

No of pages: 1

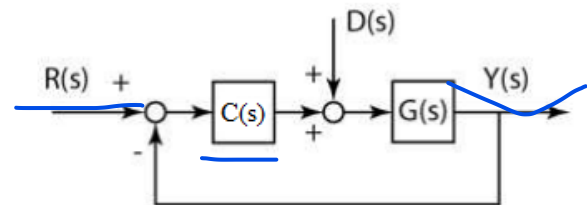
Time allowed: 60 min

Total marks: 20

### Question (1): (10 Marks)

- (a) Why does the standard output range, 4-20 mA, of a transmitter in process control start from 4 mA and not from 0 mA?
- (b) Consider the following closed-loop system, where

$$C(s) = 1 + \frac{1}{s}, \quad G(s) = \frac{1}{(s+1)^2}$$



- 1- Find the transfer function  $Y(s)/D(s)$ .
- 2- Is the controller ( $C(s)$ ) able to remove the effect of disturbance at steady state?
- 3- Sketch the response for a step disturbance.
- (c) With the aid of linearization, find the transfer function of the following nonlinear system around  $u = 2$ .

$$\frac{dy}{dt} + y = u^3$$

### Question (2): (10 Marks)

- (a) Consider the following process graph.
- [1] Does this process have positive or negative gain?
  - [2] Can we predict the shape of the step response from this graph? Why or why not?
  - [3] For which values of controller output (in %) is the process gain maximum?

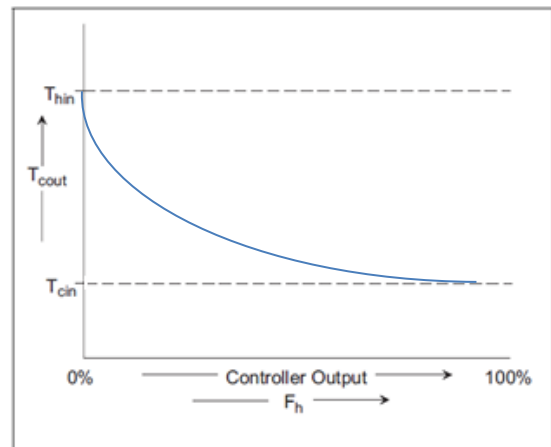


Figure 3-2. The Process Graph

- (b) For the following transfer functions, sketch the unit step response showing the final value and if there is overshoot or inverse response?

$$\frac{T(s)}{F(s)} = \frac{-5s + 18}{s^2 + 6s + 9}$$

- (c) True or False:

- [1] The proportional control action depends on past errors.
- [2] Integral control is slow compared to proportional control.
- [3] Derivative control is termed the “persistent mode”.

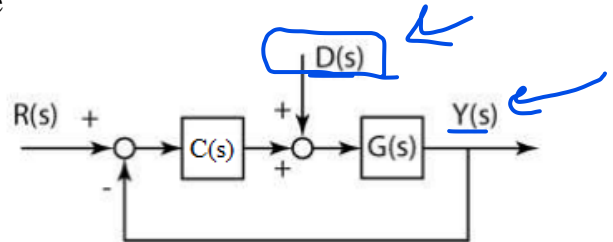
*All best wishes....*

## Model Answer

### Question (1): (10 Marks)

- (a) The standard output range, 4-20 mA, of a transmitter in process control start from 4 mA to avoid the ambiguity between minimum reading and open-circuit fault.'
- (b) Consider the following closed-loop system, where

