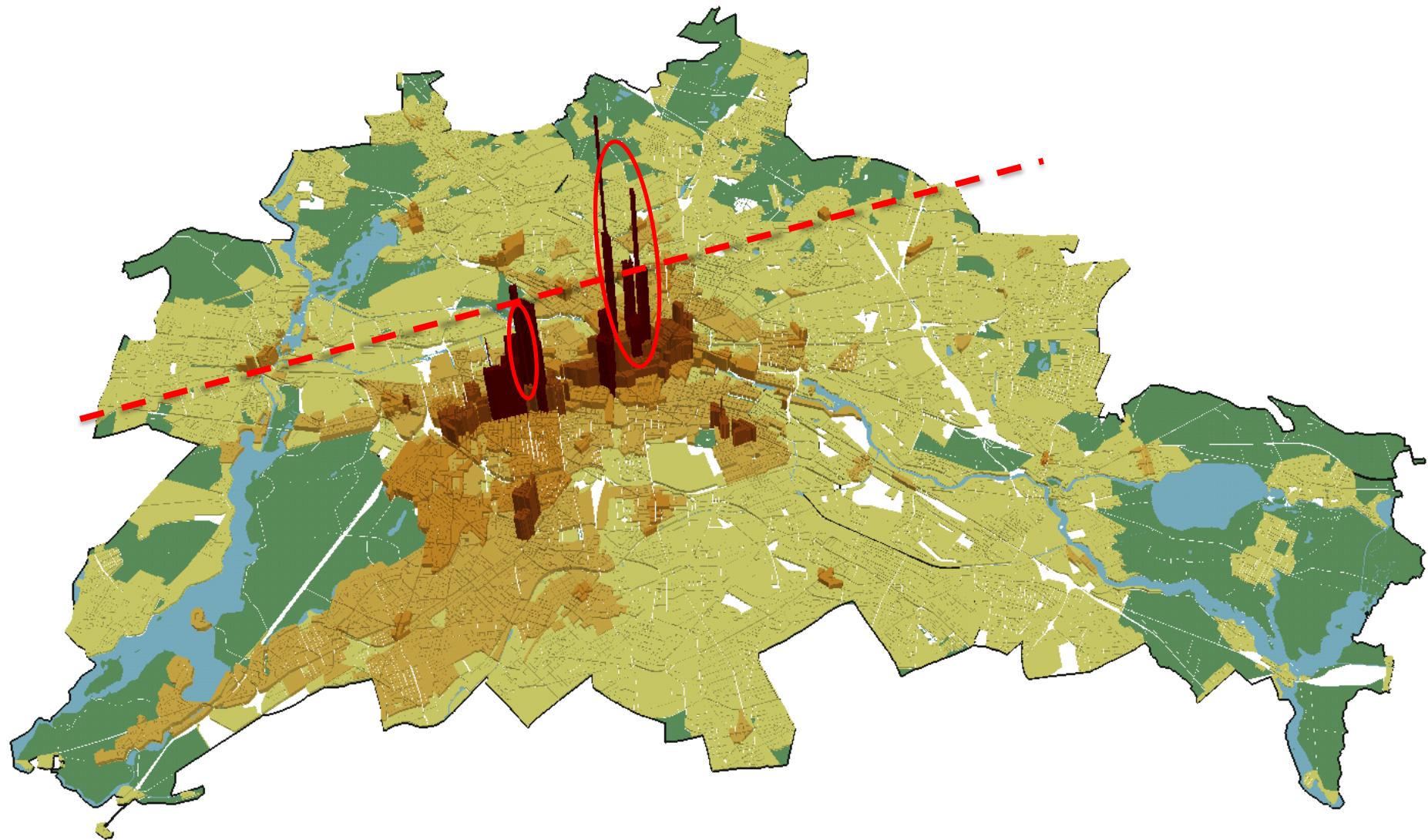
### III LAND PRICES IN 1936 (PRE-DIVISION)

separating spillovers from location fundamentals



### III LAND PRICES IN 2006 (POST-DIVISION)

separating spillovers from location fundamentals



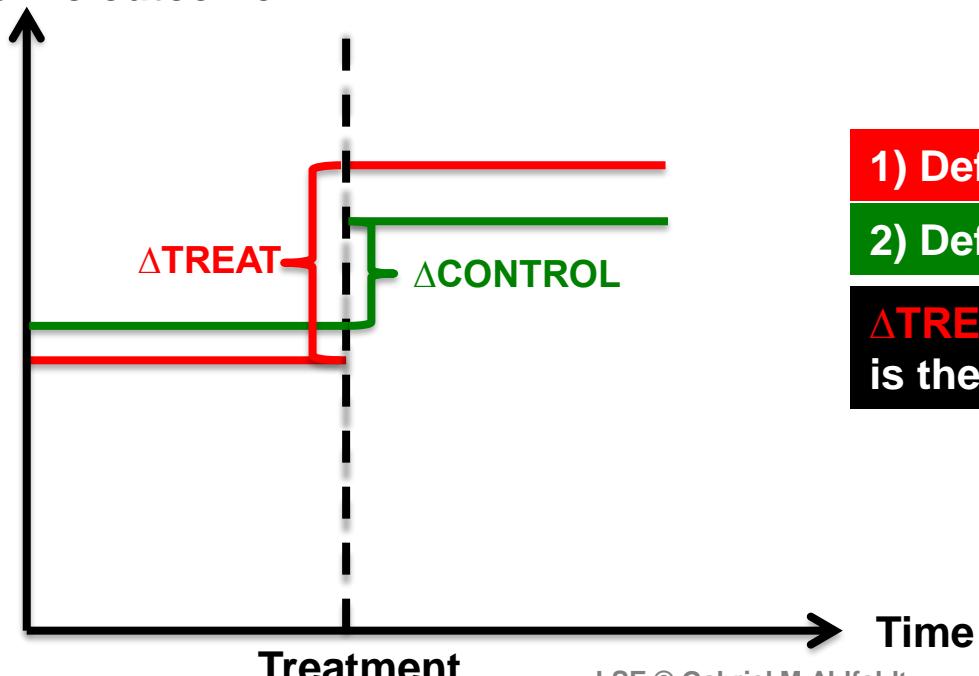
# III HOW TO QUANTIFY THE EFFECT STATISTICALLY?

separating spillovers from location fundamentals

## ▪ Difference-in-differences

- Standard and simple framework for before-after comparisons
- More detail during econometrics classes (GY458)

Economic outcome



1) Define group of treated

2) Define control group

$\Delta\text{TREAT} - \Delta\text{CONTROL}$   
is the difference-in-difference!

# III HOW TO IMPLEMENT HERE?

separating spillovers from location fundamentals

- Event

- Division of the city: Berlin Wall in 1961
- Re-unification in 1989

One DD analysis for division effects

One DD analysis for re-unification effects

- Treatment group

- West Berlin areas close to the CBD
  - Lost/gained spillovers from CBD



- Control group

- West Berlin areas further away
  - Less exposed to changes in spillovers

# III DIFFERENCE-IN-DIFFERENCES SPECIFICATION

separating spillovers from location fundamentals

- **Standard specification:**  $Y_{ist} = \alpha + \beta T_s + \gamma P_t + \delta T_s P_t + \varepsilon_{ist}$ 
  - i: spatial units
  - t: time periods
    - 0 indexes before, 1 indexes after
  - s: group
    - 0 indexes control, 1 indexes treatment
- **Treatment effect:**

$$\delta = (\bar{Y}_{s=1,t=1} - \bar{Y}_{s=1,t=0}) - (\bar{Y}_{s=0,t=1} - \bar{Y}_{s=0,t=0})$$

### III DIFFERENCE-IN-DIFFERENCES SPECIFICATION

separating spillovers from location fundamentals

- **Standard specification:**  $Y_{ist} = \alpha + \beta T_s + \gamma P_t + \delta T_s P_t + \varepsilon_{ist}$ 
  - Can be estimated using standard OLS regressions
- Alternative way of putting it:  $Y_{it} = \alpha + \delta T_i P_t + \mu_i + \varphi_t + \varepsilon_{it}$ 
  - Where  $\mu_i$  and  $\varphi_t$  are individual fixed effects and time fixed effects that replace group ( $T_s$ ) and period ( $P_t$ ) indicators
- In a two-period setting, we can take time differences to get

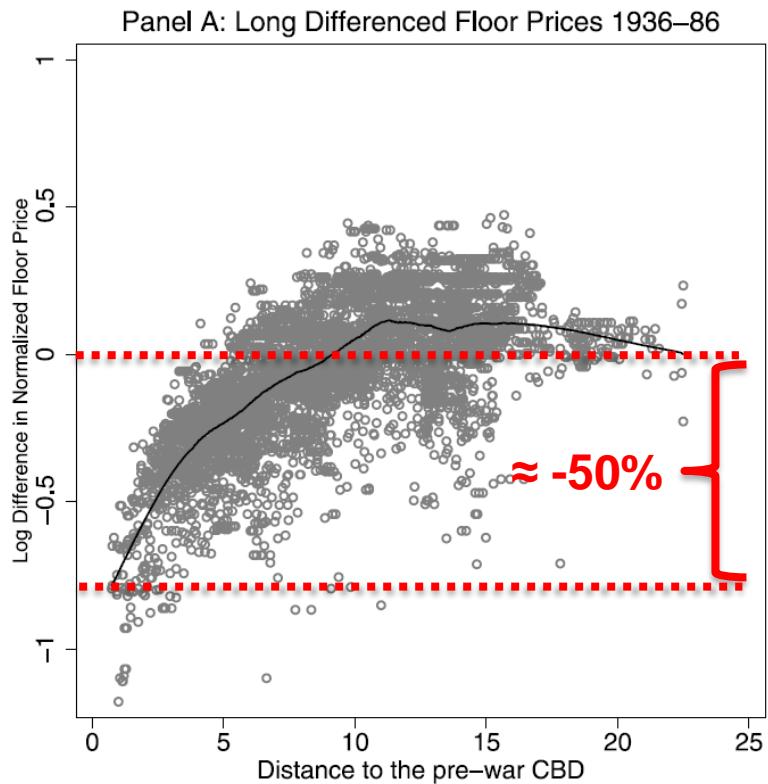
$$\Delta Y_{is} = \varphi + \delta T_s + \varepsilon_{is} \quad \longleftrightarrow \quad \text{ARSW specification}$$

- $\Delta$  denotes before-after difference ( $(Y_{i,s=1} - Y_{i,s=0})$ )
- $\alpha$  and  $\mu_i$  are differenced out since time-invariant
- $\varphi_t$  become a regression constant

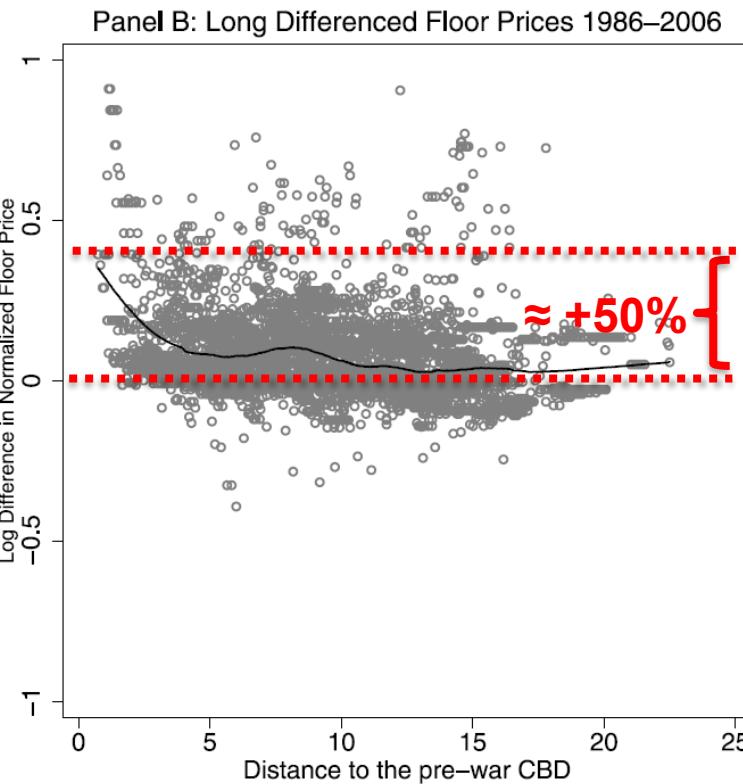
# III TREATMENT EFFECTS ON LAND PRICES

separating spillovers from location fundamentals

## Division



## Unification



“% effect” =  $\exp(\text{“log-point effect”}) - 1$

Spillover effects create huge investment opportunities!

