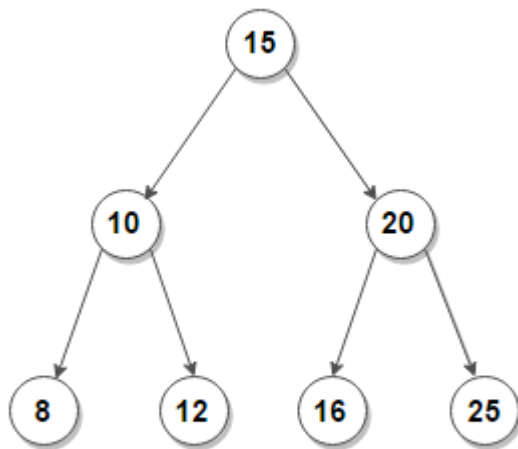


Build a Binary Search Tree from a preorder sequence

Given a distinct sequence of keys representing the preorder sequence of a binary search tree (BST), construct a BST from it.

For example, the following BST corresponds to the preorder traversal { 15, 10, 8, 12, 20, 16, 25 }.



Binary Search Tree

Practice this problem

We can easily build a BST for a given preorder sequence by recursively repeating the following steps for all keys in it:

1. Construct the root node of BST, which would be the first key in the preorder sequence.
2. Find index `i` of the first key in the preorder sequence, which is greater than the root node.
3. Recur for the left subtree with keys in the preorder sequence that appears before the `i'th` index (excluding the first index).
4. Recur for the right subtree with keys in the preorder sequence that appears after the `i'th` index (including the `i'th` index).

Let's consider the preorder traversal `{15, 10, 8, 12, 20, 16, 25}` to make the context more clear.

1. The first item in the preorder sequence 15 becomes the root node.
2. Since 20 is the first key in the preorder sequence, which greater than the root node, the left subtree consists of keys `{10, 8, 12}` and the right subtree consists of keys `{20, 16, 25}`.
3. To construct the complete BST, recursively repeat the above steps for preorder sequence `{10, 8, 12}` and `{20, 16, 25}`.

The algorithm can be implemented as follows in C, Java, and Python:

C

Java

Python

```
1  #include <stdio.h>
2  #include <stdlib.h>
3
4  // Data structure to store a binary tree node
5  struct Node
6  {
7      int key;
8      struct Node *left, *right;
9  };
10
11 // Function to create a new binary tree node having a given key
12 struct Node* newNode(int key)
13 {
14     struct Node* node = (struct Node*)malloc(sizeof(struct Node));
15     node->key = key;
16     node->left = node->right = NULL;
17
18     return node;
19 }
20
21 // Recursive function to perform inorder traversal on a given binary tree
22 void inorder(struct Node* root)
23 {
24     if (root == NULL) {
25         return;
26     }
27
28     inorder(root->left);
29     printf("%d ", root->key);
30     inorder(root->right);
31 }
32
33 // Recursive function to build a BST from a preorder sequence.
34 struct Node* constructBST(int preorder[], int start, int end)
35 {
36     // base case
37     if (start > end) {
```

```

38     return NULL;
39 }
40
41 // Construct the root node of the subtree formed by keys of the
42 // preorder sequence in range `[start, end]`
43 struct Node* node = newNode(preorder[start]);
44
45 // search the index of the first element in the current range of preorder
46 // sequence larger than the root node's value
47 int i;
48 for (i = start; i <= end; i++)
49 {
50     if (preorder[i] > node->key) {
51         break;
52     }
53 }
54
55 // recursively construct the left subtree
56 node->left = constructBST(preorder, start + 1, i - 1);
57
58 // recursively construct the right subtree
59 node->right = constructBST(preorder, i, end);
60
61 // return current node
62 return node;
63 }
64
65 int main(void)
66 {
67     /* Construct the following BST
68           15
69          /  \
70         /    \
71        10     20
72       /  \   /  \
73      /    \ /    \
74     8      12 16   25
75    */
76
77     int preorder[] = { 15, 10, 8, 12, 20, 16, 25 };
78     int n = sizeof(preorder)/sizeof(preorder[0]);
79

