	Course Name:	Applied Calculus	Course Code:	MT1001
	Program:	Electrical Engineering	Semester:	Fall 2023
	Duration:	1 hour	Total Marks:	40
	Exam Date:	30-09-2023	Weight:	15
	Section:	All	Page(s):	4
	Exam Type:	Sessional 1	CLO #	1,2,3

Rubrics

Student Name:	Roll No.	Section:
Instruction/Note	1. Do not forget to write your Name, Roll Number and Section.	
s:	2. Solve on the paper and Return.	

Question No. 1 (CLO No. 1)

Marks: 6+4+5

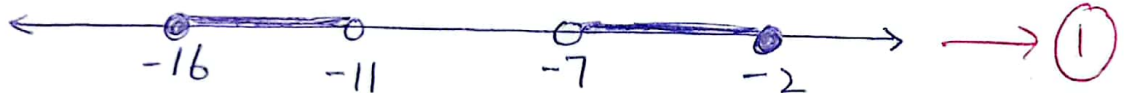
(a). Illustrate the given inequality in terms of intervals and find the solution set on the real number line.

$$2 < |x + 9| \leq 7$$

$$\begin{aligned} 2 < |x + 9| \\ x + 9 > 2 \text{ or } x + 9 < -2 \\ x > -7 \text{ or } x < -11 \end{aligned}$$

$$\begin{aligned} |x + 9| \leq 7 &\rightarrow \textcircled{1} \\ -7 \leq x + 9 \leq 7 &\rightarrow \textcircled{1} \\ -16 \leq x \leq -2 &\rightarrow \textcircled{1} \end{aligned}$$

$$S. S. = [-16, -11) \cup (-7, -2] \rightarrow \textcircled{2}$$



(b). Illustrate the given inequality by using properties of absolute value

$$|x + 3| < -5$$

→ $\textcircled{4}$

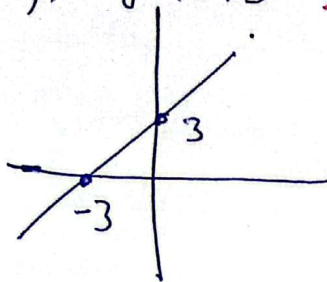
As we knew that, the absolute value interpreted the "distance" between two numbers on the number line and we also the knew that the distance can't be "-ve". 0049
So, above inequality has "no" solution.

(c) Identify whether the given function is even, odd, or neither and also sketch the graph of the function

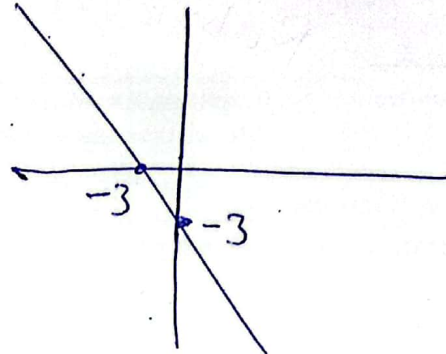
$y = 1 + 9\sqrt{-(x+3)}$, not by plotting points, but by starting with the graph of one of the standard function.

Function is neither even nor odd \rightarrow ①

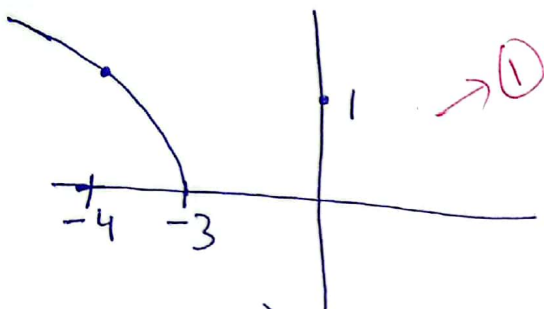
(a). $y = x + 3$



(b). $y = -(x + 3)$

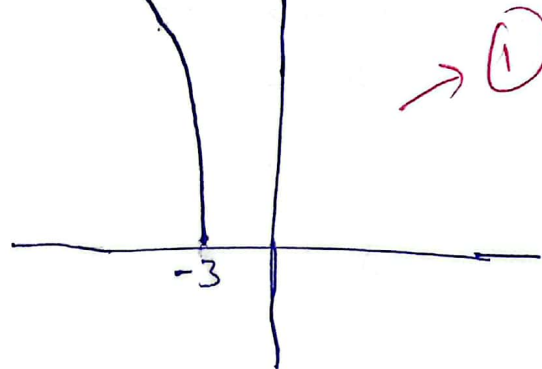


(c) $y = \sqrt{-(x+3)}$



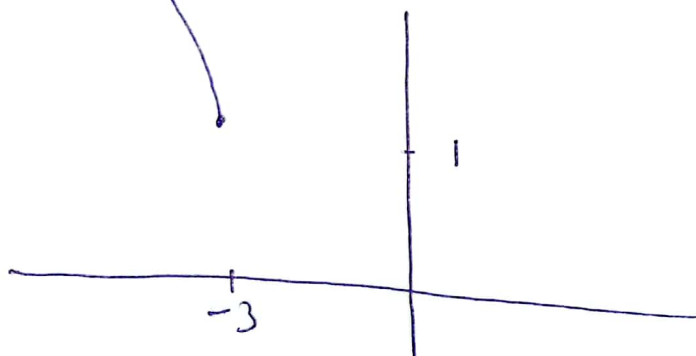
(d)

$y = 9\sqrt{-(x+3)}$

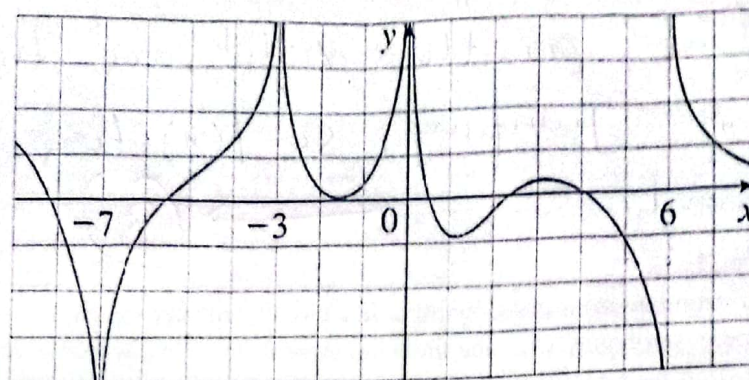


(e)

$y = 1 + 9\sqrt{-(x+3)}$



(a). For the function f represented by the graph, provide the following information.



