

# Relational Database Design

## Module 7: Basic Normalization (Part 2)

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# Outline

- Normalization
- Functional dependencies
- Basic normal forms
  - First Normal Form (1NF)
  - Second Normal Form (2NF)
  - Third Normal Form (3NF)
- **Finding functional dependencies**

# Second Normal Form

- **Requirements for Second Normal Form (2NF):**
  - Table must be in First Normal Form
  - Non-key attributes must not depend on subset of any candidate key
    - “Non-key attributes” – not part of *any* candidate key
    - “Subset of candidate key” – requires at least one composite candidate key

**No composite keys**

Attr 1
Attr 2 Attr 3 Attr 4 (AK2.1) Attr 5 Attr 6 (AK1.1)

**No non-key attributes**

Attr 1 Attr 2 Attr 3 (AK2.1)
Attr 4 (AK2.2) Attr 5 (AK2.3) Attr 6 (AK1.1)

# Second Normal Form

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    - “Subset of candidate key” – requires at least one composite candidate key

Example

A
B (AK1.1)
C (AK1.2)
D
E
F

$A \rightarrow B$

$B \rightarrow E$

$D \rightarrow F$

$\{B, C\} \rightarrow A$

$A \rightarrow C$

$\{B, C\} \rightarrow D$

$A \rightarrow D$

$\{B, C\} \rightarrow F$

$A \rightarrow E$

$A \rightarrow F$

# Second Normal Form

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B (AK1.1)
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$A \rightarrow B$

$B \rightarrow E$

$D \rightarrow F$

$\{B, C\} \rightarrow A$

$A \rightarrow C$

$A \rightarrow D$

$A \rightarrow E$

$A \rightarrow F$

$\{B, C\} \rightarrow D$

$\{B, C\} \rightarrow F$

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Example

A
B (AK1.1)
C (AK1.2)
D
E
F

$A \rightarrow B$

$A \rightarrow C$

$A \rightarrow D$

$A \rightarrow E$

$A \rightarrow F$

$B \rightarrow E$

$D \rightarrow F$

$\{B, C\} \rightarrow A$

$\{B, C\} \rightarrow D$

$\{B, C\} \rightarrow F$

# Second Normal Form

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  - Table must be in First Normal Form
  - Non-key attributes must not depend on subset of any candidate key
    - “Non-key attributes” – not part of *any* candidate key
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Example

A
B (AK1.1)
C (AK1.2)
D
E
F

$A \rightarrow B$

$A \rightarrow C$

$A \rightarrow D$

$A \rightarrow E$

$A \rightarrow F$

$B \rightarrow E$

$D \rightarrow F$

$\{B, C\} \rightarrow A$

$\{B, C\} \rightarrow D$

$\{B, C\} \rightarrow F$

# Second Normal Form

- **Requirements for Second Normal Form (2NF):**
  - Table must be in First Normal Form
  - Non-key attributes must not depend on subset of any candidate key
- **Fixing 2NF violations:**
  - New entity type for offending functional dependency

Example

A
B (AK1.1)
C (AK1.2)
D
E
F

Fix2NF

B
E

$A \rightarrow B$

$A \rightarrow C$

$A \rightarrow D$

$A \rightarrow E$

$A \rightarrow F$

$B \rightarrow E$

$D \rightarrow F$

$\{B, C\} \rightarrow A$

$\{B, C\} \rightarrow D$

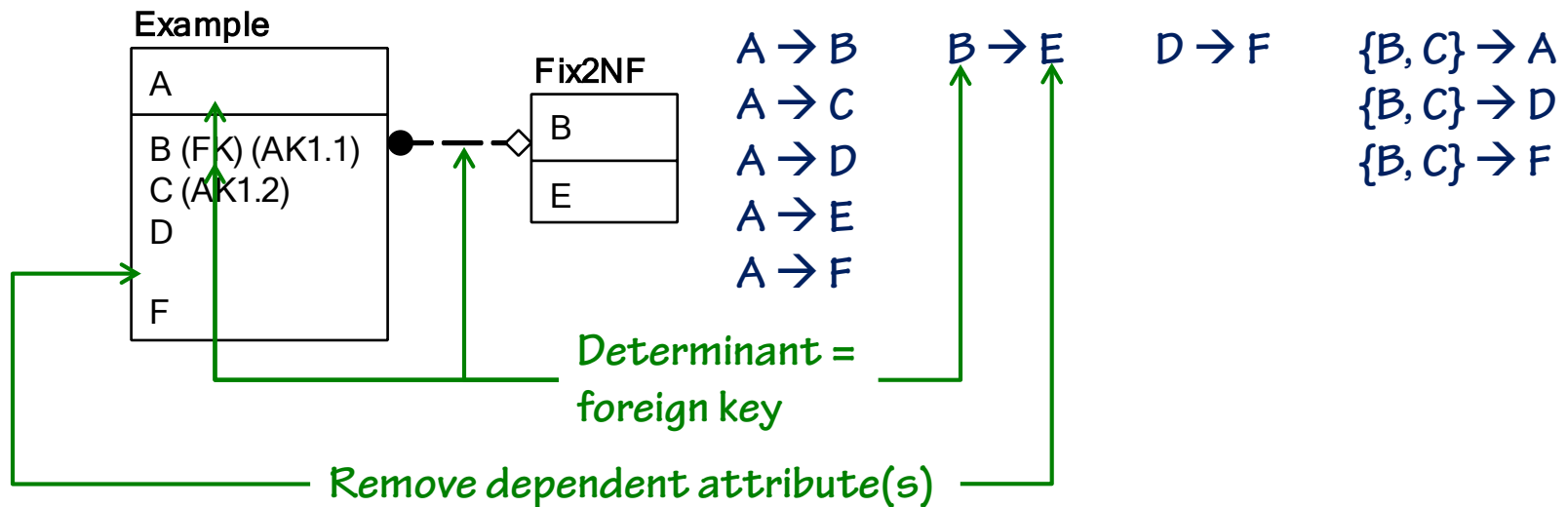
$\{B, C\} \rightarrow F$

Determinant = key



# Second Normal Form

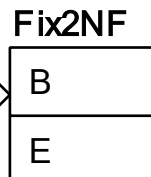
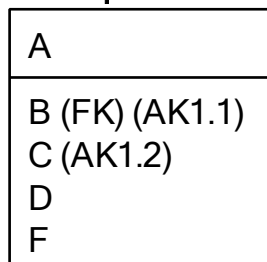
- **Requirements for Second Normal Form (2NF):**
  - Table must be in First Normal Form
  - Non-key attributes must not depend on subset of any candidate key
- **Fixing 2NF violations:**
  - New entity type for offending functional dependency
  - Original entity type:
    - Remove dependent attributes
    - Determinant implements relationship



# Second Normal Form

- **Requirements for Second Normal Form (2NF):**
  - Table must be in First Normal Form
  - Non-key attributes must not depend on subset of any candidate key
- **Fixing 2NF violations:**
  - New entity type for offending functional dependency
  - Original entity type:
    - Remove dependent attributes
    - Determinant implements relationship

## Example



$A \rightarrow B$

$A \rightarrow C$

$A \rightarrow D$

$A \rightarrow E$

$A \rightarrow F$

$B \rightarrow E$

$D \rightarrow F$

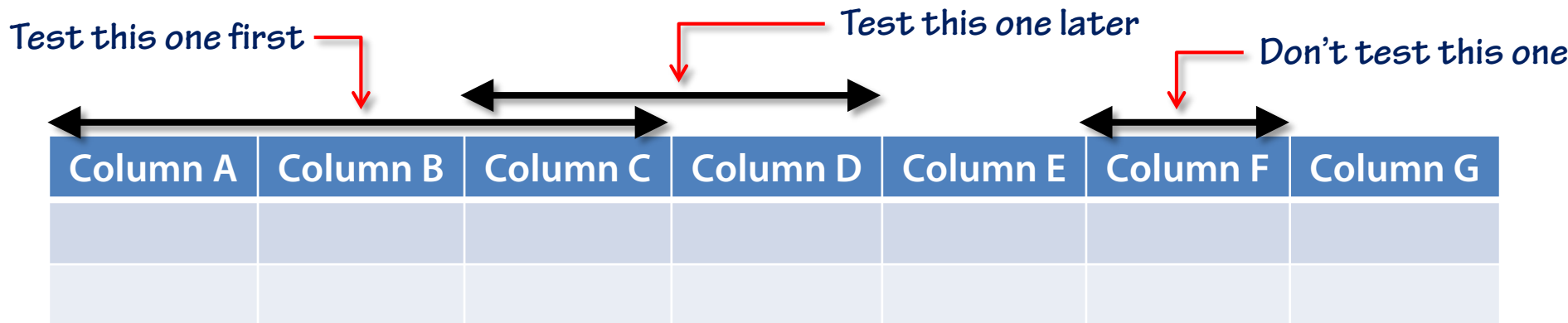
$\{B, C\} \rightarrow A$

$\{B, C\} \rightarrow D$

$\{B, C\} \rightarrow F$

# Finding functional dependencies, part 3

- Dependencies on subsets of candidate keys
  - Violations of 2NF
    - (and a few extra functional dependencies)
  - Skip for tables with:
    - Only single-column candidate keys
    - One candidate key on *all* columns
      - (many-to-many relationships!)
    - Exactly one composite key **AND** no non-key columns
  - Remaining tables:
    - Procedure executed for each *composite* (multi-column) key



# Finding functional dependencies, part 3

- Dependencies on subsets of candidate keys

- Pattern to be populated:
  - Columns in “current” candidate key:
    - One column different, rest equal
  - Columns not in “current” candidate key and not single-column key:
    - One column different, rest irrelevant

Currently checking

Column A	Column B	Column C	Column D	Column E	Column F	Column G
a1	b1	c1	d1	?	?	?
a2	b1	c1	d2	?	?	?

# Finding functional dependencies, part 3

- Dependencies on subsets of candidate keys

- Pattern to be populated:

- Columns in “current” candidate key:

- One column different, rest equal

- Columns not in “current” candidate key and not single-column key:

- One column different, rest irrelevant
      - Optionally combine different columns
        - Faster if there’s no dependency, more work if there is

Currently checking

Column A	Column B	Column C	Column D	Column E	Column F	Column G
a1	b1	c1	d1	e1	?	g1
a2	b1	c1	d2	e2	?	g2

# Finding functional dependencies, part 3

- Dependencies on subsets of candidate keys
  - Impossible to create **valid** example with the required pattern?
    - Column with difference depends on column(s) with no difference
      - Can be a normal dependency or a derivation rule
    - Don't change data model (yet)

Functional dependency found:  $\{B, C\} \rightarrow D$

Currently checking

Column A	Column B	Column C	Column D	Column E	Column F	Column G
a1	b1	c1	d1	?	?	?
a2	b1	c1	d2	?	?	?

# Finding functional dependencies, part 3

- Dependencies on subsets of candidate keys
  - Impossible to create **valid** example with the required pattern?
    - Column with difference depends on column(s) with no difference
      - Can be a normal dependency or a derivation rule
    - Don't change data model (yet)
    - Continue testing
      - Other columns

Functional dependency found:  $\{B, C\} \rightarrow D$

Currently checking


Column A	Column B	Column C	Column D	Column E	Column F	Column G
a1	b1	c1	?	?	?	g1
a2	b1	c1	?	?	?	g2

# Finding functional dependencies, part 3

- Dependencies on subsets of candidate keys
  - Impossible to create **valid** example with the required pattern?
    - Column with difference depends on column(s) with no difference
      - Can be a normal dependency or a derivation rule
    - Don't change data model (yet)
    - Continue testing
      - Other columns
      - Other subsets of current candidate key

Functional dependency found:  $\{B, C\} \rightarrow D$

Currently checking



Column A	Column B	Column C	Column D	Column E	Column F	Column G
a1	b1	c1				
a1	b1	c2				



# Finding functional dependencies, part 3

- Dependencies on subsets of candidate keys
  - Impossible to create **valid** example with the required pattern?
    - Column with difference depends on column(s) with no difference
      - Can be a normal dependency or a derivation rule
    - Don't change data model (yet)
    - Continue testing
      - Other columns
      - Other subsets of current candidate key
      - Other composite candidate keys

Functional dependency found:  $\{B, C\} \rightarrow D$

Test this one next!

Don't test this one

Column A	Column B	Column C	Column D	Column E	Column F	Column G

# Finding functional dependencies, part 3


- Dependencies on subsets of candidate keys
  - All functional dependencies on subset of keys found
    - Might not be full!

Actual dependency:  $A \rightarrow E$

Dependencies found:  $\{A, B, C\} \rightarrow E$   
 $\{A, B, D\} \rightarrow E$   
 $\{A, C, D\} \rightarrow E$

Actual dependency:  $\{A, B\} \rightarrow E$

Dependencies found:  $\{A, B, C\} \rightarrow E$   
 $\{A, B, D\} \rightarrow E$



Column A	Column B	Column C	Column D	Column E	Column F	Column G

# Finding functional dependencies, part 3

## ▪ Dependencies on subsets of candidate keys

- All functional dependencies on subset of keys found
  - Might not be full!
  - Look for common subset ...
    - ... for which every superset was found


*Actual dependency:*  $A \rightarrow E$

*Actual dependencies:*  $\{A, B\} \rightarrow E$   
 $\{A, C, D\} \rightarrow E$

*Actual dependencies:*  $\{A, C\} \rightarrow E$   
 $\{A, B, D\} \rightarrow E$

*Actual dependencies:*  $\{A, D\} \rightarrow E$   
 $\{A, B, C\} \rightarrow E$

*Dependencies found:*  $\{A, B, C\} \rightarrow E$   
 $\{A, B, D\} \rightarrow E$   
 $\{A, C, D\} \rightarrow E$



Column A	Column B	Column C	Column D	Column E	Column F	Column G

# Finding functional dependencies, part 3

## ▪ Dependencies on subsets of candidate keys

- All functional dependencies on subset of keys found
  - Might not be full!
  - Look for common subset ...
    - ... for which every superset was found
    - Multiple common subsets possible


Dependencies found:  $\{A, B, C\} \rightarrow E$   
 $\{A, B, D\} \rightarrow E$   
 $\{A, C, D\} \rightarrow E$

Actual dependencies:  $\{A, B\} \rightarrow E$   
 $\{A, C\} \rightarrow E$

Actual dependencies:  $\{A, B\} \rightarrow E$   
 $\{A, D\} \rightarrow E$

Actual dependencies:  $\{A, C\} \rightarrow E$   
 $\{A, D\} \rightarrow E$

Actual dependencies:  $\{A, B\} \rightarrow E$   
 $\{A, C\} \rightarrow E$   
 $\{A, D\} \rightarrow E$



Column A	Column B	Column C	Column D	Column E	Column F	Column G


# Finding functional dependencies, part 3

- Dependencies on subsets of candidate keys
  - All functional dependencies on subset of keys found
    - Might not be full!
    - Look for common subset ...
      - ... for which **every** superset was found
      - Multiple common subsets possible

Dependencies found:  $\{A, B, C\} \rightarrow E$   
 $\{A, B, D\} \rightarrow E$   
 $\{A, C, D\} \rightarrow E$

Not a dependency:  $\{B, C\} \rightarrow E$   
would have implied:  $\{B, C, D\} \rightarrow E$

Not a dependency:  $B \rightarrow E$   
would have implied:  $\{B, C, D\} \rightarrow E$   
 $\{B, C\} \rightarrow E$   
etcetera



Column A	Column B	Column C	Column D	Column E	Column F	Column G


# Finding functional dependencies, part 3

## ▪ Dependencies on subsets of candidate keys

- All functional dependencies on subset of keys found
  - Might not be full!
  - Look for common subset ...
    - ... for which **every** superset was found
    - Multiple common subsets possible
    - Confirmation (by testing) required
      - If confirmed: Add new dependency, remove implied dependencies
    - Check all possibilities!

Dependencies found:  $\{A, B, C\} \rightarrow E$   
 $\{A, B, D\} \rightarrow E$   
 $\{A, C, D\} \rightarrow E$

Possible dependencies:  $A \rightarrow E$   
 $\{A, B\} \rightarrow E$   
 $\{A, C\} \rightarrow E$   
 $\{A, D\} \rightarrow E$



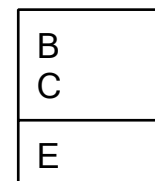
Column A	Column B	Column C	Column D	Column E	Column F	Column G
a1	b1	c1	d1	e1	?	?
a1	b2	c1	d2	e2	?	?

# Finding functional dependencies, part 3

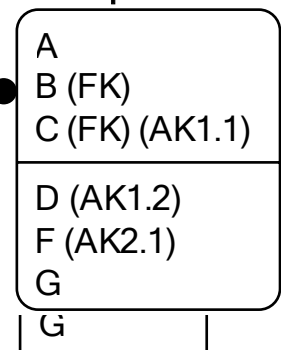
## ■ Dependencies on subsets of candidate keys

- All **full** functional dependencies on subset of keys found
  - Caused by derivation rule? → handled later
  - Non-key column depends on subset of key → violates 2NF
    - Create new entity type
    - Remove dependent attribute

Fix2NF



Example



Full functional dependencies found:  $\{B, C\} \rightarrow E$   
 $D \rightarrow A$

Column A	Column B	Column C	Column D	Column E	Column F	Column G

# Finding functional dependencies, part 3

- Dependencies on subsets of candidate keys
  - All **full** functional dependencies on subset of keys found
    - Caused by derivation rule? → handled later
    - Non-key column depends on subset of key → violates 2NF
      - Create new entity type
      - Remove dependent attribute
    - Subset of one key depends on subset of another key → No 2NF violation
      - No schema change required

