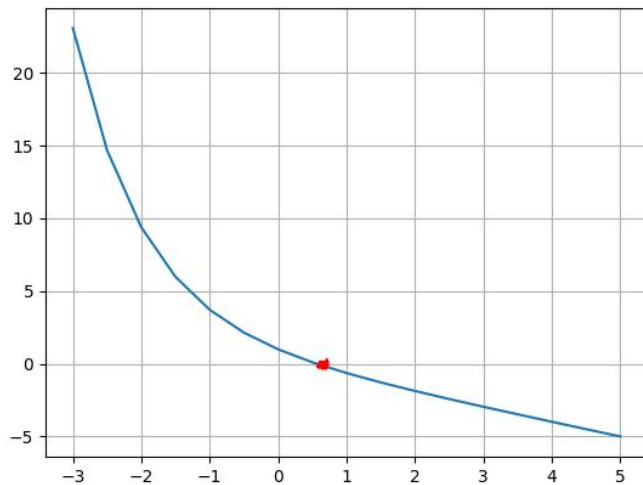


Find the root of the following equation:

$$y = f(x) = e^{-x} - x = 0$$

by using the Fixed Point Method with initial guess  $x_0 = 0$  and tolerance  $\varepsilon = 10^{-3}$

**Solution:**



$$y = f(x_0 = 0) = 1$$

Since  $|y_r| > \varepsilon$ , then we continue to the iteration

**Iteration 1:** -----

$$x_1 = x_0 + f(x_0) = 0 + e^{-0} - 0 = 1$$

$$y_1 = f(x_1) = -0.63212$$

Since  $|y_1| > \varepsilon$ , then we continue the iteration

**Iteration 2:** -----

$$x_2 = x_1 + f(x_1) = 1 + e^{-1} - 1 = 0.36788$$

$$y_2 = f(x_2) = 0.32432$$

Since  $|y_2| > \varepsilon$ , then we continue the iteration

**Iteration 3:** -----

$$x_3 = x_2 + f(x_2) = 0.36788 + e^{-0.36788} - 0.36788 = 0.69220$$

$$y_3 = f(x_3) = -0.19173$$

Since  $|y_3| > \varepsilon$ , then we continue the iteration

**Iteration 4:** -----

$$x_4 = x_3 + f(x_3) = 0.69220 + e^{-0.69220} - 0.69220 = 0.50047$$

$$y_4 = f(x_4) = 0.10577$$

Since  $|y_4| > \varepsilon$ , then we continue the iteration

Let's skip iterations 5-12 and proceed to iteration 13

**Iteration 13:** -----

$$x_{13} = x_{12} + f(x_{12}) = 0.56641 + e^{-0.56641} - 0.56641 = 0.56756$$

$$y_{13} = f(x_{13}) = -0.00065$$

Since  $|y_{13}| < \varepsilon$ , then we stop the iteration. The solution is  $x = 0.56756$