



MISR UNIVERSITY FOR SCIENCE AND TECHNOLOGY
COLLEGE OF ENGINEERING
MECHATRONICS ENGINEERING DEPARTMENT
MTE 408 ROBOTICS

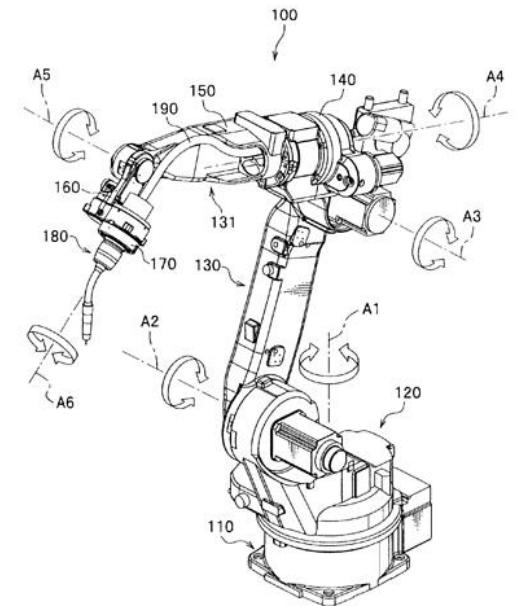


SESSION 2

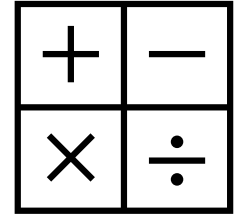
INTRODUCTION TO ROBOTICS LAB

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SHEET 1



1. *Use matrices to solve the following system of equations*

$$x + y - 2z = 3$$

$$3x - y + z = 5$$

$$3x + 3y - 6z = 9$$

SOLUTION

Taking the variables coefficients and arranging it into a matrix form

$$A = \begin{bmatrix} 1 & 1 & -2 \\ 3 & -1 & 1 \\ 3 & 3 & -6 \end{bmatrix}$$

$$|A| = 1(-1 * -6 - 1 * 3) - (1)(3 * -6 - 1 * 3) + (-2)(3 * 3 - -1 * 3)$$



SHEET 1

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SOLUTION

Taking the variables coefficients and arranging it into a matrix form

$$A = \begin{bmatrix} 1 & 1 & -2 \\ 3 & -1 & 1 \\ 3 & 3 & -6 \end{bmatrix}$$

$$|A| = 1(-1 * -6 - 1 * 3) - (1)(3 * -6 - 1 * 3) + (-2)(3 * 3 - -1 * 3)$$

$$|A| = 1(3) - (1)(-21) + (-2)(12)$$

$$|A| = 3 + 21 - 24 = 0$$

$|A| = 0 \rightarrow$ The solution doesn't exist



SHEET 1

MATLAB VERIFICATION

$$A = \begin{bmatrix} 1 & 1 & -2 \\ 3 & -1 & 1 \\ 3 & 3 & -6 \end{bmatrix}$$

```
Command Window
>> A = [1 1 -2; 3 -1 1; 3 3 -6]

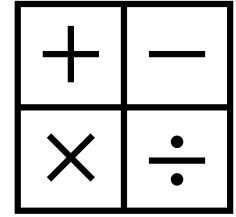
A =

     1     1    -2
     3    -1     1
     3     3    -6

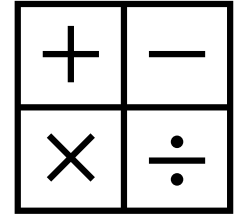
>> det(A)

ans =

-3.3307e-15
```



SHEET 1



2. Use matrices to solve the following system of equations

$$4x + 8y + z = -6$$

$$2x - 3y + 2z = 0$$

$$x + 7y - 3z = -8$$

SOLUTION

Taking the variables coefficients and arranging it into a matrix form

$$A = \begin{bmatrix} 4 & 8 & 1 \\ 2 & -3 & 2 \\ 1 & 7 & -3 \end{bmatrix} \quad Y = \begin{bmatrix} -6 \\ 0 \\ -8 \end{bmatrix}$$

$$|A| = (4)(-3 * -3 - 2 * 7) - (8)(2 * -3 - 2 * 1) + (1)(2 * 7 - -3 * 1)$$



SHEET 1

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SOLUTION

Taking the variables coefficients and arranging it into a matrix form

$$A = \begin{bmatrix} 4 & 8 & 1 \\ 2 & -3 & 2 \\ 1 & 7 & -3 \end{bmatrix} \quad Y = \begin{bmatrix} -6 \\ 0 \\ -8 \end{bmatrix}$$

$$|A| = (4)(-3 * -3 - 2 * 7) - (8)(2 * -3 - 2 * 1) + (1)(2 * 7 - -3 * 1)$$

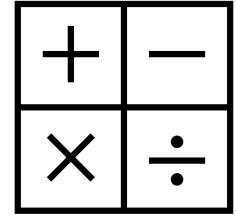
$$|A| = (4)(9 - 14) - (8)(-6 - 2) + (1)(14 + 3)$$

