His claim is not true because, the time complexity for his method is O(n^2).

Use, bucket sort implementation and handle duplicates by using linked lists.   
First create array of linked lists and then insert in the respective list which takes O(1) time.

The index is calculated by multiplying with the array size and then inserted at the respective index. The size of array is the maximum element in the original array.