$$C(s) = 1 + \frac{1}{s}, \quad G(s) = \frac{1}{(s+1)^2}$$



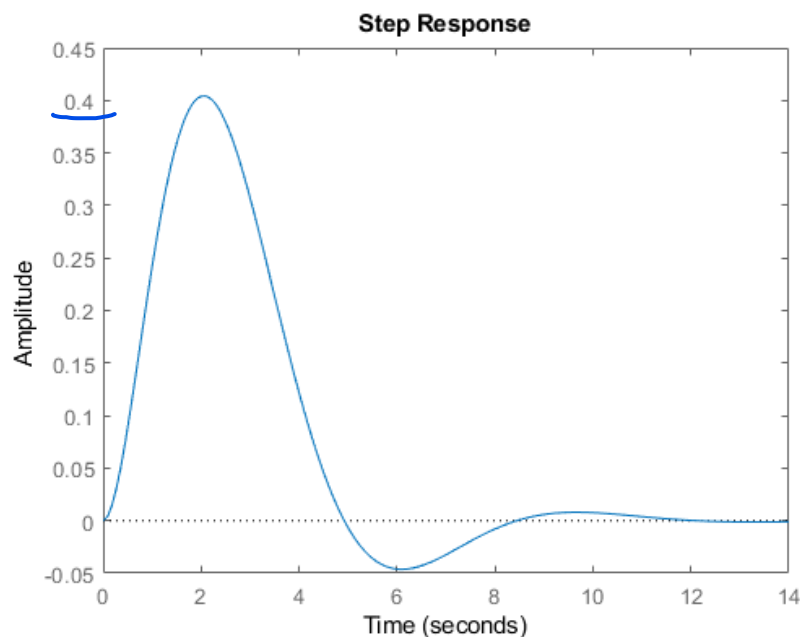
- 1- Find the transfer function  $Y(s)/D(s)$ .

$$\frac{Y(s)}{D(s)} = \frac{G(s)}{1 + C(s)G(s)} = \frac{\frac{1}{(s+1)^2}}{1 + \left(\frac{s+1}{s}\right)\frac{1}{(s+1)^2}} = \frac{s}{s^3 + 2s^2 + 2s + 1}$$

- 2- Is the controller ( $C(s)$ ) able to remove the effect of disturbance at steady state?

→ As the dc gain of the transfer function above is ZERO, the disturbance will be removed at steady state.

- 3- The step disturbance response



- (c) With the aid of linearization, find the transfer function of the following nonlinear system around  $u = 2$ .

$$\frac{dy}{dt} + y = u^3.$$

$$\frac{dy}{dt} = f(y, u) = -y + u^3.$$

$$\dot{y}^* = \frac{\partial f}{\partial y} y^* + \frac{\partial f}{\partial u} \bigg|_{u=2} u^* = -y^* + 3u^2 u^* = -y^* + 12u^*$$

So the transfer function will be

$$\frac{Y^*(s)}{U^*(s)} = \frac{12}{s + 1}$$

## **Question (2): (10 Marks)**

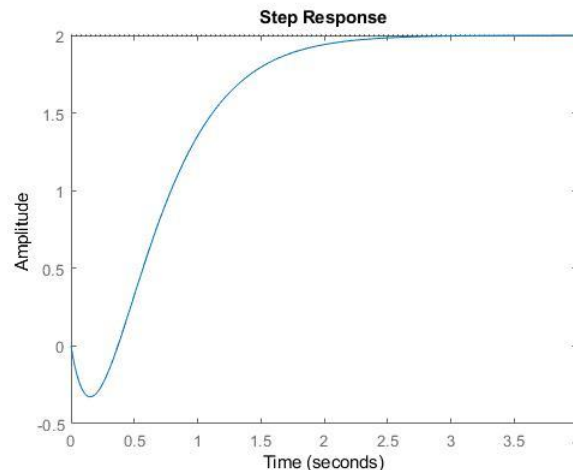
- (a) Consider the following process graph.

[1] Does this process have positive or negative gain? **NEGATIVE GAIN**

[2] **We can't predict the shape** of the step response from this graph because the process graph describes only steady state relationship between MV and PV.

[3] For which values of controller output (in %) is the process gain maximum? **At 0%.**

- (b) The response shows an inverse response



- (c) **True or False:**

[1] The proportional control action depends on past errors. **False**

[2] Integral control is slow compared to proportional control. **True**

[3] Derivative control is termed the "persistent mode". **False**