# III DD RESULTS: DIVISON

separating spillovers from location fundamentals

TABLE I  
BASELINE DIVISION DIFFERENCE-IN-DIFFERENCE RESULTS (1936–1986)<sup>a</sup>

	(1) $\Delta \ln Q$	(2) $\Delta \ln Q$	(3) $\Delta \ln Q$	(4) $\Delta \ln Q$	(5) $\Delta \ln Q$	(6) $\Delta \ln \text{EmpR}$	(7) $\Delta \ln \text{EmpR}$	(8) $\Delta \ln \text{EmpW}$	(9) $\Delta \ln \text{EmpW}$
CBD 1	-0.800*** (0.071)	-0.567*** (0.071)	-0.524*** (0.071)	-0.503*** (0.071)	-0.565*** (0.077)	-1.332*** (0.383)	-0.975*** (0.311)	-0.691* (0.408)	-0.639* (0.338)
CBD 2	-0.655*** (0.042)	-0.422*** (0.047)	-0.392*** (0.046)	-0.360*** (0.043)	-0.400*** (0.050)	-0.715** (0.299)	-0.361 (0.280)	-1.253*** (0.293)	-1.367*** (0.243)
CBD 3	-0.543*** (0.034)	-0.306*** (0.039)	-0.294*** (0.037)	-0.258*** (0.032)	-0.247*** (0.034)	-0.911*** (0.239)	-0.460** (0.206)	-0.341 (0.241)	-0.471** (0.190)
CBD 4	-0.436*** (0.022)	-0.207*** (0.033)	-0.193*** (0.033)	-0.166*** (0.030)	-0.176*** (0.026)	-0.356** (0.145)	-0.259 (0.159)	-0.512*** (0.199)	-0.521*** (0.169)
CBD 5	-0.353*** (0.016)	-0.139*** (0.024)	-0.123*** (0.024)	-0.098*** (0.023)	-0.100*** (0.020)	-0.301*** (0.110)	-0.143 (0.113)	-0.436*** (0.151)	-0.340*** (0.124)
CBD 6	-0.291*** (0.018)	-0.125*** (0.019)	-0.094*** (0.017)	-0.077*** (0.016)	-0.090*** (0.016)	-0.360*** (0.100)	-0.135 (0.089)	-0.280** (0.130)	-0.142 (0.116)
Inner Boundary 1–6			Yes	Yes	Yes		Yes		Yes
Outer Boundary 1–6			Yes	Yes	Yes		Yes		Yes
Kudamm 1–6				Yes	Yes		Yes		Yes
Block Characteristics					Yes		Yes		Yes
District Fixed Effects		Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Observations	6,260	6,260	6,260	6,260	6,260	5,978	5,978	2,844	2,844
R <sup>2</sup>	0.26	0.51	0.63	0.65	0.71	0.19	0.43	0.12	0.33

<sup>a</sup> $Q$  denotes the price of floor space. EmpR denotes employment by residence. EmpW denotes employment by workplace. CBD1–CBD6 are six 500 m distance grid cells for distance from the pre-war CBD. Inner Boundary 1–6 are six 500 m grid cells for distance to the Inner Boundary between East and West Berlin. Outer Boundary 1–6 are six 500 m grid cells for distance to the outer boundary between West Berlin and East Germany. Kudamm 1–6 are six 500 m grid cells for distance to Breitscheid Platz on the Kurfürstendamm. The coefficients on the other distance grid cells are reported in Table A.2 of the Technical Data Appendix. Block characteristics include the log distance to schools, parks and water, the land area of the block, the share of the block's built-up area destroyed during the Second World War, indicators for residential, commercial and industrial land use, and indicators for whether a block includes a government building and urban regeneration policies post-reunification. Heteroscedasticity and Autocorrelation Consistent (HAC) standard errors in parentheses (Conley (1999)). \* significant at 10%; \*\* significant at 5%; \*\*\* significant at 1%.

Significant and robust treatment effects on land prices, population, and employment!

# III DD RESULTS: REUNIFICATION

separating spillovers from location fundamentals

TABLE II  
BASELINE REUNIFICATION DIFFERENCE-IN-DIFFERENCE RESULTS (1986–2006)<sup>a</sup>

	(1) $\Delta \ln Q$	(2) $\Delta \ln Q$	(3) $\Delta \ln Q$	(4) $\Delta \ln Q$	(5) $\Delta \ln Q$	(6) $\Delta \ln \text{EmpR}$	(7) $\Delta \ln \text{EmpR}$	(8) $\Delta \ln \text{EmpW}$	(9) $\Delta \ln \text{EmpW}$
CBD 1	0.398*** (0.105)	0.408*** (0.090)	0.368*** (0.083)	0.369*** (0.081)	0.281*** (0.088)	1.079*** (0.307)	1.025*** (0.297)	1.574*** (0.479)	1.249** (0.517)
CBD 2	0.290*** (0.111)	0.289*** (0.096)	0.257*** (0.090)	0.258*** (0.088)	0.191** (0.087)	0.589* (0.315)	0.538* (0.299)	0.684** (0.326)	0.457 (0.334)
CBD 3	0.122*** (0.037)	0.120*** (0.033)	0.110*** (0.032)	0.115*** (0.032)	0.063** (0.028)	0.340* (0.180)	0.305* (0.158)	0.326 (0.216)	0.158 (0.239)
CBD 4	0.033*** (0.013)	0.031 (0.023)	0.030 (0.022)	0.034 (0.021)	0.017 (0.020)	0.110 (0.068)	0.034 (0.066)	0.336** (0.161)	0.261 (0.185)
CBD 5	0.025*** (0.010)	0.018 (0.015)	0.020 (0.014)	0.020 (0.014)	0.015 (0.013)	-0.012 (0.056)	-0.056 (0.057)	0.114 (0.118)	0.066 (0.131)
CBD 6	0.019** (0.009)	-0.000 (0.012)	-0.000 (0.012)	-0.003 (0.012)	0.005 (0.011)	0.060 (0.039)	0.053 (0.041)	0.049 (0.095)	0.110 (0.098)
Inner Boundary 1–6			Yes	Yes	Yes		Yes		Yes
Outer Boundary 1–6			Yes	Yes	Yes		Yes		Yes
Kudamm 1–6				Yes	Yes		Yes		Yes
Block Characteristics					Yes		Yes		Yes
District Fixed Effects		Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Observations	7,050	7,050	7,050	7,050	7,050	6,718	6,718	5,602	5,602
R <sup>2</sup>	0.08	0.32	0.34	0.35	0.43	0.04	0.07	0.03	0.06

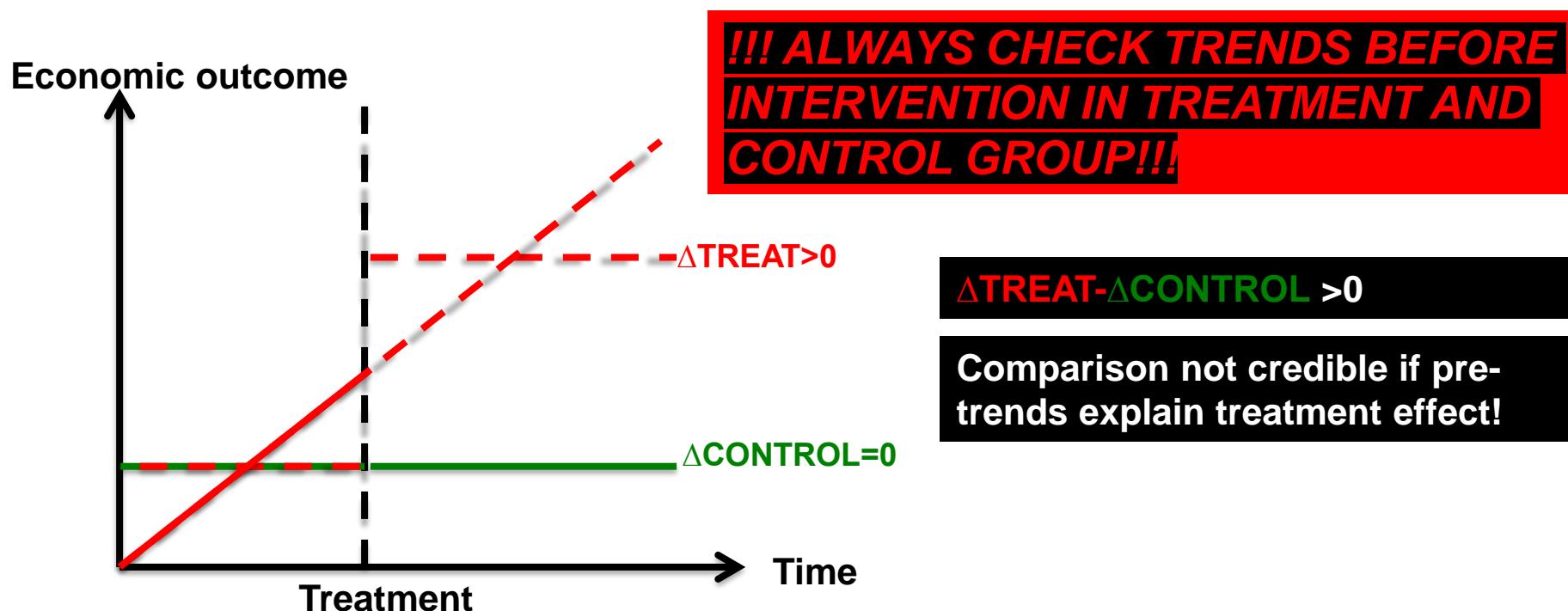
<sup>a</sup>  $Q$  denotes the price of floor space. EmpR denotes employment by residence. EmpW denotes employment by workplace. CBD1–CBD6 are six 500 m distance grid cells for distance from the pre-war CBD. Inner Boundary 1–6 are six 500 m grid cells for distance to the Inner Boundary between East and West Berlin. Outer Boundary 1–6 are six 500 m grid cells for distance to the outer boundary between West Berlin and East Germany. Kudamm 1–6 are six 500 m grid cells for distance to Breitscheid Platz on the Kurfürstendamm. The coefficients on the other distance grid cells are reported in Table A.4 of the Technical Data Appendix. Block characteristics include the log distance to schools, parks and water, the land area of the block, the share of the block's built-up area destroyed during the Second World War, indicators for residential, commercial and industrial land use, and indicators for whether a block includes a government building and urban regeneration policies post-reunification. Heteroscedasticity and Autocorrelation Consistent (HAC) standard errors in parentheses (Conley (1999)). \* significant at 10%; \*\* significant at 5%; \*\*\* significant at 1%.

