

CS342: Software Engineering

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Lecture 12 ANALYSIS WORKFLOW

*Adapted from Software Engineering, by Dr. Paul E. Young
& slides by Dr. Mohammad Daoud*

Finite State Machines State Transitions

Current State + Event + Predicate \Rightarrow Next State

- A **State** is a description of the status of a system waiting to execute a transition.
- A **Transition** is a set of actions to be executed when a condition is satisfied, or an event received.
- An **Event** is an occurrence within a particular system or domain; it is something that has happened or is expected to happen in that domain.
- A **Predicate** is a function or a statement that returns a Boolean value depending on the data passed to the predicate.

The Power of Finite State Machines (FSM)

- Advantages of using an FSM, a specification is
 - Easy to write it down
 - Easy to validate
 - Easy to convert into a design
 - Easy to convert into code
 - Easy to understand
 - Easy to maintain
 - More precise than graphical methods
- Disadvantages of FSM
 - Timing considerations are not handled

Difficulty with Specifying Real-Time Systems

- A major difficulty with specifying real-time systems is **timing**
 - Synchronization problems
 - Race conditions (*perform two or more operations at the same time*)
 - Deadlock
- Often a consequence of poor specifications
- **Solution? \Rightarrow Petri Nets.**

Petri Nets

- A **Petri net** (also known as a **place/transition net** or **P/T net**) is one of several **mathematical modeling languages** for the description of distributed systems that have **timing problems**.
- A powerful technique for **specifying systems** that have potential **timing problems**.

Petri Nets Specifications

- A Petri net consists of four parts:
- A set of **places** P
- A set of **transitions** T
- An **input function** $I(t)$
 - Mapping from **transitions** to a set of **places**
- An **output function** $O(t)$
 - Mapping from **transitions** to a set of **places**

Petri Nets Mathematical Model

A Petri net is a 4-tuple $C = (P, T, I, O)$

- $P = \{p_1, p_2, \dots, p_n\}$ is a **finite set of *places***, $n \geq 0$
- $T = \{t_1, t_2, \dots, t_m\}$ is a **finite set of *transitions***,
 $m \geq 0$, with disjoint P and T
- $I : T \rightarrow P^\infty$ is the ***input function***, a **mapping** from
set of ***transitions*** to a set of ***places***.

Petri Nets Mathematical Model

- $O : T \rightarrow P^\infty$ is the *output function*, a mapping from *transitions* to a set of *places*
- A *marking* of a Petri net is an assignment of *tokens* to that Petri net.
- Any *distribution of tokens over the places* will represent a configuration of the net called a *marking*.

Petri Nets Architecture – Example 1

- Set of **places** P is $\{p_1, p_2, p_3, p_4\}$
- Set of **transitions** T is $\{t_1, t_2\}$