$$|A| = (4)(-5) - (8)(-8) + (1)(17)$$

$$|A| = -20 + 64 + 17 = 61 \rightarrow \text{Solution exists}$$



SHEET 1



SOLUTION

Taking the variables coefficients and arranging it into a matrix form

$$A = \begin{bmatrix} 4 & 8 & 1 \\ 2 & -3 & 2 \\ 1 & 7 & -3 \end{bmatrix} \quad |A| = -20 + 64 + 17 = 61 \rightarrow \text{Solution exists}$$

```
Command Window
>> A = [4 8 1;2 -3 2;1 7 -3]

A =

     4     8     1
     2    -3     2
     1     7    -3

>> det(A)

ans =

    61.0000
```

MATLAB CHECK



SHEET 1

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SOLUTION

Taking the variables coefficients and arranging it into a matrix form

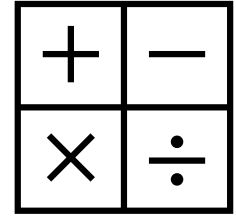
$$A = \begin{bmatrix} 4 & 8 & 1 \\ 2 & -3 & 2 \\ 1 & 7 & -3 \end{bmatrix} \quad |A| = -20 + 64 + 17 = 61 \rightarrow \text{Solution exists}$$

Matrix of minors , Cofactors and Adjoint

$$M = \begin{bmatrix} -5 & -8 & 17 \\ -31 & -13 & 20 \\ 19 & 6 & -28 \end{bmatrix} \quad C = \begin{bmatrix} -5 & 8 & 17 \\ 31 & -13 & -20 \\ 19 & -6 & -28 \end{bmatrix} \quad Adj = \begin{bmatrix} -5 & 31 & 19 \\ 8 & -13 & -6 \\ 17 & -20 & -28 \end{bmatrix}$$



SHEET 1



SOLUTION

Taking the variables coefficients and arranging it into a matrix form

$$A = \begin{bmatrix} 4 & 8 & 1 \\ 2 & -3 & 2 \\ 1 & 7 & -3 \end{bmatrix} \quad |A| = -20 + 64 + 17 = 61 \rightarrow \text{Solution exists}$$

$$Adj = \begin{bmatrix} -5 & 31 & 19 \\ 8 & -13 & -6 \\ 17 & -20 & -28 \end{bmatrix}$$

```
Command Window
>> A = [4 8 1; 2 -3 2; 1 7 -3]

A =

     4     8     1
     2    -3     2
     1     7    -3

>> adjoint(A)

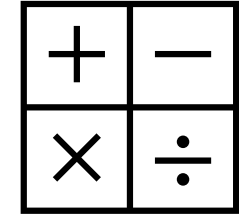
ans =

    -5.0000    31.0000    19.0000
     8.0000   -13.0000    -6.0000
    17.0000   -20.0000   -28.0000
```

MATLAB CHECK



SHEET 1



SOLUTION

Taking the variables coefficients and arranging it into a matrix form

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = A^{-1}Y = \frac{1}{|A|} \text{Adj}(A)Y = \frac{1}{61} \begin{bmatrix} -5 & 31 & 19 \\ 8 & -13 & -6 \\ 17 & -20 & -28 \end{bmatrix} \begin{bmatrix} -6 \\ 0 \\ -8 \end{bmatrix}$$

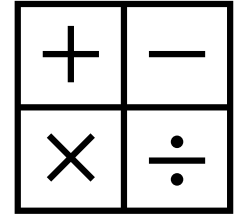
$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} -2.0 \\ 0.0 \\ 2.0 \end{bmatrix}$$

MATLAB CHECK

```
A =  
     4     8     1  
     2     -3     2  
     1     7    -3  
  
>> Y = [-6 ; 0 ; -8]  
  
Y =  
  
    -6  
     0  
    -8  
  
>> inv(A)*Y  
  
ans =  
  
   -2.0000  
    0.0000  
    2.0000
```



SHEET 1



Determine if this matrix is *singular* or *not*

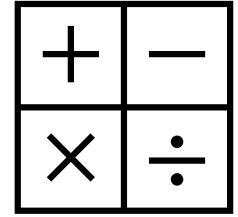
$$A = \begin{bmatrix} 1 & 2 & -1 \\ -3 & 4 & 5 \\ -4 & 2 & 6 \end{bmatrix}$$

SOLUTION

$$|A| = (1)(14) - (2)(2) - (1)(10) = 14 - 4 - 10 = \mathbf{0} \rightarrow \textit{Singular}$$



SHEET 1



Find the K value causing the value to be singular

$$A = \begin{bmatrix} K & 6 \\ 4 & 3 \end{bmatrix}$$

SOLUTION

$$|A| = 3K - 24 = 0 \rightarrow K = \frac{24}{3} = \mathbf{8}$$