Significant and robust treatment effects on land prices, population, and employment!

### III NON-PARALLEL TRENDS

separating spillovers from location fundamentals

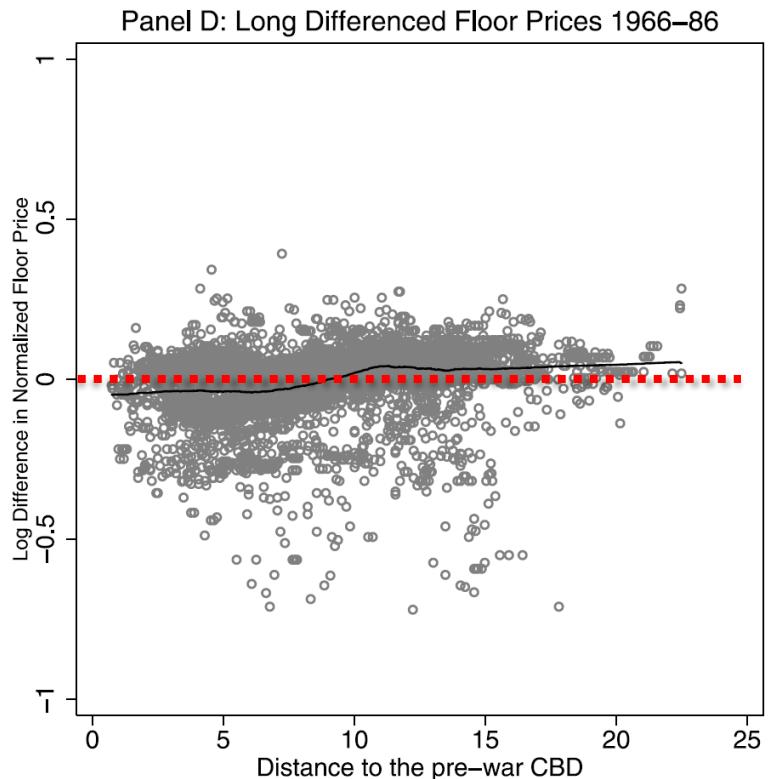
- Key DD assumption: In absence of treatment, treatment and control group would follow parallel trend
- Counterfactual trends cannot be observed, but “pre-trends” can



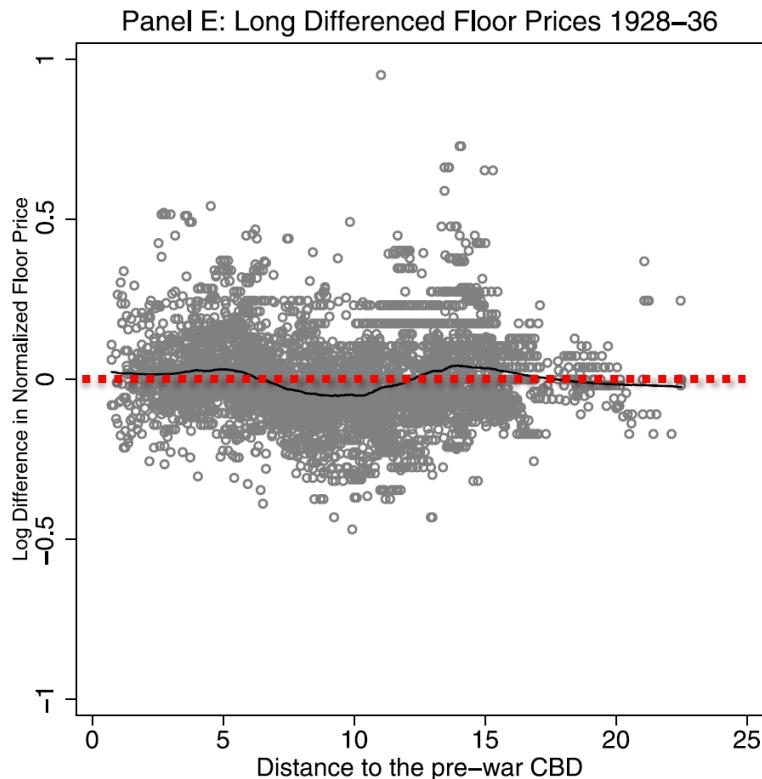
# III PRE-TREND EVALUATION

separating spillovers from location fundamentals

## Before unification



## Before division



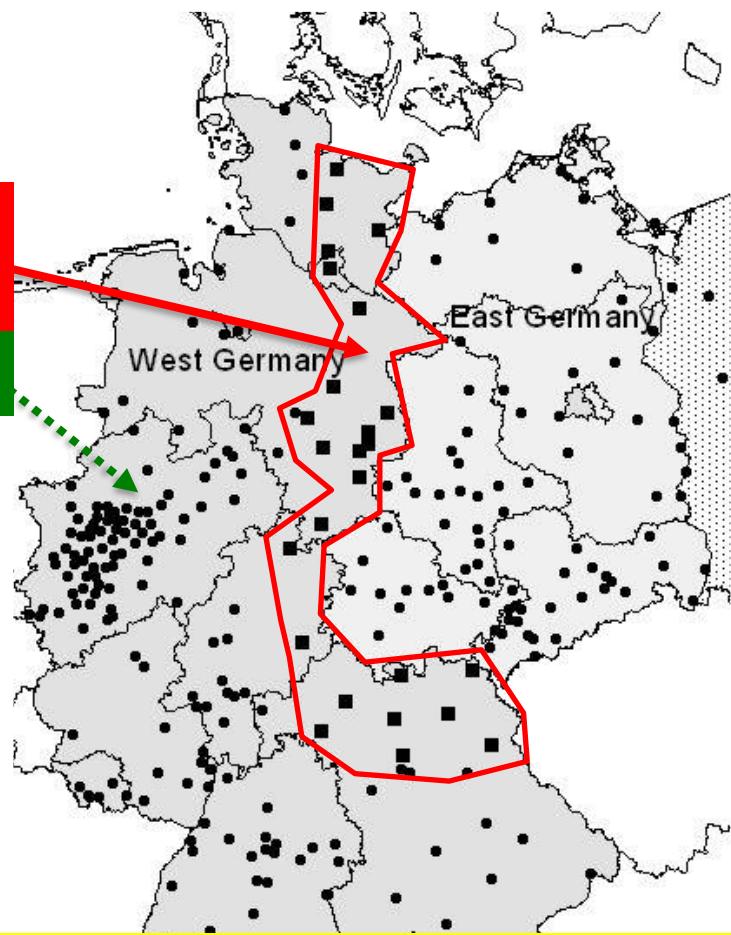
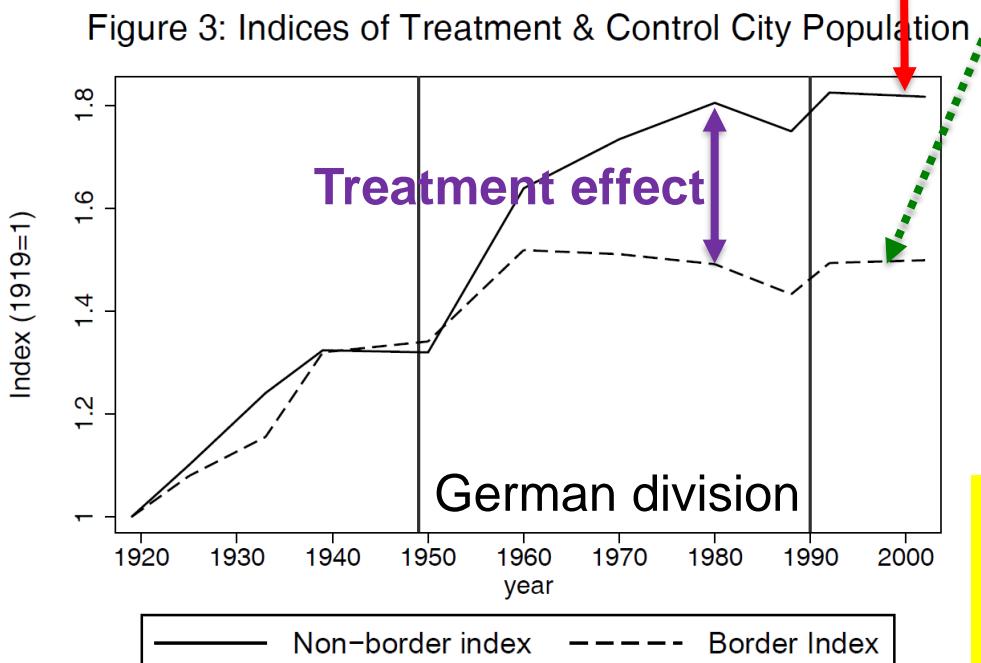
**Placebo tests: No effect of treatment effect where no treatment  
=> parallel-trends assumption credible**