- **Input functions:**

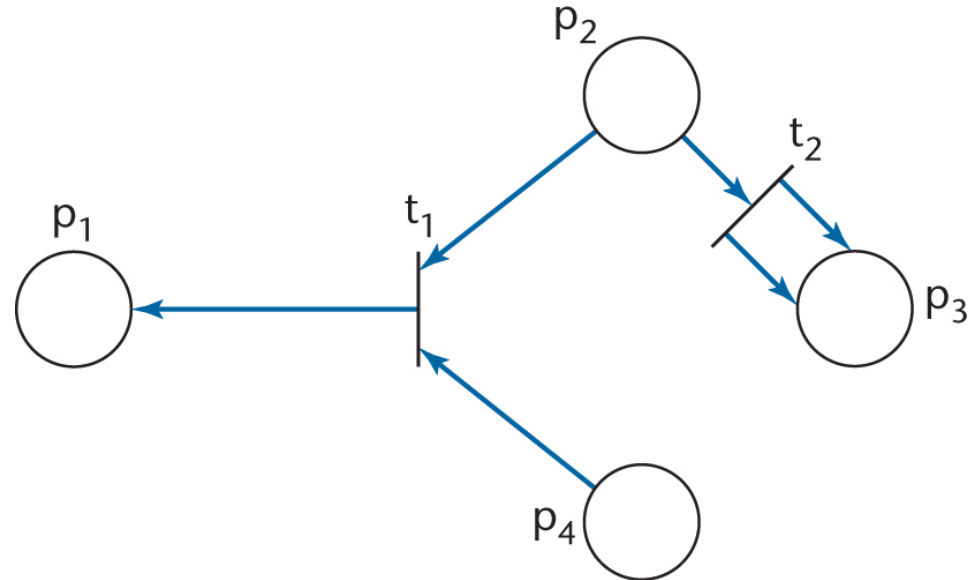
$$I(t_1) = \{p_2, p_4\}$$

$$I(t_2) = \{p_2\}$$

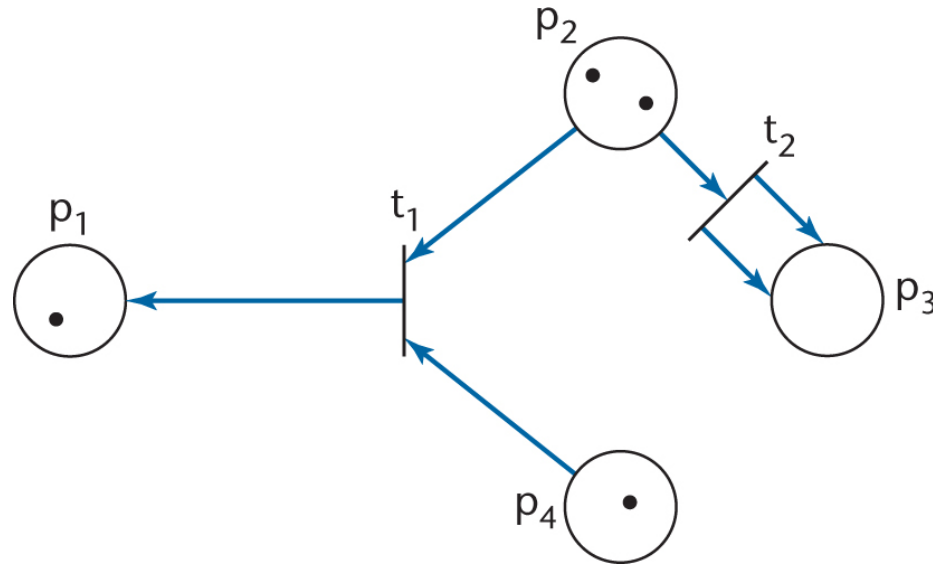
- **Output functions:**

$$O(t_1) = \{p_1\}$$

$$O(t_2) = \{p_3, p_3\}$$



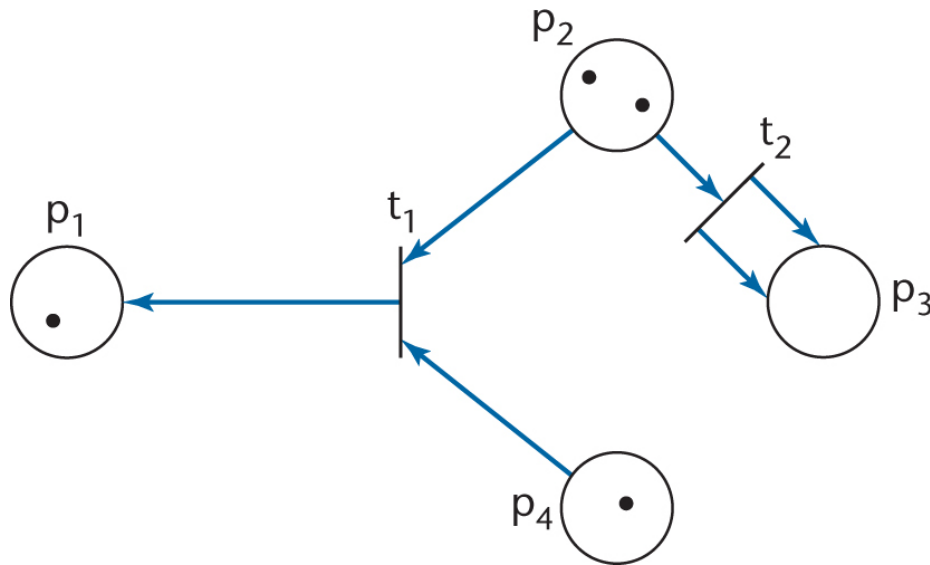
Petri Nets Marking – Example 2



- Four tokens: one in p_1 , two in p_2 , none in p_3 , and one in p_4 are represented by the **vector (1, 2, 0, 1)**