```

```
80 // construct the BST
81 struct Node* root = constructBST(preorder, 0, n - 1);
82
83 // print the BST
84 printf("Inorder traversal of BST is ");
85
86 // inorder on the BST always returns a sorted sequence
87 inorder(root);
88
89 return 0;
90 }
```

[Download](#) [Run Code](#)**Output:**

Inorder traversal of BST is 8 10 12 15 16 20 25

The time complexity of the above solution is $O(n^2)$, where n is the size of the BST, and requires space proportional to the tree's height for the call stack. We can reduce the time complexity to $O(n)$ by following a different approach that doesn't involve searching for an index that separates the left and right subtree keys in a preorder sequence:

We know that each node has a key that is greater than all keys present in its left subtree, but less than the keys present in the right subtree of a BST. The idea to pass the information regarding the valid range of keys for the current root node and its children in the recursion itself.

We start by setting the range as `[-INFINITY, INFINITY]` for the root node. It means that the root node and any of its children can have keys ranging between `-INFINITY` and `INFINITY`. Like the previous approach, construct BST's root node from the first item in the preorder sequence. Suppose the root node has value `x`, recur for the right subtree with range `(x, INFINITY)` and recur for the left subtree with range `[-INFINITY, x)`. To construct the complete BST, recursively set the range for each recursive call and return if the next element in preorder traversal is out of the valid range.

Following is the C++, Java, and Python program that demonstrates it:

C++

Java

Python

```
1  #include <iostream>
2  #include <vector>
3  #include <climits>
4  using namespace std;
5
6  // Data structure to store a binary tree node
7  struct Node
8  {
9      int data;
10     Node* left = nullptr, *right = nullptr;
11
12     Node() {}
13     Node(int data): data(data) {}
14 };
15
16 // Function to print the inorder traversal on a given binary tree
17 void inorder(Node* root)
18 {
19     if (root == nullptr) {
20         return;
21     }
22
23     inorder(root->left);
```

```
24     cout << root->data << ' ';
25     inorder(root->right);
26 }
27
28 // Recursive function to build a BST from a preorder sequence.
29 Node* buildTree(vector<int> const &preorder, int &pIndex,
30               int min, int max)
31 {
32     // Base case
33     if (pIndex == preorder.size()) {
34         return nullptr;
35     }
36
37     // Return if the next element of preorder traversal is not in the valid range
38     int val = preorder[pIndex];
39     if (val < min || val > max) {
40         return nullptr;
41     }
42
43     // Construct the root node and increment `pIndex`
44     Node* root = new Node(val);
45     pIndex++;
46
47     // Since all elements in the left subtree of a BST must be less
48     // than the root node's value, set range as `[min, val-1]` and recur
49     root->left = buildTree(preorder, pIndex, min, val - 1);
50
51     // Since all elements in the right subtree of a BST must be greater
52     // than the root node's value, set range as `[val+1...max]` and recur
53     root->right = buildTree(preorder, pIndex, val + 1, max);
54
55     return root;
56 }
57
58 // Build a BST from a preorder sequence
59 Node* buildTree(vector<int> const &preorder)
60 {
61     // start from the root node (the first element in a preorder sequence)
62     int pIndex = 0;
63
64     // set the root node's range as [-INFINITY, INFINITY] and recur
65     return buildTree(preorder, pIndex, INT_MIN, INT_MAX);
```

```

66 }
67
68 int main()
69 {
70     /* Construct the following BST
71         15
72        /  \
73       /    \
74      10     20
75     /  \   /  \
76    /    \ /    \
77   8      12 16   25
78 */
79
80 // preorder traversal of BST
81 vector<int> preorder = { 15, 10, 8, 12, 20, 16, 25 };
82
83 // construct the BST
84 Node* root = buildTree(preorder);
85
86 // print the BST
87 cout << "Inorder traversal of BST is ";
88
89 // inorder on the BST always returns a sorted sequence
90 inorder(root);
91
92 return 0;
93 }

```

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Output:

Inorder traversal of BST is 8 10 12 15 16 20 25

📁 [BST](#)

🔗 [Depth-first search](#), [Hard](#), [Recursive](#)