### III REDDING & STURM (2008)

separating spillovers from location fundamentals

**Treatment group: West German cities close to inner-German border**

**Control group: Other West German cities**



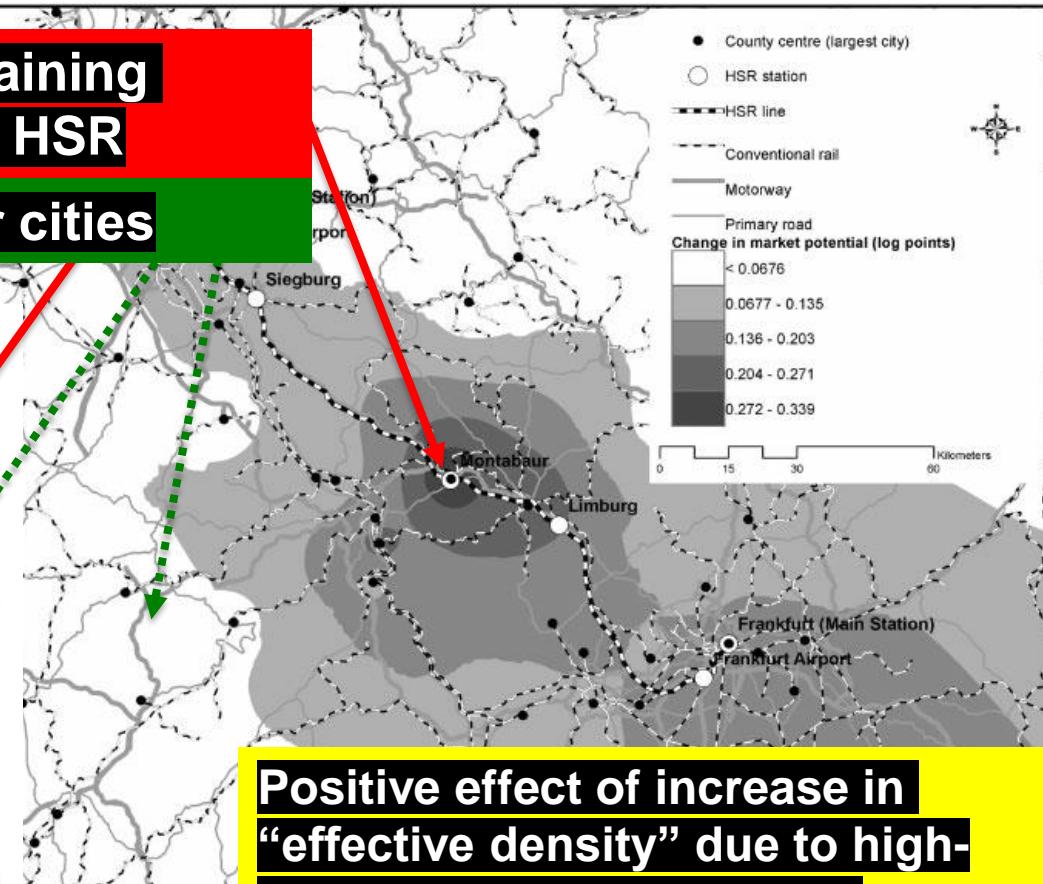
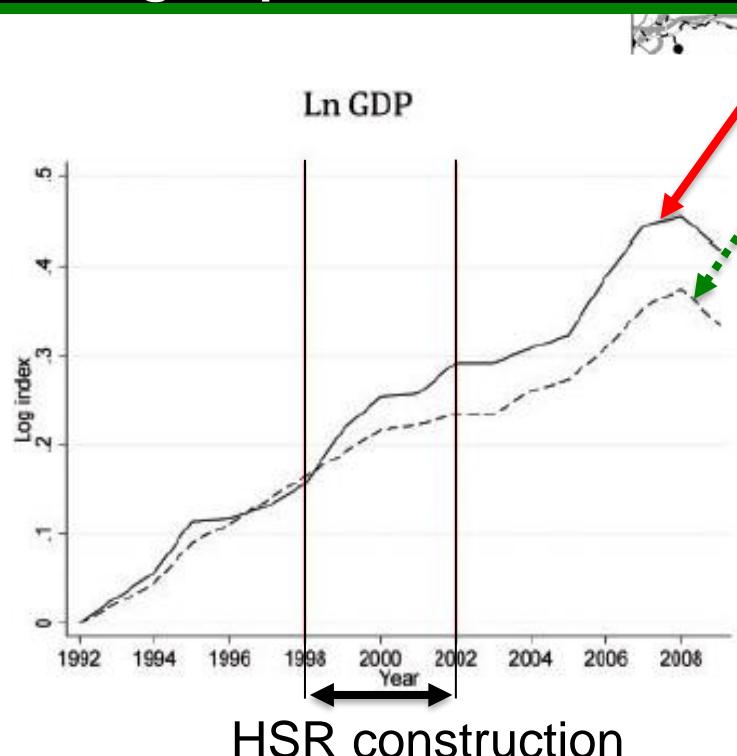
**Negative impact of loss of agglomeration due to division on population growth**

### III AHLFELDT & FEDDERSEN (2018)

separating spillovers from location fundamentals

**Treatment group: Small cities gaining access to agglomeration due to HSR**

**Control group: “Matched” other cities**



**Positive effect of increase in  
“effective density” due to high-  
speed rail connections on  
productivity and GDP**

# III CHECK LIST FOR A GOOD DD STUDY

separating spillovers from location fundamentals

- 1) Show descriptive stats for treatment and control group
    - Mean, s.d., etc. for outcome variable and other observables
  - 2) Show trends in outcome for treatment and control group
    - Plot the trends in the outcome over time
    - Are the trends parallel before the treatment?
    - Conduct an event study (Autor, 2003)
  - 3) “Narrow” the control group to improve comparability
    - Propensity score matching
      - Rosenbaum and Rubin, 1983
    - Synthetic control method
      - Abadie and Gardeazabal, 2003
    - Inverse probability weighting
      - E.g. Hernan et al., 2001
    - Entropy balancing
      - Hainmueller, 2012
  - 4) Address non-parallel trends
    - Parametric control for trends
      - E.g. Ahlfeldt, Moeller, Waights, Wendland, (2017)
    - Time differencing
      - Lee, 2016
  - 5) Coupled with discontinuity designs
    - Ahlfeldt, Koutroumpis, Valletti, 2017
    - Duranton, Gobillon, Overman, 2011
- 
- Always do!
- Always do!
- Makes an impression...
- Do if 1) does not look right!  
(always makes an impression)
- Do if 2) does not look right!
- Do if possible

# III SEPARATING SPILLOVERS FROM FUNDAMENTALS

roadmap

- This time: *The urban economy in general equilibrium*
  - 1) Recap
    - Compensating differentials, location choice, supply side
  - 2) The Ahlfeldt-Redding-Sturm-Wolf model
    - Model setup
  - 3) Separating spillovers from location fundamentals
    - Reduced-form evidence
    - Difference-in-difference analysis
  - 4) Structural estimation and simulation
    - Identifying structural parameters
    - Simulating the effect of a new metro line

# IV BACK TO ARSW

structural estimation and simulation

- **ARSW model is a structural general equilibrium model**
  - Once structural parameters are identified (or plausibly assumed), we can use the model to **simulate effects of shocks**
- **GMM estimation strategy**
  - Use the structure of the model and the shock from the Berlin Wall to **identify structural parameters**
  - **Find parameters** that ensure changes in fundamentals over time are uncorrelated with distance from the CBD
    - **A: Fundamentals don't change systematically over time**
- **Simulation strategy**
  - **Shock the system, e.g. by building a new metro line**
  - **Let model converge to a new equilibrium**

# IV STRUCTURAL ESTIMATION RESULTS I

structural estimation and simulation

TABLE V

GENERALIZED METHOD OF MOMENTS (GMM) ESTIMATION RESULTS<sup>a</sup>

	(1) Division Efficient GMM	(2) Reunification Efficient GMM	(3) Division and Reunification Efficient GMM
Commuting Travel Time Elasticity ( $\kappa\epsilon$ )	0.0951*** (0.0016)	0.1011*** (0.0016)	0.0987*** (0.0016)
Commuting Heterogeneity ( $\varepsilon$ )	6.6190*** (0.0939)	6.7620*** (0.1005)	6.6941*** (0.0934)
Productivity Elasticity ( $\lambda$ )	0.0793*** (0.0064)	0.0496*** (0.0079)	0.0710*** (0.0054)
Productivity Decay ( $\delta$ )	0.3585*** (0.1030)	0.9246*** (0.3525)	0.3617*** (0.0782)
Residential Elasticity ( $\eta$ )	0.1548*** (0.0092)	0.0757** (0.0313)	0.1553*** (0.0083)
Residential Decay ( $\rho$ )	0.9094*** (0.2968)	0.5531 (0.3979)	0.7595*** (0.1741)

**Workers provide more labour at a location if wage is higher!**

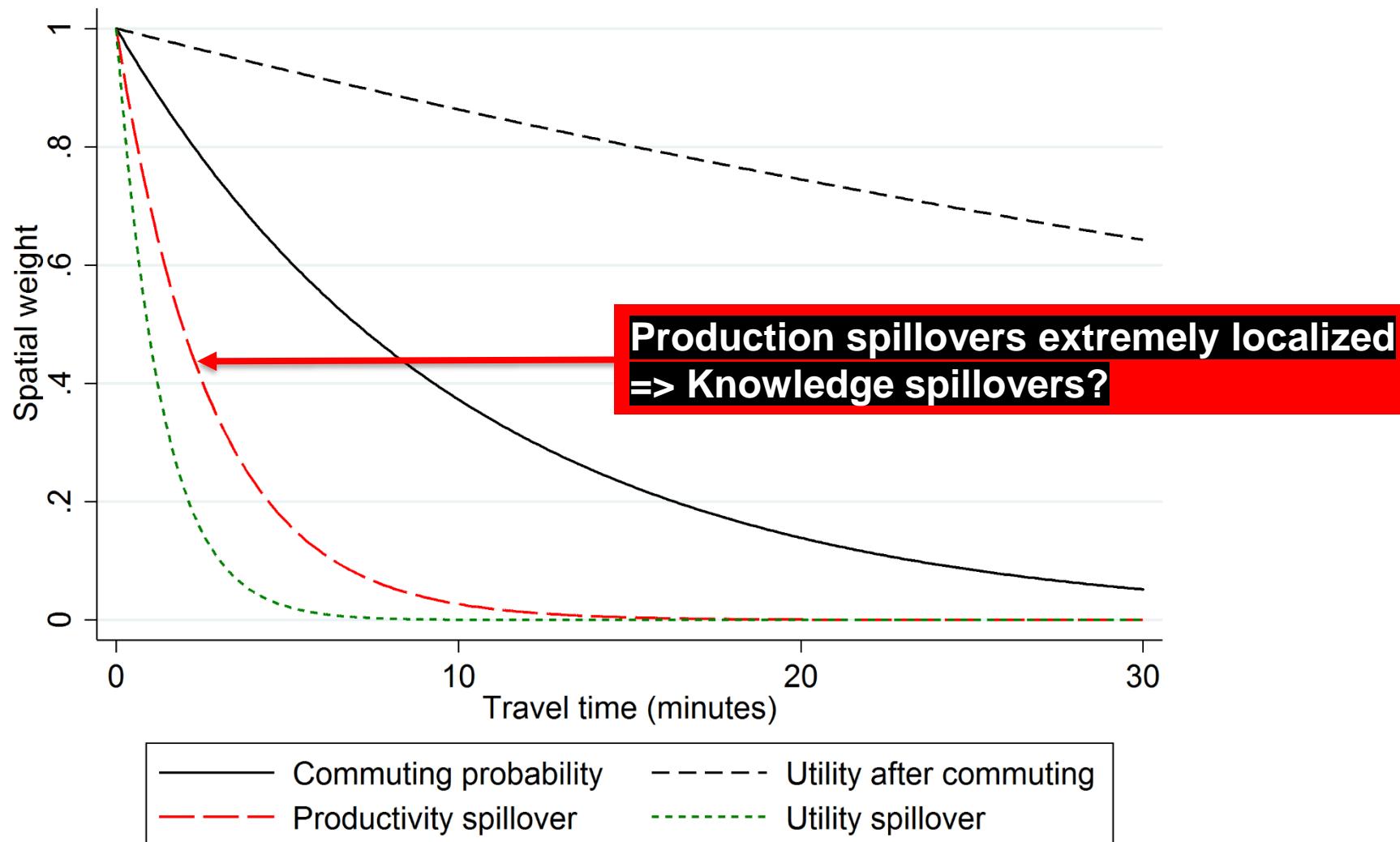
**Production spillovers matter**

**Residential spillovers matter, too**

<sup>a</sup>Generalized Method of Moments (GMM) estimates. Heteroscedasticity and Autocorrelation Consistent (HAC) standard errors in parentheses (Conley (1999)). \* significant at 10%; \*\* significant at 5%; \*\*\* significant at 1%.