Full functional dependencies found:  $\{B, C\} \rightarrow E$

$D \rightarrow A$

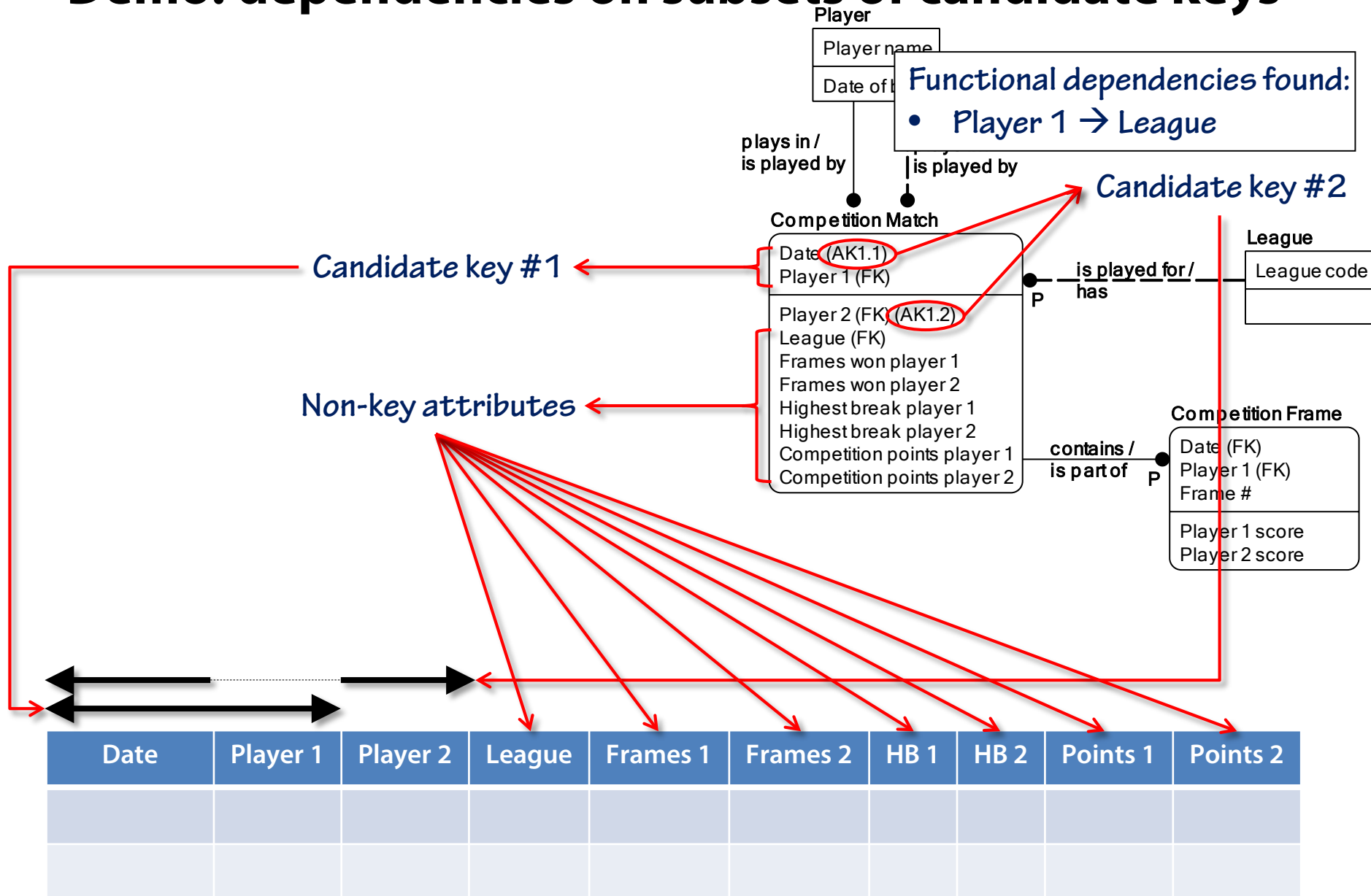
Column A	Column B	Column C	Column D	Column E	Column F	Column G



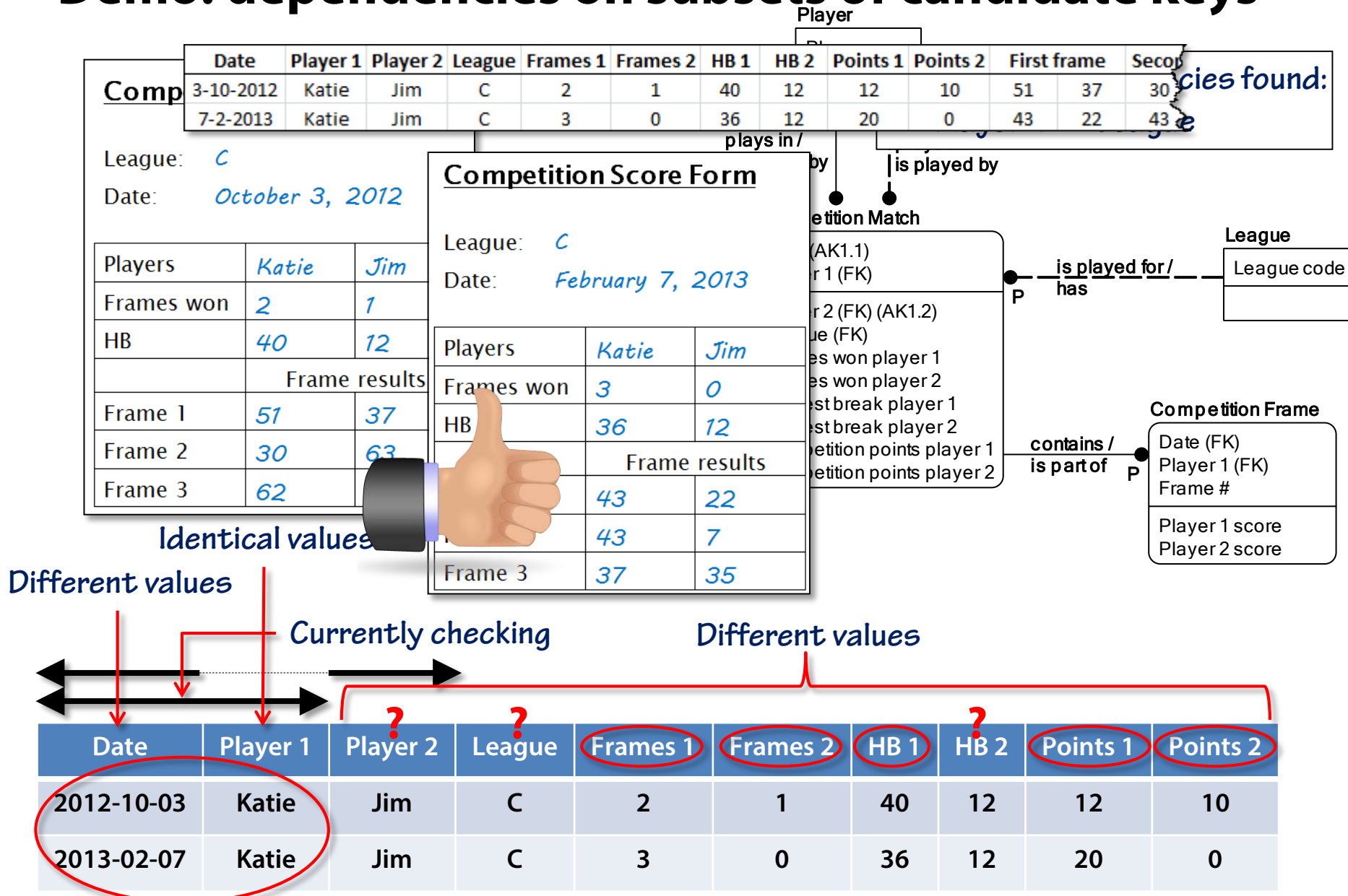
# Finding functional dependencies, part 3

- Dependencies on subsets of candidate keys
  - All **full** functional dependencies on subset of keys found
    - Caused by derivation rule? → handled later
    - Non-key column depends on subset of key → violates 2NF
      - Create new entity type
      - Remove dependent attribute
    - Subset of one key depends on subset of another key → No 2NF violation
      - No schema change required
  - **(Rare)** One non-key column depends on two (or more) subset of keys
    - New entity type for each dependency
      - Causes redundancy
      - Allows data that violates dependencies
    - New entity type for one of the dependencies
      - Allows data that violates dependencies
    - Leave original entity type unchanged
      - Violates 2NF

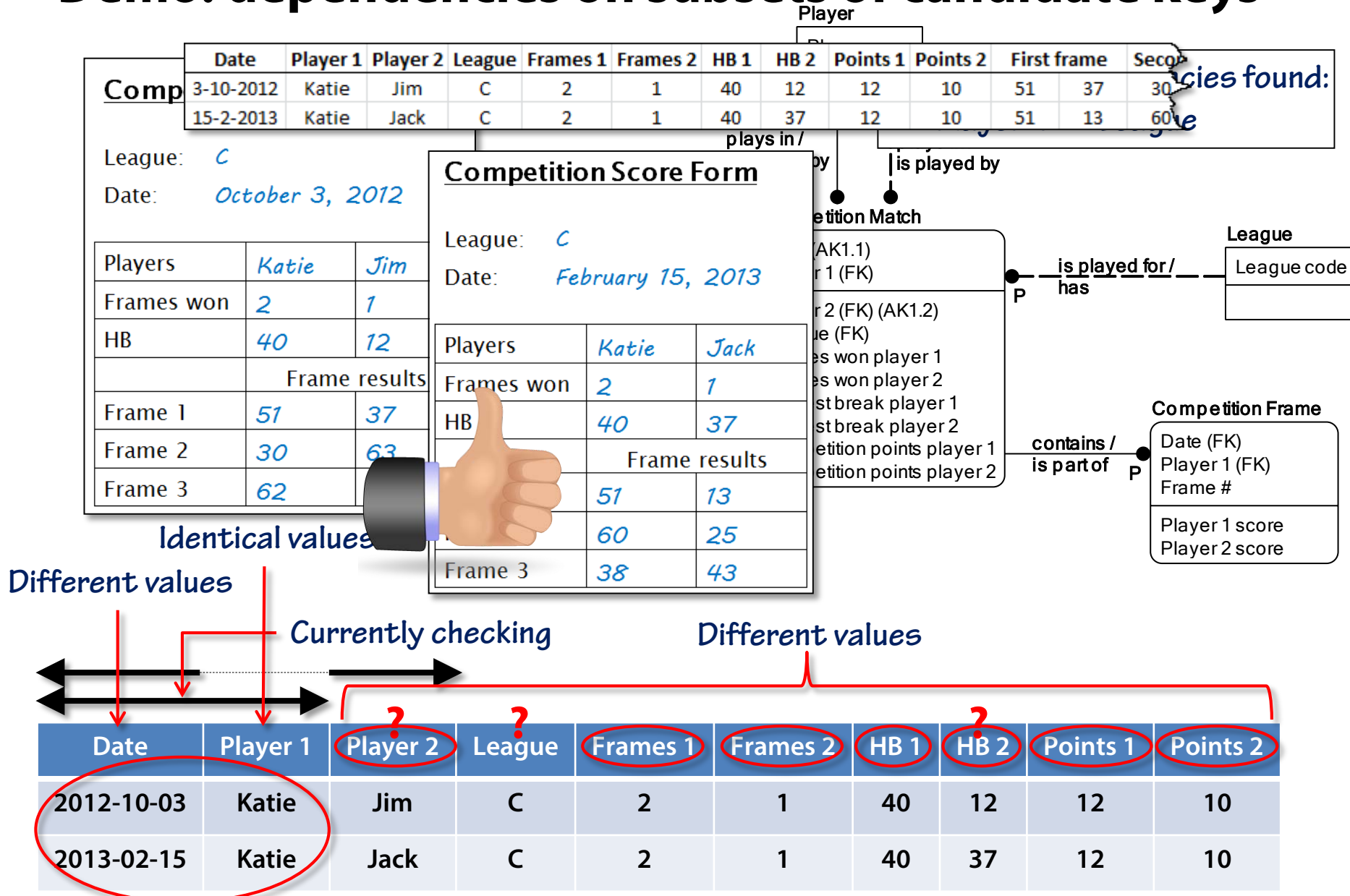
# Demo: dependencies on subsets of candidate keys



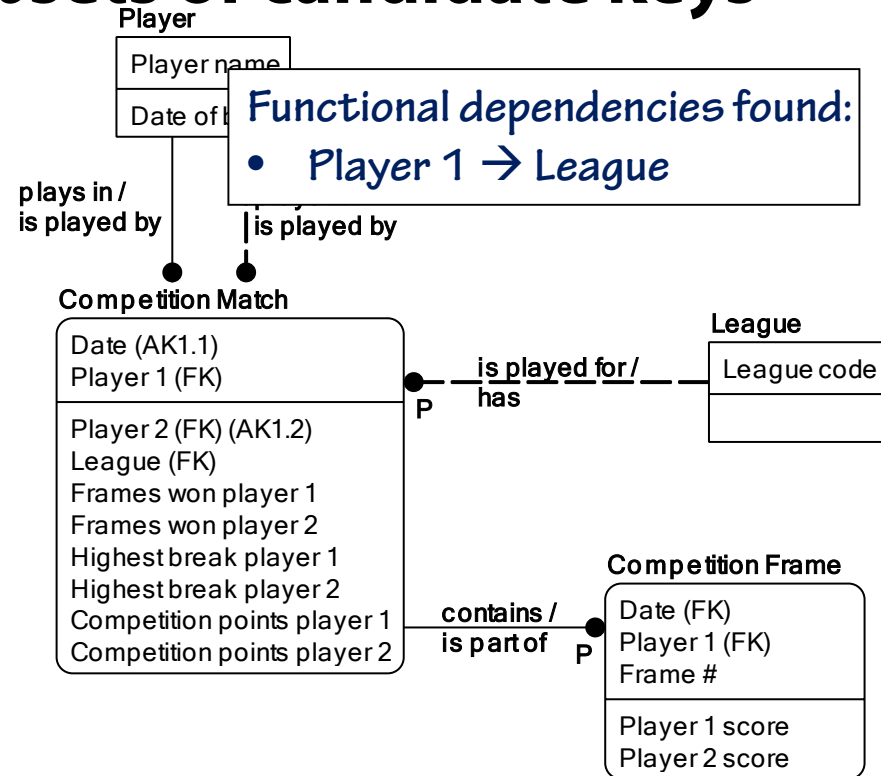
# Demo: dependencies on subsets of candidate keys



# Demo: dependencies on subsets of candidate keys



# Demo: dependencies on subsets of candidate keys



Identical values

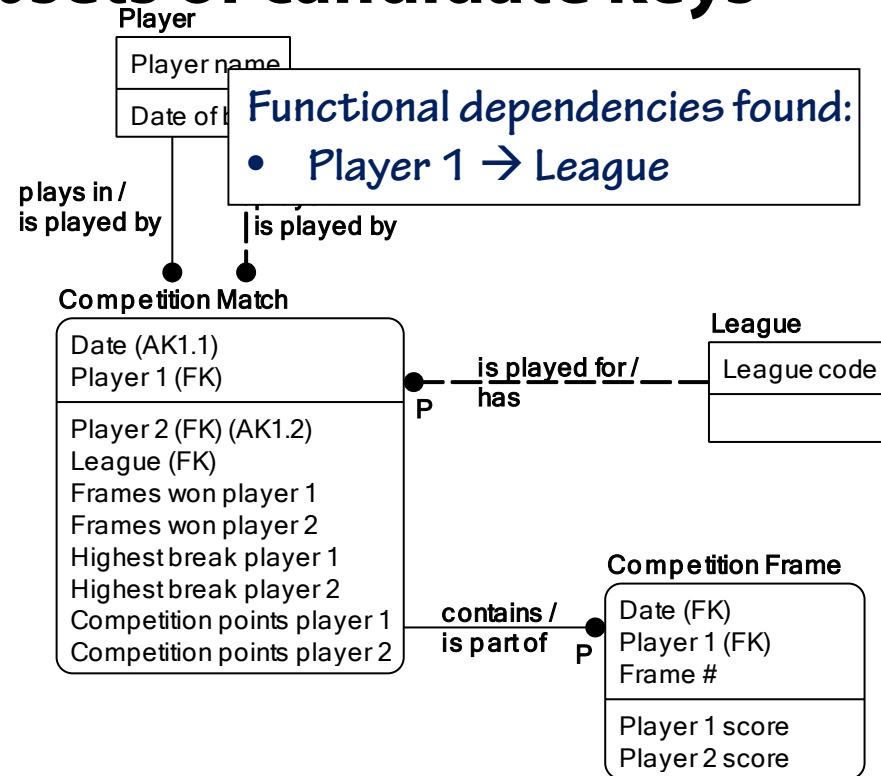
Different values

Currently checking

Different values

Date	Player 1	Player 2	League	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2
2012-10-03	Katie	Jim	C	2	1	40	12	12	10
2013-02-15	Katie	Jim	C	2	1	40	37	12	10

