

visualization

November 28, 2018

1 Disclaimer: Vote!

- What: Akademischer Senat, Akademische Versammlung (elects President), StuPa, ...
- Where: Beneath Mensa
- When

	4. Dec (Tuesday)	5. Dec (Wednesday)	6. Dec (Thursday)
Von	9:30	11:30	9:30
Bis	14:00	16:00	12:30

2 Python for Data Science

Visualization

...make both calculations and graphs. Both sorts of output should be studied; each will contribute to understanding.

F. J. Anscombe, 1973

(and echoed in nearly all talks about data visualization...)

3 Anscombe's Quartet

[Wikipedia on Anscombe](#)

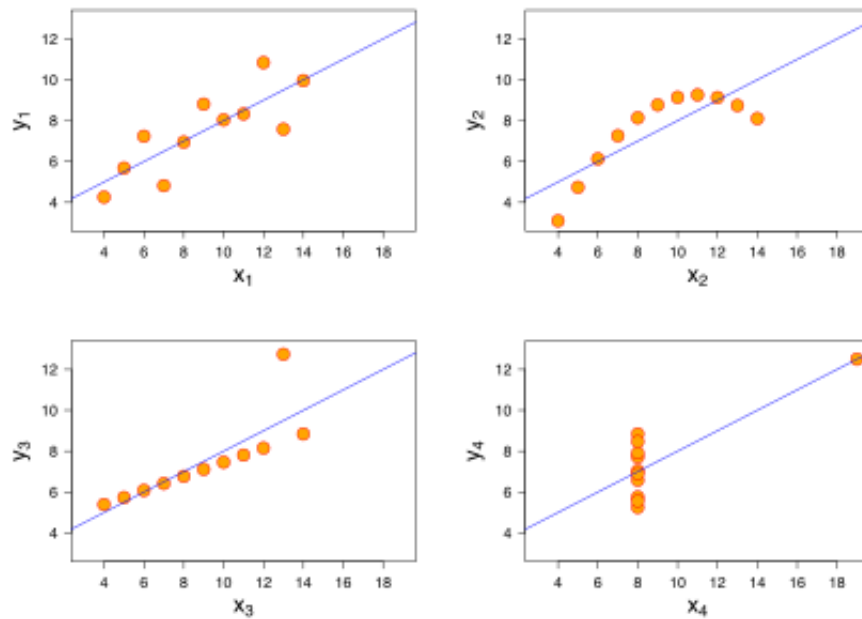
4 Anscombe's Quartet - Reloaded

[DataSaurus Rex](#)

[Justin Matejka and George Fitzmaurice, *Same Stats, Different Graphs: Generating Datasets with Varied Appearance and Identical Statistics through Simulated Annealing*](#)

5 Overview

- Plotting Basics with matplotlib
- Plotting complex data from pandas
- Even more abstraction with seaborn



Anscombe's Quartet

- Map visualizations with folium

6 Other plotting libraries

- [ggpy](#)
- [HoloViews](#)
- [Altair](#)
- [bokeh](#)
- [plotly](#)

7 Matplotlib

- Multi-platform data visualization library built on NumPy
- Works well on many operating systems / graphics backends
- Many output formats
- First version released in 2003 by [John D. Hunter](#)
- Substantial support by Space Telescope Science Institute (researchers behind Hubble telescope)

7.1 Importing Matplotlib

```
In [486]: import matplotlib.pyplot as plt
plt.style.use('ggplot')
import matplotlib
matplotlib.rcParams['lines.linewidth'] = 2
```

```
matplotlib.rcParams['savefig.dpi'] = 300
matplotlib.rcParams['figure.figsize'] = [12,6]
```

7.2 Three ways of plotting

- In Jupyter Notebook (Convenient, code and figures in one place)
- From IPython Shell
- From Python script (Reproducible, versionable code)

7.2.1 Plotting from a script

Write a file called *myplot.py* containing the following:

```
# ----- file: myplot.py -----
import matplotlib.pyplot as plt
import numpy as np

x = np.linspace(0, 10, 100)

plt.plot(x, np.sin(x))
plt.plot(x, np.cos(x))

plt.savefig('myplot.pdf')

plt.show()
```

Running this script from the command-line prompt will result in a window opening with your figure displayed:

```
$ python myplot.py
```

(On OSX you might need to try `pythonw` instead)

7.3 Plotting from an IPython shell

IPython is built to work well with Matplotlib if you specify Matplotlib mode. To enable this mode, use the `%matplotlib` magic command:

```
In [1]: %matplotlib
Using matplotlib backend: TkAgg
```

```
In [2]: import matplotlib.pyplot as plt
```

Any `plt` plot command will cause a figure window to open, and further commands can be run to update the plot.

To force an update of a plot, use `plt.draw()`. Using `plt.show()` in Matplotlib mode is not required.

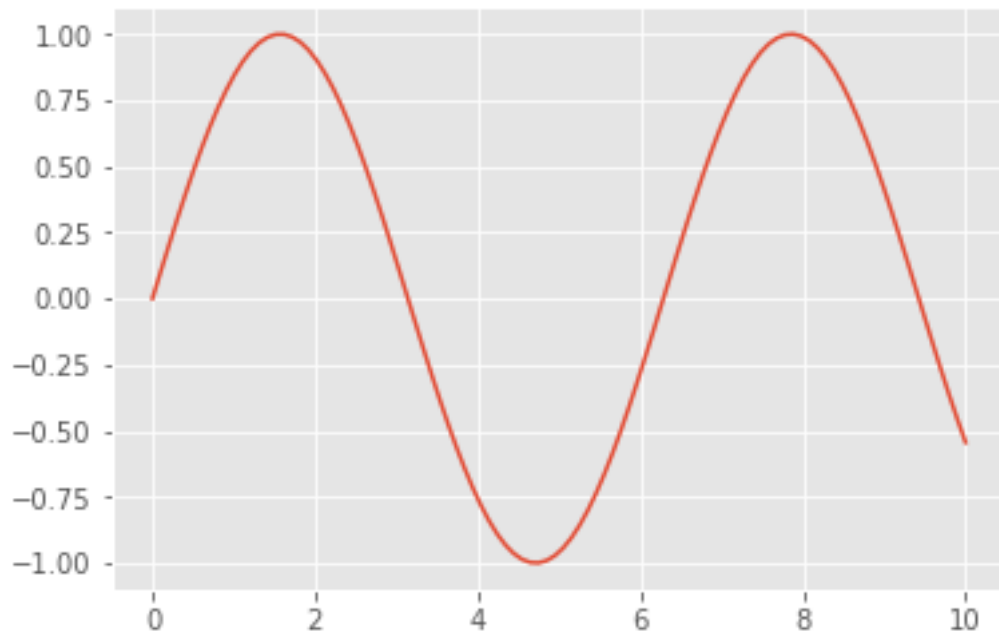
7.3.1 Plotting from a Jupyter Notebook

- Like in IPython, use the `%matplotlib` magic command
- Two options of embedding graphics directly in the notebook:
 - `%matplotlib notebook:interactive` plots
 - `%matplotlib inline:static` images of your plot embedded in the notebook

For this book, we will generally opt for `%matplotlib inline`

```
In [17]: %matplotlib inline
import matplotlib.pyplot as plt
plt.style.use('ggplot')
import numpy as np
x = np.linspace(0, 10, 100)

fig = plt.figure()
plt.plot(x, np.sin(x), '-');
```



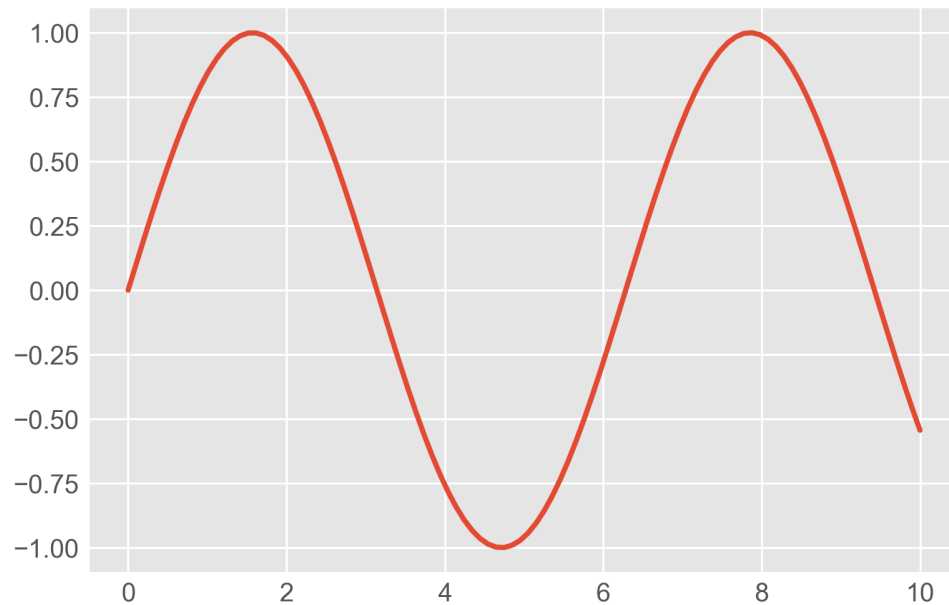
7.3.2 Saving Figures to File

- Variety of output formats
- No need to call `plt.show()` before

```
In [489]: fig.savefig('my_figure.png')
```

```
In [490]: from IPython.display import Image
          Image('my_figure.png')
```

Out[490]:



```
In [424]: fig.canvas.get_supported_filetypes()
```

```
Out[424]: {'ps': 'Postscript',
            'eps': 'Encapsulated Postscript',
            'pdf': 'Portable Document Format',
            'pgf': 'PGF code for LaTeX',
            'png': 'Portable Network Graphics',
            'raw': 'Raw RGBA bitmap',
            'rgba': 'Raw RGBA bitmap',
            'svg': 'Scalable Vector Graphics',
            'svgz': 'Scalable Vector Graphics',
            'jpg': 'Joint Photographic Experts Group',
            'jpeg': 'Joint Photographic Experts Group',
            'tif': 'Tagged Image File Format',
            'tiff': 'Tagged Image File Format'}
```

7.3.3 MATLAB Style API

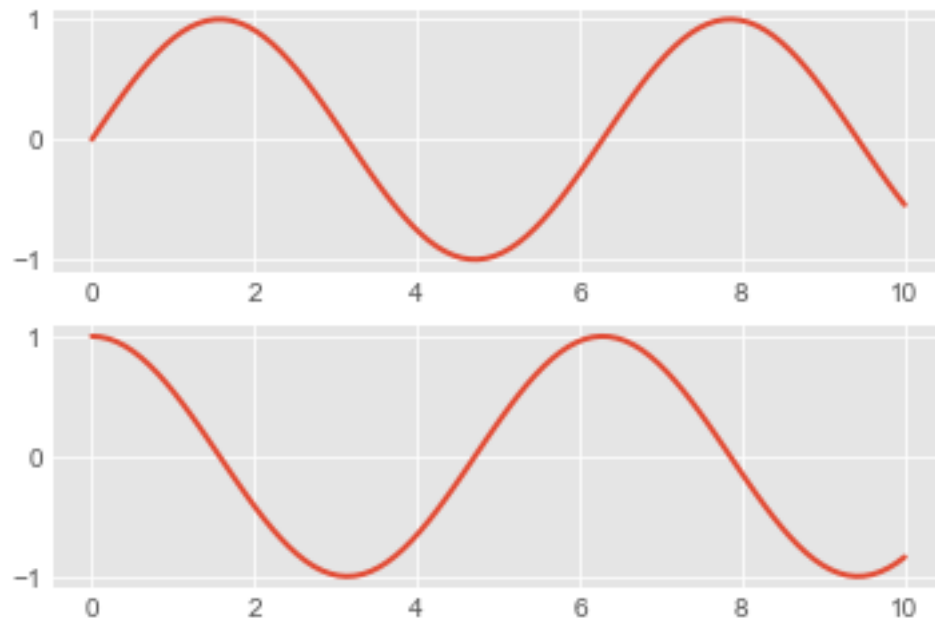
```
In [491]: plt.figure() # create a plot figure
```

```

# create the first of two panels and set current axis
plt.subplot(2, 1, 1) # (rows, columns, panel number)
plt.plot(x, np.sin(x))

# create the second panel and set current axis
plt.subplot(2, 1, 2)
plt.plot(x, np.cos(x));