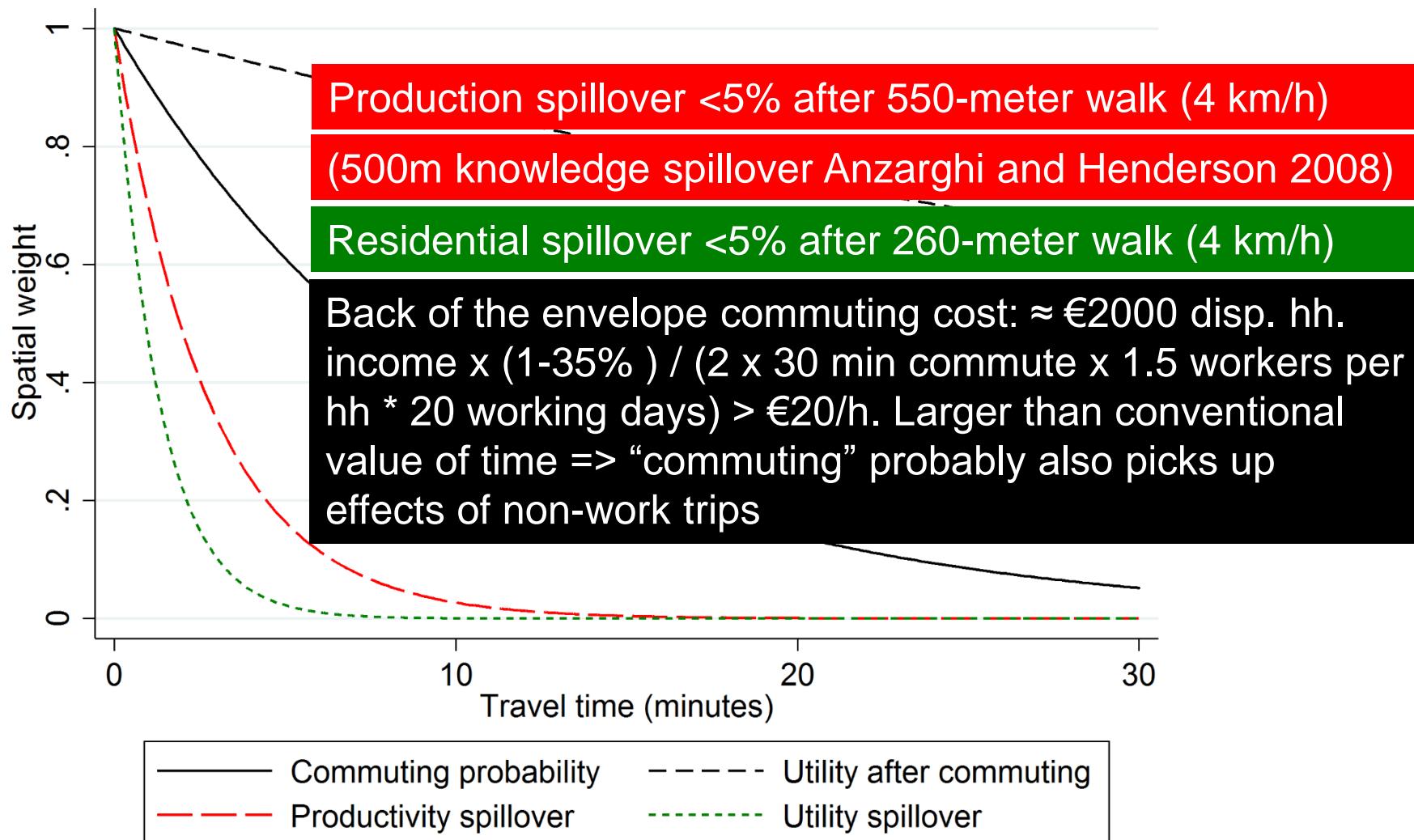
# IV STRUCTURAL ESTIMATION RESULTS II

structural estimation and simulation



## IV STRUCTURAL ESTIMATION RESULTS II

structural estimation and simulation



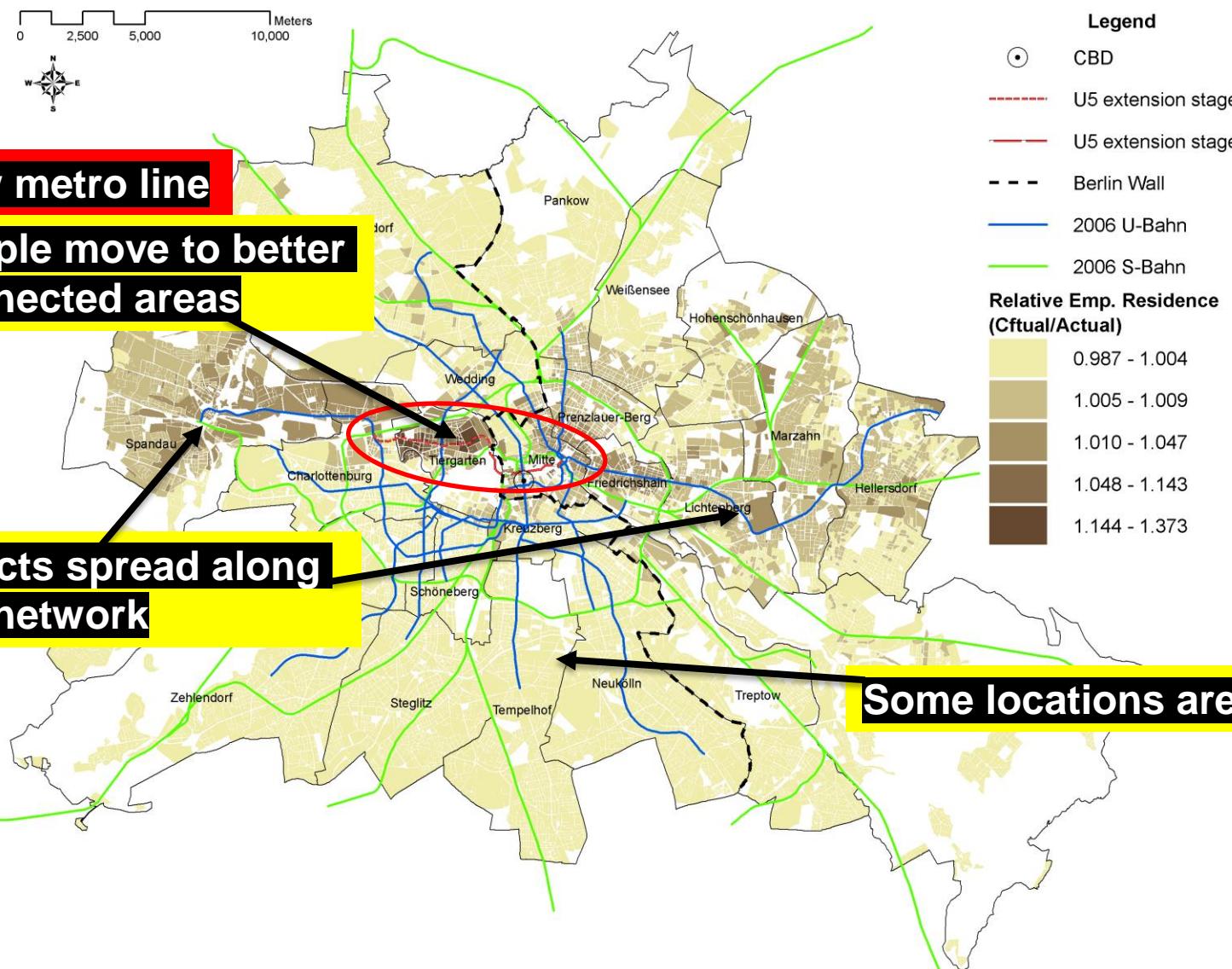
# IV SIMULATION

structural estimation and simulation

- **Can use the model to predict the effects of exogenous shocks on various outcomes**
  - Distributions of rent, wages, population, employment, in/outmigration
- **General equilibrium implies that we can model relocations**
  - If some locations win, others can lose
- **Ahlfeldt, Redding, Sturm (2016)**
  - Focus on the effect of a **new metro line** to be open in 2020.  
But could also predict effects of other things
    - A new edge city
    - Change in height regulation
    - Increase in agglomeration economies

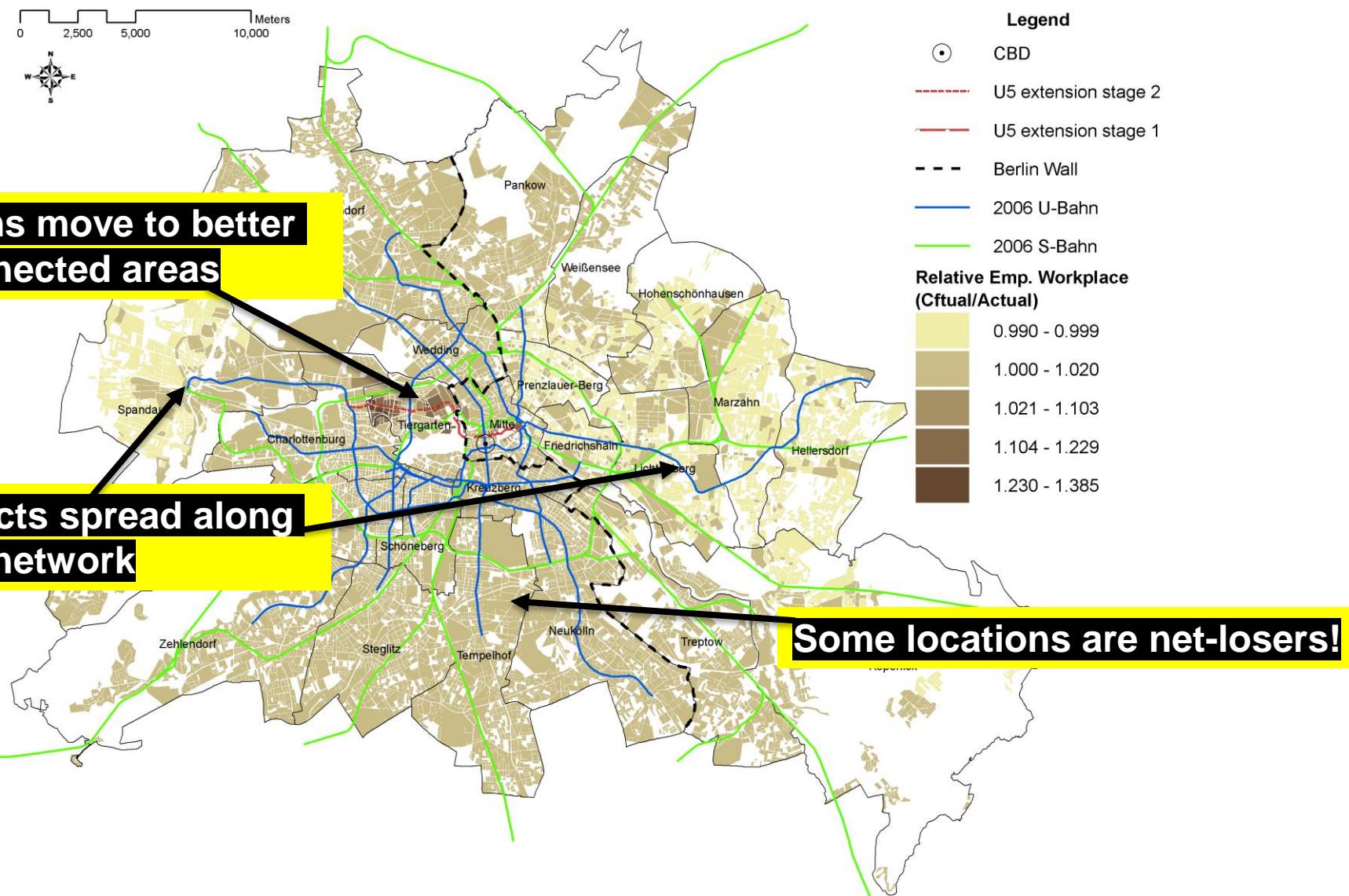
# IV SIMULATED IMPACT OF “U5” ON POPULATION