# Demo: dependencies on subsets of candidate keys



Identical values

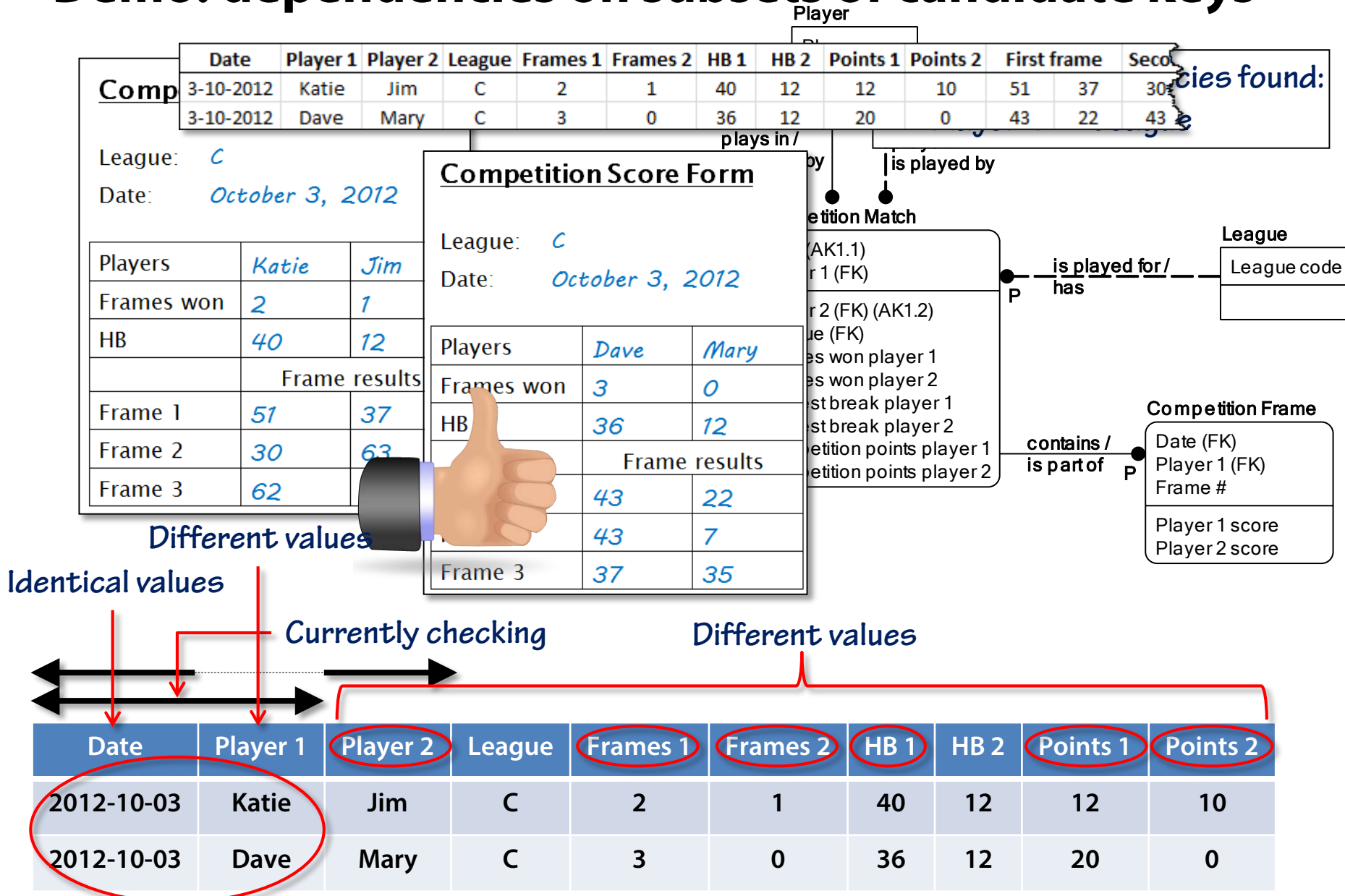
Different values

Currently checking

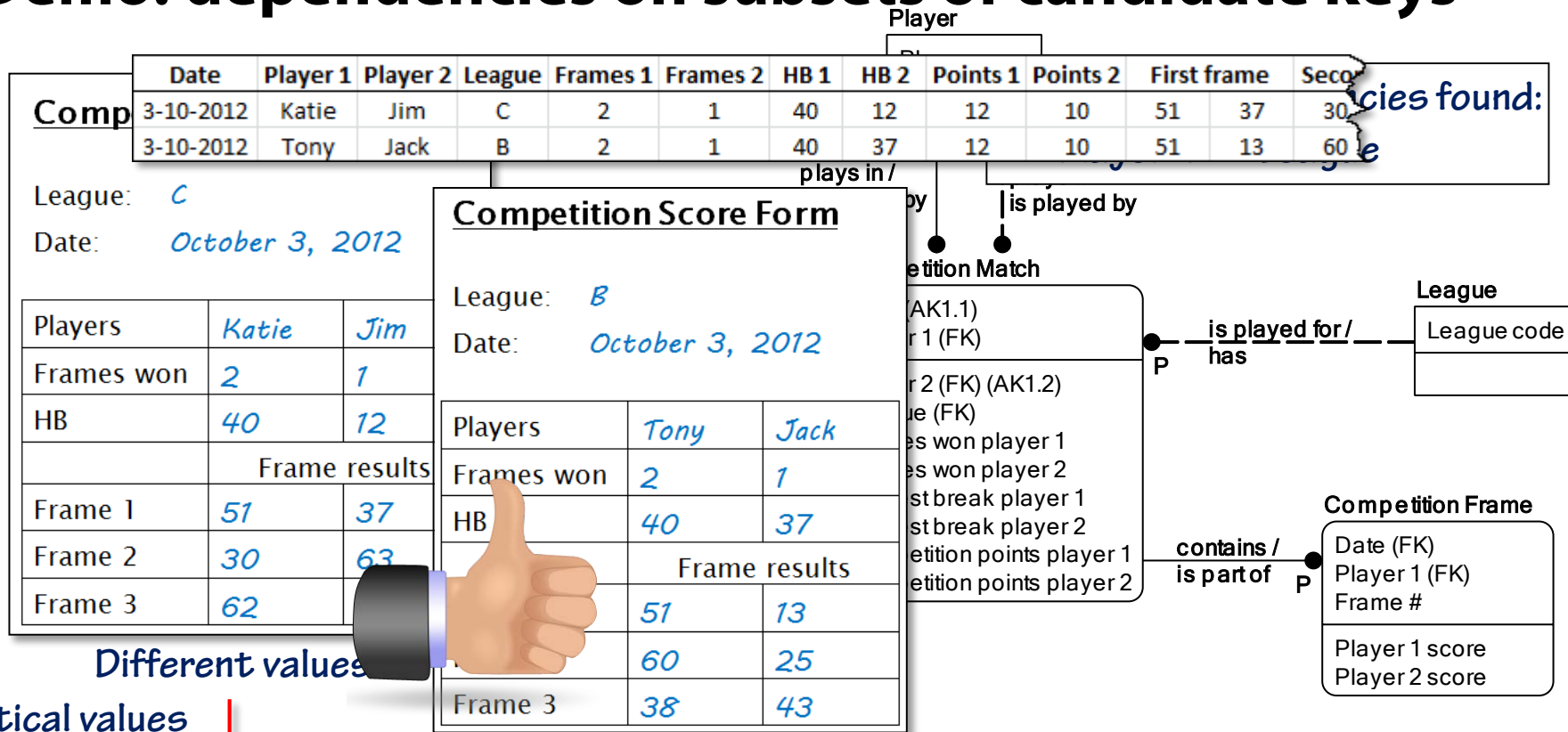
Different values

Date	Player 1	Player 2	League	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2
2012-10-03	Katie	Jim	C	2	1	40	12	12	10
2013-02-15	Katie	Jim	C	2	1	40	12	12	10

# Demo: dependencies on subsets of candidate keys



# Demo: dependencies on subsets of candidate keys



Different values

Identical values

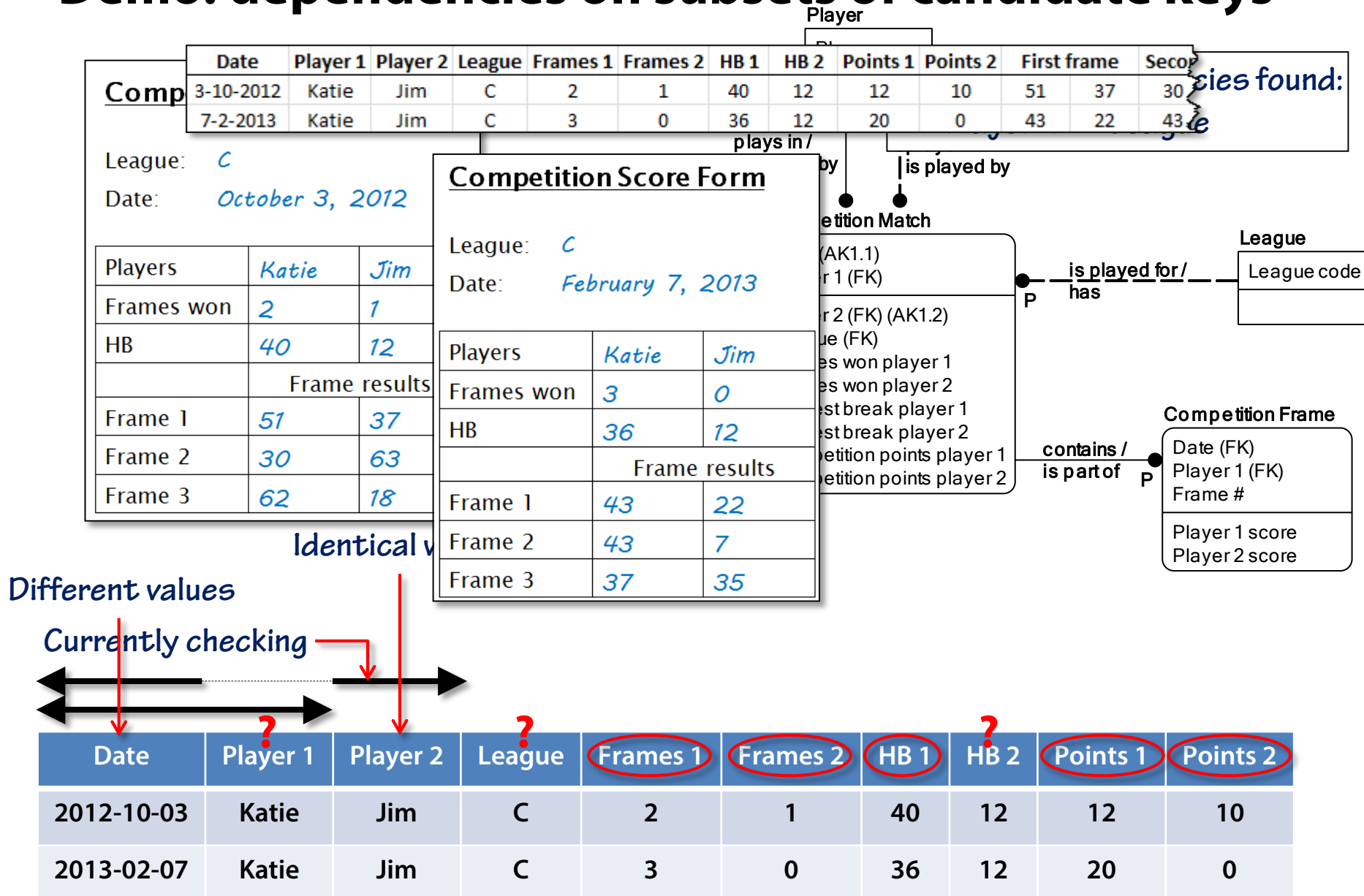
Currently checking

Different values

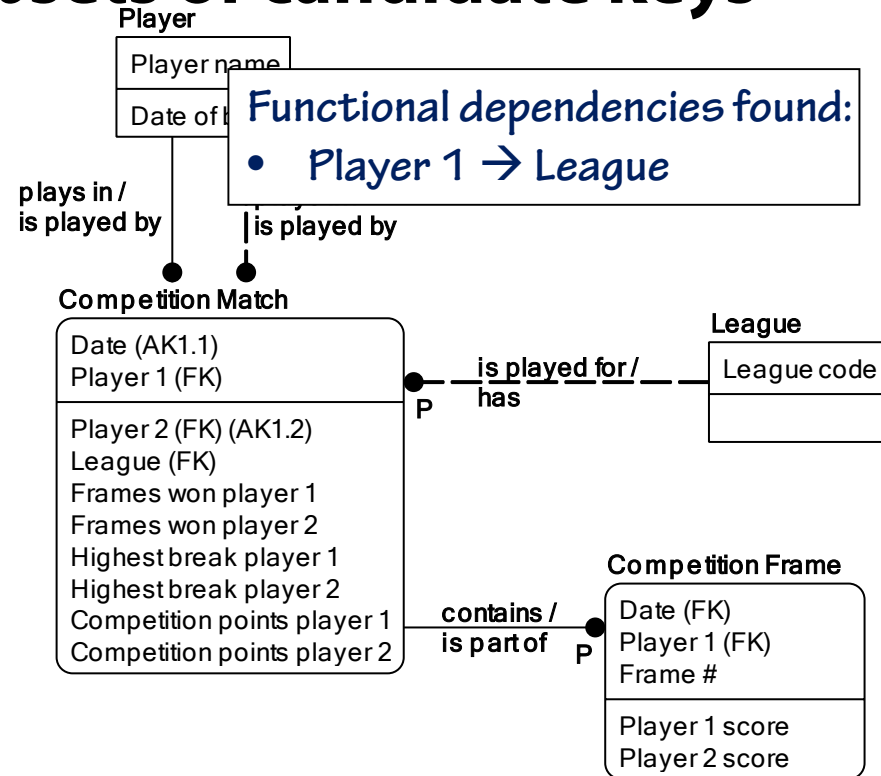
Date	Player 1	Player 2	League	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2
2012-10-03	Katie	Jim	C	2	1	40	12	12	10
2012-10-03	Tony	Jack	B	2	1	40	37	12	10



# Demo: dependencies on subsets of candidate keys



# Demo: dependencies on subsets of candidate keys



Identical values

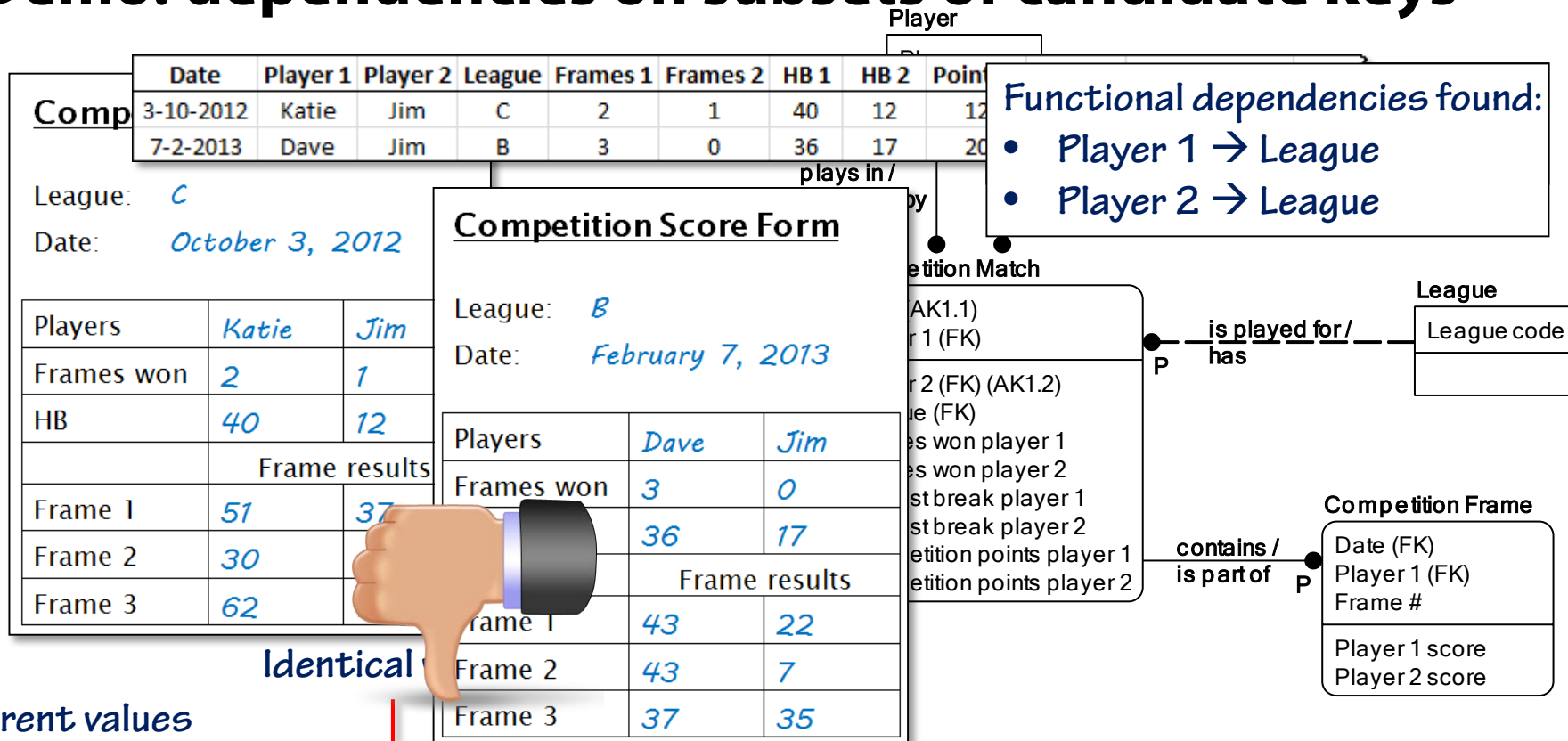
Different values

Currently checking



Date	Player 1	Player 2	League	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2
2012-10-03	?	Jim	?	?	?	?	12	?	?
2013-02-07	?	Jim	?	?	?	?	17	?	?

# Demo: dependencies on subsets of candidate keys



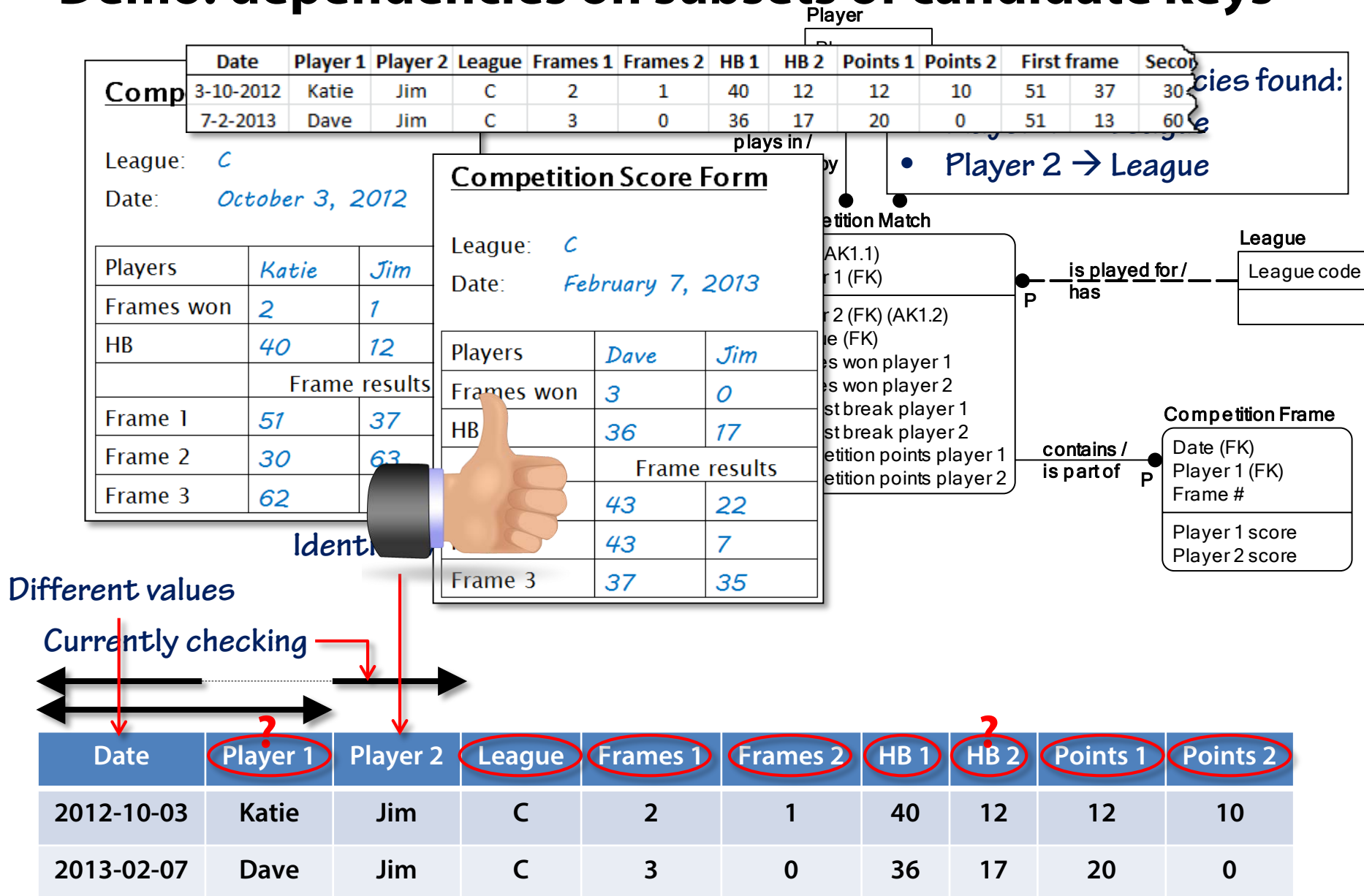
Different values

Currently checking

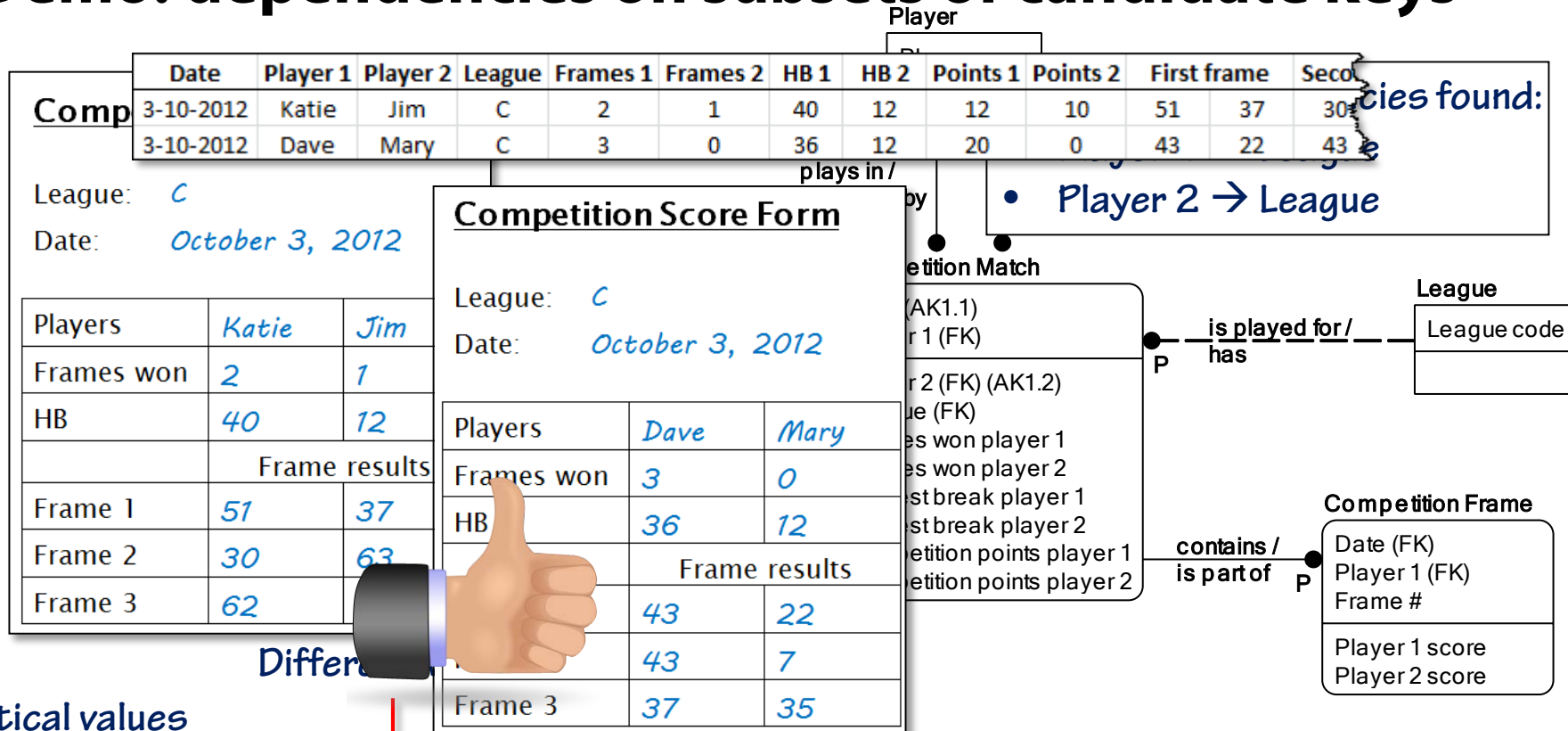


Date	Player 1	Player 2	League	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2
2012-10-03	Katie	Jim	C	2	1	40	12	12	10
2013-02-07	Dave	Jim	B	3	0	36	17	20	0