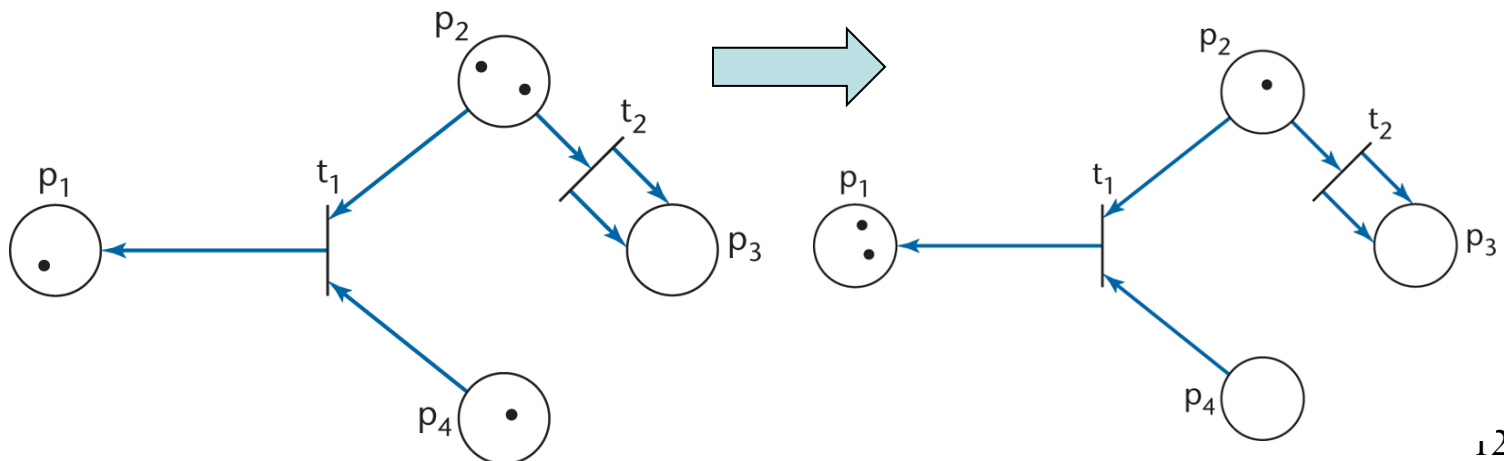
Enabled Transitions

- A **transition is enabled** (ready to fire) if each of its **input** places has number of tokens greater than or equal to the number of **arcs from the input place to that transition**. In the following figure, both **t1** and **t2** are enabled.