structural estimation and simulation



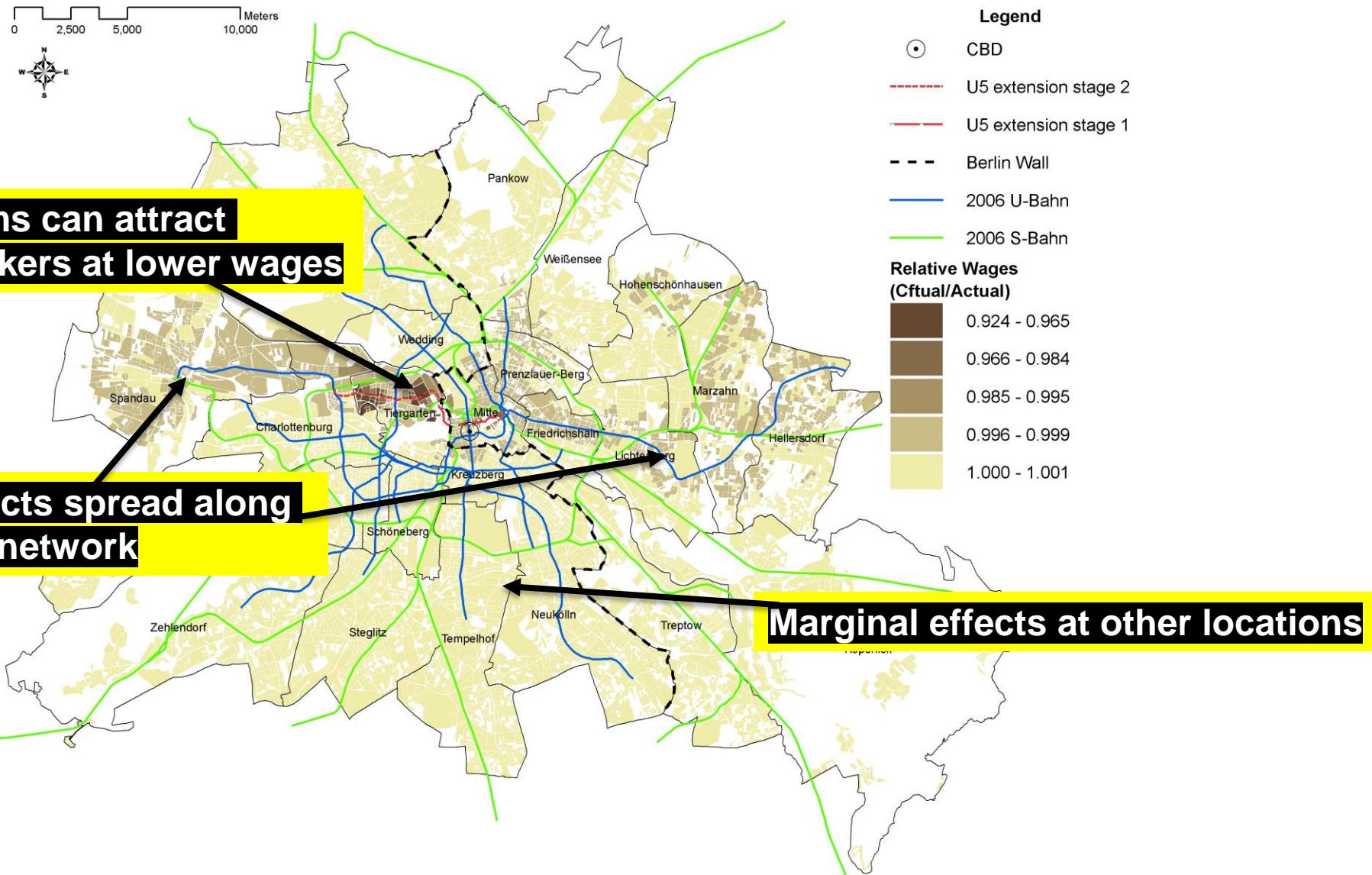
# IV SIMULATED IMPACT OF “U5” ON EMPLOYMENT

structural estimation and simulation



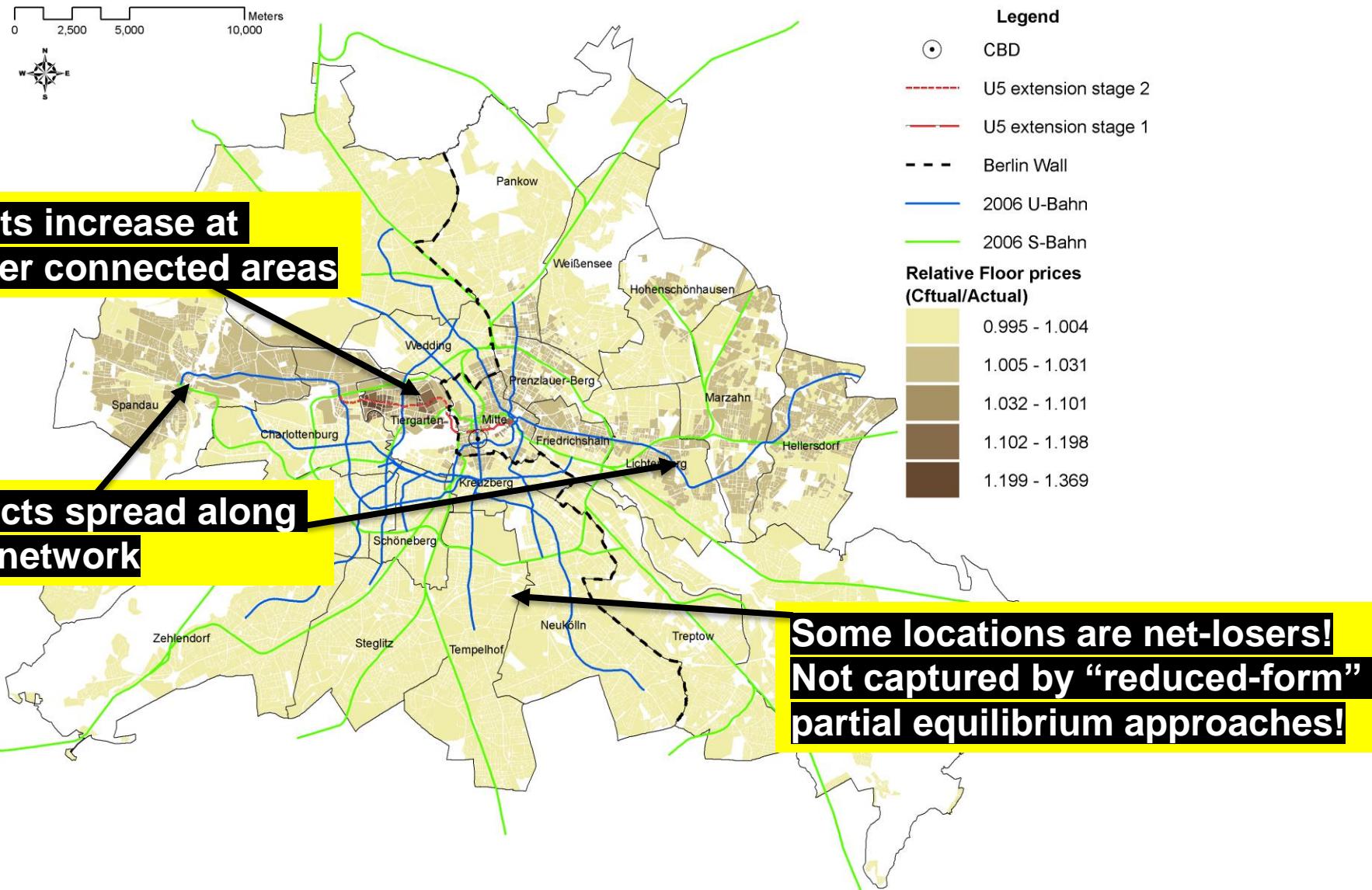
# IV SIMULATED IMPACT OF “U5” ON WAGES

structural estimation and simulation



# IV SIMULATED IMPACT OF “U5” ON RENTS

structural estimation and simulation



# IV TESTING THE MODEL'S PREDICTIONS

structural estimation and simulation

- How to evaluate the „out-of-sample“ predictive power?
  - Want to test the model using data that model hasn't used
    - Model simulation based on 2006 data
    - Test the model predictions using 2000-2015 data
      - Credible announcement: 2009
  - Approach similar to Ahlfeldt (2013), but in general equilibrium

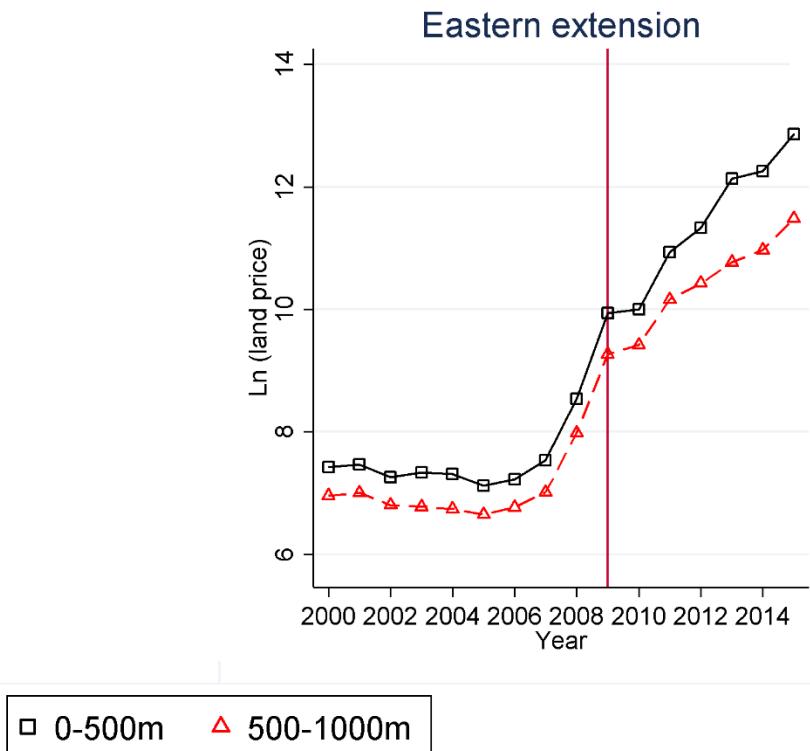
**Q: Do adjustment in the real word match the ex-ante model predictions?**