# Demo: dependencies on subsets of candidate keys

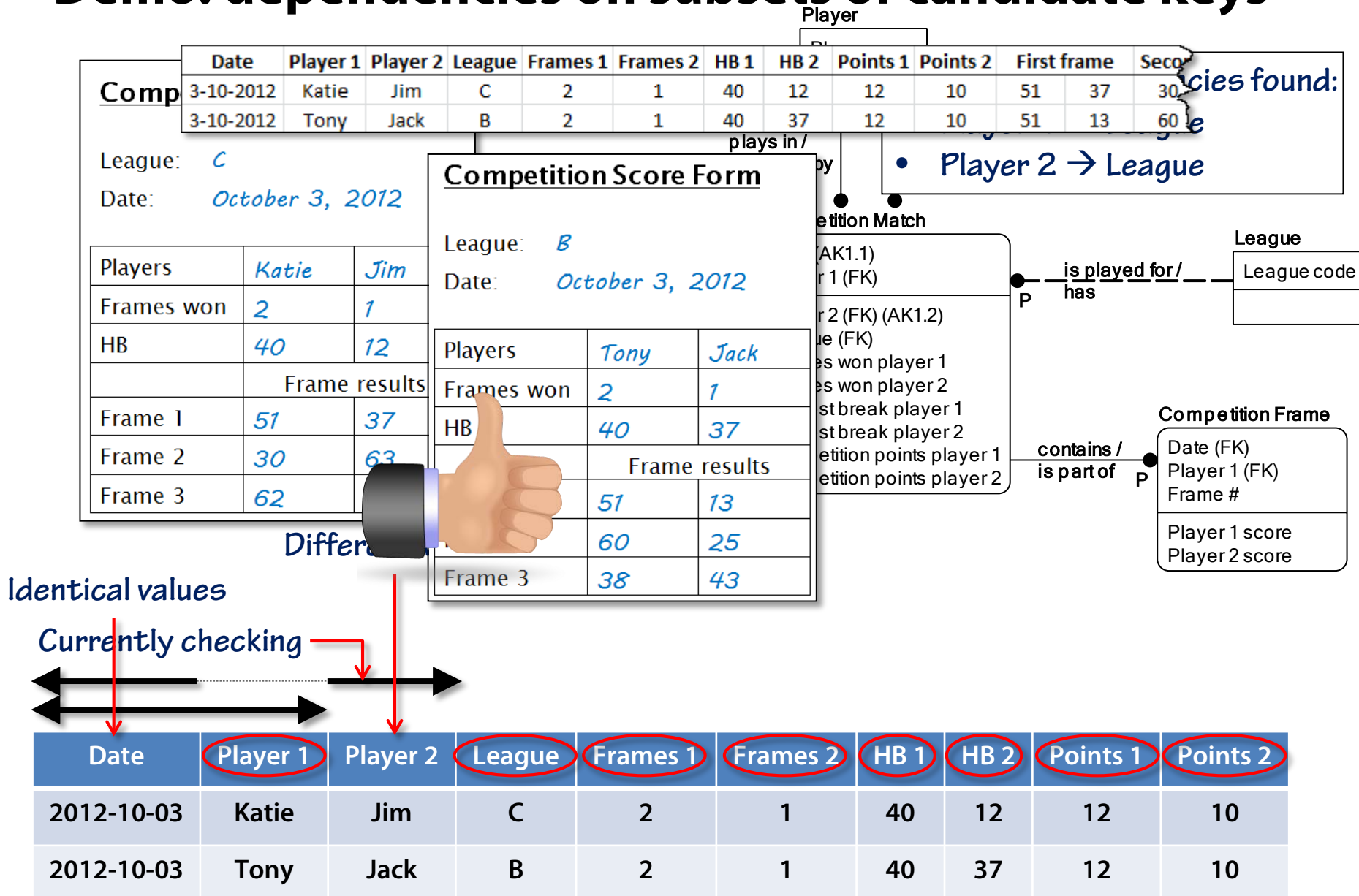


# Demo: dependencies on subsets of candidate keys




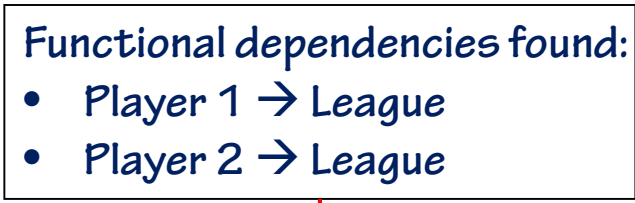
Date	Player 1	Player 2	League	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2
2012-10-03	Katie	Jim	C	2	1	40	12	12	10
2012-10-03	Dave	Mary	C	3	0	36	12	20	0

# Demo: dependencies on subsets of candidate keys



Player

Player name
Date of birth

[illegible]

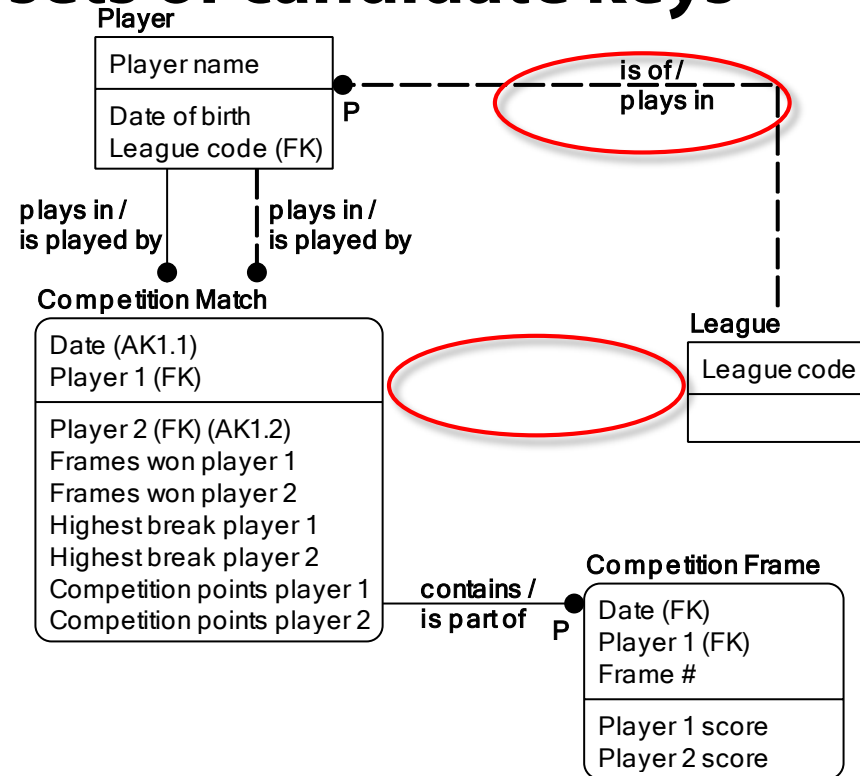
# Demo: dependencies on subsets of candidate keys

Functional dependencies found:

- Player 1 → League
- Player 2 → League

Actual functional dependency:

- Player → League



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2



# Third Normal Form

- **Requirements for Third Normal Form (3NF):**
  - Table must be in Second Normal Form
  - Non-prime attributes must be non-transitively dependent on every superkey
    - or: No dependency of non-key attribute on attribute(s) that is/are not a key
      - A non-key attribute depends on one non-key attribute

## 3NF example

Attr 1 Attr 2
Attr 3 (AK1.1) Attr 4 (AK1.2) Attr 5 Attr 6 Attr 7

## Examples of violations:

- $\text{Attr5} \rightarrow \text{Attr7}$
- $\text{Attr7} \rightarrow \text{Attr6}$

# Third Normal Form

- **Requirements for Third Normal Form (3NF):**
  - Table must be in Second Normal Form
  - Non-prime attributes must be non-transitively dependent on every superkey
    - or: No dependency of non-key attribute on attribute(s) that is/are not a key
      - A non-key attribute depends on one non-key attribute
      - A non-key attribute depends on multiple non-key attributes

## 3NF example

Attr 1 Attr 2
Attr 3 (AK1.1) Attr 4 (AK1.2) Attr 5 Attr 6 Attr 7

## Examples of violations:

- $\{\text{Attr5}, \text{Attr6}\} \rightarrow \text{Attr7}$
- $\{\text{Attr5}, \text{Attr7}\} \rightarrow \text{Attr6}$

# Third Normal Form

- **Requirements for Third Normal Form (3NF):**
  - Table must be in Second Normal Form
  - Non-prime attributes must be non-transitively dependent on every superkey
    - or: No dependency of non-key attribute on attribute(s) that is/are not a key
      - A non-key attribute depends on one non-key attribute
      - A non-key attribute depends on multiple non-key attributes
      - A non-key attribute depends on combination of candidate key subset and non-key

## 3NF example

Attr 1 Attr 2
Attr 3 (AK1.1) Attr 4 (AK1.2) Attr 5 Attr 6 Attr 7

## Examples of violations:

- $\{Attr1, Attr5\} \rightarrow Attr7$
- $\{Attr3, Attr5, Attr7\} \rightarrow Attr6$

# Third Normal Form

- **Requirements for Third Normal Form (3NF):**
  - Table must be in Second Normal Form
  - Non-prime attributes must be non-transitively dependent on every superkey
    - or: No dependency of non-key attribute on attribute(s) that is/are not a key
      - A non-key attribute depends on one non-key attribute
      - A non-key attribute depends on multiple non-key attributes
      - A non-key attribute depends on combination of candidate key subset and non-key
      - A non-key attribute depends on combination of multiple candidate key subsets

## 3NF example

Attr 1 Attr 2
Attr 3 (AK1.1) Attr 4 (AK1.2) Attr 5 Attr 6 Attr 7

## Examples of violations:

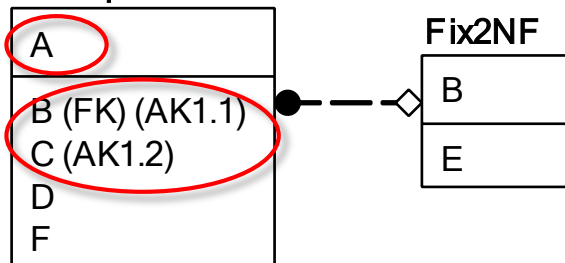
- {Attr1, Attr4} → Attr6
- {Attr2, Attr3} → Attr6
- {Attr2, Attr3, Attr5, Attr6} → Attr7

# Third Normal Form

## ■ Requirements for Third Normal Form (3NF):

- Table must be in Second Normal Form
- Non-prime attributes must be non-transitively dependent on every superkey
  - or: No dependency of non-key attribute on attribute(s) that is/are not a key
- □ A non-key attribute depends on one non-key attribute
- A non-key attribute depends on multiple non-key attributes
- A non-key attribute depends on combination of candidate key subset and non-key
- A non-key attribute depends on combination of multiple candidate key subsets

### Example



$A \rightarrow B$   
 $A \rightarrow C$   
 $A \rightarrow D$   
 $A \rightarrow F$

$D \rightarrow F$

$\{B, C\} \rightarrow A$   
 $\{B, C\} \rightarrow D$   
 $\{B, C\} \rightarrow F$

# Third Normal Form

- **Requirements for Third Normal Form (3NF):**
  - Table must be in Second Normal Form
  - Non-prime attributes must be non-transitively dependent on every superkey
    - or: No dependency of non-key attribute on attribute(s) that is/are not a key
- **Fixing 3NF violations:**
  - New entity type for offending functional dependency

Example

A
B (FK) (AK1.1)
C (AK1.2)
D
F



Fix2NF

B
E

Fix3NF

D
F

$A \rightarrow B$

$A \rightarrow C$

$A \rightarrow D$

$A \rightarrow F$

$D \rightarrow F$

$\{B, C\} \rightarrow A$

$\{B, C\} \rightarrow D$

$\{B, C\} \rightarrow F$



# Third Normal Form

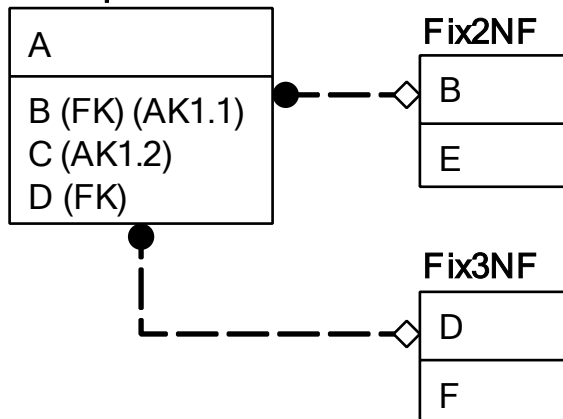
- **Requirements for Third Normal Form (3NF):**

- Table must be in Second Normal Form
- Non-prime attributes must be non-transitively dependent on every superkey
  - or: No dependency of non-key attribute on attribute(s) that is/are not a key

- **Fixing 3NF violations:**

- New entity type for offending functional dependency
- Original entity type:
  - Remove dependent attributes
  - Determinant implements relationship

**Example**



$$A \rightarrow B$$

$$A \rightarrow C$$

$$A \rightarrow D$$

$$A \rightarrow F$$

$$D \rightarrow F$$

$$\{B, C\} \rightarrow A$$

$$\{B, C\} \rightarrow D$$

$$\{B, C\} \rightarrow F$$


# Finding functional dependencies, part 4

- **Possible violations of Third Normal Form:**
  - Dependency of a non-key attribute on a non-key attribute
  - Dependency of a non-key attribute on a combination of attributes
    - Not subset of any candidate key
    - Not superset of any candidate key
- **Testing for:**
  - Dependency of **any** attribute on a non-key attribute
    - Can be skipped for tables with no non-key attributes
  - Dependency of **any** attribute on a combination of attributes
    - Can be skipped for tables with:
      - No composite keys and  $\leq 1$  non-key attribute
      - One composite key and no non-key attributes



# Finding functional dependencies, part 4

- Dependencies on a single non-key attribute
  - Pattern to be populated:
    - One non-key column equal
    - All other columns different
  - **Valid** example with required pattern found or created?
    - No dependencies on non-key column being tested
  - Impossible to create **valid** example with the required pattern?
    - One or more other columns depend on column being tested
      - But which one(s)?



Column A	Column B	Column C	Column D	Column E	Column F	Column G
a1	b1	c1	d1	e1	f1	g1
a2	b2	c2	d1	e2	f2	g2


# Finding functional dependencies, part 4

- Dependencies on a single non-key attribute
  - Impossible to create **valid** example with the required pattern?
    - One or more other columns depend on column being tested
      - But which one(s)?
    - Check which other columns depend on column being tested
      - Listen to reason for rejecting example
      - Or test, one possibly dependent column at a time

Column A	Column B	Column C	Column D	Column E	Column F	Column G
a1	?	?	d1	?	?	?
a2	?	?	d1	?	?	?

# Finding functional dependencies, part 4

- Dependencies on a single non-key attribute
  - Impossible to create **valid** example with the required pattern?
    - One or more other columns depend on column being tested
      - But which one(s)?
    - Check which other columns depend on column being tested
      - Listen to reason for rejecting example
      - Or test, one possibly dependent column at a time



Column A	Column B	Column C	Column D	Column E	Column F	Column G
?	b1	?	d1	?	?	?
?	b2	?	d1	?	?	?

# Finding functional dependencies, part 4

- Dependencies on a single non-key attribute
  - Impossible to create **valid** example with the required pattern?
    - One or more other columns depend on column being tested
      - But which one(s)?
    - Check which other columns depend on column being tested
      - Listen to reason for rejecting example
      - Or test, one possibly dependent column at a time

Column A	Column B	Column C	Column D	Column E	Column F	Column G
?	?	c1	d1	?	?	?
?	?	c2	d1	?	?	?

# Finding functional dependencies, part 4

- Dependencies on a single non-key attribute
  - Impossible to create **valid** example with the required pattern?
    - One or more other columns depend on column being tested
      - But which one(s)?
  - Check which other columns depend on column being tested
    - Listen to reason for rejecting example
    - Or test, one possibly dependent column at a time

Column A	Column B	Column C	Column D	Column E	Column F	Column G
?	?	?	d1	e1	?	?
?	?	?	d1	e2	?	?

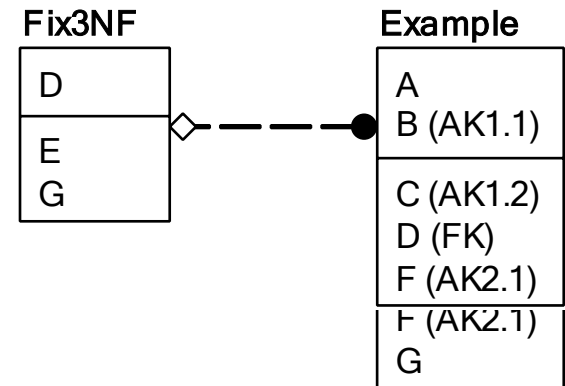
# Finding functional dependencies, part 4

- Dependencies on a single non-key attribute
  - Impossible to create **valid** example with the required pattern?
    - One or more other columns depend on column being tested
      - But which one(s)?
    - Check which other columns depend on column being tested
      - Listen to reason for rejecting example
      - Or test, one possibly dependent column at a time
      - When rejected, that column depends on column being tested
        - (Usually)
      - Make sure to find *all* dependent columns!
    - For each dependency: “normal” functional dependency, or derivation rule?