```



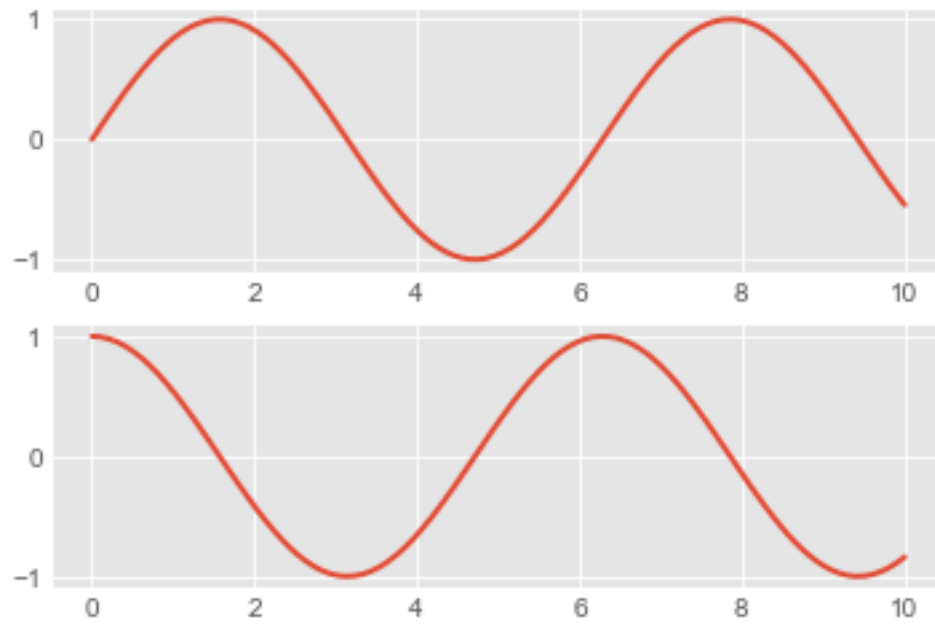
7.3.4 Object Oriented API

```

In [492]: # First create a grid of plots
# ax will be an array of two Axes objects
fig, ax = plt.subplots(2)

# Call plot() method on the appropriate object
ax[0].plot(x, np.sin(x))
ax[1].plot(x, np.cos(x));

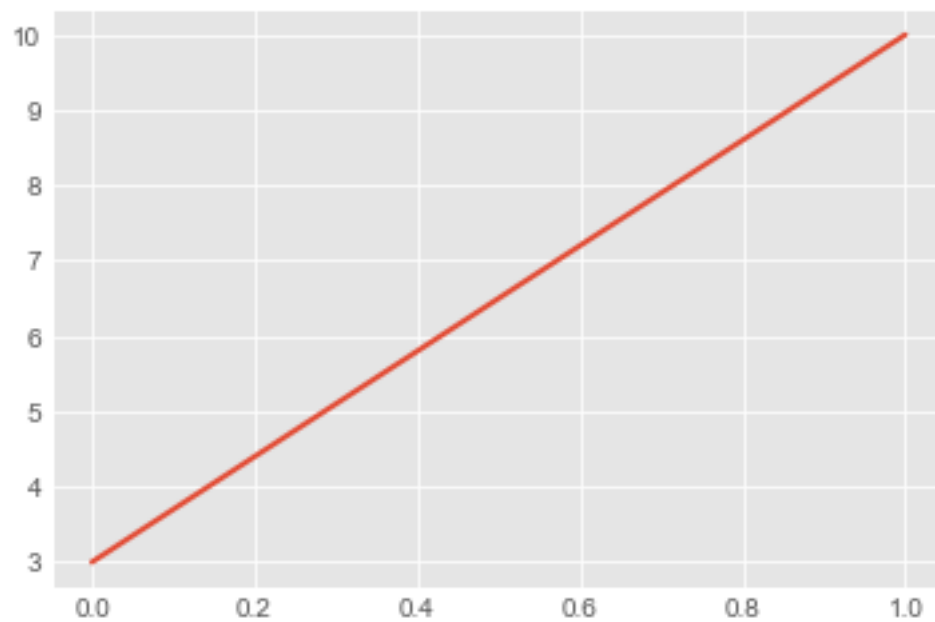
```



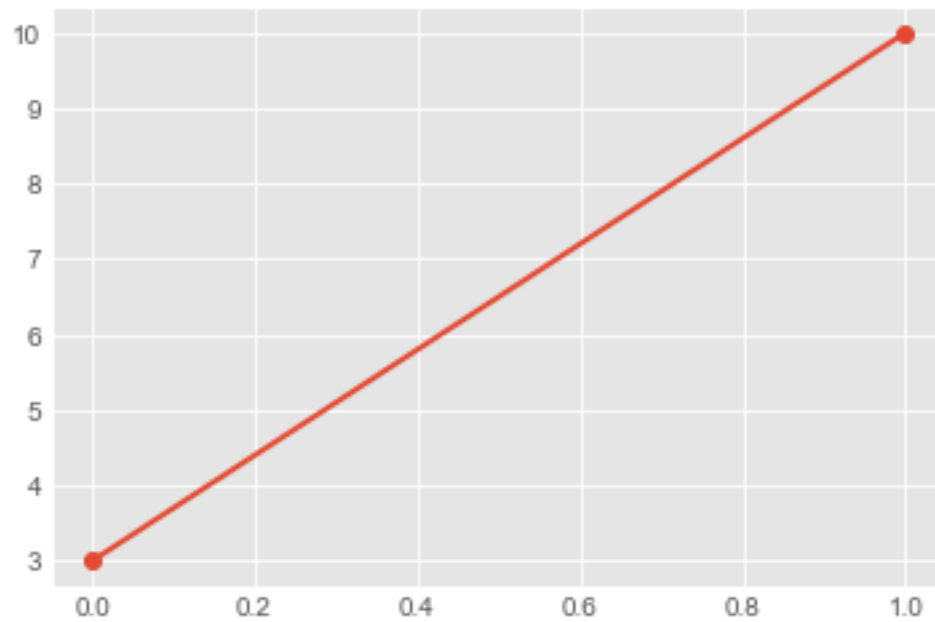
7.4 Simple Line Plots

Simple here means functions of the type $y = f(x)$

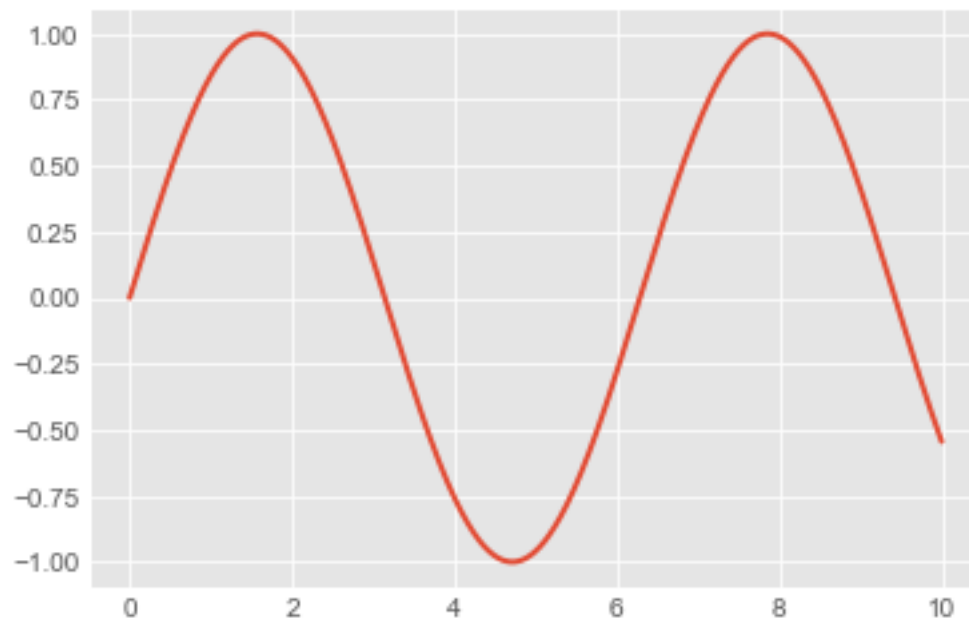
In [493]: `plt.plot([0,1],[3,10]);`



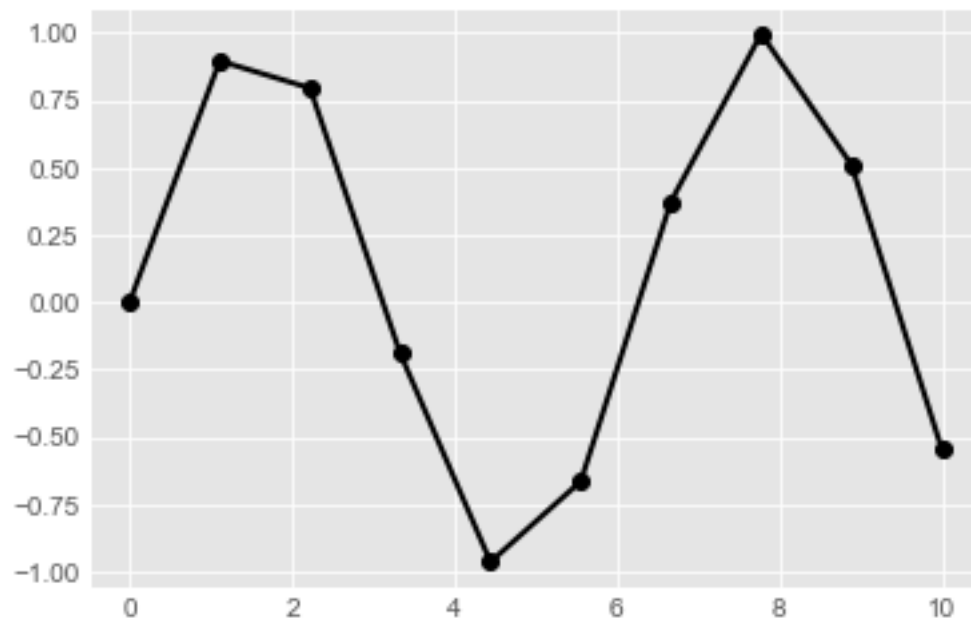
```
In [494]: plt.plot([0,1],[3,10], '-o');
```



```
In [495]: x = np.linspace(0, 10, 1000)
plt.plot(x, np.sin(x));
```

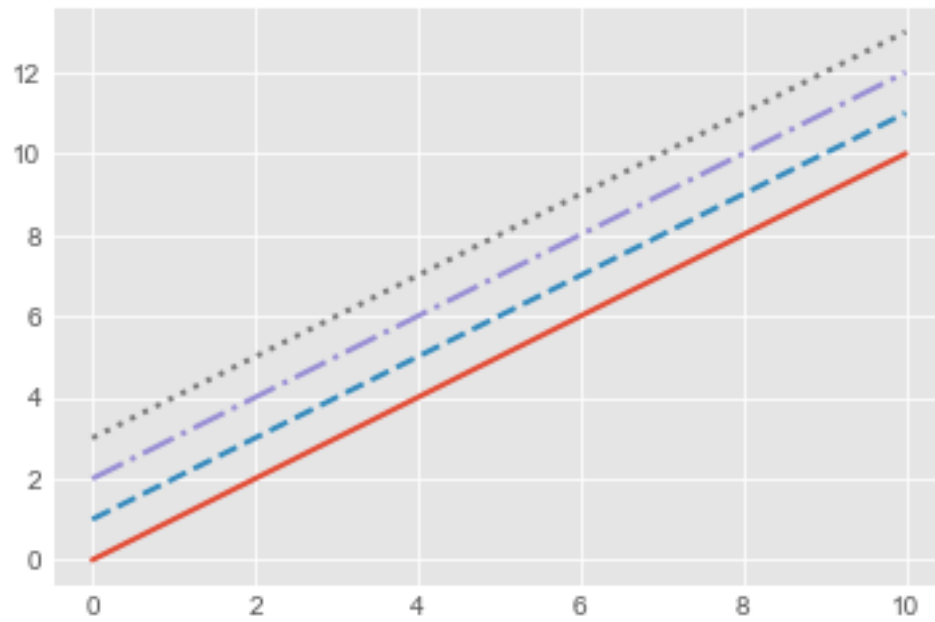



```
In [496]: x = np.linspace(0, 10, 10)
plt.plot(x, np.sin(x), 'k-o');
```

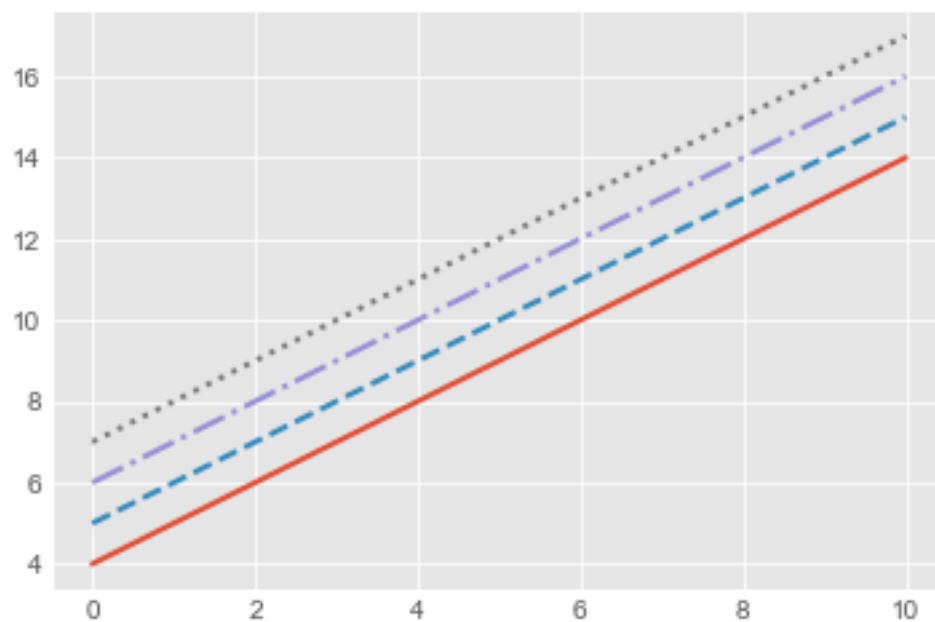


7.4.1 Line Styles

```
In [497]: x = np.linspace(0, 10, 1000)
plt.plot(x, x + 0, linestyle='solid')
plt.plot(x, x + 1, linestyle='dashed')
plt.plot(x, x + 2, linestyle='dashdot')
plt.plot(x, x + 3, linestyle='dotted');
```