**Q: Should we make investment decisions based on model predictions?**

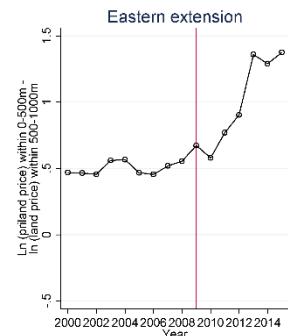
# IV TREATED VS CONTROL

structural estimation and simulation

Price trends at varying distances from U5 stations



Relative price trends within 500m vs. 500-1000m of U5 stations



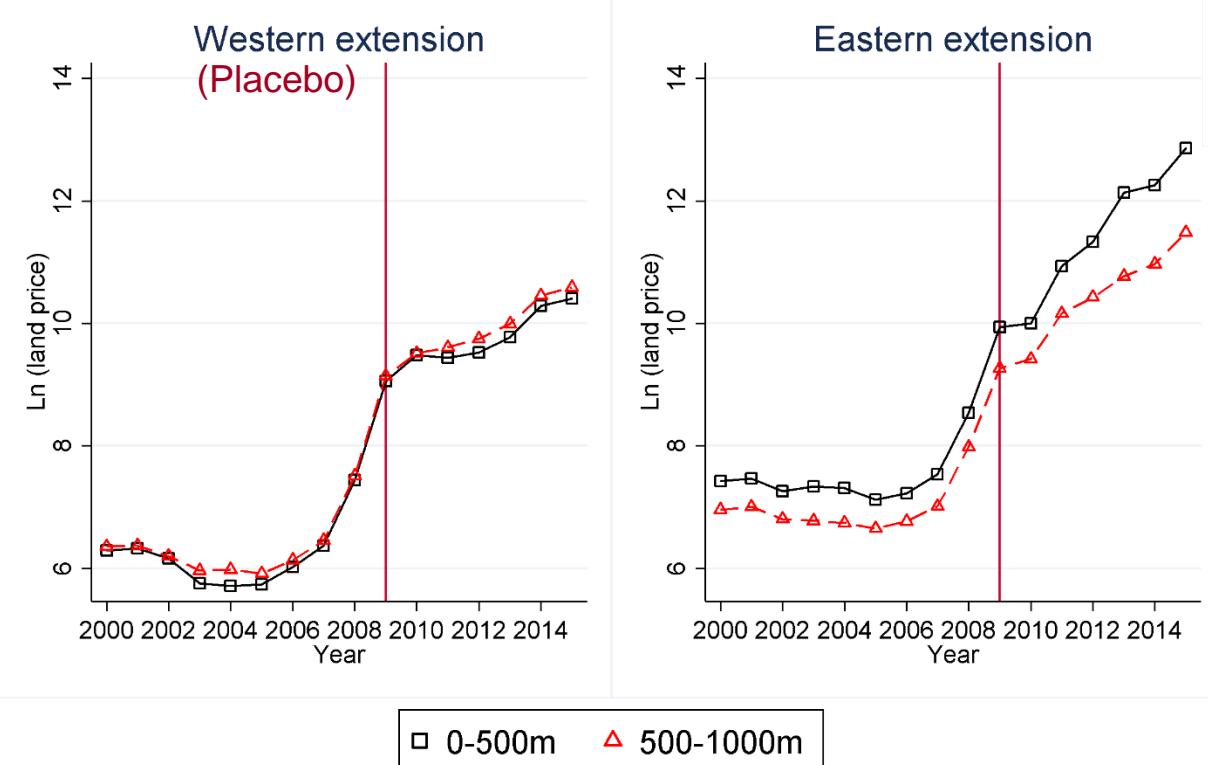
Notes: Markers denote differences in mean prices within year bins.  
Horizontal line denotes the completion of the U55 segment.

**Measurable capitalization effects after partial completion of line**

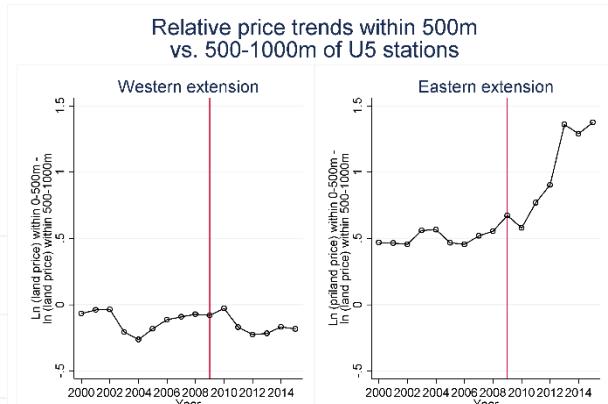
# IV “PLACEBO” TEST

structural estimation and simulation

## Price trends at varying distances from U5 stations



Notes: Markers denote mean prices within year bins.  
Horizontal line denotes the completion of the U55 segment.



**Measurable capitalization effects after partial completion of line**

# IV DID SEE IT COMING...

structural estimation and simulation



f t g+ LOGIN REGISTRIEREN  
 Bitte Suchbegriff eingeben

STARTSEITE **1** POLITIK BERLIN WIRTSCHAFT SPORT KULTUR WELT MEINUNG MEDIEN WISSEN QUEER VERBRAUCHER  
 BEZIRKE MEHR BERLIN POLIZEI STADTLEBEN FAHRRAD VERKEHR SCHULE FAMILIE NACHRUGE BER

Home > Berlin > Immobilien: U5 treibt Mieten in die Höhe

Anzeige

0

Immobilien

## U5 treibt Mieten in die Höhe

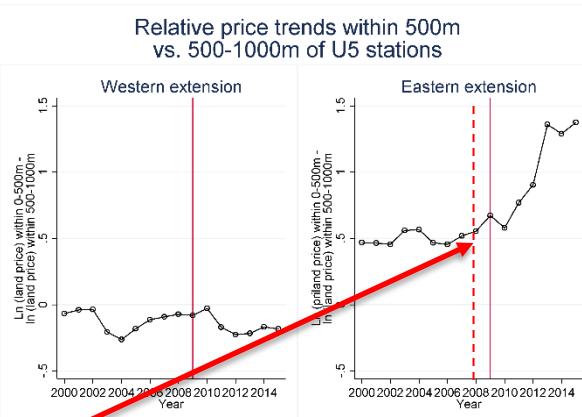


Anzeige

Die Grundstücke an der Linienführung der U5 gewinnen deutlich an Wert. Ein Wissenschaftler schlägt deshalb vor, die Anrainer an den Kosten zu beteiligen. Der Senat hält davon nichts. KLAUS KURPUWEIT

Von einem besseren Anschluss des Hauptbahnhofs an das Netz von U- und S-Bahn würden nicht nur Fahrgäste, sondern auch Immobilieneigentümer profitieren. Mieter dagegen müssten damit rechnen, dass sie mehr für ihre Läden oder Wohnungen zahlen müssen. Der Gesamtwert der Grundstücke im Einzugsgebiet des Hauptbahnhofs könnte sich nach einer wissenschaftlichen Untersuchung um bis zu 133 Millionen Euro erhöhen. Einzelne Grundstücke könnten maximal elf Prozent wertvoller werden. Ökonomisch sinnvoll wäre es deshalb, die Eigentümer der Grundstücke, die im Wert steigen, an den Kosten des S- und U-Bahn-Ausbaus zu beteiligen, schlägt der Volkswirt Gabriel Ahlfeldt von der Universität Hamburg vor. Die Stadtentwicklungsverwaltung lehnt dies ab. Nach Ahlfeldts Berechnungen würde allein der Bau der U 5 vom Brandenburger Tor bis zum Alexanderplatz den Wert der Grundstücke um bis zu 93 Millionen Euro steigen lassen. Die Effekte seien hier besonders stark, weil wegen der hohen Immobilienpreise im Bereich Unter den Linden selbst relativ kleine prozentuale Veränderungen zu hohen Summen führen, sagte Ahlfeldt.

08.06.2008 00:00 Uhr



**Measurable capitalization effects after partial completion of line**

### Aktuell im Ressort



Charlottenburg/Neukölln  
Mehrere Verkehrsunfälle mit...



Volksentscheide in Berlin  
Bringt nichts, gilt nicht

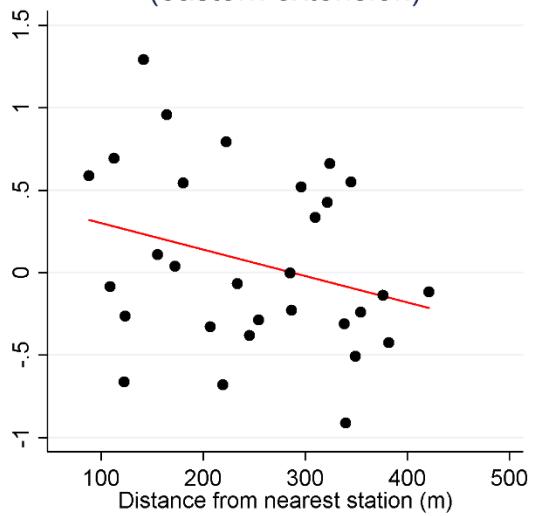


Berlin-Lichtenberg  
Schwerverletzter nach Schlägerei

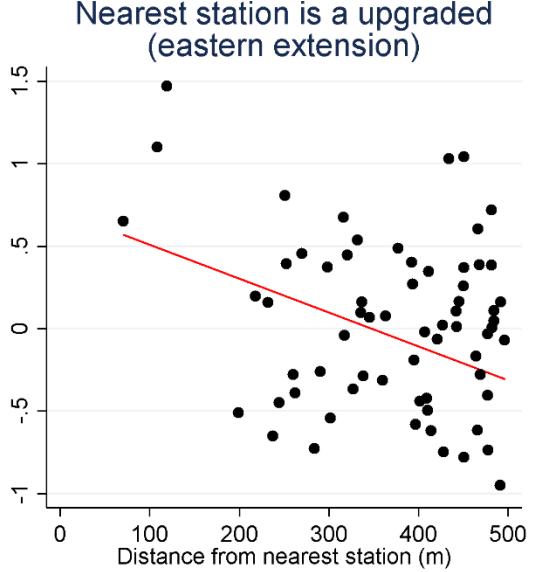
# IV STATION EFFECTS

structural estimation and simulation

Nearest station is a new station  
(eastern extension)

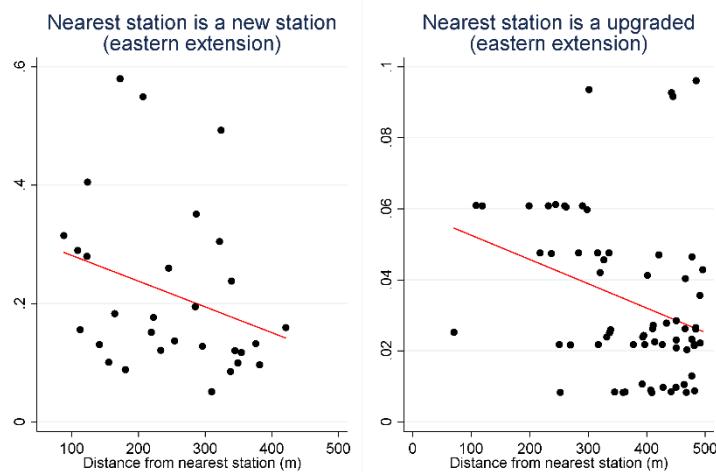


Nearest station is a upgraded  
(eastern extension)

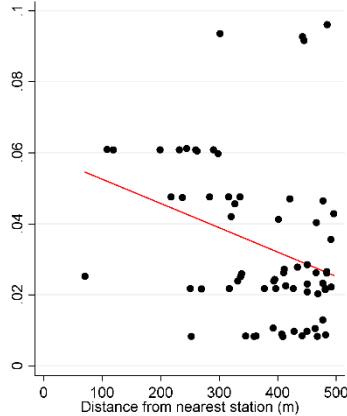


**Capitalization effects large and highly localized as predicted by the model**

Nearest station is a new station  
(eastern extension)



Nearest station is a upgraded  
(eastern extension)



Fitted values

● Ln (2015 land price) - ln (2006 land price) (residual)

Fitted values

● Ln relative land prices (model simulation)

Notes: Residuals are from regressions of log differences in land prices on lagged ln land prices in levels (2000) and trends (2005-2000), Cartesian coordinates, number of listed buildings within block, noise pressure within block, school quality (IDW of nearby blocks), distance from nearest water space, park, U-/S-Bahn station (in 2006), the share of block area affected by WWII destruction, and a full set of 500 m distance from CBD effects.

