



Statistical Inferences

Statistical analysis

Statistical analysis has two main focuses:

1. Descriptive statistics
2. Inferential statistics.

Descriptive statistics summarize data using graphs and summary values such as the mean and interquartile range.

- Descriptive statistics can help us identify relationships and patterns.
- Descriptive statistics do not draw conclusions

Inferential statistical analysis does allow us to make conclusions beyond the data we have to the population from which it was drawn.

A definition of inference is: The process of drawing conclusions about population parameters based on a sample taken from the population



Inference

- A sample is likely to be a good representation of the population
- There is an element of uncertainty as to how well the sampler presents the population
- The way the sample is taken matters

How to Make Statistical Inferences





Inferences in statistics can help you make predictions and conclusions about the populations you are looking at by interpreting the results of random samples from that population. The two main applications of inferential statistics that help us to draw these conclusions are **hypothesis testing** and **confidence intervals** of the data.

Statistical inferences are dependent on three main components:

- The **size of samples**;
- Variability in the samples**; and
- The **size of the observed differences**.

1. The data for the experiment should be obtained through **random samples or randomized experiments**
2. The distribution of the sample means must be approximately normal
3. Individual observations must be independent



Sampling Process

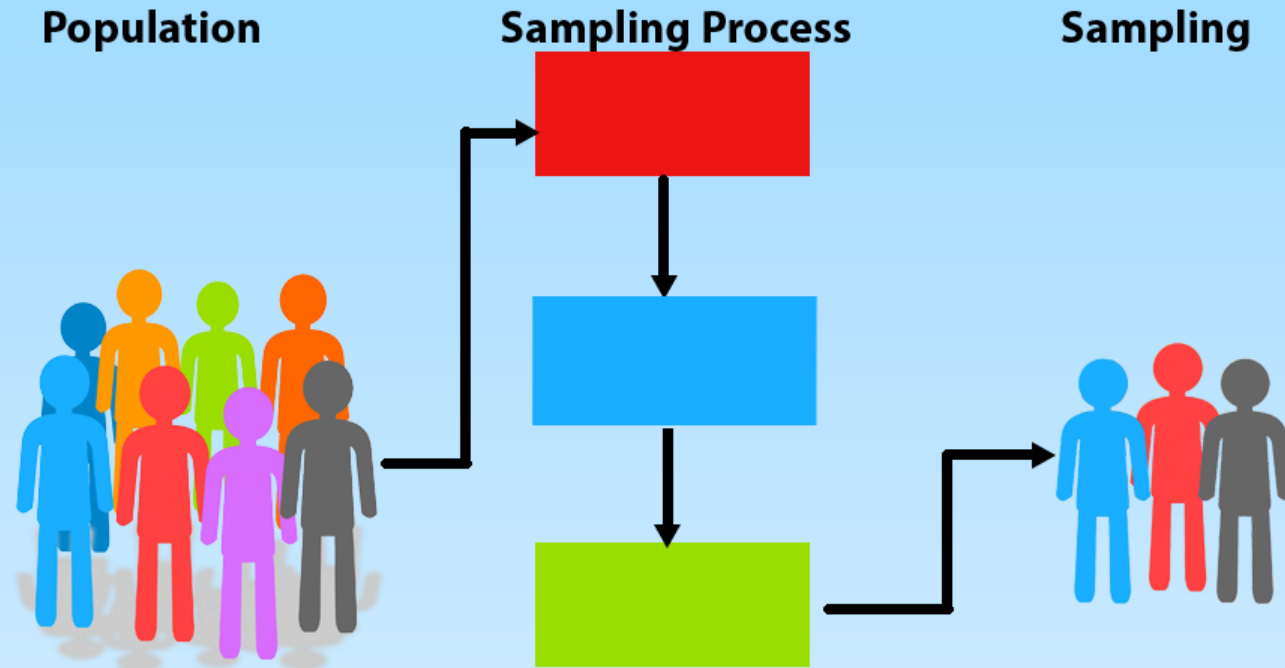
Sampling is the process of selecting a subset of a population to study. The goal of sampling is to collect data from a representative sample that accurately reflects the characteristics of the population. There are several types of sampling methods, including random sampling, stratified sampling, and cluster sampling.