Column A	Column B	Column C	Column D	Column E	Column F	Column G
?	?	?	d1	?	?	g1
?	?	?	d1	?	?	g2

# Finding functional dependencies, part 4

- Dependencies on a single non-key attribute
  - Impossible to create **valid** example with the required pattern?
    - “Normal” (not derived) dependencies of non-key column → violates 3NF
      - Create new entity type
      - Remove dependent attribute(s)



Functional dependencies found:

$D \rightarrow E$

$D \rightarrow G$

Column A	Column B	Column C	Column D	Column E	Column F	Column G

# Finding functional dependencies, part 4

- Dependencies on a single non-key attribute
  - Impossible to create **valid** example with the required pattern?
    - Derived dependencies / dependent key columns
      - No schema change needed
      - Make note for later use
      - Exclude dependent column from rest of test
        - But do check for transitive dependencies if new dependency on determinant is found!

## Example

A
B (AK1.1)
C (AK1.2)
D
E
F (AK2.1)
G

Functional dependencies found:

$D \rightarrow E$

$D \rightarrow G$

Column A	Column B	Column C	Column D	Column E	Column F	Column G



# Finding functional dependencies, part 4

- Dependencies on a single non-key attribute
  - When tests for a column are completed:
    - **First** fix model (if needed)
    - Then continue with next column
      - Repeat until all columns verified

Column A	Column B	Column C	Column D	Column E	Column F	Column G

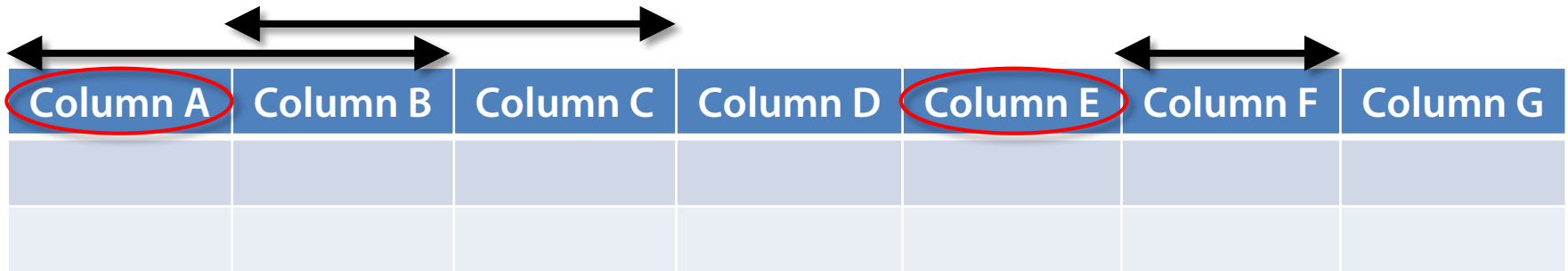
# Finding functional dependencies, part 4

- Dependencies on combination of attributes that are not a key
  - Test possible combinations of two columns, then three, ...
    - Combination of several non-key columns

Column A	Column B	Column C	Column D	Column E	Column F	Column G

# Finding functional dependencies, part 4

- Dependencies on combination of attributes that are not a key
  - Test possible combinations of two columns, then three, ...
    - Combination of several non-key columns
    - Combination of non-key column(s) with subset of a candidate key

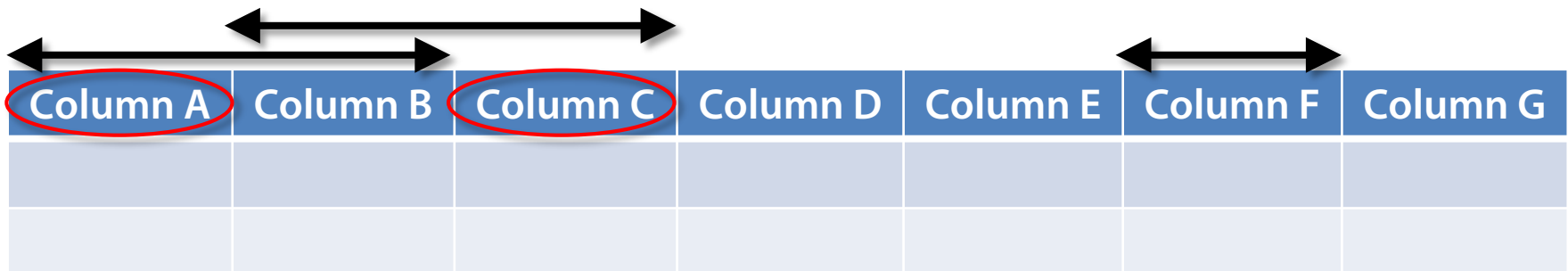


# Finding functional dependencies, part 4

- Dependencies on combination of attributes that are not a key
  - Test possible combinations of two columns, then three, ...
    - Combination of several non-key columns
    - Combination of non-key column(s) with subset of a candidate key
    - Combination of several subsets of different candidate keys
  - Problem: This results in a LOT of test cases!
    - Solution: use your experience to avoid “silly” tests
    - But remember that this involves assumptions!

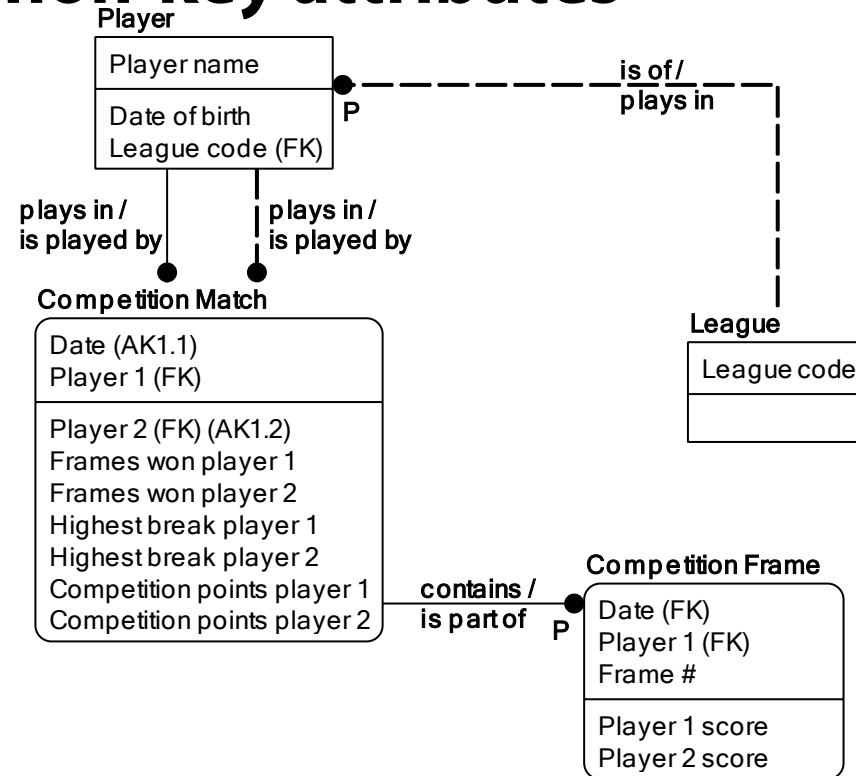
*Not a subset of a candidate key*

*Not a superset of a candidate key*



Column A	Column B	Column C	Column D	Column E	Column F	Column G

# Demo: dependencies on non-key attributes



Currently checking

Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2
a1	b1	c1	d1	e1	f1	g1	h1	j1
a2	b2	c2	d1	e2	f2	g2	h2	j2

## Player

## League

League code


contains /  
is part of

## Competition Frame

Date (FK)  
Player 1 (FK)  
Frame #

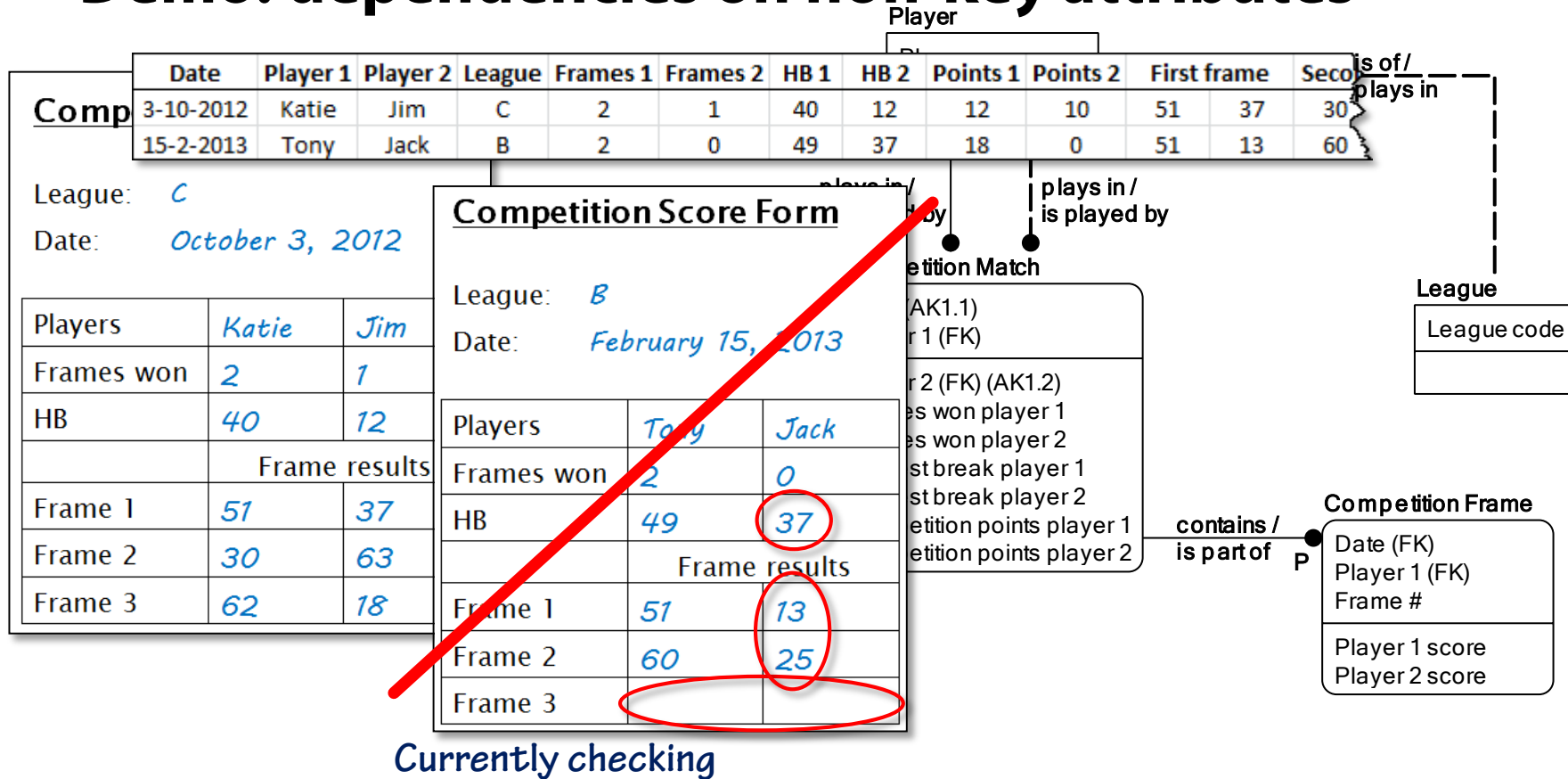
Player 1 score  
Player 2 score

Currently checking



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2
2012-10-03	Katie	Jim	2	1	40	12	12	10
2013-02-15	Tony	Jack	2	1	49	37	12	10

# Demo: dependencies on non-key attributes



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2
2012-10-03	Katie	Jim	2	1	40	12	12	10
2013-02-15	Tony	Jack	2	0	49	37	18	0

## Player

## League

League code


contains /  
is part of

## Competition Frame

Date (FK)  
Player 1 (FK)  
Frame #

Player 1 score  
Player 2 score

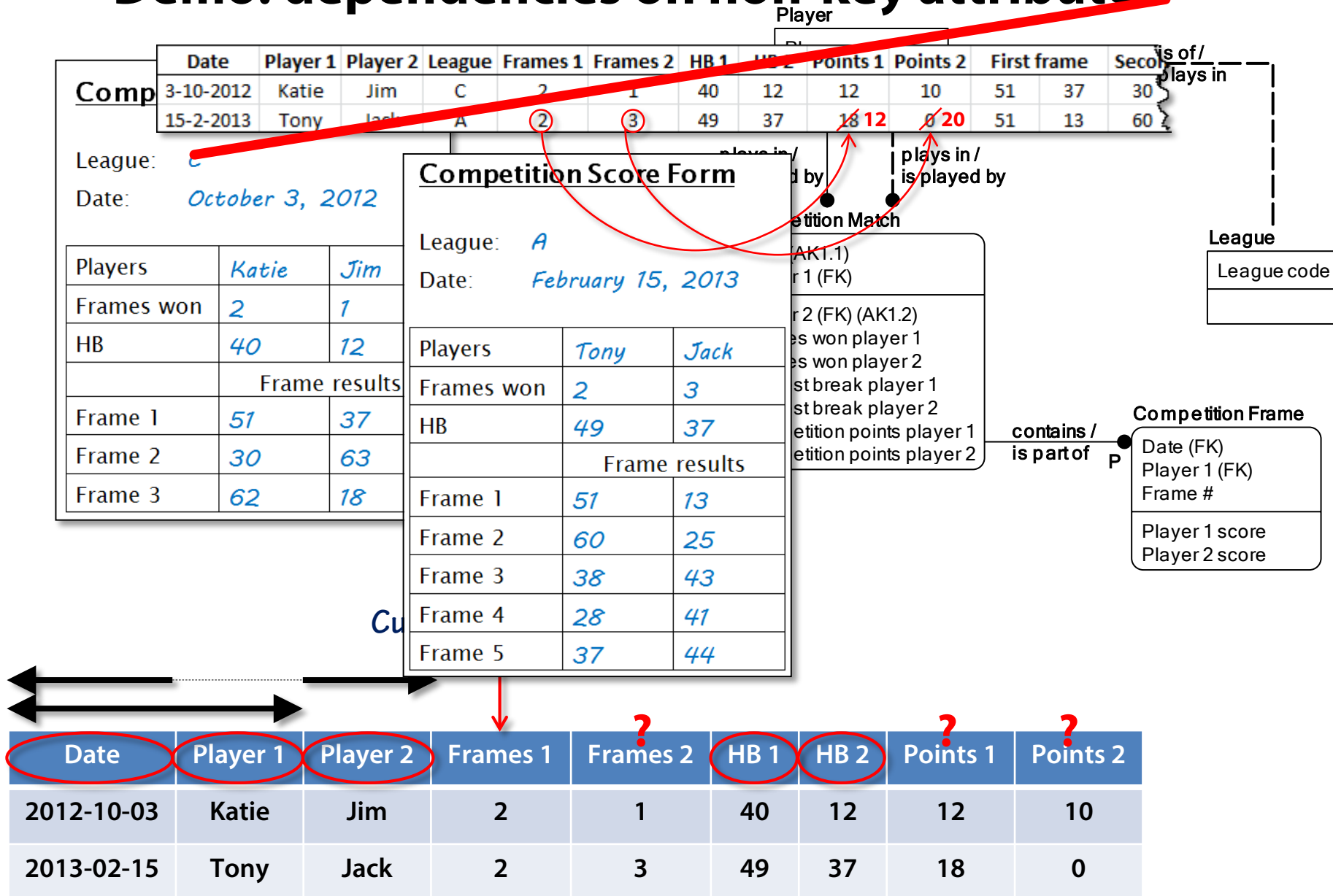
Currently checking



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2
2012-10-03	Katie	Jim	2	1	40	12	12	10
2013-02-15	Tony	Jack	2	0	49	37	18	0



# Demo: dependencies on non-key attributes



## Player

## League

League code

## Competition Frame

Date (FK)  
Player 1 (FK)  
Frame #

Player 1 score  
Player 2 score

contains /  
is part of

**P**

Cu

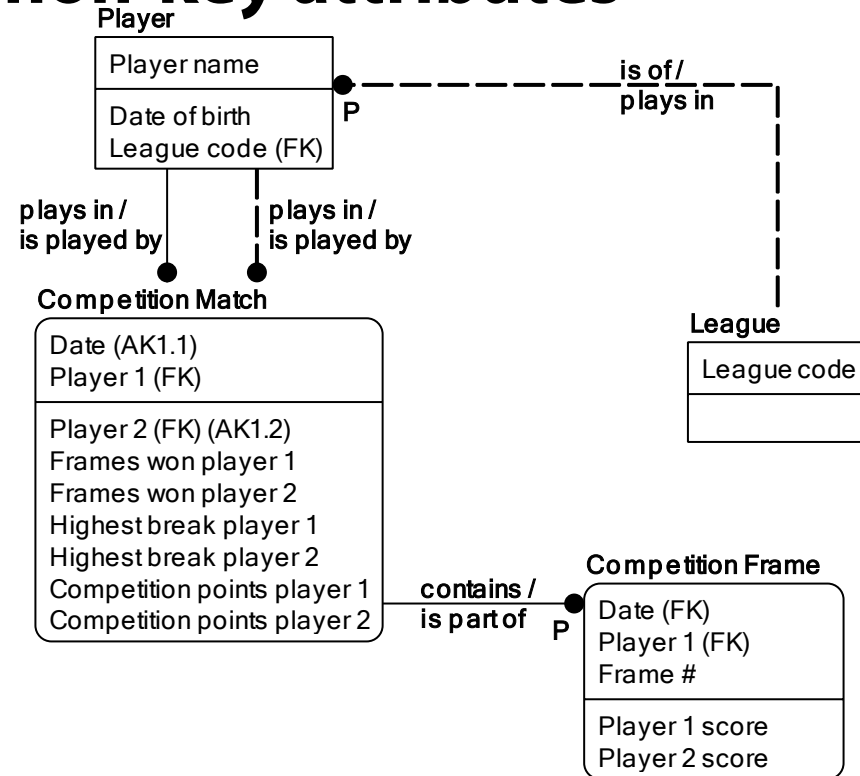
Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2
2012-10-03	Katie	Jim	2	1	40	12	12	10
2013-02-15	Tony	Jack	2	3	49	37	12	20

## Demo: dependencies on non-key attributes

## Dependency found:

- Frames 1  $\rightarrow$  Points 1

## Functional dependency or derivation rule?



## Currently checking

The diagram shows a table with 9 columns: Date, Player 1, Player 2, Frames 1, Frames 2, HB 1, HB 2, Points 1, and Points 2. The first three columns are circled in red. A red arrow points down to the 'Frames 1' column. A red 'X' is over the 'Points 1' column.