# IV AGGREGATE EFFECTS I

structural estimation and simulation

## MOBILE POPULATION

Percentage Increase	Counterfactual / Actual		IMMOBILE POP.	
	Exogenous	Endogenous	Exogenous	Endogenous
Utility	0%	0%	0.22%	0.33%
Net City Employment	0.55%	1.06%	0%	0%
Value Total City Income	0.46%	1.01%	0.02%	0.11%
Value Total City Land Rents	0.46%	1.01%	0.02%	0.11%
Total Factor Productivity	0.03%	0.18%	0.03%	0.13%
Sum of Absolute Changes as Percent of Aggregate	Exogenous	Endogenous	Exogenous	Endogenous
Workplace Employment	0.58%	1.06%	0.70%	0.92%
Residence Employment	0.55%	1.06%	0.36%	0.44%
Output	0.49%	1.01%	0.58%	0.78%

# IV AGGREGATE EFFECTS II (MOBILE POPULATION) II

structural estimation and simulation

Variable	Exogenous	Endogenous
Berlin GDP (2012 1,000s Euro)		105,148,850
Increase GDP (2012 1,000s Euro)	479,421	1,056,767
Increase Land Rents (2012 1,000s Euro)	39,952	88,064
NPV Increase GDP (60 year, 3%)	13,747,679	30,303,380
NPV Increase GDP (60 year, 5%)	9,554,528	21,060,609
NPV Increase GDP (60 year, 10%)	5,257,890	11,589,726
NPV Increase Land Rents (60 year, 3%)	1,145,640	2,525,282
NPV Increase Land Rents (60 year, 5%)	796,211	1,755,051
NPV Increase Land Rents (60 year, 10%)	438,157	965,811

## Cost of construction

U55 HBF-Brandenburger Tor (completed)	320,000,000
Incl. U5 Brandenburger Tor Alexanderplatz (estimated)	845,000,000
Incl. U5 HBF-Jungfernheide (own estimate, 2012 prices)	1,975,000,000

**Official CBA: Benefit (mainly direct user benefits) / cost (construction) ratio ≈ 2 (at 3%)**

# SUMMARY

conclusion

- **Ahlfeldt-Redding-Sturm-Wolfg model**
  - Household and firm location choice model
  - Features agglomeration and dispearsion forces
- **Separating location fundamentals from spillovers**
  - Correlation between density and productivity can stem from fundamentals
  - Agglomeration effects can be identified using exogenous varion over time
- **Model can be used for out-of-sample simulation in general equilibirum**
  - Model predictions take into account relocation and displacement effects
  - Model seems to predict changes in property prices well
- **Next: The vertical dimension of cities**
  - Vertical rent gradients
  - Determinants of the urban height profile



**THANKS**

# READING

- Core readings:
  - Ahlfeldt, G. M., Redding, S. J., Sturm, D. M., Wolf, N. (2015): The Economics of Density: Evidence From the Berlin Wall. *Econometrica*, Vol. 83, No. 6 (November, 2015), 2127–2189
- Complementary readings and references:
  - Ahlfeldt, G. M., Redding, S. J., Sturm, D. M. (2016): “A Quantitative Framework for Evaluating the Impact of Urban Transport Improvements,” Working Paper.:.
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  - Ahlfeldt, G. M., Feddersen, A. (2017), From periphery to core: measuring agglomeration effects using high-speed rail, *Journal of Economic Geography*, Volume 18, Issue 2, 1 March 2018, Pages 355–390
  - Ahlfeldt, G. M., K. Moeller, S. Waights, and N. Wendland (2017), “Game of Zones: The Political Economy of Conservation Areas”, *The Economic Journal* 127, F421–45.
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  - Duranton, Gilles and Gobillon, Laurent and Overman, Henry G. (2011) Assessing the effects of local taxation using microgeographic data. *The economic journal*, 121 (555). pp. 1017-1046.
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  - Gibbons, Stephen (2015) Gone with the wind: valuing the visual impacts of wind turbines through house prices. *Journal of Environmental Economics and Management*, 72. pp. 177-196
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  - Redding, S., Sturm, D. (2008), The Costs of Remoteness: Evidence from German Division and Reunification. *American Economic Review* 2008, 98:5, 1766–1797
  - Rosenbaum, P. R. and D. B. Rubin (1983), “The Central Role of the Propensity Score in Observational Studies for Causal Effects”, *Biometrika* 70, 41–55.

# III ROLE OF SPILLOVERS

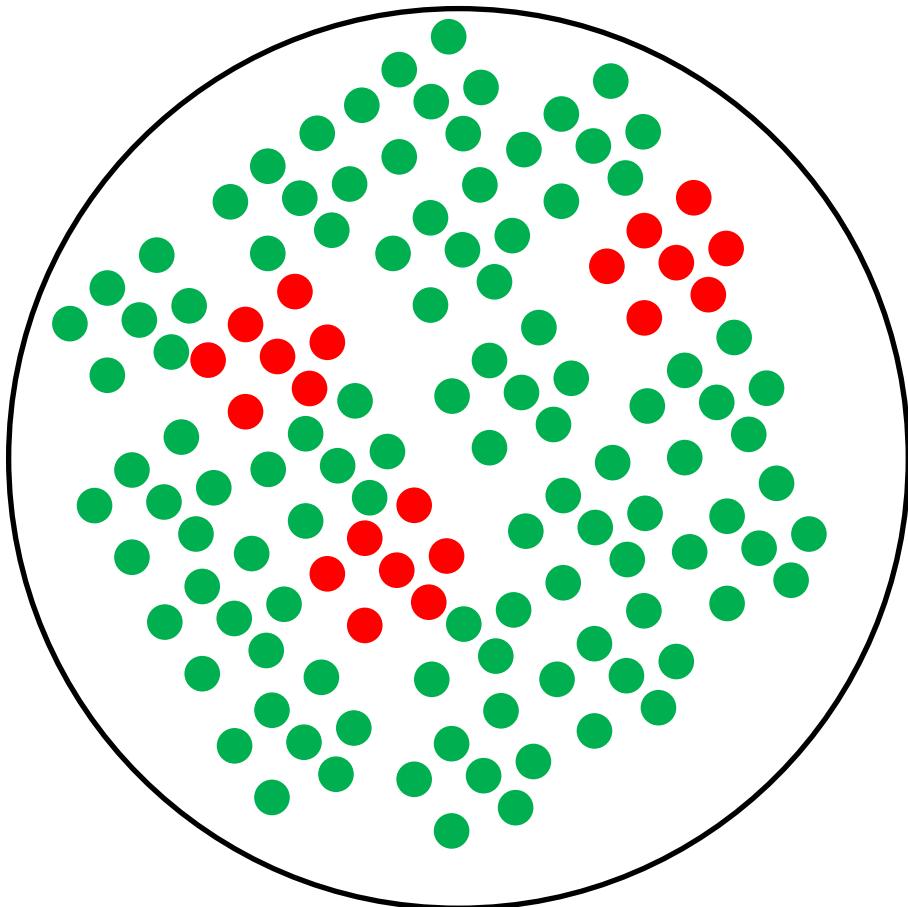
separating spillovers from location fundamentals

- ARSW model stresses the role of spillovers effects
  - Lead to concentration and higher rents!
- In a tradition of an empirical literature on agglomeration (topic II)
  - Fundamental identification problem
    - If rents increase in agglomeration:
      - Is there a causal effects of agglomeration on rents?
      - Is there a third fundamental factor leading to higher rents and agglomeration (correlation)?

**Q: Why does it matter for policy and practice whether it is correlation or causation?**

# III ROLE OF SPILLOVERS

separating spillovers from location fundamentals



**Can we realistically create a new sub-centre?**

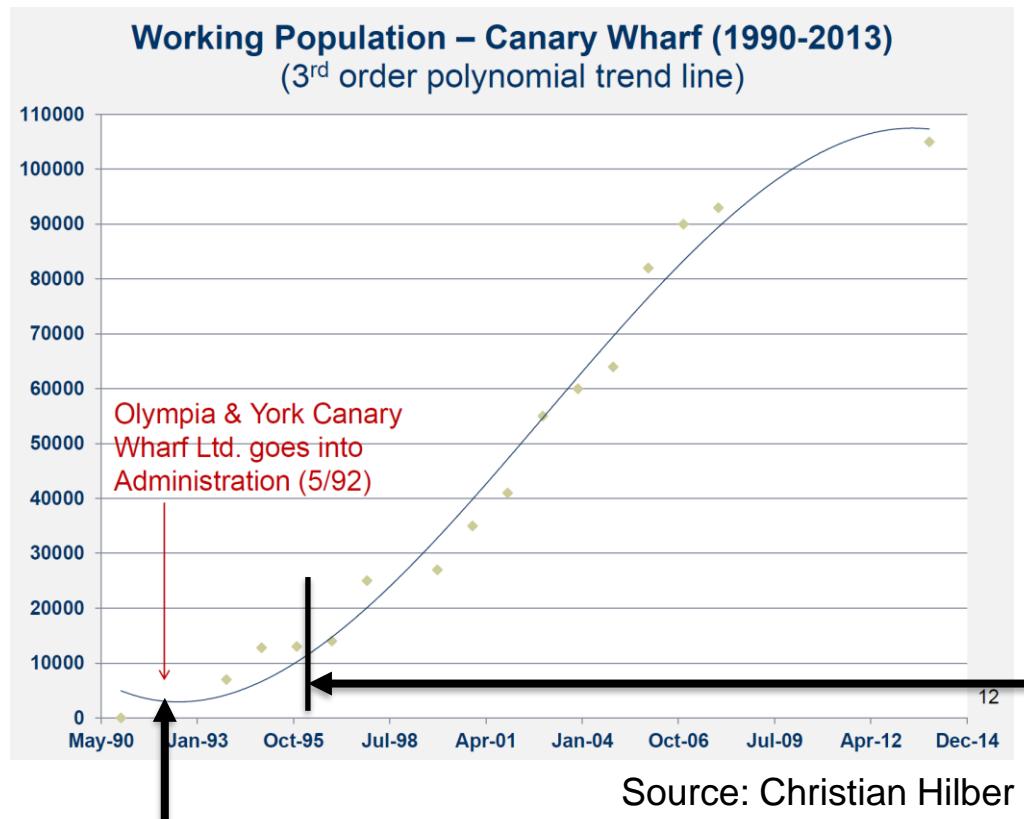
**Yes, if spillover effect is causal  
No, if it is all about fundamentals**

**Matters to investors:**  
**Can buy cheap land, invest into development and attraction of anchor tenants and benefit from increasing rents due to spillovers**

**Matters to planners:**  
**Can try to create new centres to mitigate overcongestion in CBDs**

### III EXAMPLE CANARY WHARF

separating spillovers from location fundamentals



No key firms were there initially  
CW-developer went into administration in 1992 (recession did not help)



Developer bought back in 1993 and tried again. Citybank announces to come in 1996, in 1998 HSBC follows, etc.  
Spillovers kick in, self-reinforcing process begins (Jubilee line extension helps)

### III NEW CAPITAL DISTRICT CAIRO

separating spillovers from location fundamentals

New administrative district planned  
about 45km out of Cairo  
\$3 billion investment, financed by  
Chinese loans

Q: Will it work? Critically depends  
on spillover effects (proximity to  
government might help)



Project features 20 towers, including the (at 345 meters) tallest building in Africa