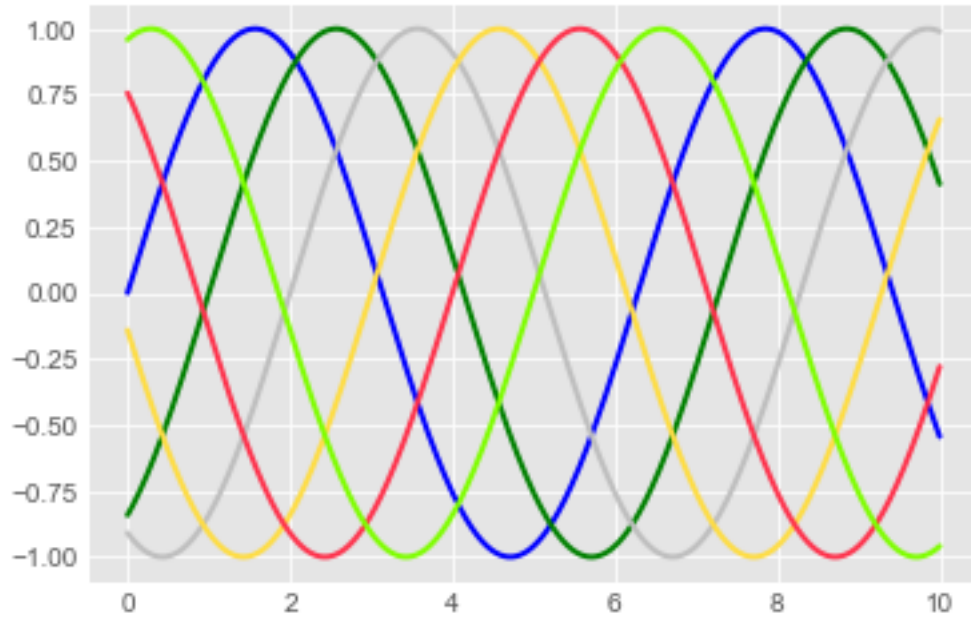


In [498]: *# For short, you can use the following codes:*
`plt.plot(x, x + 4, linestyle='-')` *# solid*
`plt.plot(x, x + 5, linestyle='--')` *# dashed*
`plt.plot(x, x + 6, linestyle='-.')` *# dashdot*
`plt.plot(x, x + 7, linestyle=':');` *# dotted*



7.4.2 Line Colors

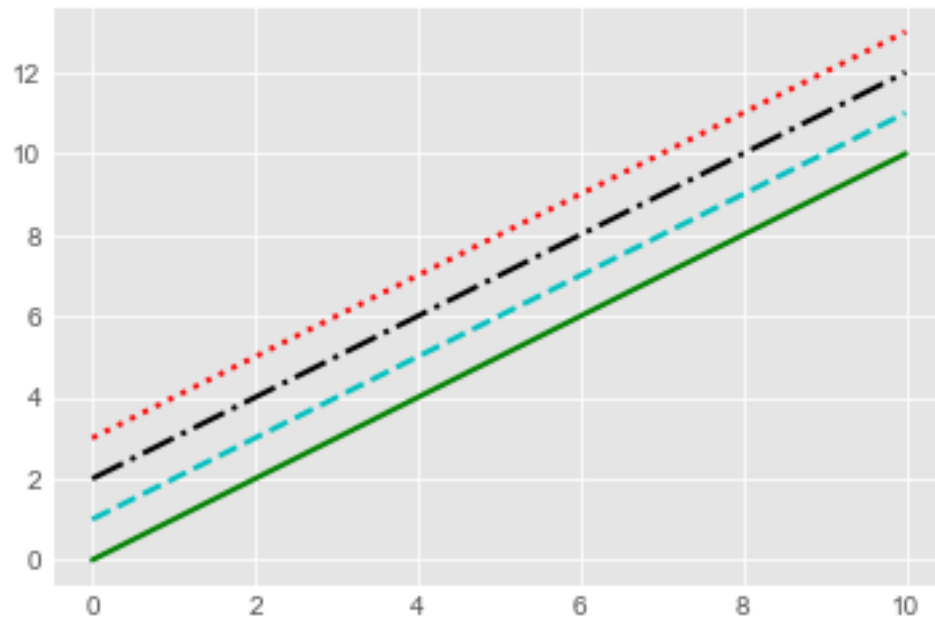
```
In [499]: x = np.linspace(0, 10, 1000)
plt.plot(x, np.sin(x - 0), color='blue')      # specify color by name
plt.plot(x, np.sin(x - 1), color='g')        # short color code (rgbcmyk)
plt.plot(x, np.sin(x - 2), color='0.75')     # Grayscale between 0 and 1
plt.plot(x, np.sin(x - 3), color='#FFDD44')  # Hex code (RRGGBB from 00 to FF)
plt.plot(x, np.sin(x - 4), color=(1.0,0.2,0.3)) # RGB tuple, values 0 to 1
plt.plot(x, np.sin(x - 5), color='chartreuse'); # all HTML color names supported
```



```
In [500]: # If you really don't want to write a lot
```

```
x = np.linspace(0, 10, 1000)

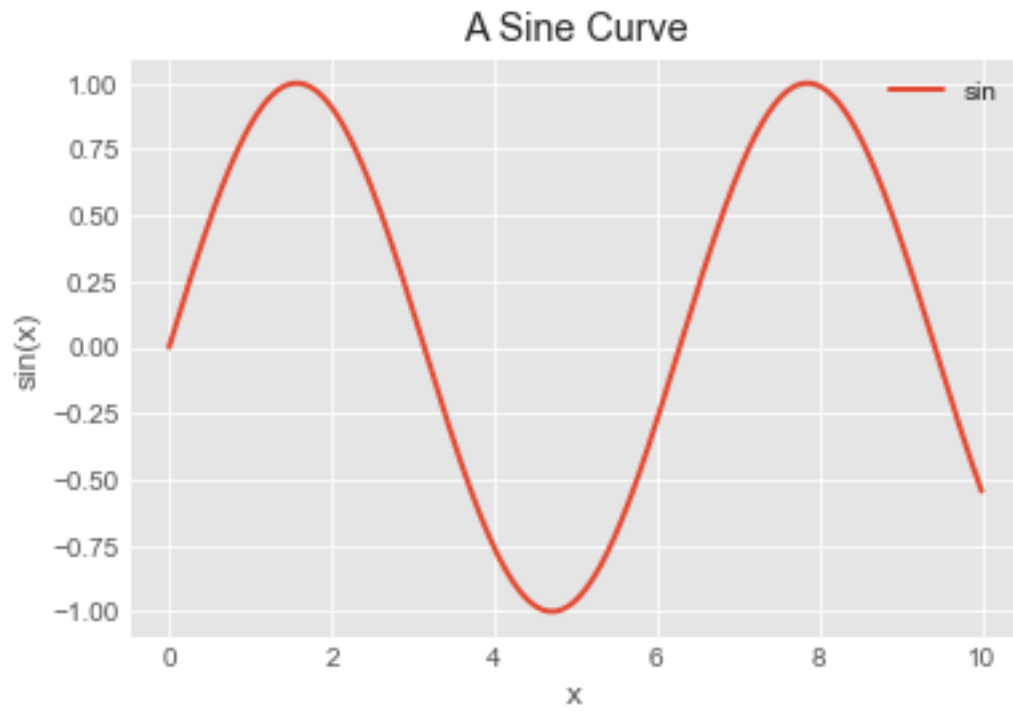
plt.plot(x, x + 0, '-g') # solid green
plt.plot(x, x + 1, '--c') # dashed cyan
plt.plot(x, x + 2, '-.k') # dashdot black
plt.plot(x, x + 3, ':r'); # dotted red
```



7.4.3 Annotations

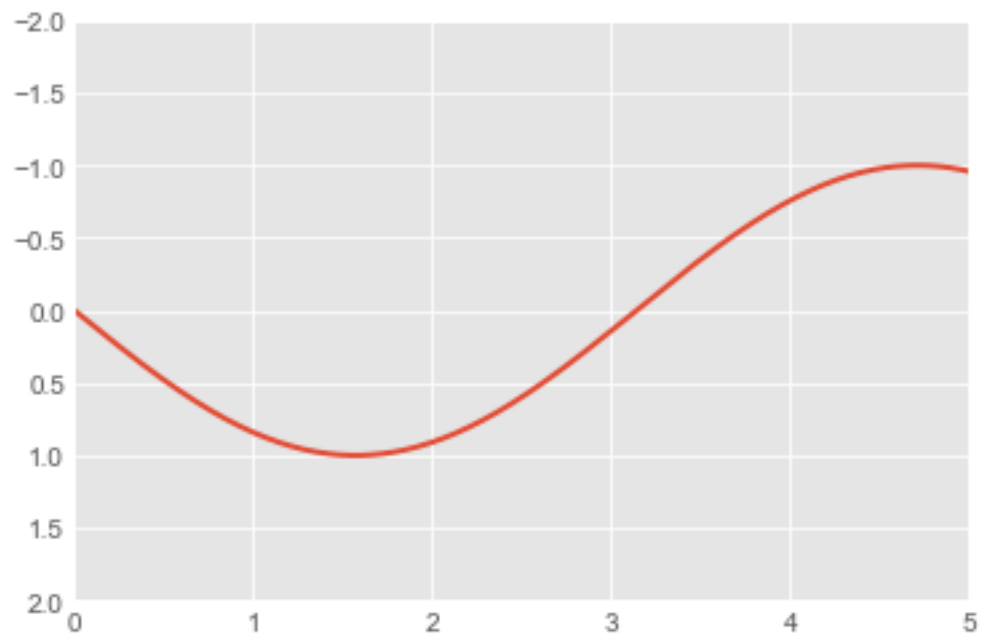
```
In [501]: plt.plot(x, np.sin(x))  
          plt.title("A Sine Curve")  
          plt.xlabel("x")  
          plt.ylabel("sin(x)");  
          plt.legend(["sin"])
```

```
Out[501]: <matplotlib.legend.Legend at 0x1a2ba2b208>
```



7.4.4 Axis Limit

```
In [502]: plt.plot(x, np.sin(x))  
          plt.xlim(0, 5)  
          plt.ylim(2, -2);
```

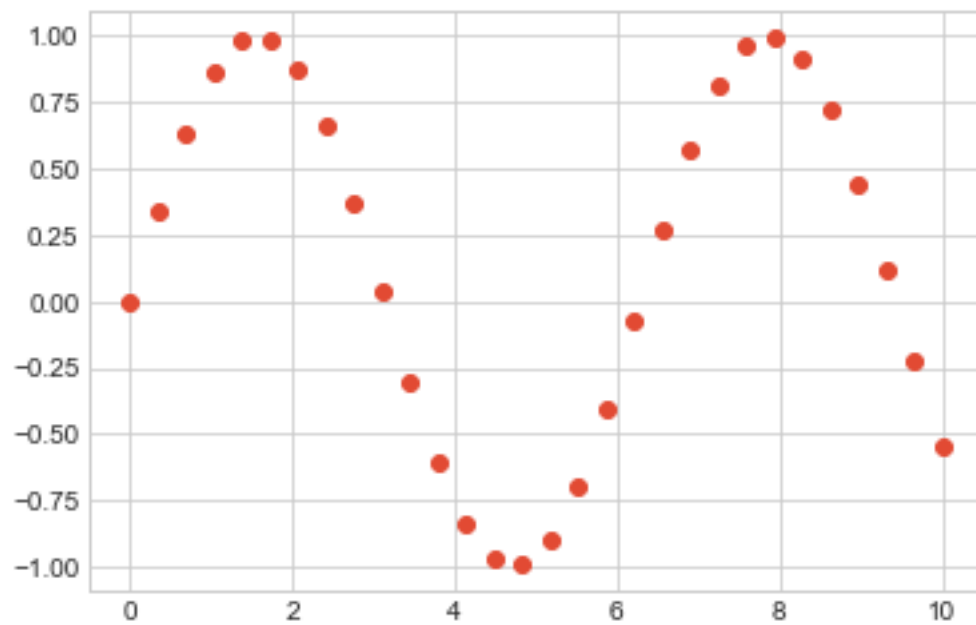


7.4.5 For more on styles

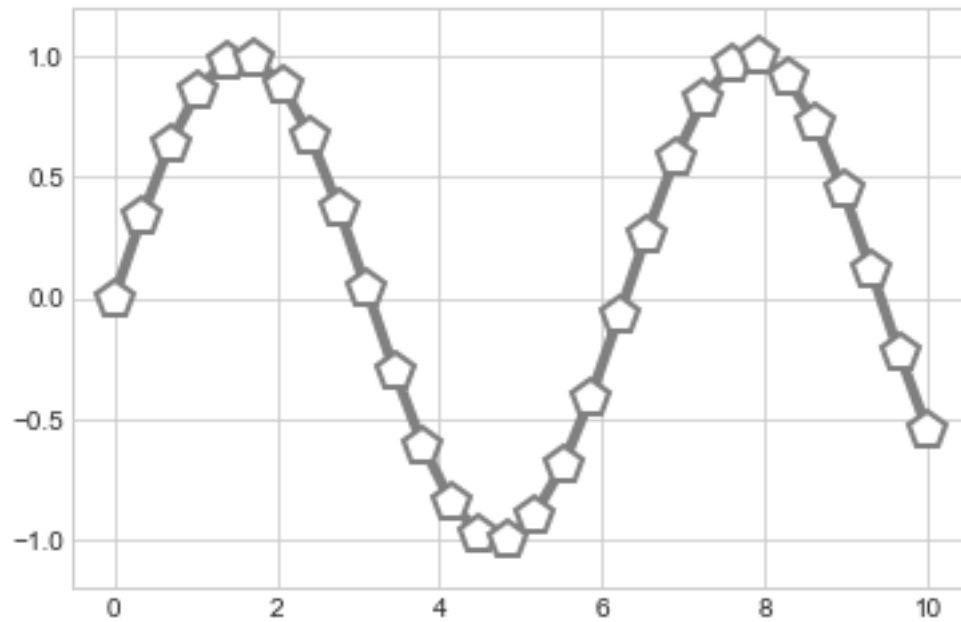
[SciPy Lecture Notes on Matplotlib](#)