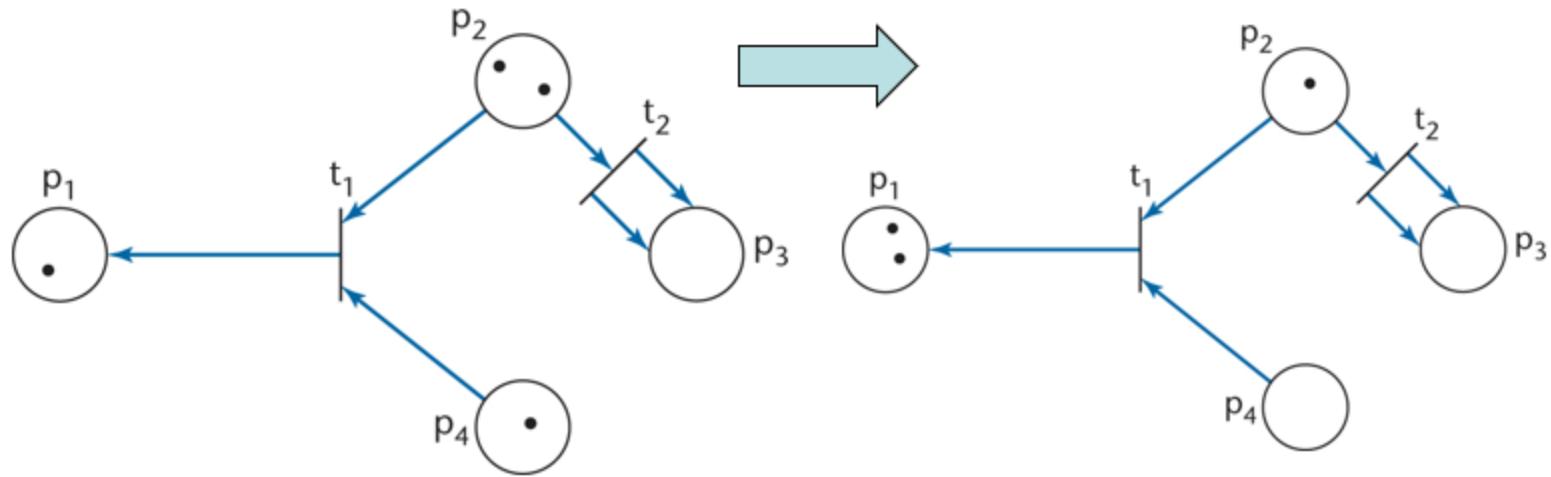
Petri Nets Tokens

- Transition t_1 is enabled (ready to fire)
 - If t_1 fires, one token is removed from p_2 and one from p_4 , and one new token is placed in p_1
- ⇒ Number of tokens is not conserved
- Transition t_2 is also enabled



Petri Nets Indeterminate

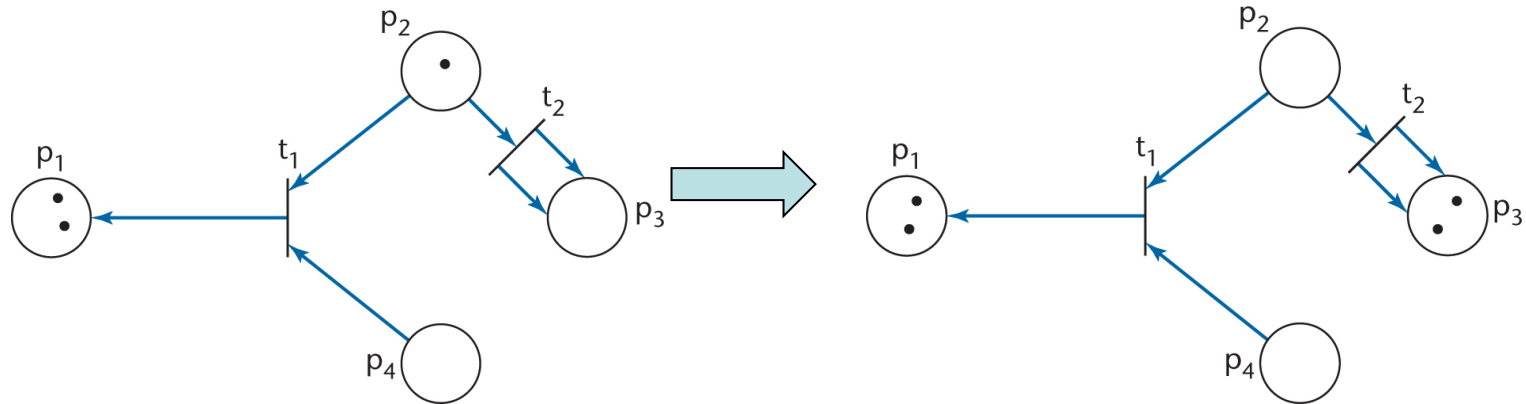
- Petri nets are **indeterminate**
 - Suppose t_1 is fired