(i). Formulate $\lim_{x \rightarrow -7} f(x)$

$$\lim_{x \rightarrow -7^-} f(x) = -\infty \text{ \& \> } \lim_{x \rightarrow -7^+} f(x) = +\infty, \text{ so, } \lim_{x \rightarrow -7} f(x) = \infty$$

(ii). Formulate $\lim_{x \rightarrow -3} f(x)$

$$\lim_{x \rightarrow -3^-} f(x) = +\infty \text{ \& \> } \lim_{x \rightarrow -3^+} f(x) = +\infty, \text{ so } \lim_{x \rightarrow -3} f(x) = +\infty$$

(iii). Formulate $\lim_{x \rightarrow 6} f(x)$

$$\lim_{x \rightarrow 6^-} f(x) = -\infty \text{ and } \lim_{x \rightarrow 6^+} f(x) = +\infty, \text{ so limit does not exist}$$

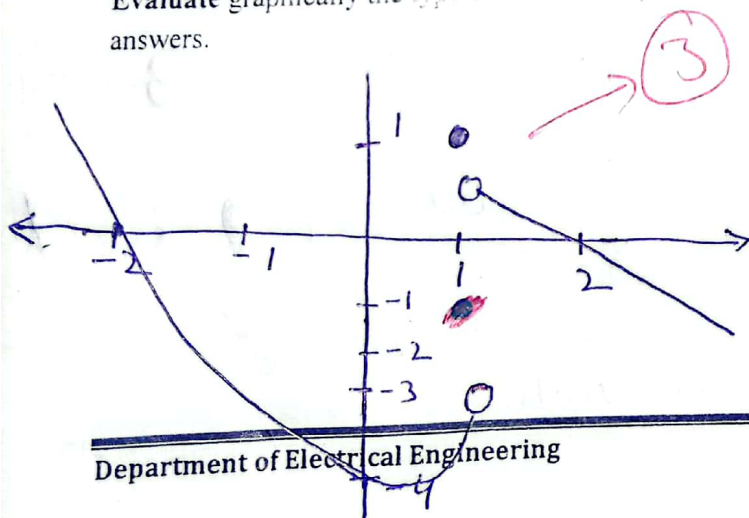
(iv). Determine the equations of the vertical asymptotes, if any.

$$x = -7, x = -3, x = 0 \text{ and } x = 6.$$

(b). Determine the points where the function is discontinuous.

$$f(x) = \begin{cases} x^2 - 4, & x < 1 \\ 1, & x = 1 \\ -\frac{1}{2}x + 1, & x > 1 \end{cases}$$

Evaluate graphically the type of discontinuity shown in the piecewise function, and provide reasons for your answers.



Function is discontinuous at only $x = 1$.

①

First portion of piecewise function describes parabola on left, a single pt. in the middle and a portion of a line on the right, as the value of function is jumping, so $f(x)$ has jump discontinuity at $x=1$. \rightarrow (3)

Question No. 3 (CLO No. 3)

Marks: 10

Two electric currents originate from the same point in a circuit. One current flows in a southerly direction with a rate of 40 amperes per hour (A/h), and the other current flows in a westerly direction at a rate of 15 A/h. After two hours, find the rate at which the distance between the two currents is increasing?

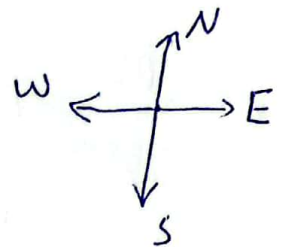
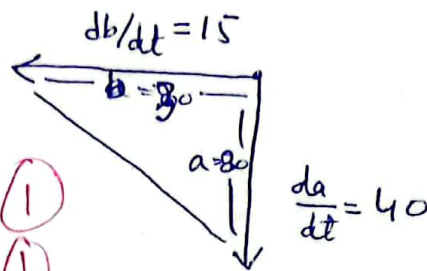
Given, $t = 2$ hrs.

we know that

$$d = s \times t$$

$$b = d_w = 15 \times 2 = 30 \rightarrow (1)$$

$$a = d_s = 40 \times 2 = 80 \rightarrow (1)$$



By using Pythagorean th.,

$$c^2 = a^2 + b^2 \Rightarrow c = 10\sqrt{73} \rightarrow (2)$$

Diff. w.r.t. t , to find rate of change,

$$2c \frac{dc}{dt} = 2a \frac{da}{dt} + 2b \frac{db}{dt} \Rightarrow c \frac{dc}{dt} = a \frac{da}{dt} + b \frac{db}{dt} \rightarrow (2)$$

$$\begin{aligned} \Rightarrow \frac{dc}{dt} &= \frac{1}{c} \left[a \frac{da}{dt} + b \frac{db}{dt} \right] = \frac{1}{10\sqrt{73}} [80(40) + 30(15)] \\ &= \frac{3850}{85.4} = 42.72 \text{ A/h.} \end{aligned}$$

The distance between two currents is increasing at the rate of 42.72 A/h. \rightarrow (3)