7.5 Scatter Plots

```
In [503]: plt.style.use('seaborn-whitegrid')
x = np.linspace(0, 10, 30)
y = np.sin(x)
plt.plot(x, y, 'o');
```



```
In [504]: plt.plot(x, y, '-p', color='gray',
                  markersize=15, linewidth=4,
                  markerfacecolor='white',
                  markeredgecolor='gray',
                  markeredgewidth=2)
plt.ylim(-1.2, 1.2);
```

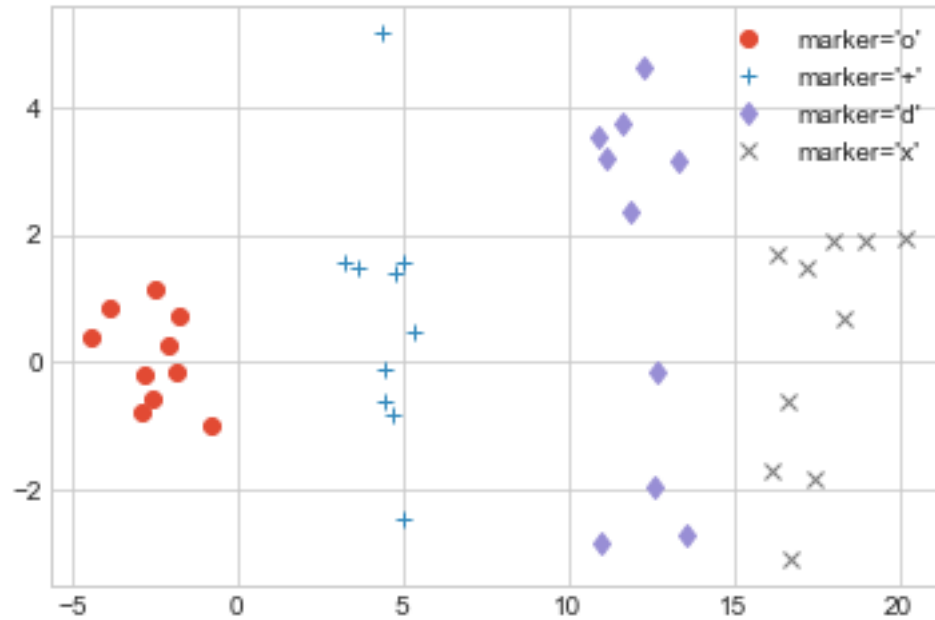


7.6 More Markers

```
In [505]: means = [-2,5,12,18]
stds = [1,5,6,3]
markers = ['o', '+', 'd', 'x']

plt.figure()
for mu,stdev,mark in zip(means,stds,markers):
    x = np.random.multivariate_normal([mu,0],np.diag([1,stdev]),10)
    plt.plot(x[:,0],x[:,1], mark, label="marker='{}'".format(mark))

plt.legend(numpoints=1);
```



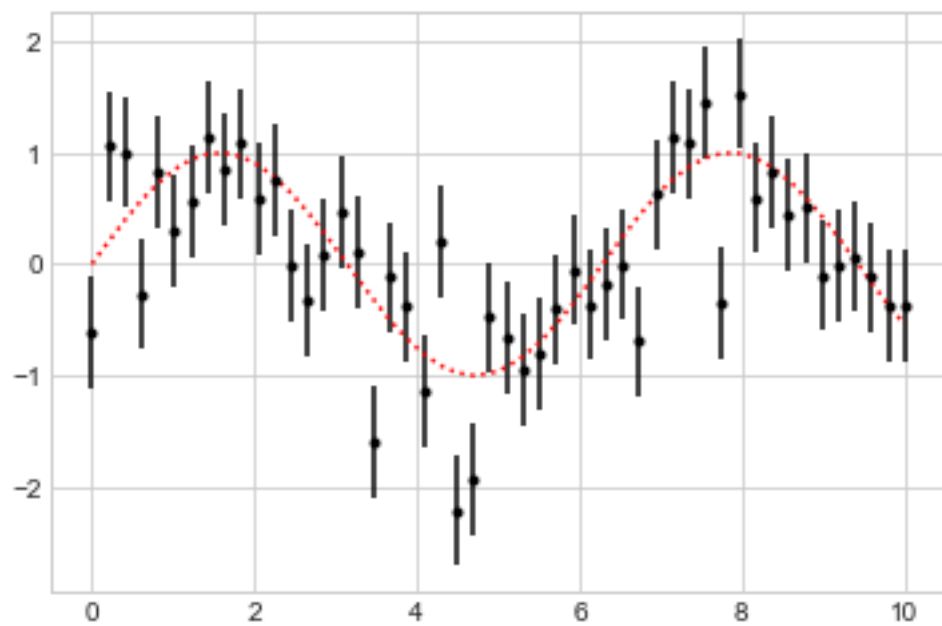
```
In [506]: import time
import pandas as pd
# Get Gapminder Life Expectancy data (csv file is hosted on the web)
url = 'https://python-graph-gallery.com/wp-content/uploads/gapminderData.csv'
data = pd.read_csv(url)
data.to_csv("data/gapminder.csv", index=False)
```

7.7 Visualizing Errors - Errorbars

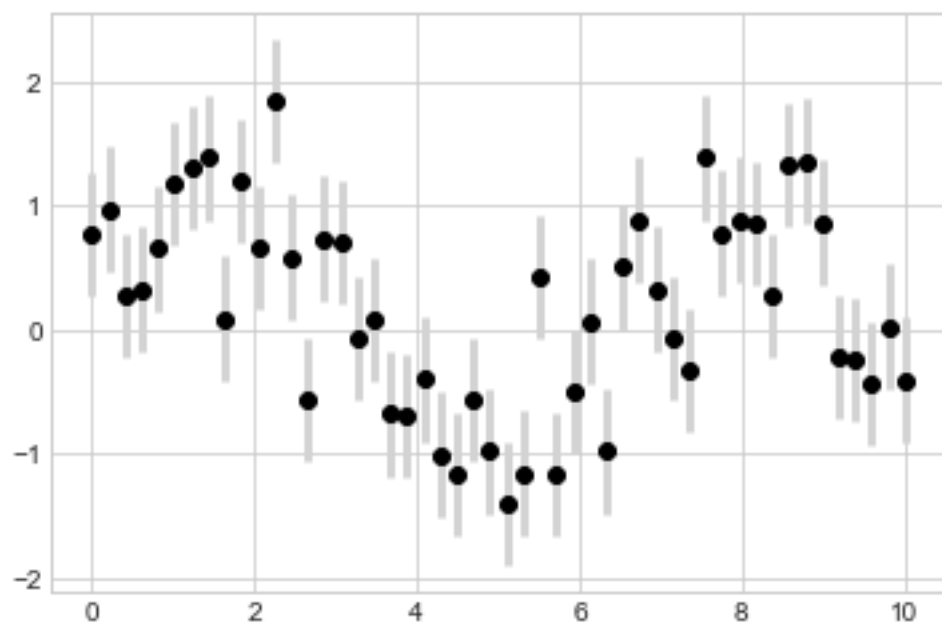
```
In [20]: plt.style.use('seaborn-whitegrid')

N = 50
x = np.linspace(0, 10, N)
error = .5
y = np.sin(x)
y_measured = y + error * np.random.randn(N)

plt.plot(x, y, 'r:', label='true')
plt.errorbar(x, y_measured, yerr=error, fmt='.k', label='measured');
```

```
In [508]: plt.errorbar(x, y_measured, yerr=error, fmt='o', color='black',
    ecolor='lightgray', elinewidth=3, capsize=0);
```



7.8 Visualizing Errors - Errortubes

We will look at an example of [Gaussian Process Regression](#)

Taken from [Scikit Learn Tutorials](#)

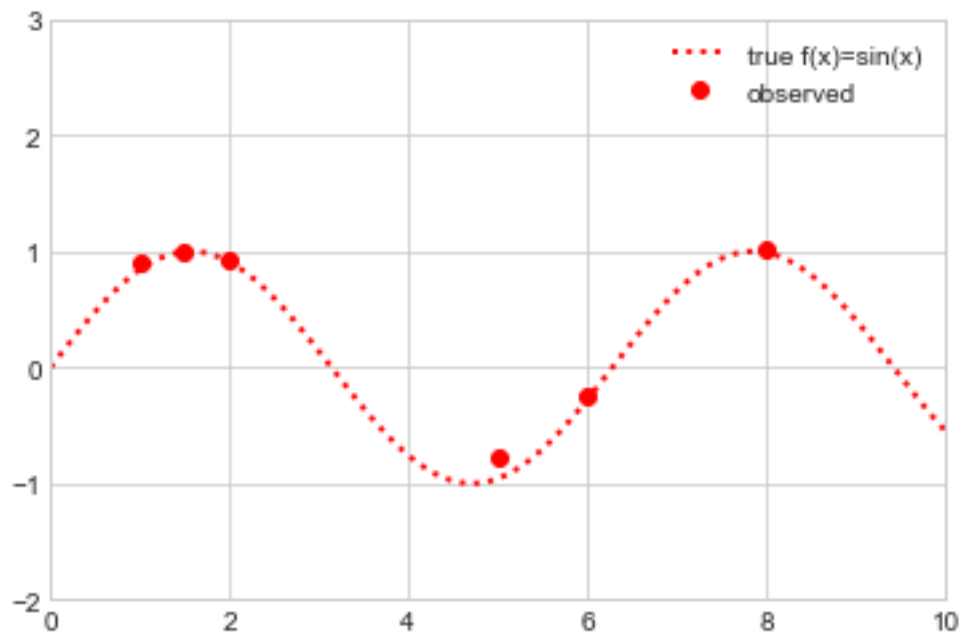
```
In [509]: from sklearn.gaussian_process import GaussianProcessRegressor
          from sklearn.gaussian_process.kernels import RBF

          def f(x):
              """The function to predict."""
              return np.sin(x)

          xdata = np.array([[1, 1.5, 2, 5, 6, 8]]).T
          ydata = f(xdata)
          ydata_with_noise = ydata + .2 * np.random.random(ydata.shape)

          xfit = np.linspace(0, 10, 1000)
          plt.plot(xfit, f(xfit), 'r:', label='true f(x)=sin(x)')
          plt.plot(xdata, ydata_with_noise, 'or', label='observed')

          plt.xlim(0, 10);
          plt.ylim(-2, 3);
          plt.legend();
```



```
In [510]: # Instantiate a Gaussian Process model
          kernel = RBF(.5, (1e-2, 1e1))
```

```

gp = GaussianProcessRegressor(kernel=kernel)

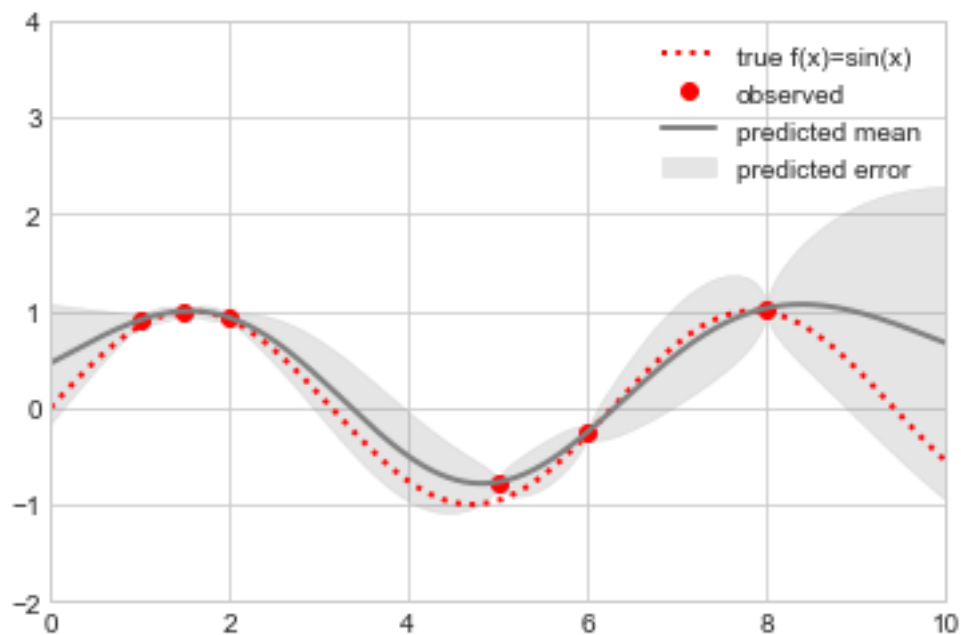
# Fit to data using Maximum Likelihood Estimation of the parameters
gp.fit(xdata, ydata_with_noise)

yfit, MSE = gp.predict(xfit[:, np.newaxis], return_std=True)
dyfit = 2 * np.sqrt(MSE) # 2*sigma ~ 95% confidence region

plt.plot(xfit, f(xfit), 'r:', label='true f(x)=sin(x)')
plt.plot(xdata, ydata_with_noise, 'or', label='observed')
plt.plot(xfit, yfit, '-', color='gray', label='predicted mean')

plt.fill_between(xfit, yfit.flatten() - dyfit, yfit.flatten() + dyfit,
                 color='gray', alpha=0.2, label='predicted error')
plt.ylim(-2, 4);
plt.xlim(0, 10);
plt.legend();