- The **resulting marking** is $(2, 1, 0, 0)$

Petri Nets Transitions

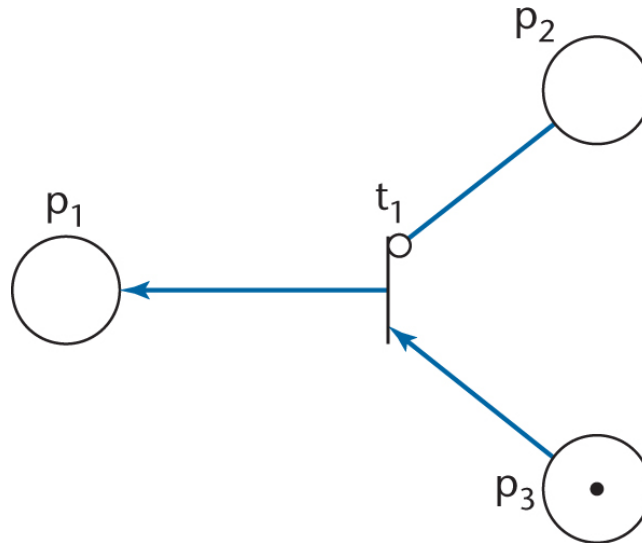
- Now, only t_2 is enabled.



- The resulting marking is $(2, 0, 2, 0)$

Petri Nets Inhibitor Arc

- **Inhibitor Arc:** imposes the precondition that the transition **may only fire when the place is empty**.
- An inhibitor arc is **marked by a small circle**, not an arrowhead.
- In the following Petri Net, transition **t_1 is enabled**



Updated Enabled Transitions

- In general, a transition is enabled if there is at least one token on each (normal) input arc places, and no tokens on any inhibitor input arcs places.

Petri Nets: Classical Real Time Systems

Analysis - Elevator Case Study

- **First Constraint on Elevator Buttons:**
 - Each elevator has a set of **m buttons**, one for each floor.
 - The **button light on** when pressed and cause the elevator to visit the corresponding floor.
 - The **button light off** when the corresponding floor is visited by an elevator.