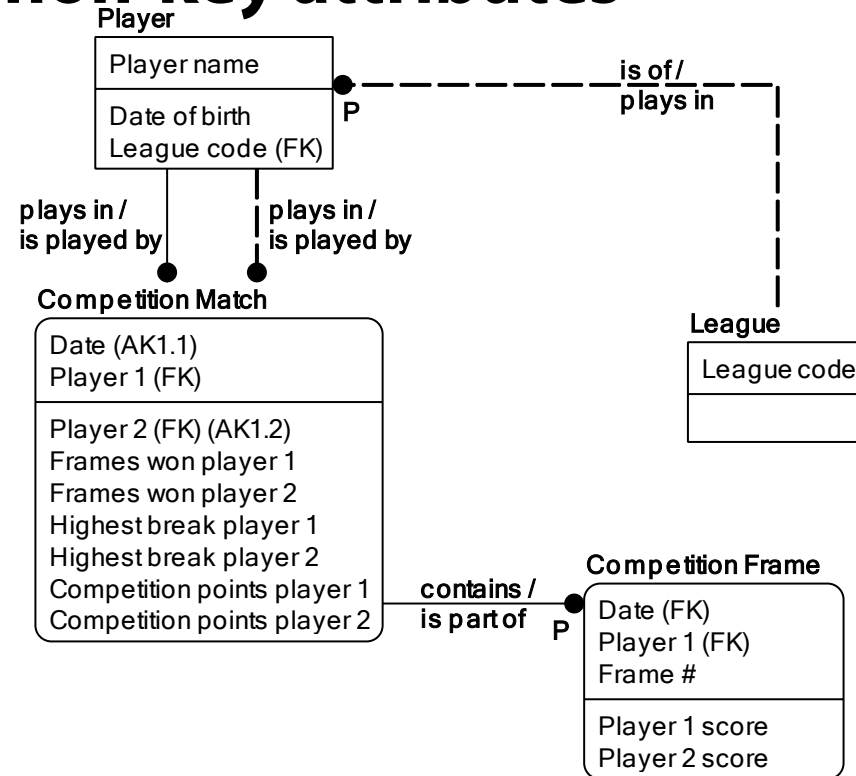
## Demo: dependencies on non-key attributes

## Dependency found:

- Frames 1  $\rightarrow$  Points 1

# Functional dependency!

# Violates 3NF!



## Currently checking

[illegible]

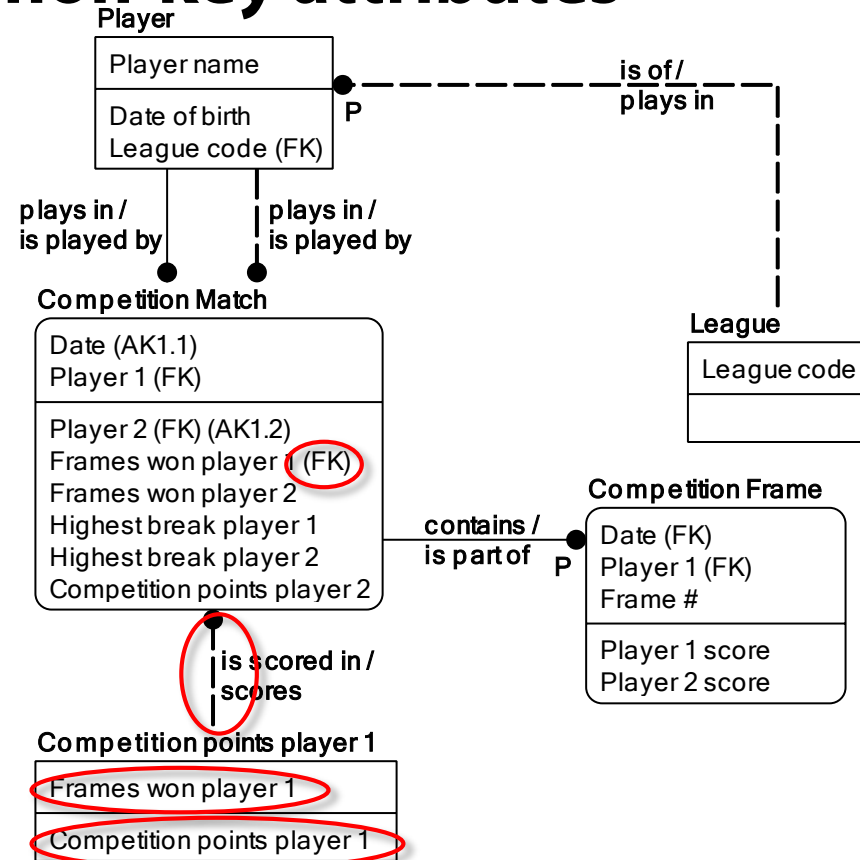
# Demo: dependencies on non-key attributes

Dependency found:

- Frames 1 → Points 1

Functional dependency!

**Violates 3NF!**



Currently checking

Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2

# Demo: dependencies on non-key attributes

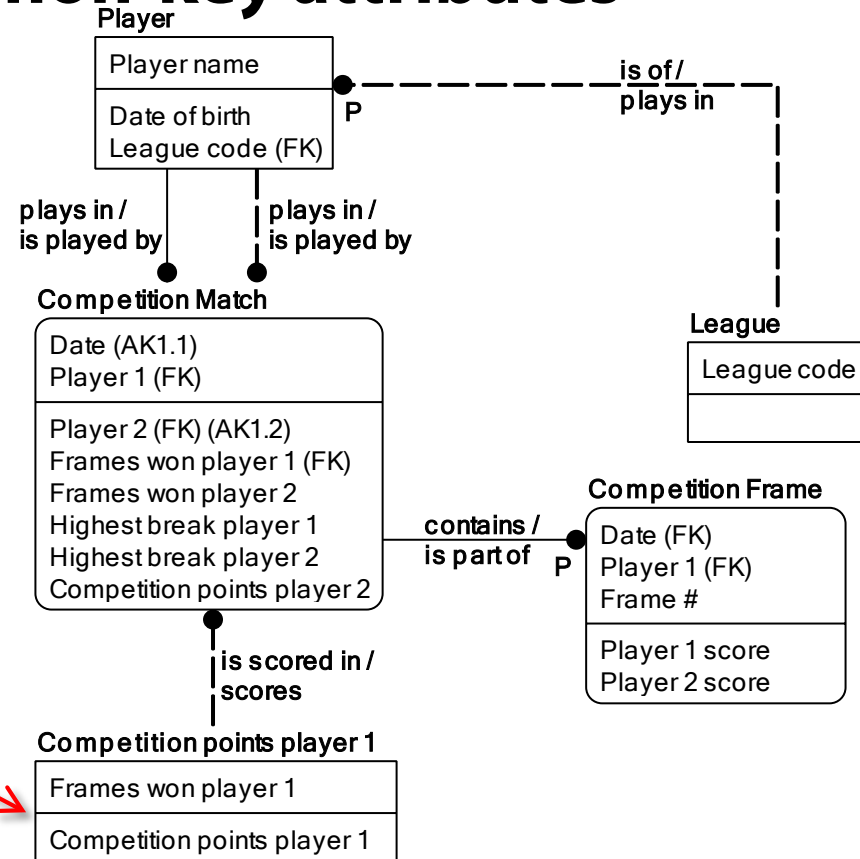
Dependency found:

- Frames 1 → Points 1

Functional dependency!

Frames won	Competition points
0	0
1	10
2	12
3	20
4	30
5	45

Currently checking



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2

# Demo: dependencies on non-key attributes

Dependency suspected:

- Frames 2 → Points 2

Date: *October 3, 2012*

Players	<i>Katie</i>	<i>Jim</i>
Frames won	<i>2</i>	<i>1</i>
HB	<i>40</i>	<i>12</i>
Frame results		
Frame 1	<i>51</i>	<i>37</i>
Frame 2	<i>30</i>	<i>63</i>
Frame 3	<i>62</i>	<i>18</i>

## Competition Score Form

League: *A*

Date: *February 15, 2013*

Players	<i>Tony</i>	<i>Jack</i>
Frames won	<i>2</i>	<i>3</i>
HB	<i>49</i>	<i>37</i>
Frame results		
Frame 1	<i>51</i>	<i>13</i>
Frame 2	<i>60</i>	<i>25</i>
Frame 3	<i>38</i>	<i>43</i>
Frame 4	<i>28</i>	<i>41</i>
Frame 5	<i>37</i>	<i>44</i>

Player

Date	Player 1	Player 2	League	Frames 1	Frames 2	HB 1	HB 2	Points 1	Points 2	First frame	Second frame	is of/ plays in
	<i>Jim</i>	<i>Katie</i>	<i>C</i>	<i>2</i>	<i>1</i>	<i>40</i>	<i>12</i>	<i>12</i>	<i>10</i>	<i>51</i>	<i>37</i>	<i>30</i>
	<i>Jim</i>	<i>Katie</i>	<i>A</i>	<i>2</i>	<i>3</i>	<i>49</i>	<i>37</i>	<i>18</i>	<i>20</i>	<i>51</i>	<i>13</i>	<i>60</i>

plays in/  
is played by

Competition Match

AK1.1)
r 1 (FK)
r 2 (FK) (AK1.2)
es won player 1 (FK)
es won player 2
st break player 1
st break player 2
etition points player 2

is scored in/  
scores

etition points player 1

es won player 1

etition points player 1

League

League code

## Competition Frame

Date (FK)  
Player 1 (FK)  
Frame #

Player 1 score  
Player 2 score

contains /  
is part of

P



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2	Points 2
2012-10-03	Katie	Jim	2	1	40	12	10
2013-02-15	Tony	Jack	2	3	49	37	0

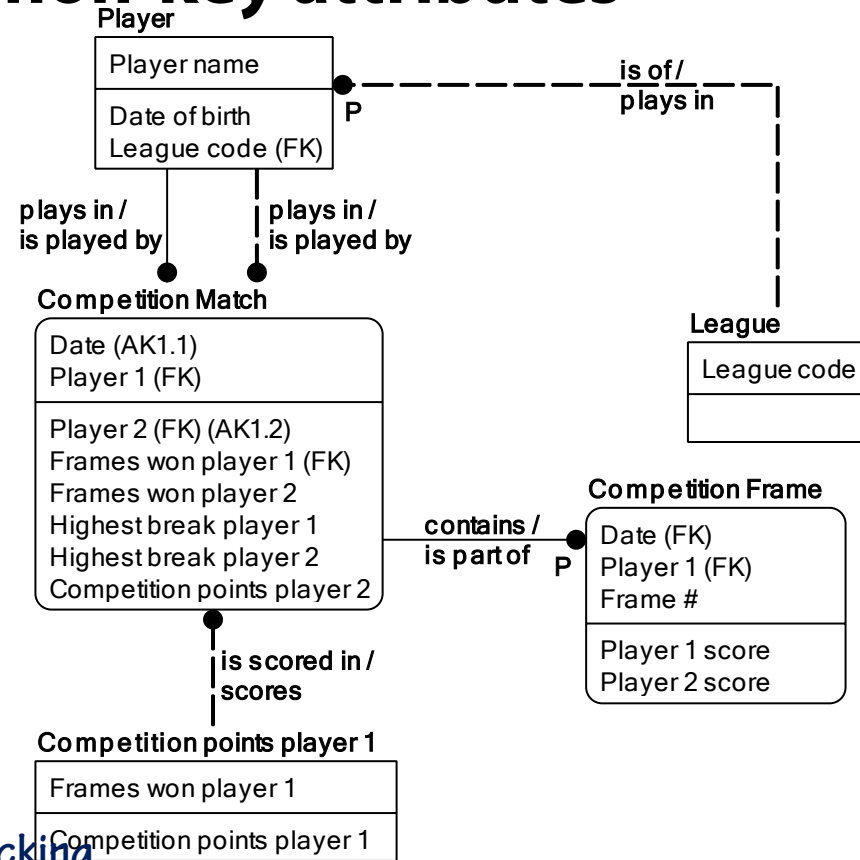
# Demo: dependencies on non-key attributes

Dependency found:

- Frames 2 → Points 2

Functional dependency!

**Violates 3NF!**



Currently checking



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2	Points 2



# Demo: dependencies on non-key attributes

Dependency found:  
• Frames 2 → Point

Functional dependency!

Competition points player 2

Frames won player 2
Competition points player 2

is scored in /  
scores

Player

Player name
Date of birth
League code (FK)

plays in /  
is played by

plays in /  
is played by

Competition Match

Date (AK1.1)
Player 1 (FK)
Player 2 (FK) (AK1.2)
Frames won player 1 (FK)
Frames won player 2 (FK)
Highest break player 1
Highest break player 2

contains /  
is part of

Competition Frame

Date (FK)
Player 1 (FK)
Frame #
Player 1 score
Player 2 score

is of /  
plays in

League

League code
-------------

is scored in /  
scores

Competition points player 1

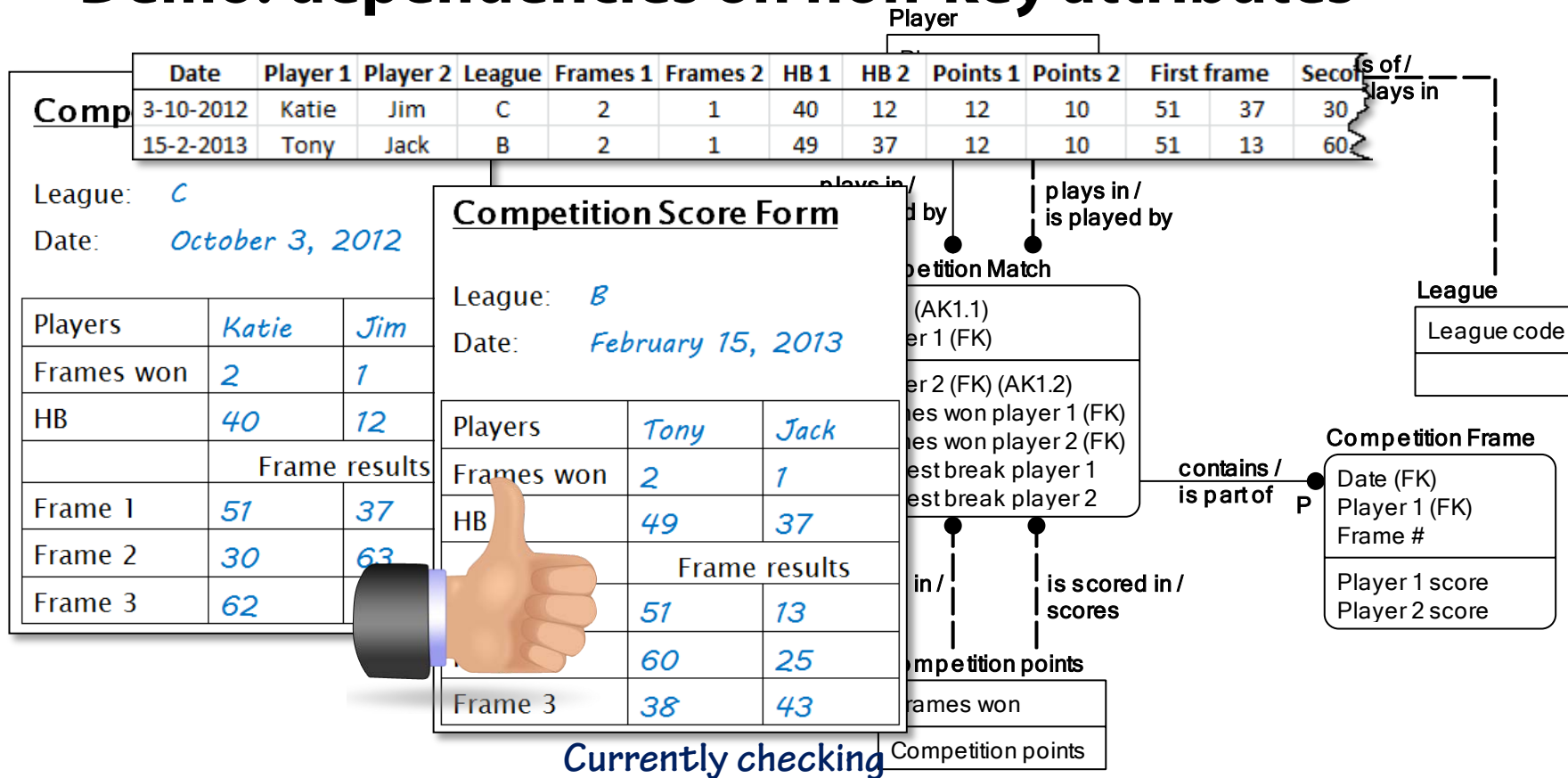
Frames won player 1
Competition points player 1

Currently checking



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2	Points 2

# Demo: dependencies on non-key attributes



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2
2012-10-03	Katie	Jim	2	1	40	12
2013-02-15	Tony	Jack	2	1	49	37

## Player

## League

League code

## Competition Frame

Date (FK)  
 Player 1 (FK)  
 Frame #

Player 1 score  
Player 2 score

## Competition Match

(AK1.1)

er 1 (FK)

er 2 (FK) (AK1.2)

Player 1 won player 1 (FK)

Player 1 won player 2 (1)

Best break player 1

● ●

in /	is scored in / scores
1	1
2	2
3	3
4	4
5	5
6	6
7	7
8	8
9	9
10	10
11	11
12	12
13	13
14	14
15	15
16	16
17	17
18	18
19	19
20	20
21	21
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96	96
97	97
98	98
99	99
100	100