```



7.9 Examples with real data

GapMinder

```

In [18]: import pandas as pd
df = pd.read_csv("data/gapminder.csv")
df.head()

```

```
Out[18]:
```

	country	year	pop	continent	lifeExp	gdpPercap
0	Afghanistan	1952	8425333.0	Asia	28.801	779.445314
1	Afghanistan	1957	9240934.0	Asia	30.332	820.853030
2	Afghanistan	1962	10267083.0	Asia	31.997	853.100710
3	Afghanistan	1967	11537966.0	Asia	34.020	836.197138
4	Afghanistan	1972	13079460.0	Asia	36.088	739.981106

7.9.1 Plot Life Expectancy and Gross Domestic Product (GDP)

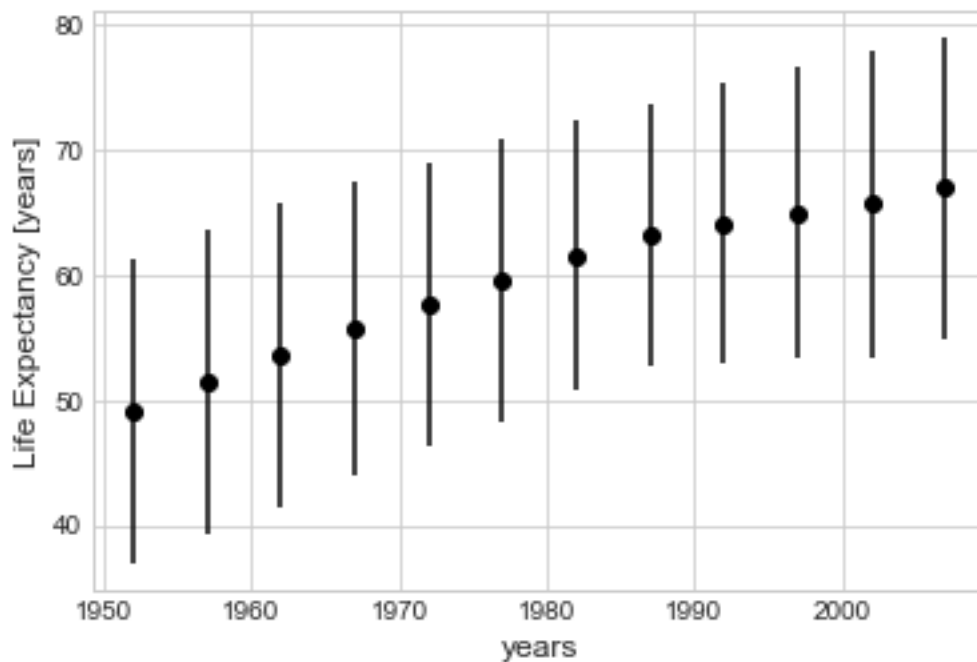
7.9.2 Mean and Standard Deviations as Errorbars

Mean and Standard Deviation are often not as informative/robust as percentiles!

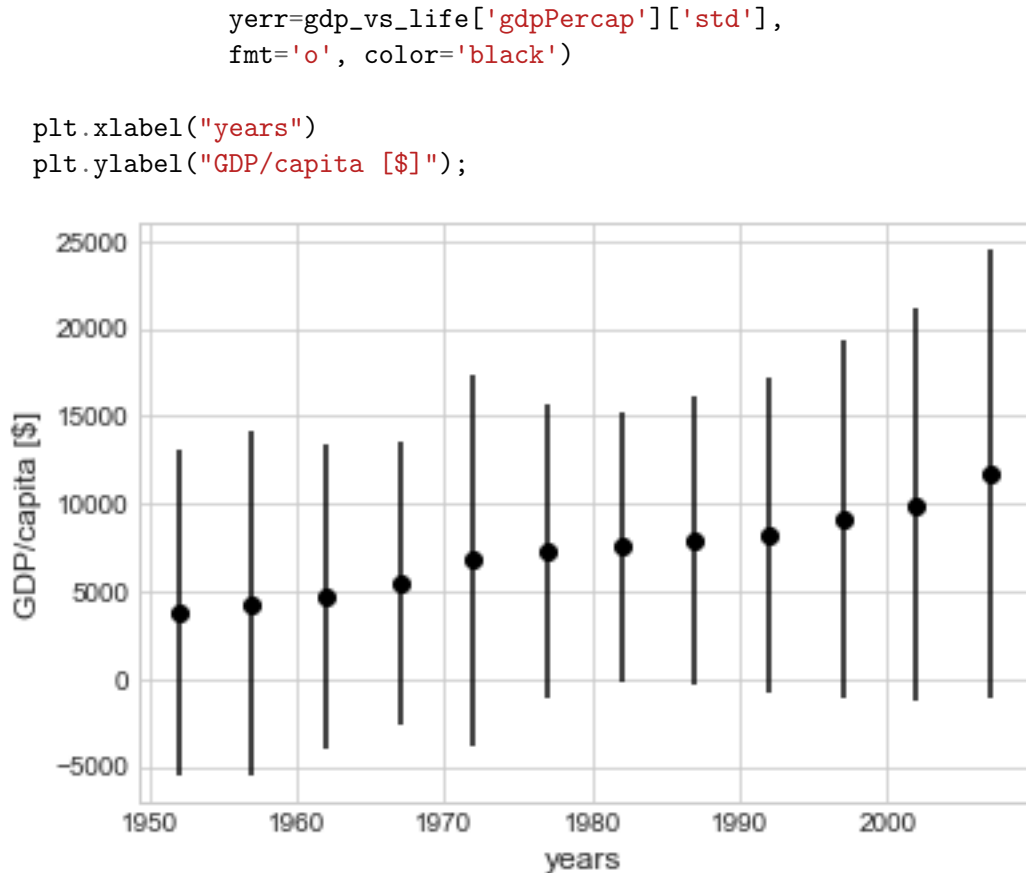
```
In [21]: gdp_vs_life = df.groupby('year')\
        .agg({'gdpPercap': ['mean', 'std'], 'lifeExp': ['mean', 'std']})

plt.errorbar(gdp_vs_life.index,
             gdp_vs_life['lifeExp']['mean'],
             yerr=gdp_vs_life['lifeExp']['std'],
             fmt='o', color='black')

plt.xlabel("years")
plt.ylabel("Life Expectancy [years]");
```



```
In [22]: plt.errorbar(gdp_vs_life.index,
                     gdp_vs_life['gdpPercap']['mean'],
```



7.9.3 Median and Percentiles as Error tubes

Mean and Standard Deviation are often not as informative/robust as percentiles!

```

In [23]: life_exp = df.groupby('year')['lifeExp'].quantile(q=[.1,.5,.9]).reset_index()

years = life_exp['year'].unique()

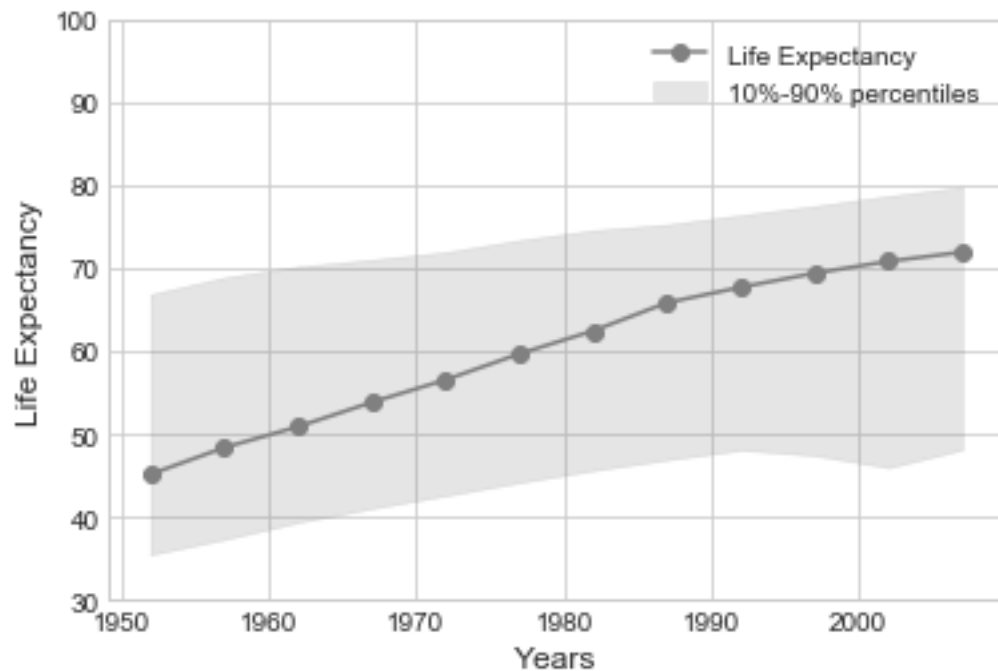
plt.plot(years,
         life_exp.loc[life_exp['level_1']==.5, 'lifeExp'],
         '-o', color='gray', label='Life Expectancy')

plt.fill_between(years,
                 life_exp.loc[life_exp['level_1']==.1, 'lifeExp'],
                 life_exp.loc[life_exp['level_1']==.9, 'lifeExp'],
                 color='gray', alpha=0.2, label='10%-90% percentiles')

plt.legend()
plt.ylim(30,100)
plt.xlabel('Years')
plt.ylabel('Life Expectancy')

```

Out[23]: Text(0,0.5,'Life Expectancy')



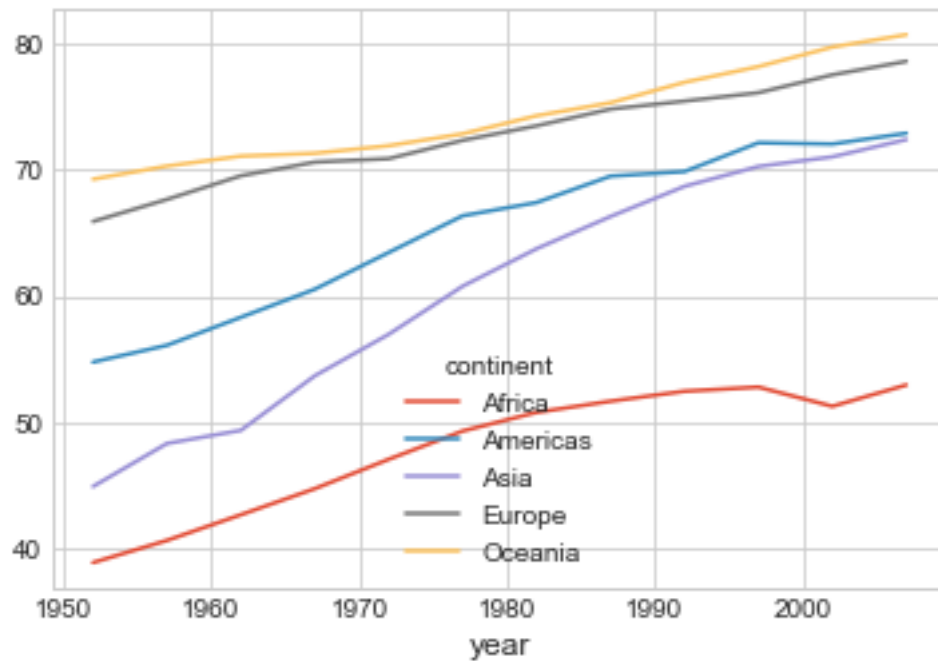
8 Plotting from pandas

- It's important to understand the plotting basics
- for modifying details
- for simple plots
- But with complex data, interactive visualization with `matplotlib` is tedious
- pandas allows to call `matplotlib` conveniently on DataFrames

```
In [ ]: df = pd.read_csv("data/gapminder.csv")
        life_exp_per_continent = df[['year', 'continent', 'lifeExp']].groupby(['year', 'continent'])
        life_exp_per_continent.columns = life_exp_per_continent.columns.droplevel(0)
        life_exp_per_continent.head()
```