Why is sampling needed?

The sampling process is used to collect the sample data which helps us make inferences about the population data. It allows us to draw conclusions about the population from sample data.

There are various reasons why sampling is needed, such as:

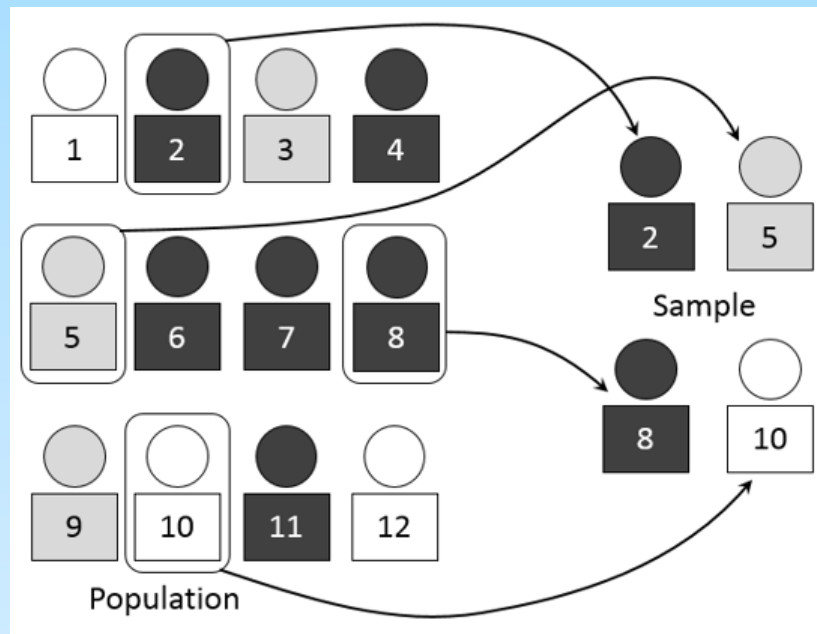
- It is a cost-efficient method as we do not have to use data from the total population to build a machine learning model.
- It is not feasible to study the total population, therefore the sampling process makes our work easier.
- The size of the sample data is always smaller, therefore we can clean and process our data with more efficacy.



Simple Random Sampling (SRS)

In Simple Random Sampling (SRS), **everyone in the population has an equal chance of being selected** for the sample.

To prepare a sample using **SRS**, we **randomly select the desired number of members from the population**.



Original Data



Student_ID	Name	Department	GPA	Age	Address	Hobby
1	Yousef Ahmed	Computer Science	3.8	21	Amman	Reading
2	Layla Mohammed	Business Administration	3.5	22	Irbid	Traveling
3	Ahmad Ibrahim	Engineering	3.9	23	Zarqa	Painting
4	Nour Ali	Psychology	3.7	20	Aqaba	Playing sports
5	Omar Hassan	Computer Science	3.6	22	Mafrq	Photography
6	Fatima Khalid	Engineering	3.8	24	Ajloun	Music
7	Salma Abdullah	Business Administration	3.4	21	Karak	Reading
8	Aya Mustafa	Computer Science	3.9	22	Madaba	Traveling
9	Reem Hussain	Engineering	3.7	23	Jerash	Playing sports
10	Mohammed Jamal	Psychology	3.5	21	Tafilah	Music
11	Khaled Salah	Computer Science	3.8	24	Ramtha	Painting
12	Sarah Ahmed	Business Administration	3.6	22	Salt	Reading
13	Hussein Mohamed	Computer Science	3.7	23	Mafrq	Painting
14	Hala Abdulaziz	Psychology	3.4	20	Ajloun	Photography
15	Yara Mansour	Computer Science	3.7	21	Karak	Playing sports
16	Yousef Hassan	Engineering	3.6	22	Mafrq	Music
17	Huda Ali	Business Administration	3.8	23	Irbid	Traveling
18	Lina Kamal	Psychology	3.5	24	Amman	Reading
19	Ali Mahmoud	Computer Science	3.9	21	Zarqa	Painting
20	Nada Abdullah	Business Administration	3.7	22	Aqaba	Playing sports

```
import pandas as pd
original_data = pd.read_csv('StudentsForSample.csv')
original_department_counts = original_data['Department'].value_counts()
# Display the counts for each department
print("Number of students for each department in the original dataset:")
print(original_department_counts)
```