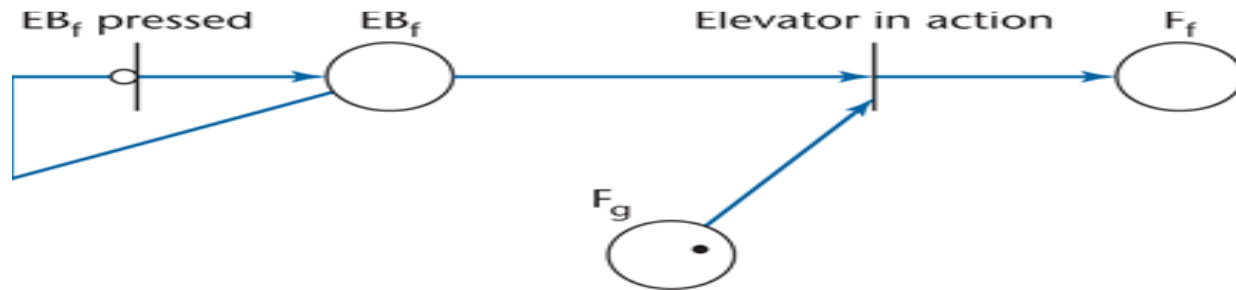
Petri Nets - Elevator Button Analysis

- The elevator button for floor f is represented by place

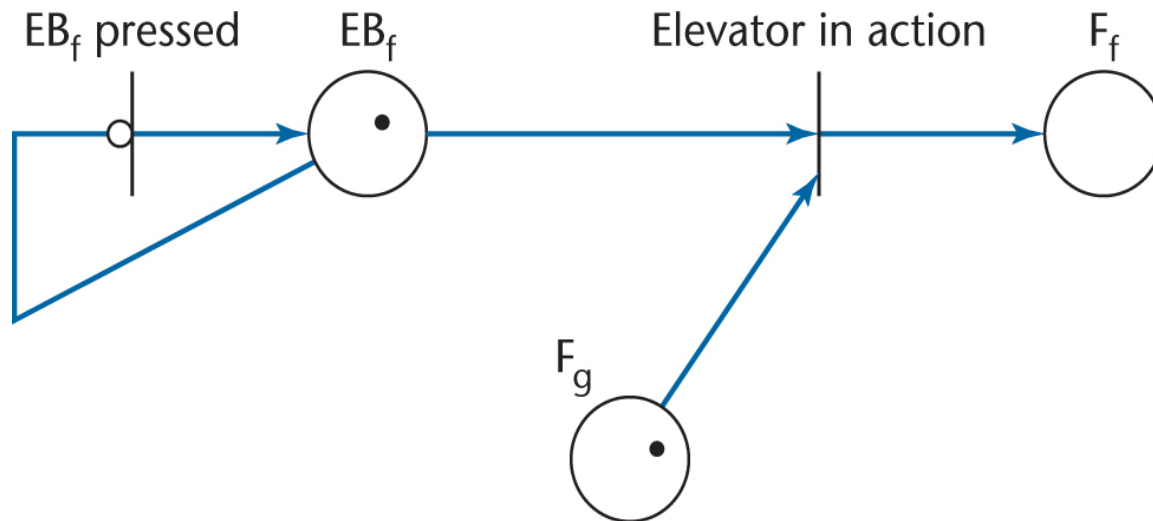
$$EB_f, 1 \leq f \leq m$$

- A **token in EB_f** denotes that the elevator button for floor f is light on.
- A button must be **light on the first time** the button is pressed, and subsequent button presses must be ignored.