8.1 Simple Line Plots

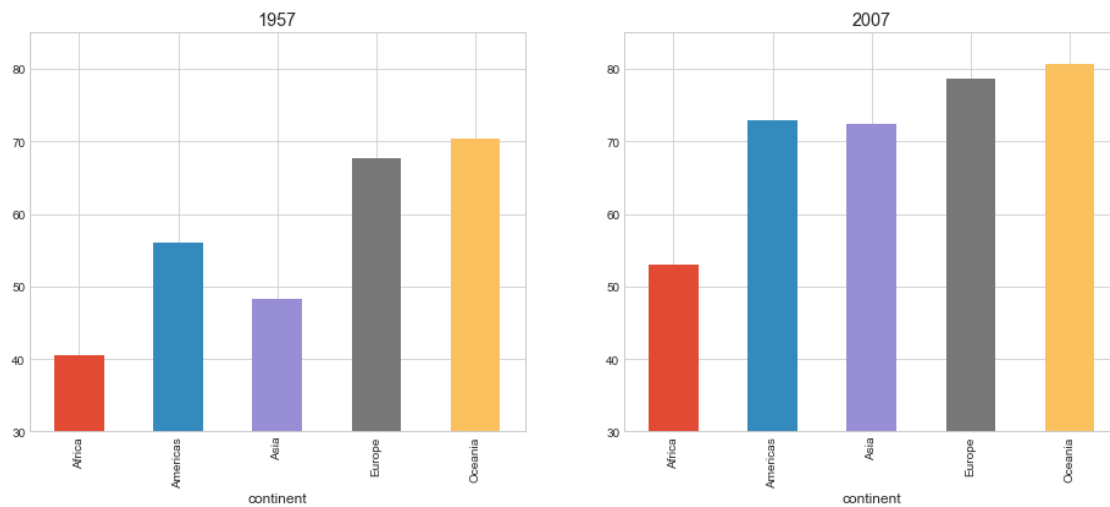
```
In [25]: life_exp_per_continent.plot();
```



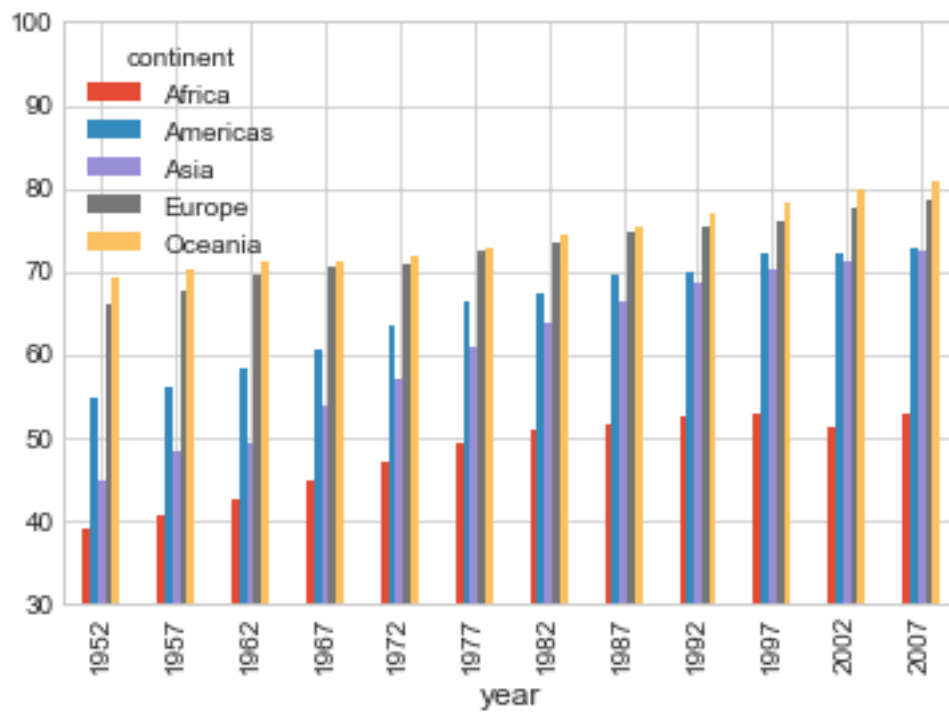
8.2 Bar Plots

8.2.1 Life Expectancy

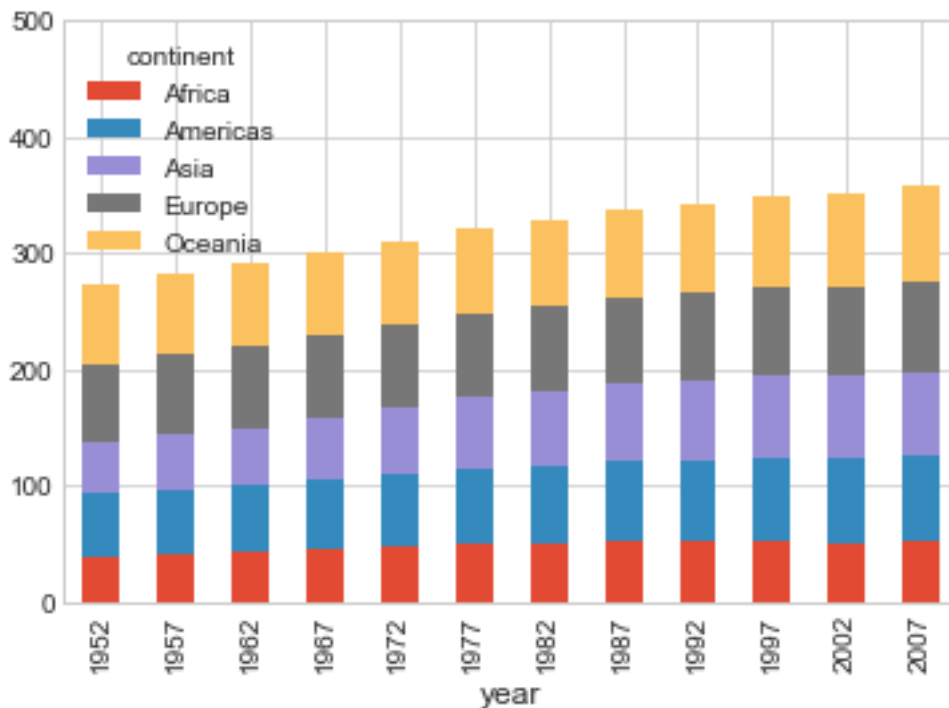
```
In [26]: plt.figure(figsize=[16,6])
plt.subplot(1,2,1)
life_exp_per_continent.loc[1957].plot(kind='bar');
plt.title('1957');
plt.ylim([30,85]);
plt.subplot(1,2,2)
life_exp_per_continent.loc[2007].plot(kind='bar');
plt.title('2007');
plt.ylim([30,85]);
```



```
In [27]: life_exp_per_continent.plot.bar();
plt.ylim([30,100]);
```



```
In [30]: life_exp_per_continent.plot.bar(stacked=True);
plt.ylim([0,500]);
```

8.3 Histograms

8.3.1 Overall GDP

```
In [ ]: df['gdpPercap'].hist();
        plt.ylabel("# Countries")
        plt.xlabel("GDP/Capita")
```

8.3.2 The differences in per capita GDP are huge

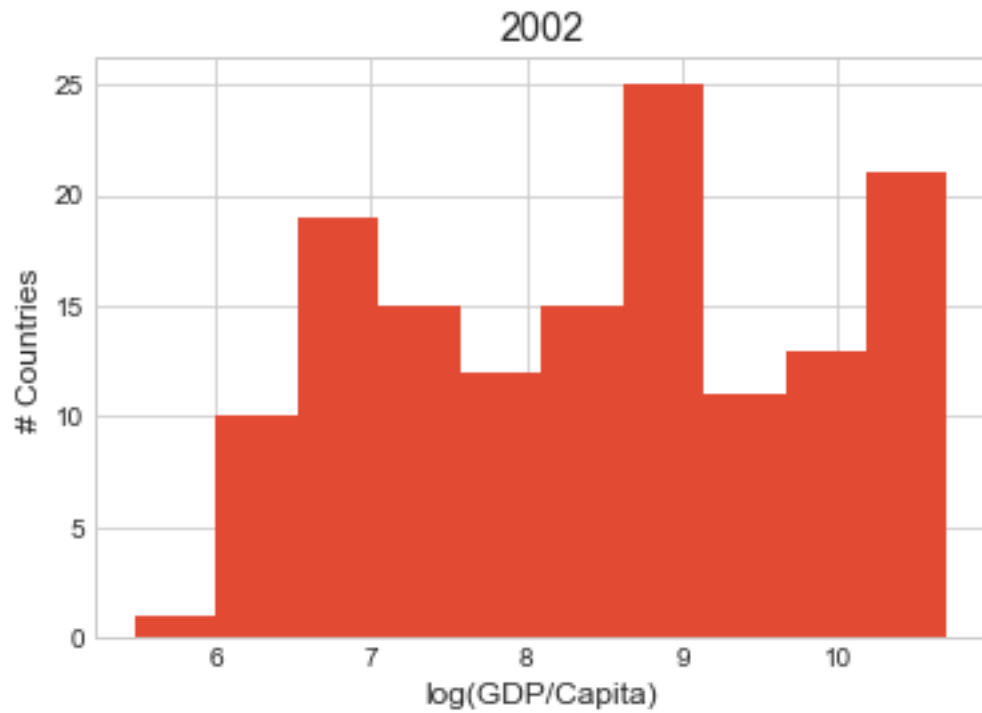
Few rich countries are much richer than the many poorer countries.

Plot is not very conclusive. How can we zoom in, without losing the bigger picture?

8.3.3 Log-Scaling Prior to Histogram Computation

Leads to log-scaled bins and more 'normal' looking distribution

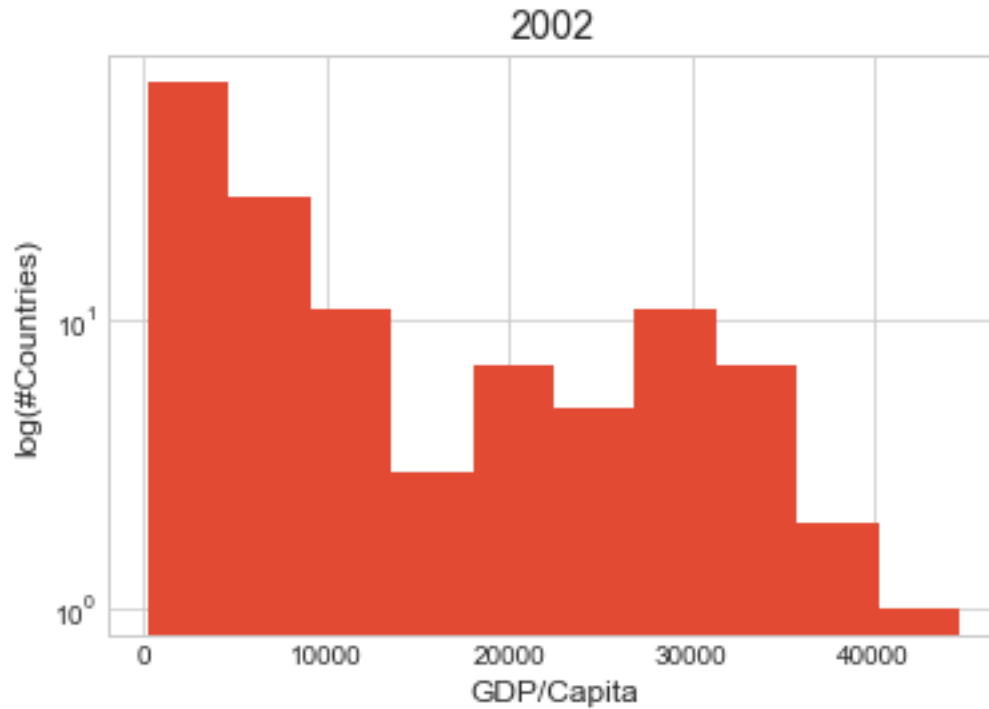
```
In [32]: df.loc[df.year==2002, 'gdpPercap'].apply(np.log).hist();
        plt.ylabel("# Countries")
        plt.xlabel("log(GDP/Capita)");
```



8.3.4 Log-Scaling Y-Axis

Linearly scaled bins but log-scaled histogram counts

```
In [33]: df.loc[df.year==2002, 'gdpPercap'].hist();  
plt.yscale('log');  
plt.ylabel('log(#Countries)');  
plt.xlabel("GDP/Capita");
```