Number of students for each department in the original dataset:

Computer Science 7

Engineering 5

Business Administration 4

Psychology 4



Random Sampling and Average Statistics

```
import pandas as pd
```

```
# Read the dataset
```

```
original_data = pd.read_csv('StudentsForSample.csv')
```

```
# Perform random sampling
```

```
random_sample = original_data.sample(n=10, random_state=42)
```

```
avg_age = random_sample['Age'].mean()
```

```
avg_gpa = random_sample['GPA'].mean()
```

```
# Display the random sample and average statistics
```

```
print("Random Sample:")
```

```
print(random_sample)
```

```
print("\nAverage Age of the Random Sample:", avg_age)
```

```
print("Average GPA of the Random Sample:", avg_gpa)
```

Random Sample:							
Student_ID	Name	Department	GPA	Age	Address	Hobby	
18	19	Ali Mahmoud	Computer Science	3.9	21	Zarqa	Painting
8	9	Reem Hussain	Engineering	3.7	23	Jerash	Playing sports
3	4	Nour Ali	Psychology	3.7	20	Aqaba	Playing sports
6	7	Salma Abdullah	Business Administration	3.4	21	Karak	Reading
14	15	Yara Mansour	Computer Science	3.7	21	Karak	Playing sports
5	6	Fatima Khalid	Engineering	3.8	24	Ajloun	Music
9	10	Mohammed Jamal	Psychology	3.5	21	Tafilah	Music
2	3	Ahmad Ibrahim	Engineering	3.9	23	Zarqa	Painting
13	14	Hala Abdulaziz	Psychology	3.4	20	Ajloun	Photography
7	8	Aya Mustafa	Computer Science	3.9	22	Madaba	Traveling

Average Age of Sampled Students: 21.6
Average GPA of Sampled Students: 3.68

Number of students for each department in the random sample:

Computer Science 3

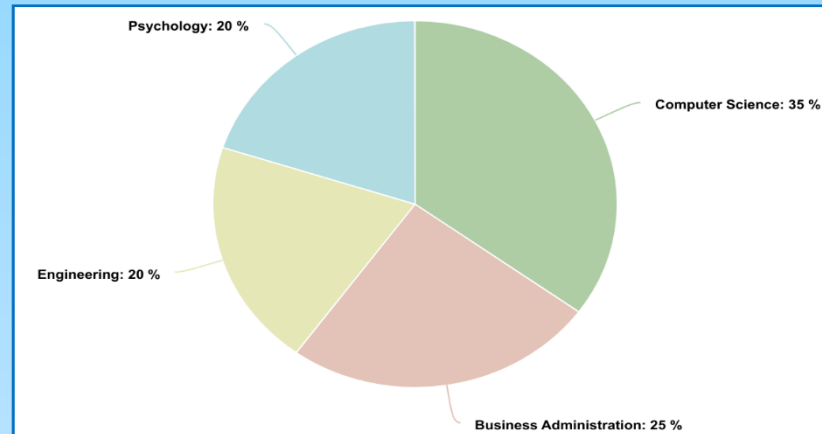
Engineering 3

Business Administration 2

Psychology 2

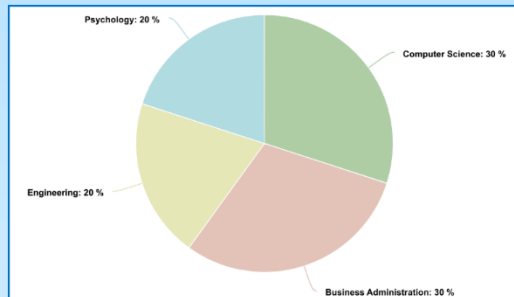


Random Samples



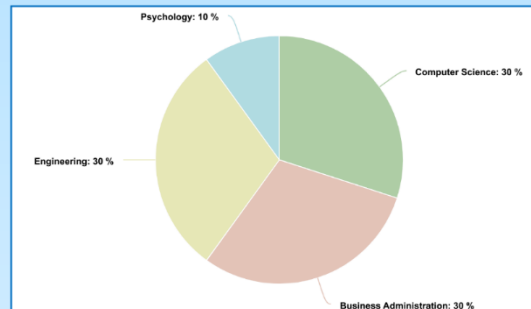
Computer Science Business Administration Engineering Psychology

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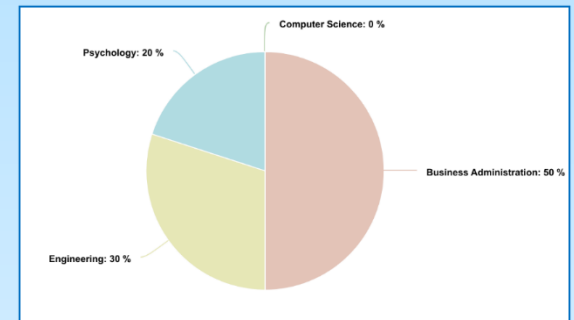
Computer Science Business Administration Engineering Psychology

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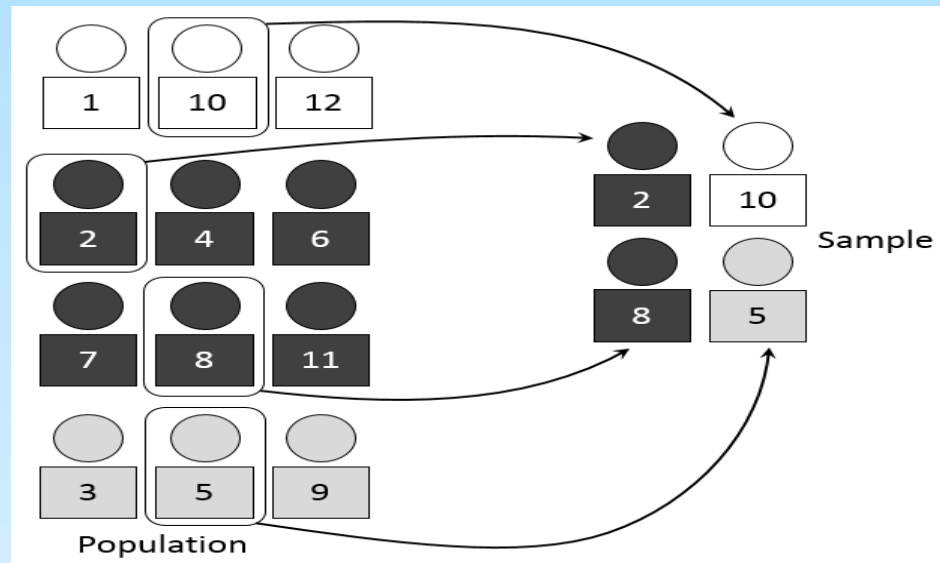


Computer Science Business Administration Engineering Psychology

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Stratified sampling

Stratified sampling is a method of obtaining a representative sample from a population that researchers have divided into relatively similar subpopulations (strata). Researchers use stratified sampling to ensure specific subgroups are present in their sample. It also helps them obtain precise estimates of each group's characteristics.