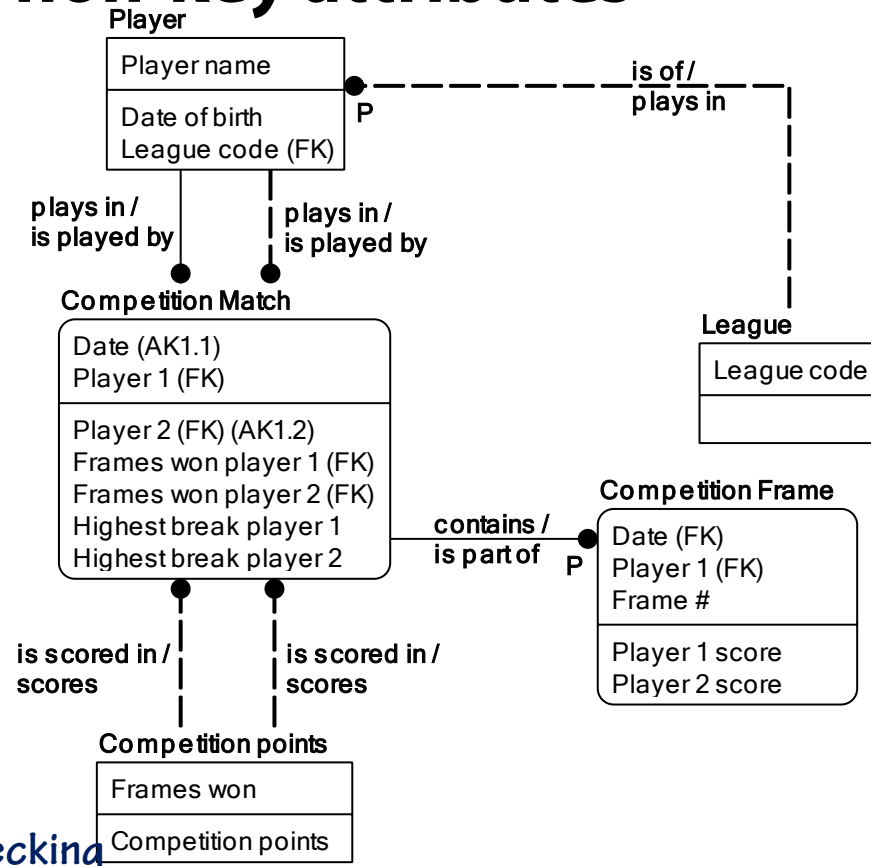
### Competition points

frames won

## Competition points

2

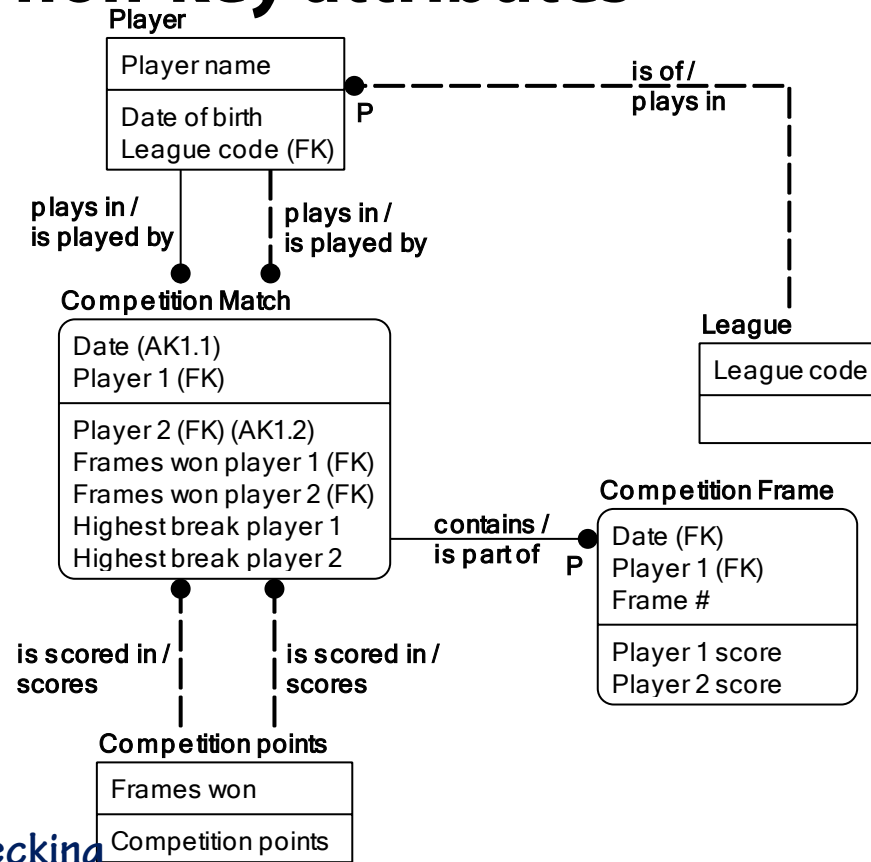
# Demo: dependencies on non-key attributes



Currently checking

Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

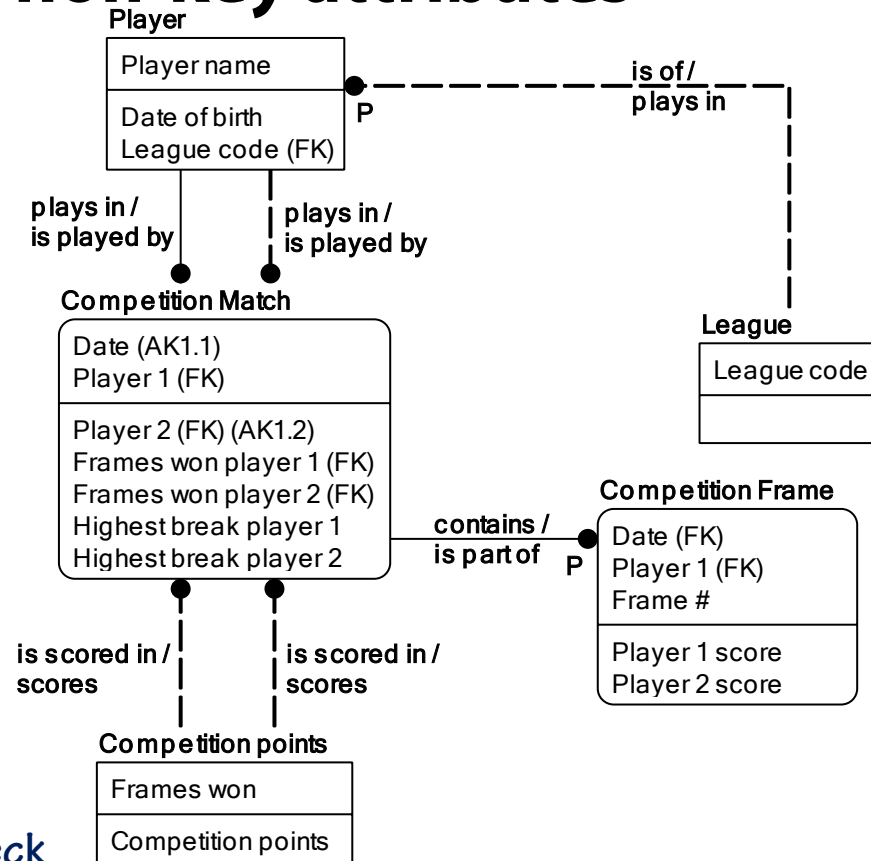
# Demo: dependencies on non-key attributes



Currently checking

Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

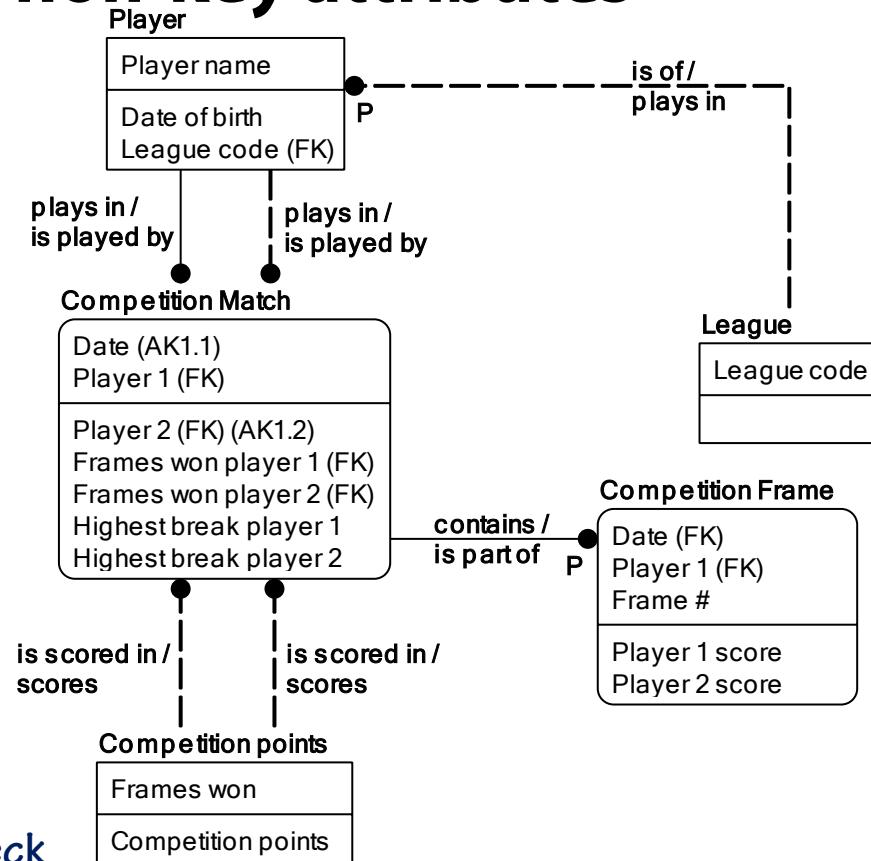
# Demo: dependencies on non-key attributes



Do not check

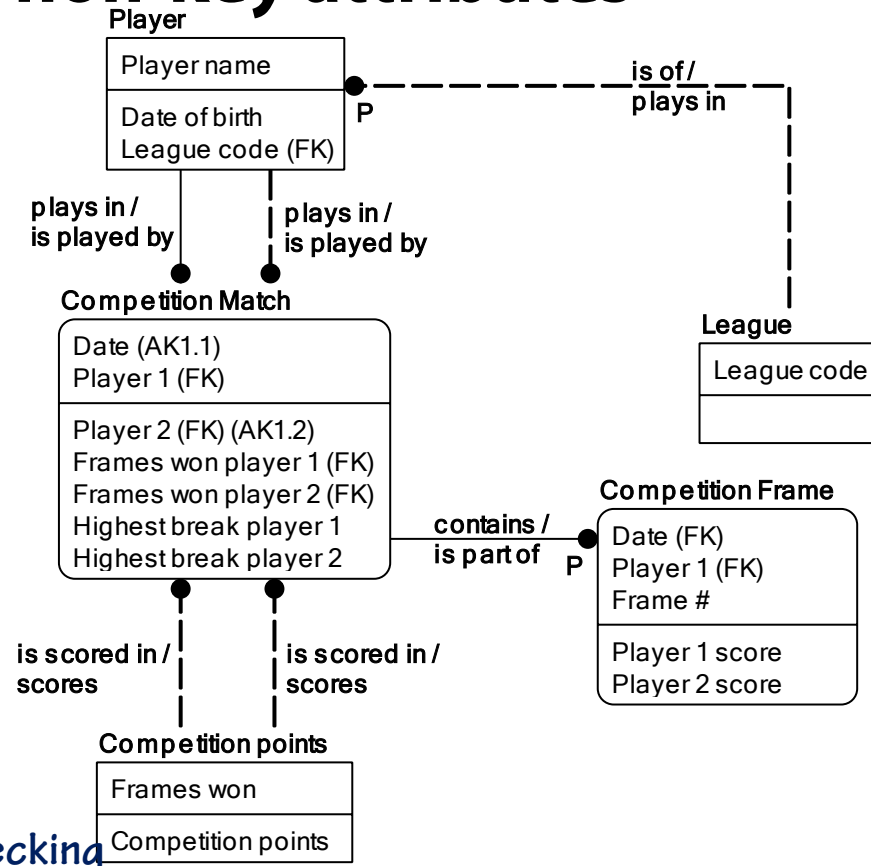
Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

# Demo: dependencies on non-key attributes



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

# Demo: dependencies on non-key attributes

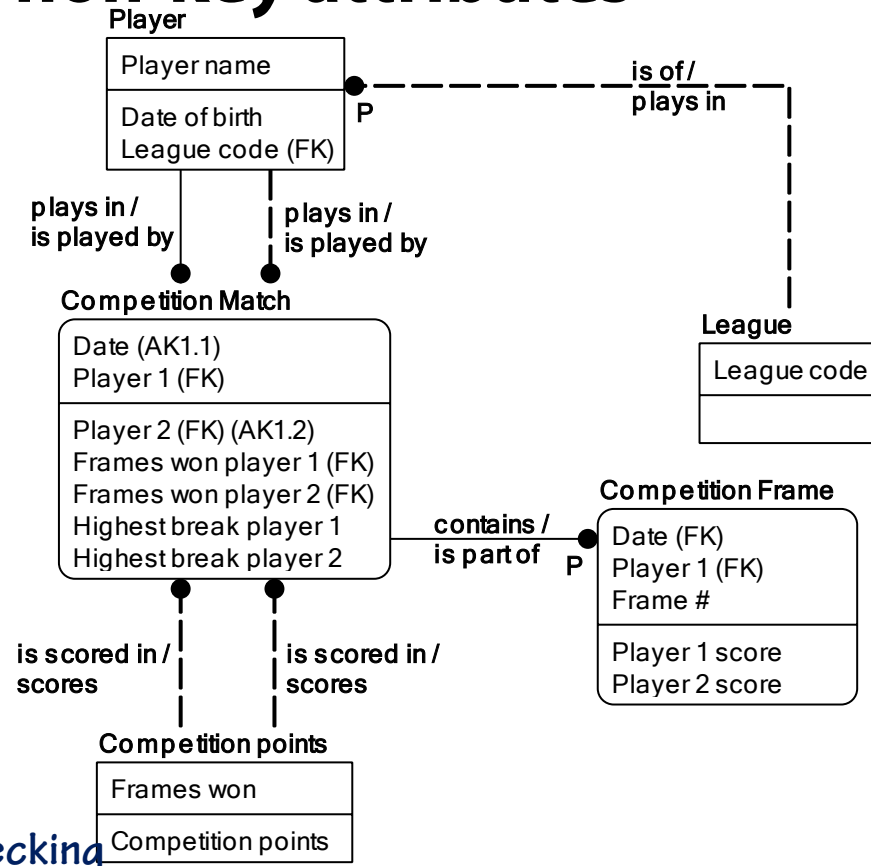


Currently checking

Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2



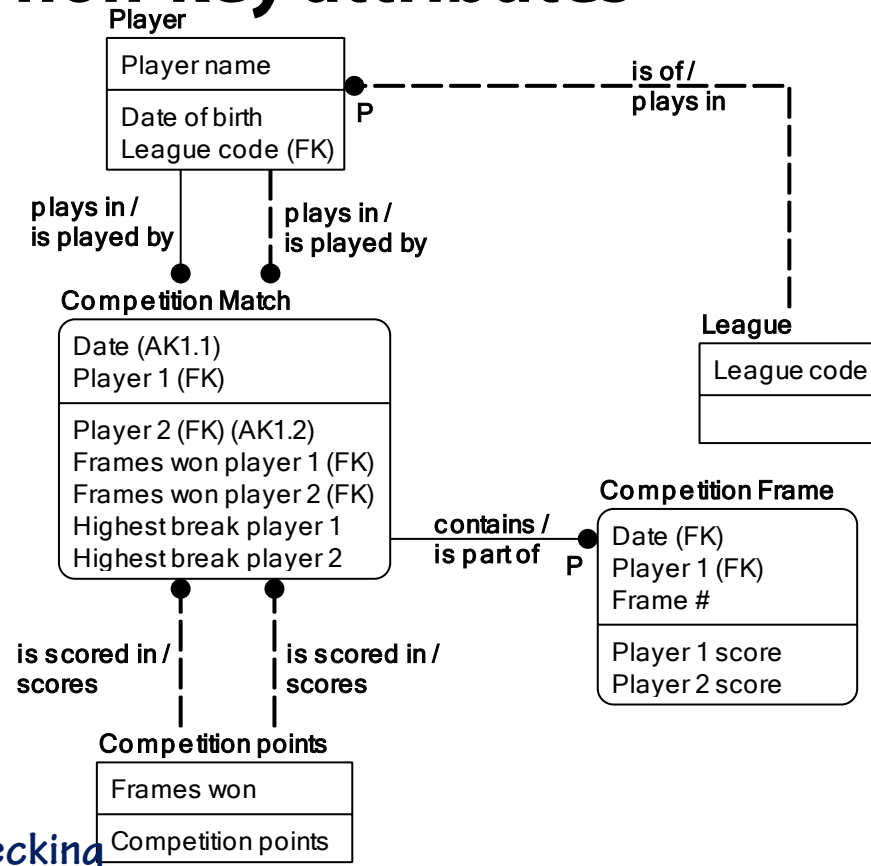
# Demo: dependencies on non-key attributes



Currently checking

Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

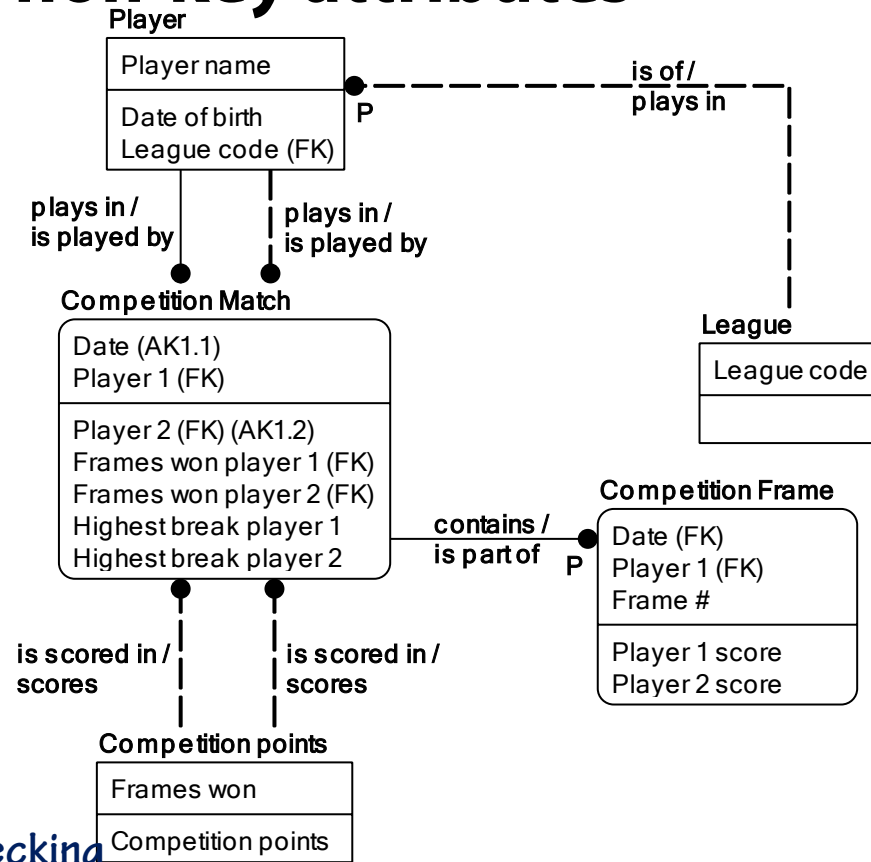
# Demo: dependencies on non-key attributes



Currently checking

Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

## Demo: dependencies on non-key attributes



Currently checking

Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

# Demo: dependencies on non-key attributes

**Competition Score Form**

League: *C*

Date: *October 3, 2012*

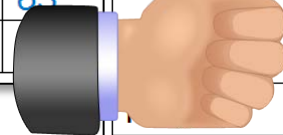
Players	<i>Katie</i>	<i>Jim</i>
Frames won	<i>2</i>	<i>1</i>
HB	<i>40</i>	<i>12</i>
Frame results		
Frame 1	<i>51</i>	<i>37</i>
Frame 2	<i>30</i>	<i>63</i>
Frame 3	<i>62</i>	