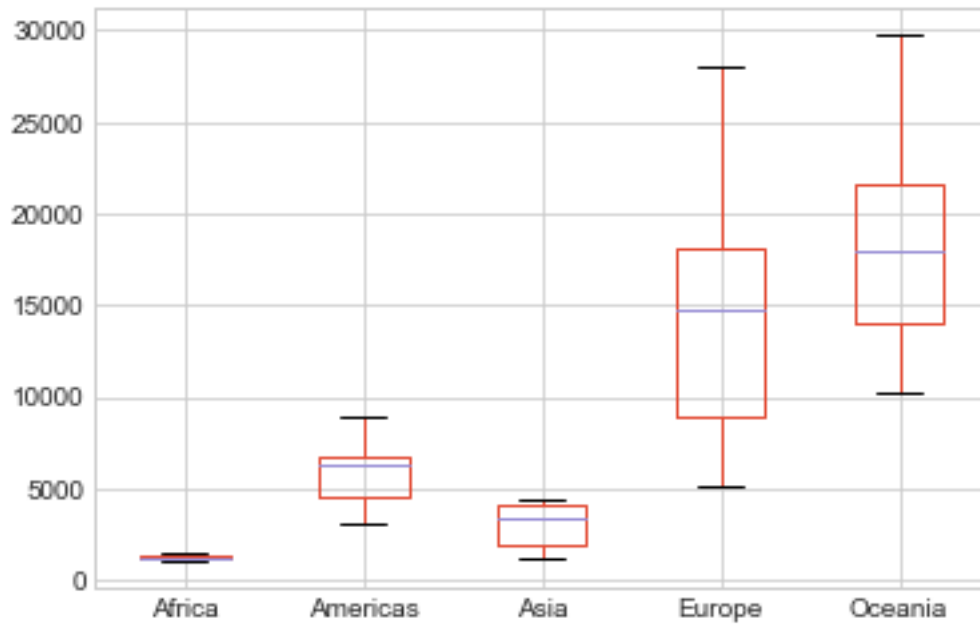
8.3.5 GDP per Continent

```
In [35]: gdp_per_continent = df[['year', 'continent', 'gdpPercap']] \
        .groupby(['year', 'continent']).median().unstack()
gdp_per_continent.columns = gdp_per_continent.columns.droplevel(0)
gdp_per_continent.head()
```

```
Out[35]: continent    Africa    Americas    Asia    Europe    Oceania
year
1952      987.025569  3048.302900  1206.947913  5142.469716  10298.085650
1957     1024.022987  3780.546651  1547.944844  6066.721495  11598.522455
1962     1133.783677  4086.114078  1649.552153  7515.733737  12696.452430
1967     1210.376379  4643.393534  2029.228142  9366.067033  14495.021790
1972     1443.372508  5305.445256  2571.423014  12326.379990  16417.333380
```

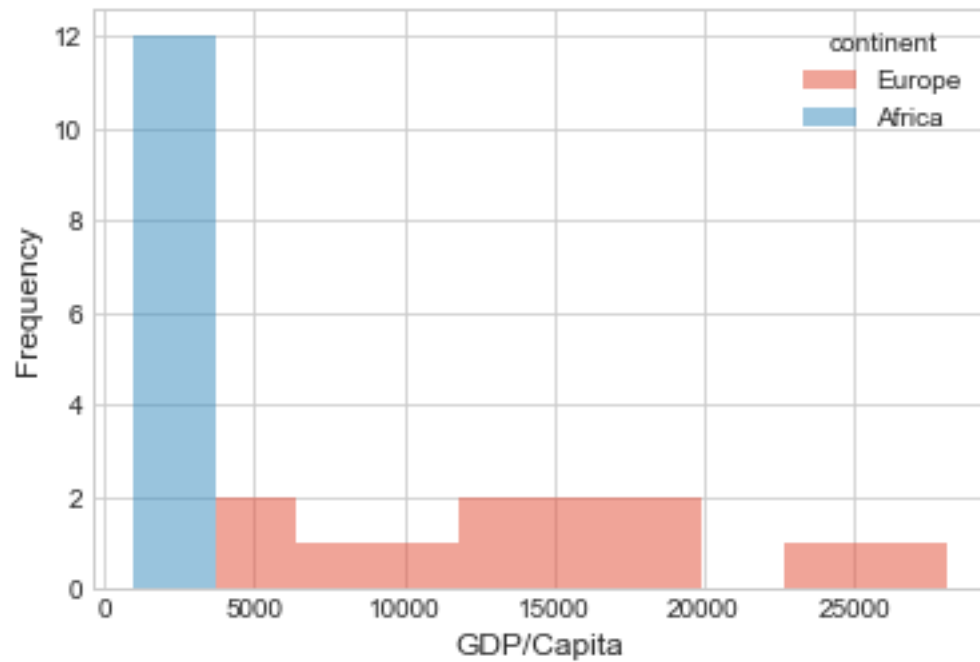
8.3.6 Box Plots

```
In [36]: gdp_per_continent.plot.box();
```

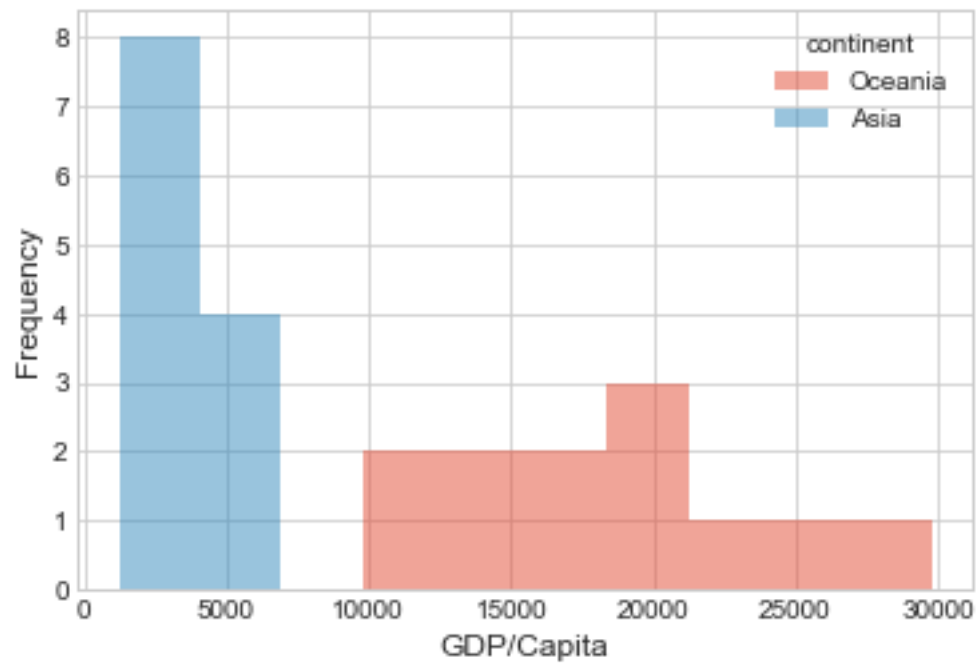


8.3.7 Histograms

```
In [37]: gdp_per_continent[['Europe', 'Africa']].plot.hist(alpha=0.5);
plt.xlabel("GDP/Capita");
```



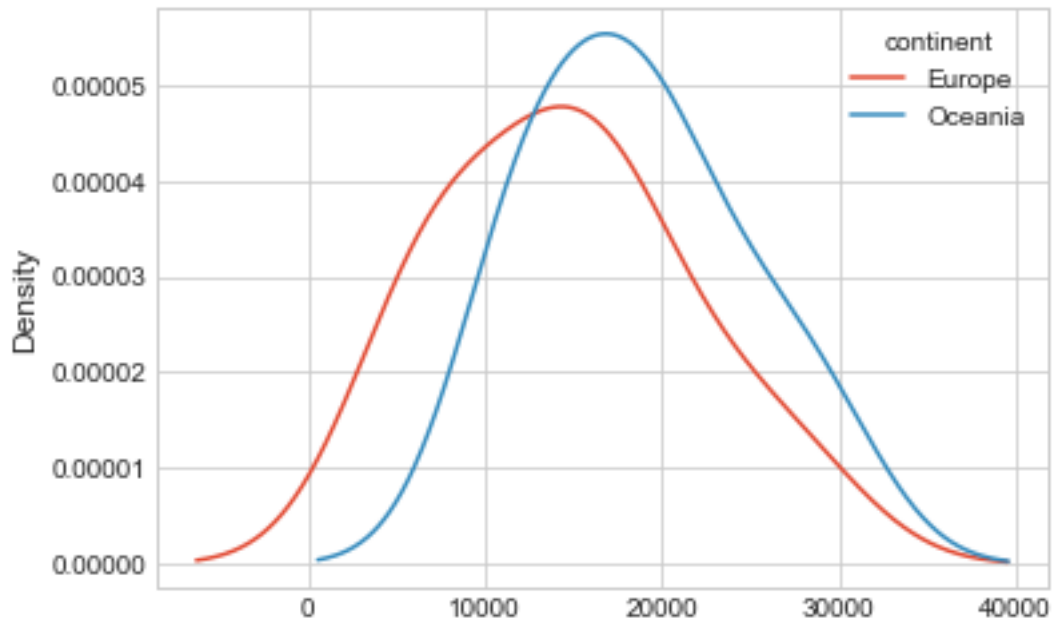
```
In [38]: gdp_per_continent[['Oceania', 'Asia']].plot.hist(alpha=0.5);  
plt.xlabel("GDP/Capita");
```



8.3.8 Kernel Density Estimate Plots

Smoothed histograms

```
In [44]: gdp_per_continent[['Europe', 'Oceania']].plot.kde();
```



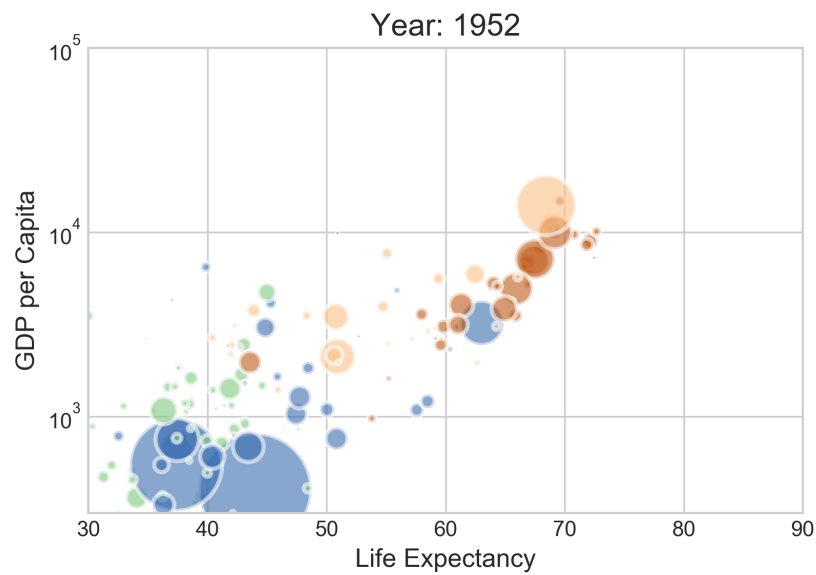
9 GapMinder Demo

```
In [42]: data = pd.read_csv("data/gapminder.csv")

# Transform Continent into numerical values group1->1, group2->2...
data['continent']=pd.Categorical(data['continent'])

def plot_gapminder(year, filename=''):
    fig = plt.figure()
    ax = plt.axes()
    year = data.loc[abs(data.year.unique() - year).argmin(), 'year']
    # Change color for the x-axis values
    tmp=data[ data.year == year ]
    ax.scatter(tmp['lifeExp'], tmp['gdpPercap'] , s=tmp['pop']/200000 ,
              c=tmp['continent'].cat.codes, cmap="Accent", alpha=0.6,
              edgecolors="white")

    # Add titles (main and on axis)
    ax.set_yscale('log')
    ax.set_xlabel("Life Expectancy")
    ax.set_ylabel("GDP per Capita")
    ax.set_title("Year: "+str(year) )
    ax.set_ylim(0,100000)
    ax.set_xlim(30, 90)
    if filename:
```