Stratified sampling



Student_ID	Name	Department	GPA	Age	Address	Hobby
17	Huda Ali	Business Administration	3.8	23	Irbid	Traveling
7	Salma Abdullah	Business Administration	3.4	21	Karak	Reading
19	Ali Mahmoud	Computer Science	3.9	21	Zarqa	Painting
8	Aya Mustafa	Computer Science	3.9	22	Madaba	Traveling
13	Hussein Mohamed	Computer Science	3.7	23	Mafrq	Painting
15	Yara Mansour	Computer Science	3.7	21	Karak	Playing sports
16	Yousef Hassan	Engineering	3.6	22	Mafrq	Music
3	Ahmad Ibrahim	Engineering	3.9	23	Zarqa	Painting
14	Hala Abdulaziz	Psychology	3.4	20	Ajloun	Photography
10	Mohammed Jamal	Psychology	3.5	21	Tafilah	Music

```
# Read the dataset
```

```
original_data = pd.read_csv('StudentsForSample.csv')
```

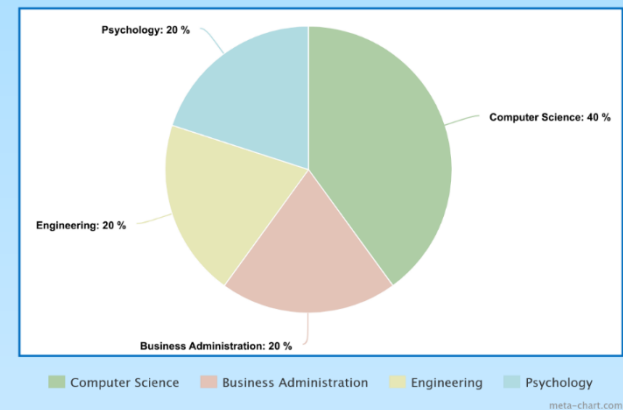
```
# Perform random sampling
```

```
stratified_sample = original_data.groupby('Department').apply(
    lambda x: x.sample(frac=0.50)
)
```

Calculate the average age and average GPA of the random sample

```
avg_age = stratified_sample['Age'].mean()
```

```
avg_gpa = stratified_sample['GPA'].mean()
```



```
# Display the random sample and average statistics
```

```
print(stratified_sample)
```

```
print("\nAverage Age of the Stratified Sample:", avg_age)
```

```
print("Average GPA of the Stratified Sample:", avg_gpa)
```

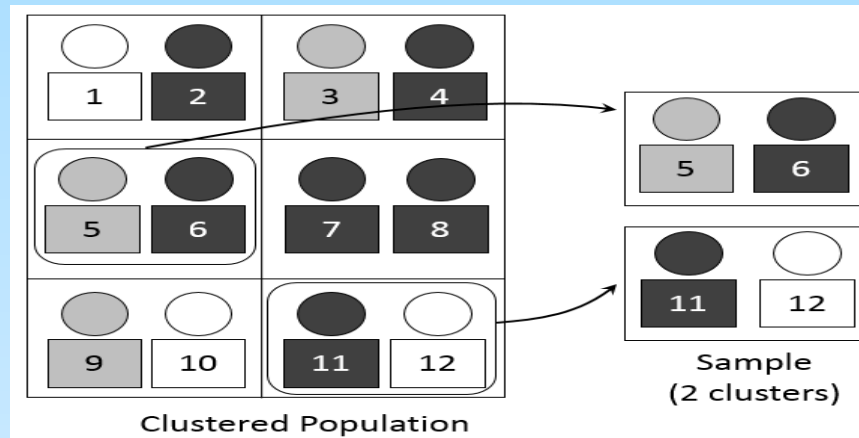
Average Age of the Random Sample: 21.7

Average GPA of the Random Sample: 3.679

Cluster Sampling



Cluster sampling is a sampling method in which the population is divided into clusters (groups of units) and a random sample of clusters is selected. It is a useful method when it is impractical or expensive to sample the entire population and the clusters are representative of the population.





```
original_data = original_data.sample(frac=1)
```

```
clusters = np.array_split(original_data, 4)
```

```
chosen_clusters = np.random.choice(len(clusters), 2, replace=False)
```

```
# Get the individuals in the chosen clusters
```

```
sample = np.concatenate([clusters[i] for i in chosen_clusters])
```

```
df = pd.DataFrame(sample, columns=['Student_ID', 'Name', 'Department', 'GPA', 'Age',  
'Address', 'Hobby'])
```