**Competition Score Form**

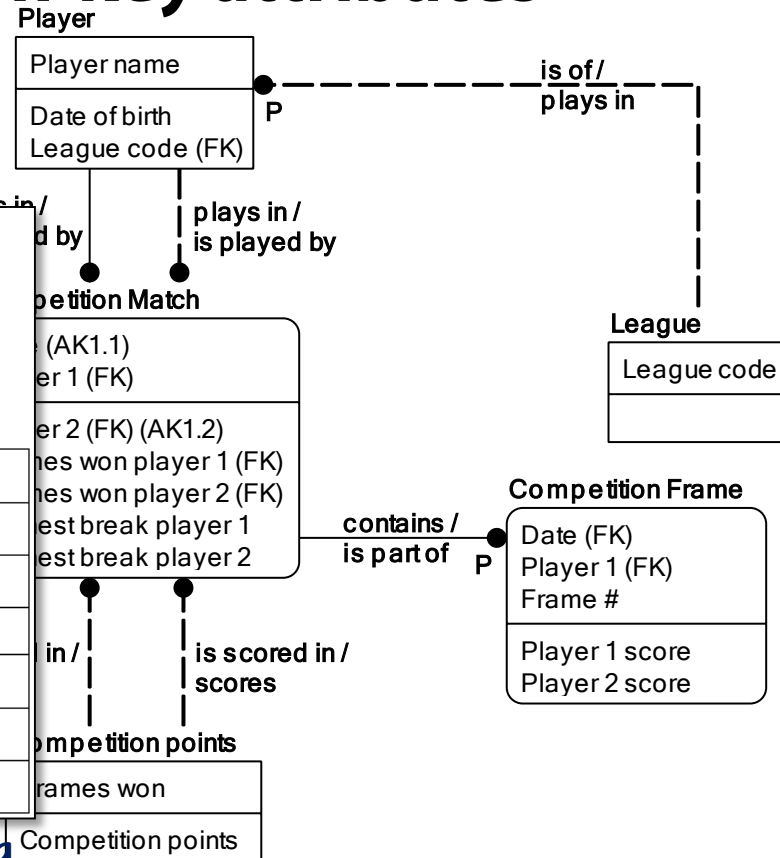
League: *C*

Date: *February 7, 2013*

Players	<i>Katie</i>	<i>Jim</i>
Frames won	<i>3</i>	<i>0</i>
HB	<i>36</i>	<i>12</i>
Frame results		
	<i>43</i>	<i>22</i>
	<i>43</i>	<i>7</i>
Frame 3	<i>37</i>	<i>35</i>

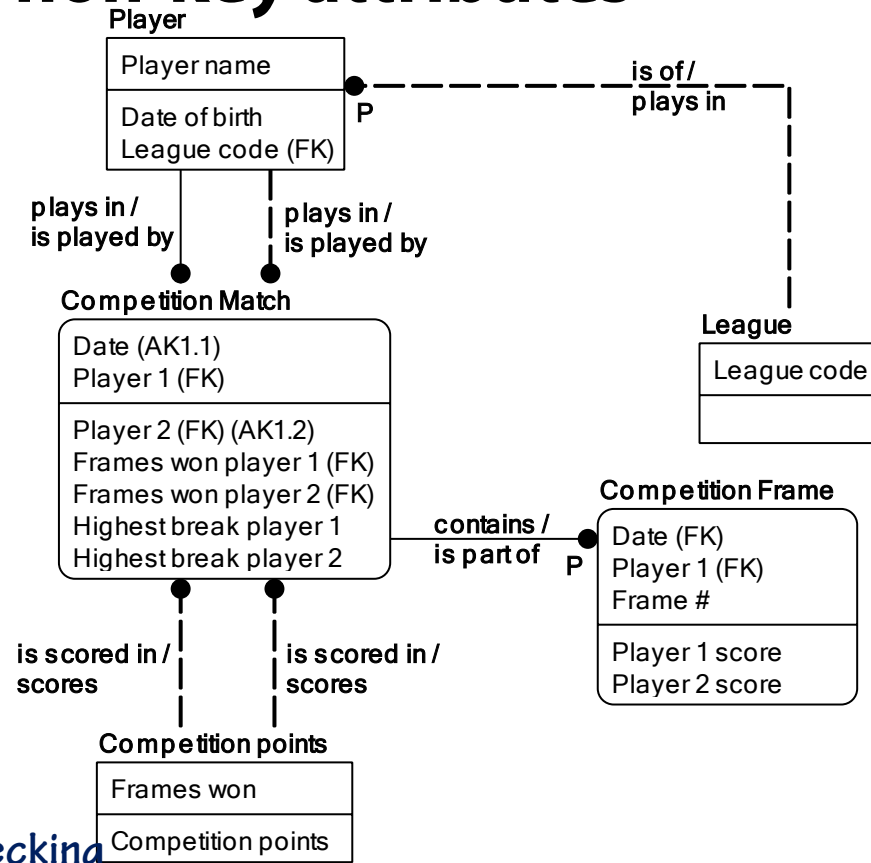


Currently checking



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2
2012-10-03	Katie	Jim	2	1	40	12
2013-02-07	Katie	Jim	3	0	36	12

# Demo: dependencies on non-key attributes



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2
2012-10-03	Katie	Jim	2	1	40	12
2013-02-15	Katie	Jim	2	1	40	37

## Player

## League

League code

## Competition Frame

Date (FK)  
 Player 1 (FK)  
 Frame #

Player 1 score  
Player 2 score


in /	is scored in / scores
1	1
2	2
3	3
4	4
5	5
6	6
7	7
8	8
9	9
10	10
11	11
12	12
13	13
14	14
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91	91
92	92
93	93
94	94
95	95
96	96
97	97
98	98
99	99
100	100

### Competition points

ames won

## Competition points

Currently checking



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2
2012-10-03	Katie	Jim	2	1	40	12
2013-02-15	Katie	Jack	2	1	40	37

## Player

## League

League code

## Competition Frame

Date (FK)  
Player 1 (FK)  
Frame #

Player 1 score  
Player 2 score

contains / is part of	P

in /	is scored in /
scores	scores
1	1
2	2
3	3
4	4
5	5
6	6
7	7
8	8
9	9
10	10
11	11
12	12
13	13
14	14
15	15
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90	90
91	91
92	92
93	93
94	94
95	95
96	96
97	97
98	98
99	99
100	100

## Competition points

frames won

## Competition points

Currently checking

Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2
2012-10-03	Katie	Jim	2	1	40	12
2013-02-15	Katie	Jack	2	1	49	37

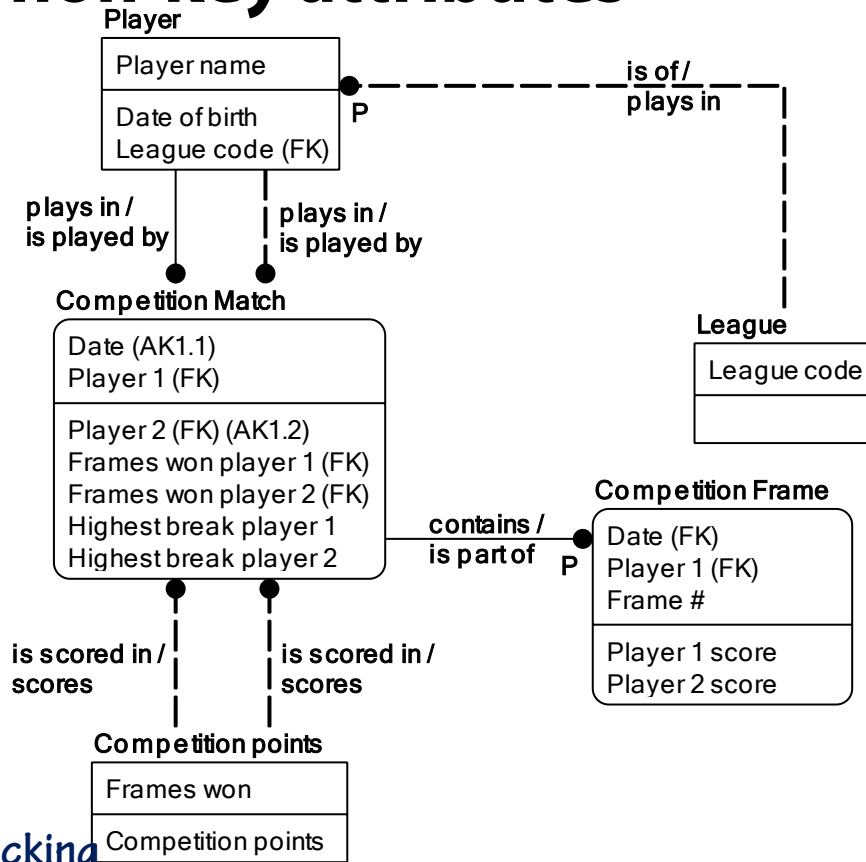
# Demo: dependencies on non-key attributes

Dependency found:

- {Player 1, Frames 1} → Frames 2

Actual underlying dependencies:

- {League, Frames 1} → Frames 2
- Player 1 → League



Currently checking

Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

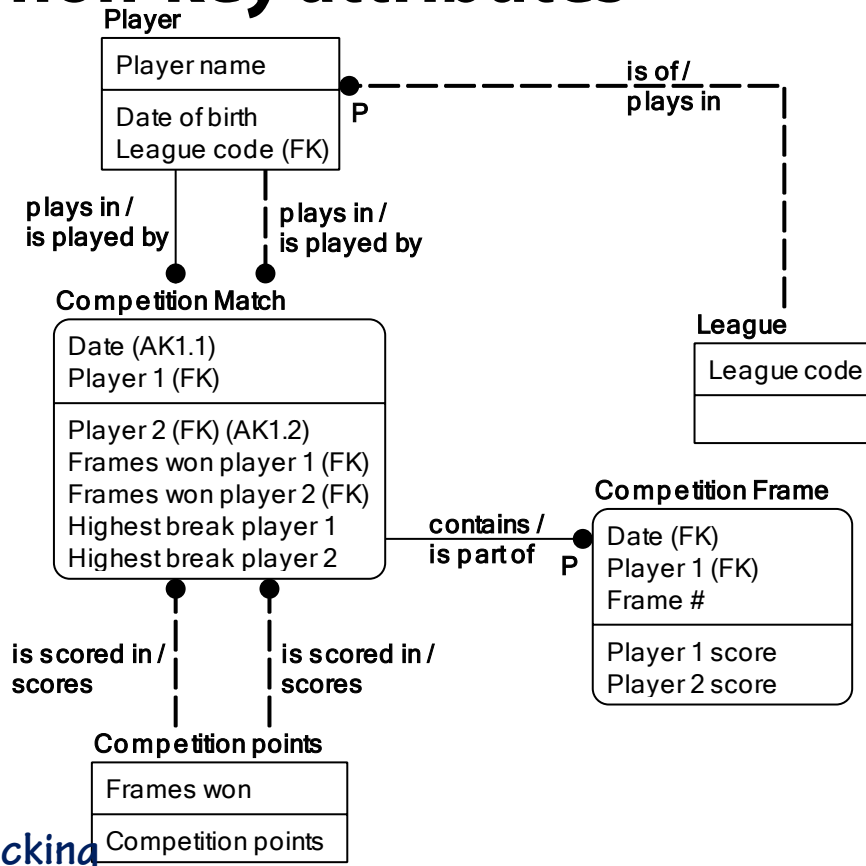


# Demo: dependencies on non-key attributes

Dependency found:

- {Player 1, Frames 1} → Frames 2

Functional dependency  
or derivation rule?



Currently checking

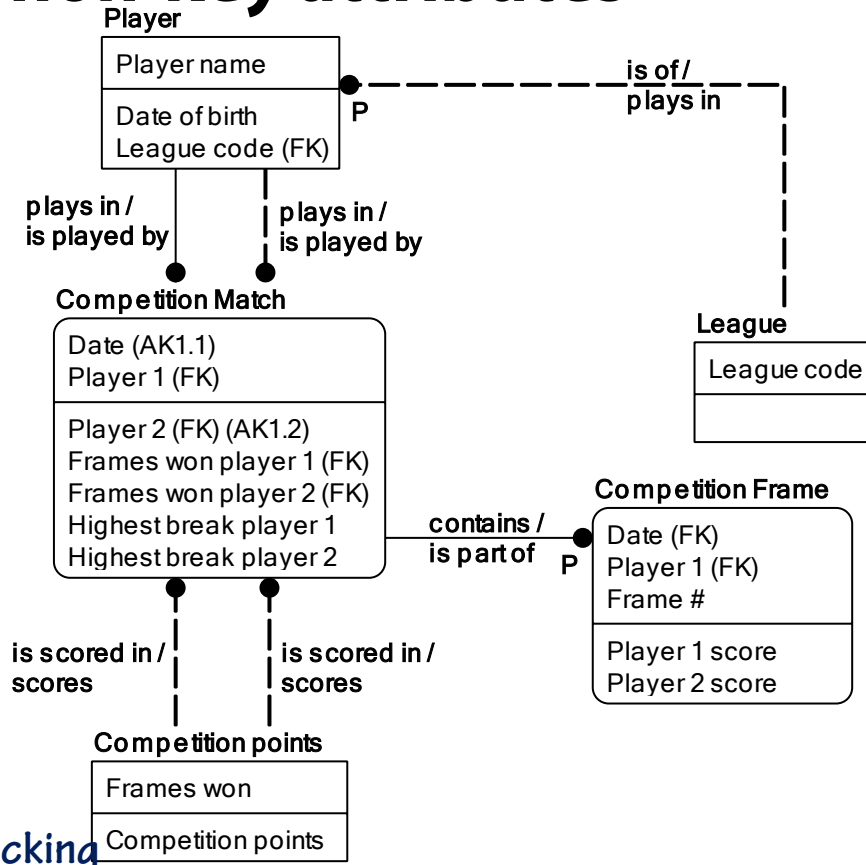
Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

# Demo: dependencies on non-key attributes

Dependency found:

- {Player 1, Frames 1} → Frames 2

Derivation rule!



Currently checking

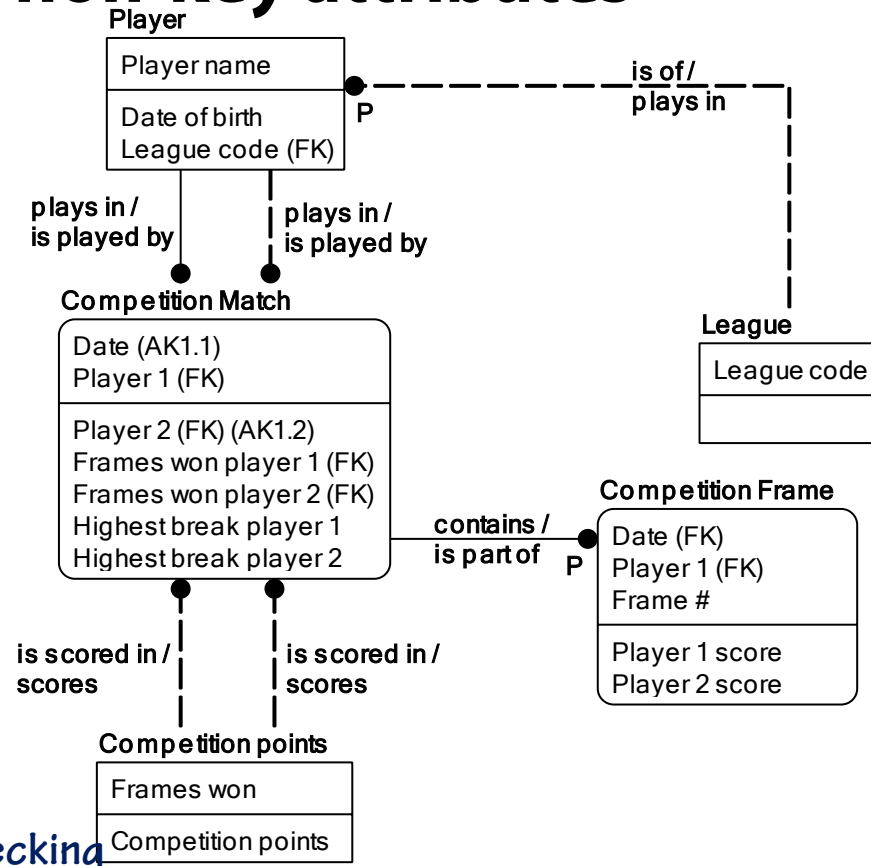
Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

# Demo: dependencies on non-key attributes

Dependency found:

- {Player 1, Frames 1} → Frames 2

Derivation rule!



Currently checking

Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

Derivation rule:

**Frames won player 2**

is computed from

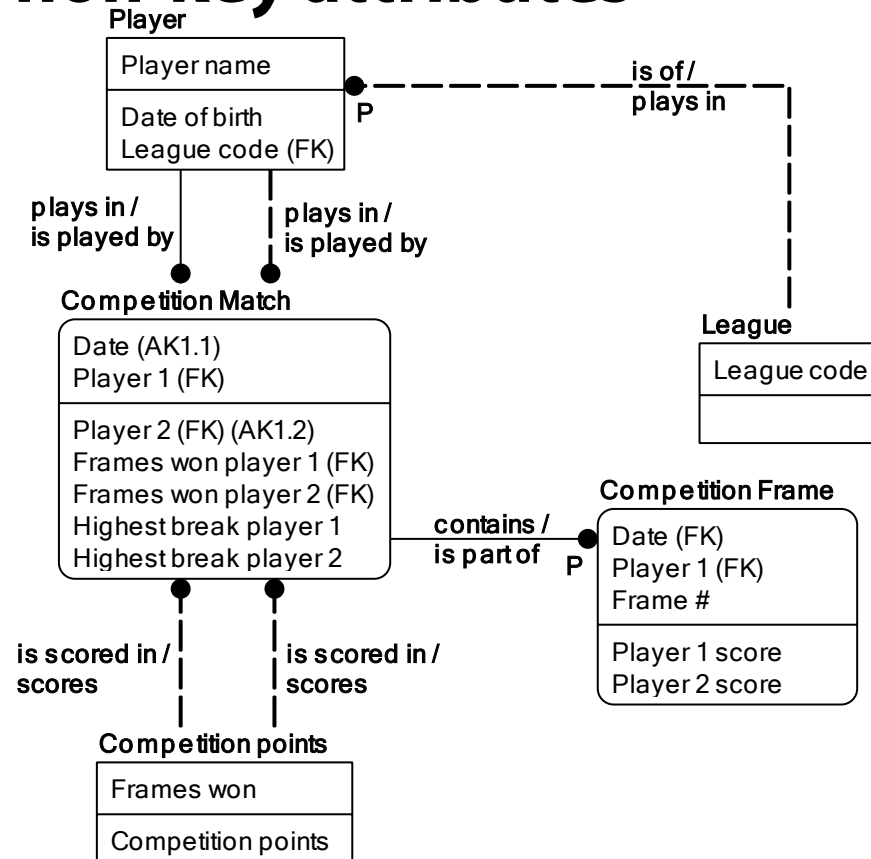
**Frames won player 1**

and

**Player 1 → League code**

(see specification in design docs)

# Demo: dependencies on non-key attributes



Date	Player 1	Player 2	Frames 1	Frames 2	HB 1	HB 2

Derivation rule:  
**Frames won player 2**  
 is computed from  
**Frames won player 1**  
 and  
**Player 1 → League code**  
*(see specification in design docs)*

# Summary

## ■ Problems

- Redundancy
- Modification anomalies
- Fixed by normalization

## ■ Functional dependencies

## ■ Normal forms

- First Normal Form
- Second Normal Form
- Third Normal Form

The key, the whole key, and nothing but the key; so help me Codd



Dr. E.J. Codd

Illustration: Michael J. Swart

# References

- **Further reading:**

- Database normalization on Wikipedia:

- [http://en.wikipedia.org/wiki/Database\\_normalization](http://en.wikipedia.org/wiki/Database_normalization)

- or

- <http://tinyurl.com/Norm-DB>

- P.A. Bernstein's algorithm for synthesis of a Third Normal Form schema:

- [http://student.bus.olemiss.edu/files/conlon/others/Others/Bus669\\_ComplInfo/DB\\_Design\\_SQL/Bernstein.pdf](http://student.bus.olemiss.edu/files/conlon/others/Others/Bus669_ComplInfo/DB_Design_SQL/Bernstein.pdf)

- or

- <http://tinyurl.com/BernAlgo>