Lab: Description Logics

Through this lab you will gain a good understanding of the basics of description logics.

Reading Materials

- Lecture slides

- Chapter 1 and 2 in Baader. The Description Logic Handbook: Theory, Implementation, and Applications. Cambridge University Press.

- $\mathcal{SROIQ}$ constructors and axioms in Table 1.

Submission

You should submit a document that contains the answers to the tasks. **Note:** Any form of plagiarism, including using AI to generate answers, will result in failing the lab.

1. Basics

Answer each of the questions below.

1) Why do we say Description Logics (DL) is a concept language? What does "description" mean in DL?

2) In DL, what do the TBox and the ABox stand for?

3) $\mathcal{AL}$ is the base DL in the family of DLs. What are the constructors provided by this language? For each of the constructors, give its semantics using interpretation.

4) We obtain more expressive description languages if we add further constructors to $\mathcal{AL}$. List at least 3 constructors. For each constructor, give its interpretation and the letter that indicates the constructor.

5) Inclusion and equality are the two forms of terminological axioms in DL. What are the differences between these two axioms?

6) In DL, what are the four decidable properties of TBox? What are the reasoning tasks for ABox?

2. Translate the DL statements into Natural Language

Translate the following DL concept descriptions into natural language.

1) Person ⊓ Happy

2) Person ⊓ Happy ⊓ ∃owns.Pet

3) Person ⊓ ∀owns.Cat

4) Person ⊓ ¬Happy ⊓ ∃owns.(Cat ⊓ Old)

5) Person ⊓ ∃owns.Pet ⊓ ∀owns.(Cat ⊔ Fish)

3. Modeling in a DL

We obtain more expressive description languages if we add further constructors to $\mathcal{AL}$. $\mathcal{SROIQ}$ is the DL currently underlying the KR language for ontology. The constructors for which each letter stands can be found on the lecture slide. Table 1 give the syntax and semantics of the constructors and axioms in the DL. Now formalize the following statements using the DL. Please state your assumptions on the atomic concepts and roles.

1) Women are persons.

2) Men are persons.

3) Johan is a man.

4) Bill is a man.

5) James is a man.

6) Johan is not Bill.

7) Johan is James.

8) A parent is a person and has a child.

9) Bill is a child of Johan.

10) A sibling is either a brother or a sister.

11) Alice is her own sibling.

12) A person is their own relative.

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13) Every grandfather is both a man and has a child who is a parent.

14) A childless person is a person but is not a parent.

15) An unmarried person is a person who does not have a spouse.

16) A happy person is one whose children are all happy persons.

17) A great-grandfather is a father who has more than four children, and all these children are parents.

18) A child is someone who is the inverse of a parent.

19) The relationship of being a father is a sub-role of being a parent.

20) A grandparent is someone's parent's parent.

21) A child cannot be both a son and a daughter at the same time.

22) A parent has a child if and only if they have a son or a daughter.

4. Create a Knowledge Base for Univeristy using $\mathcal{SROIQ}$

Create a DL knowledge base (KB) that describes the education provided by a university in a general way. Try to utilize the constructors and axioms as many as possible from $\mathcal{SROIQ}$. The KB should contain primitive and defined concepts and roles in the TBox, as well as some individuals in the ABox. Please use appropriate symbolic names for concepts, roles, and individuals.

	Syntax	Semantics
$\mathcal{SROIQ}$ constructors		
universal concept	$\top$	Δ^I
bottom concept	$\bot$	$\bot$
atomic concept	A	A^I
intersection	$C \sqcap D$	$C^I \cap D^I$
union	$C \sqcup D$	$C^I \cup D^I$
complement	$\neg C$	$\Delta^I \backslash C^I$
universal restriction	$\forall R.C$	$\{a \in \Delta^I | \forall b.(a,b) \in R^I \rightarrow b \in C^I\}$
existential restriction	$\exists R.C$	$\{a \in \Delta^I | \exists b.(a,b) \in R^I \rightarrow b \in C^I\}$
at-least restriction	$\geq n\ \exists R.C$	$\{a \in \Delta^I | \#\{b|(a,b) \in R^I \rightarrow b \in C^I\} \geq n\}$
at-most restriction	$\leq n\ \exists R.C$	$\{a \in \Delta^I | \#\{b|(a,b) \in R^I \rightarrow b \in C^I\} \leq n\}$
local reflexivity	$\exists R.Self$	$\{a|(a,a) \in R^I\}$
nominal	$\{a\}$	$\{a^I\}$
atomic role	R	R^I
inverse role	R	R^-
universal role	U	$\Delta^I \times \Delta^I$
individual name	a	a^I
$\mathcal{SROIQ}$ axioms		
concept assertion	$C(a)$	$a^I \in C^I$
role assertion	$R(a,b)$	$(a^I, b^I) \in R^I$
individual equality	$a \approx b$	$a^I = b^I$
individual inequality	$a \neq b$	$a^I \neq b^I$
concept inclusion	$C \sqsubseteq D$	$C^I \subseteq D^I$
concept eqivalence	$C \equiv D$	$C^I = D^I$
role inclusion	$R \sqsubseteq S$	$R^I \subseteq S^I$
role equivalence	$R \equiv S$	$R^I = S^I$
complex role inclusion	$R_1 \circ R_2 \sqsubseteq S$	$R_1 \circ R_2 \subseteq S$
role disjointness	$Disjoint(R,S)$	$R_1 \cap R_2 = \emptyset$

Table 1: $\mathcal{SROIQ}$ constructors and axioms