

- GGH Public Key Cryptosystem

==== Key Creation ====

1. Choose a good basis  $v_1, \dots, v_n$ .
2. Choose an integer matrix  $U$  satisfying  $\det(U) = \pm 1$ .
3. Compute a bad basis  $w_1, \dots, w_n$  as the rows of  $W = UV$ .
4. Publish the public key  $w_1, \dots, w_n$ .

==== Encryption ====

1. Choose small plaintext vector  $m$ .
2. Choose random small vector  $r$ .
3. Use Alice's public key to compute  $e = x_1 v_1 + \dots + x_n v_n + r$ .
4. Send the ciphertext  $e$  to Alice.

==== Decryption ====

1. Use Babai's algorithm to compute the vector  $v \in L$  closest to  $e$ .
2. Compute  $vW^{-1}$  to recover  $m$ .