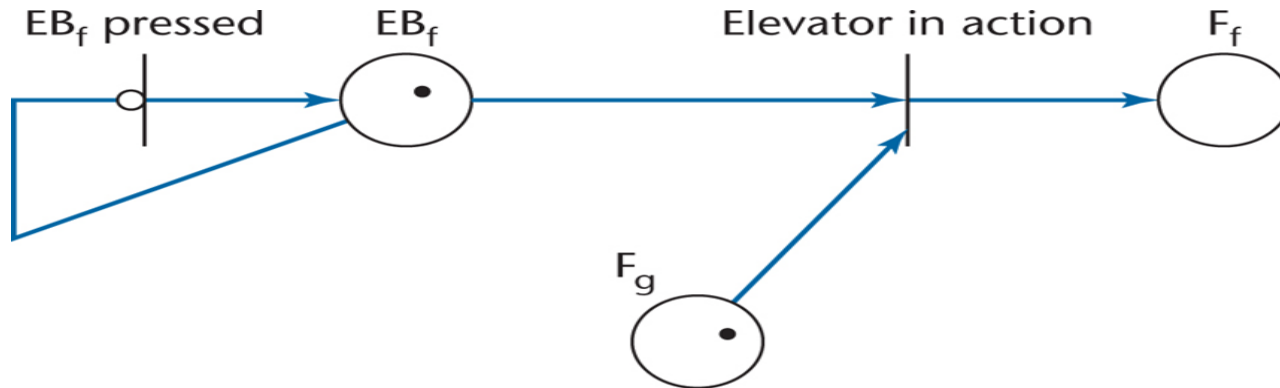
Petri Nets - Elevator Button Analysis



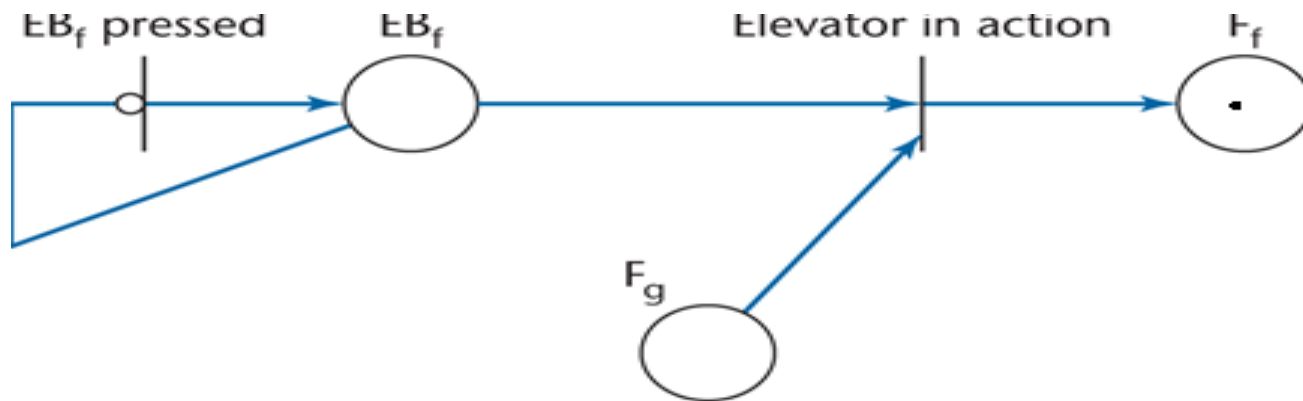
- Initial state, button EB_f is not pressed, **not lightened**, no token in place **EB_f** and transition EB_f is **not enabled**
- Next state, EB_f is pressed, new token is placed in EB_f



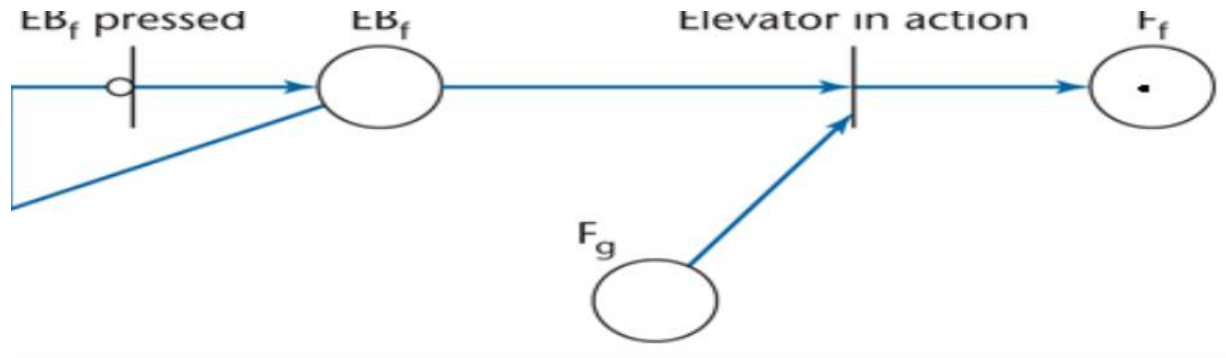
Petri Nets - Elevator Button Analysis



- Next state, when the elevator **reaches floor g**
 - The transition **Elevator in action** is enabled, and then fired
 - The tokens in EB_f and F_g are removed, and then the light in button EB_f is turned off.



Petri Nets - Elevator Button Analysis



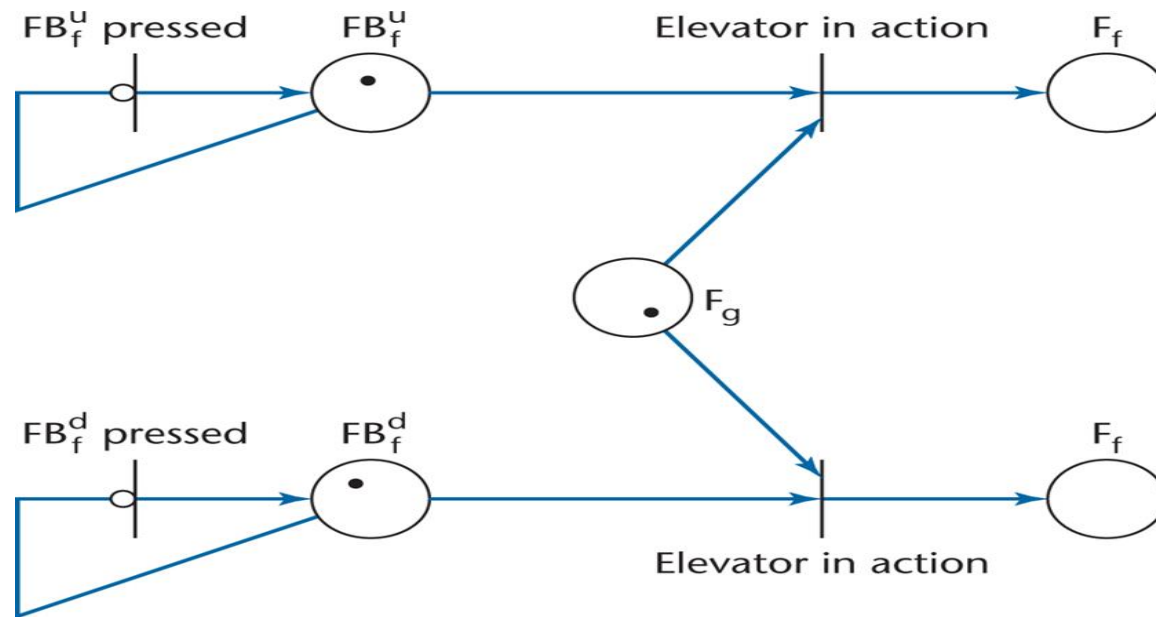
- A new token appears in F_f
 - This brings the elevator from floor g to floor f
- Motion from floor g to floor f cannot take place instantaneously
 - We need timed Petri nets

Petri Nets - Floor Button Analysis

- **Second constraint on Floor Buttons:**
- Each **floor**, except the first and the top floor, has **two buttons**, one to request elevator up, and the other to request elevator down.
- These buttons are lightened on upon pressed
- The light is **off** when the elevator **visits the floor**, and then moves in desired direction
- Floor buttons are represented by 2 places

FB_f^u and FB_f^d

Petri Nets – Floor Button Analysis



- The Petri net models the situation when an elevator reaches floor **f** from floor **g** with one or both buttons illuminated
- If both buttons are illuminated, **only one is turned off** (the button that represents the **direction of the elevator motion**).

Petri Nets - Elevator Waiting State Analysis

- **Third constraint on the Waiting State:**

If an elevator has **no requests**

- it remains at its current floor with its doors closed
- **no** Elevator in action **transition** is enabled

Comparison of Classical Analysis Techniques

1. **Formal methods** are Powerful, but **difficult to learn** and use. Example: Techniques such as **Petri nets**.
2. **Informal methods** have little power but are easy to learn and use; **written in a natural language**.
3. **Semiformal methods are** techniques between informal and formal.

Example: **S**oftware **R**equirements **E**ngineering **M**ethod (**SREM**)

- Useful for specifying real-time systems
- Powerful of finite state machine (FSM)

Comparison of Classical Analysis Techniques

4. New Classical Analysis Techniques

- Many are **untested** in practice
- Involved **risks**:
 - Training **costs**
 - **Adjustment** from the classroom to an actual project
 - **CASE tools may not work properly**
- However, possible gains *may* be huge

Computer Aided Software Engineering (CASE) Tools for Classical Analysis

- A graphical tool is very useful
- Typical tools
 - Analyst/Designer
 - Software through Pictures
 - System Architect

Comparison of Classical Analysis Techniques

- Which Analysis Technique Should Be Used?
- It depends on the
 - Project
 - Development team
 - Management team
 - Other factors?

Testing During Classical Analysis

- Specification inspection
 - Aided by fault checklist

Challenges of Classical Analysis

- A specification document must be
 - Informal enough for the client
 - Formal enough for the development team
- Analysis (“what”) should not cross the boundary into design (“how”).