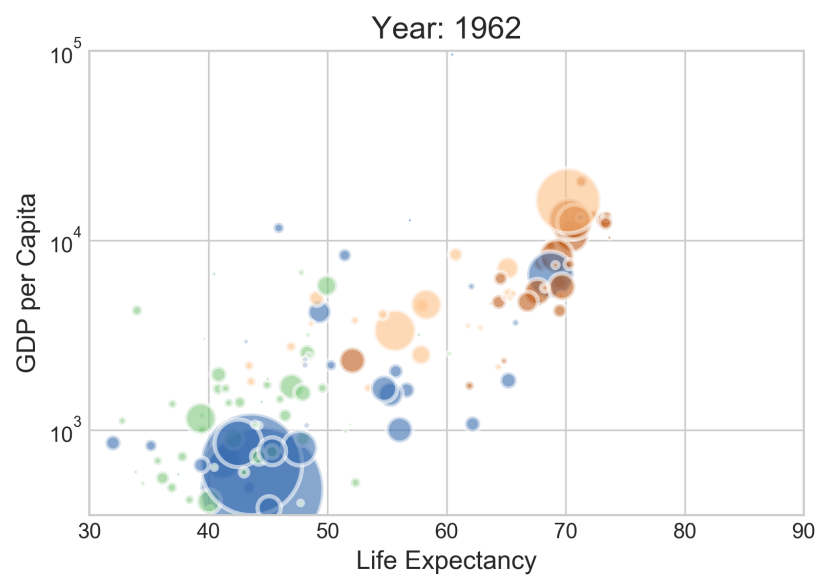
```
plt.savefig(filename)
else:
    plt.show()
```

```
In [578]: from ipywidgets import interact
import ipywidgets as widgets

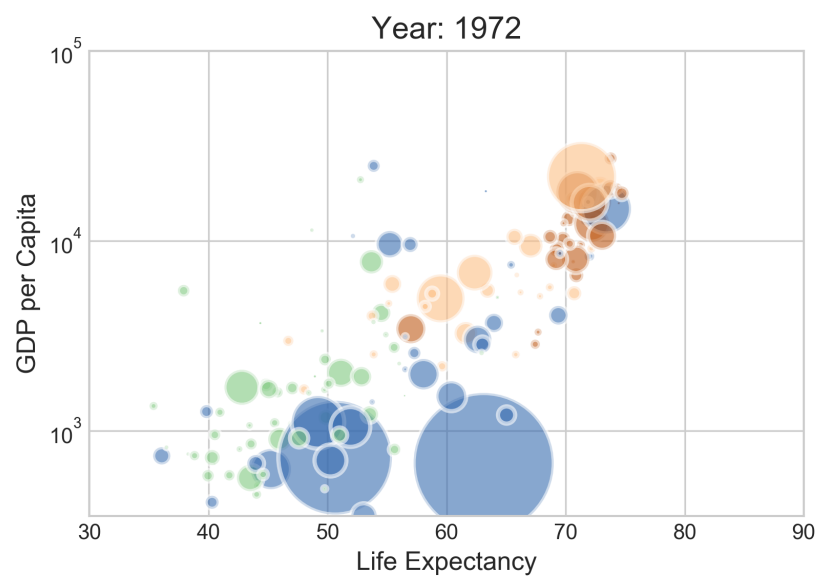
def plot_gapminder_no_savefig(year):
    plot_gapminder(year, "")

    interact(plot_gapminder_no_savefig, year=widgets.IntSlider(min=1952,max=2007,step=1,value=1952),
             interactive(children=(IntSlider(value=1952, description='year', max=2007, min=1952), Output()),

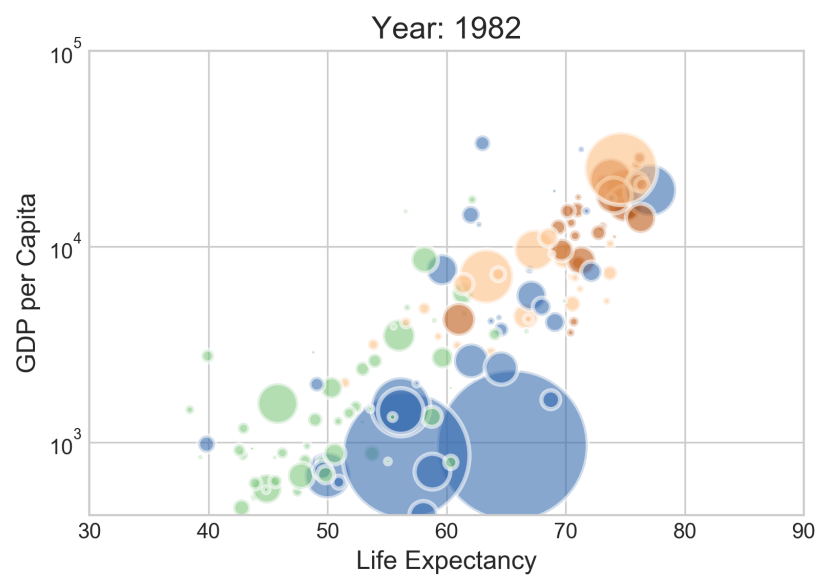
In [ ]: for year in data.year.unique():
    filename='plots/Gapminder_step'+str(year)+'.png'
    plot_gapminder(year, filename=filename)
```



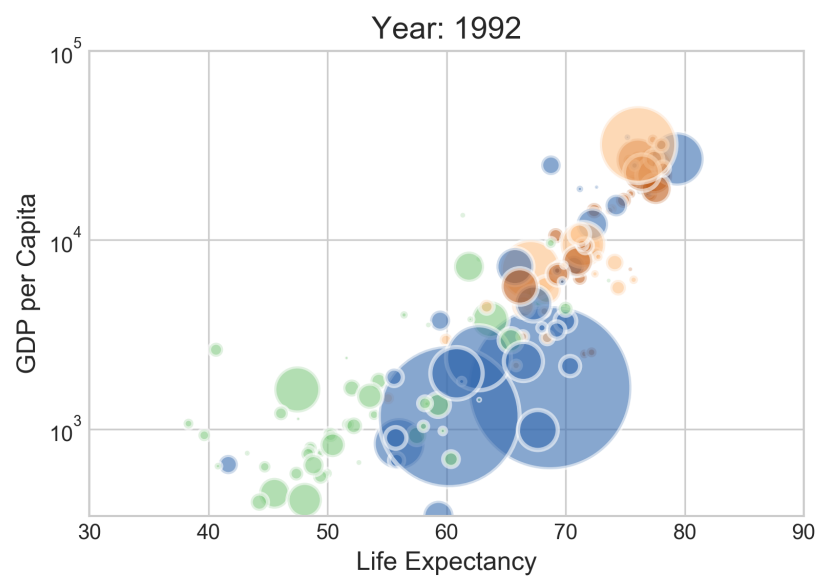
1962



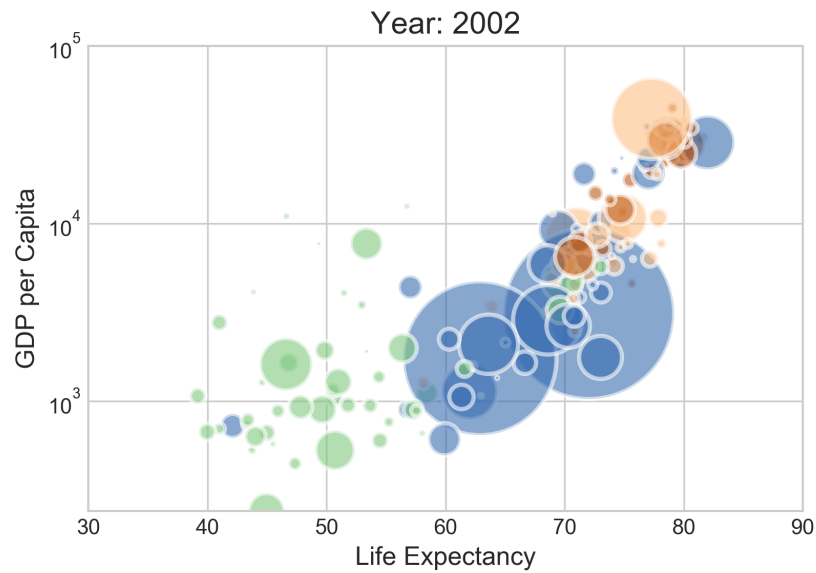
1972



1982



1992



2002

9.1 Life Expectancy vs GDP vs Time

9.2 Life Expectancy vs GDP vs Time

9.3 Life Expectancy vs GDP vs Time

9.4 Life Expectancy vs GDP vs Time

9.5 Life Expectancy vs GDP vs Time

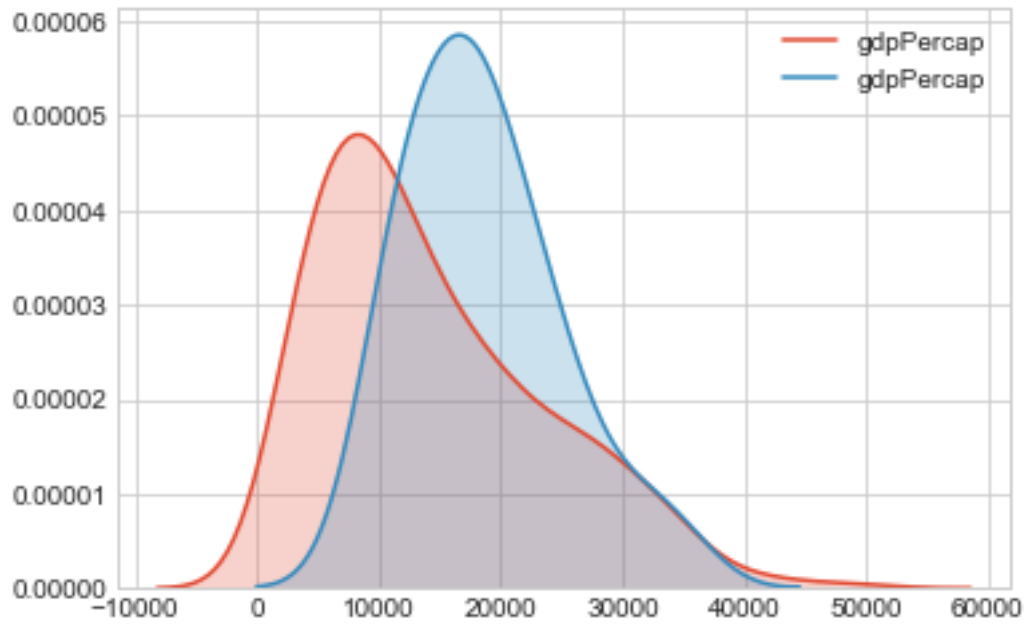
9.6 Life Expectancy vs GDP vs Time

10 Plotting with seaborn

- Matplotlib is too low level for complex interactive visualization
- pandas allows for simpler API
- Many great plots you'll find use abstractions on matplotlib

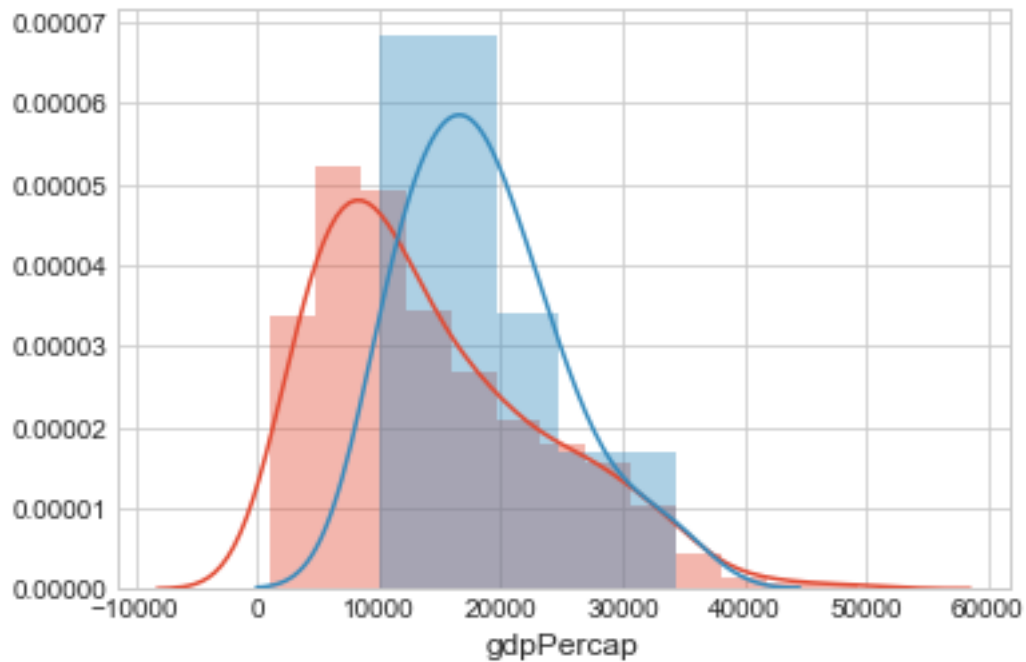
10.1 KDE Plots

```
In [74]: import seaborn as sns
data = pd.read_csv("data/gapminder.csv")
sns.kdeplot(data.loc[data.continent=='Europe', 'gdpPercap'], shade=True);
sns.kdeplot(data.loc[data.continent=='Oceania', 'gdpPercap'], shade=True);
```



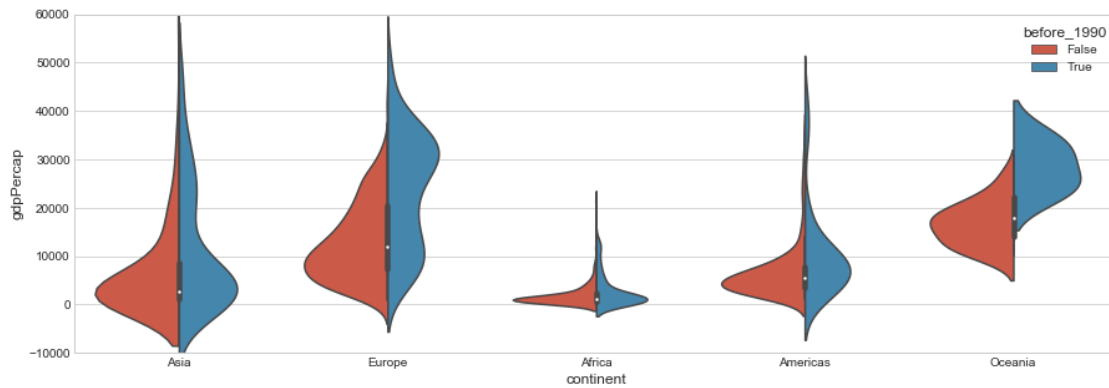
10.2 Histograms and Density Plots

```
In [75]: sns.distplot(data.loc[data.continent=='Europe','gdpPercap']);  
         sns.distplot(data.loc[data.continent=='Oceania','gdpPercap']);
```

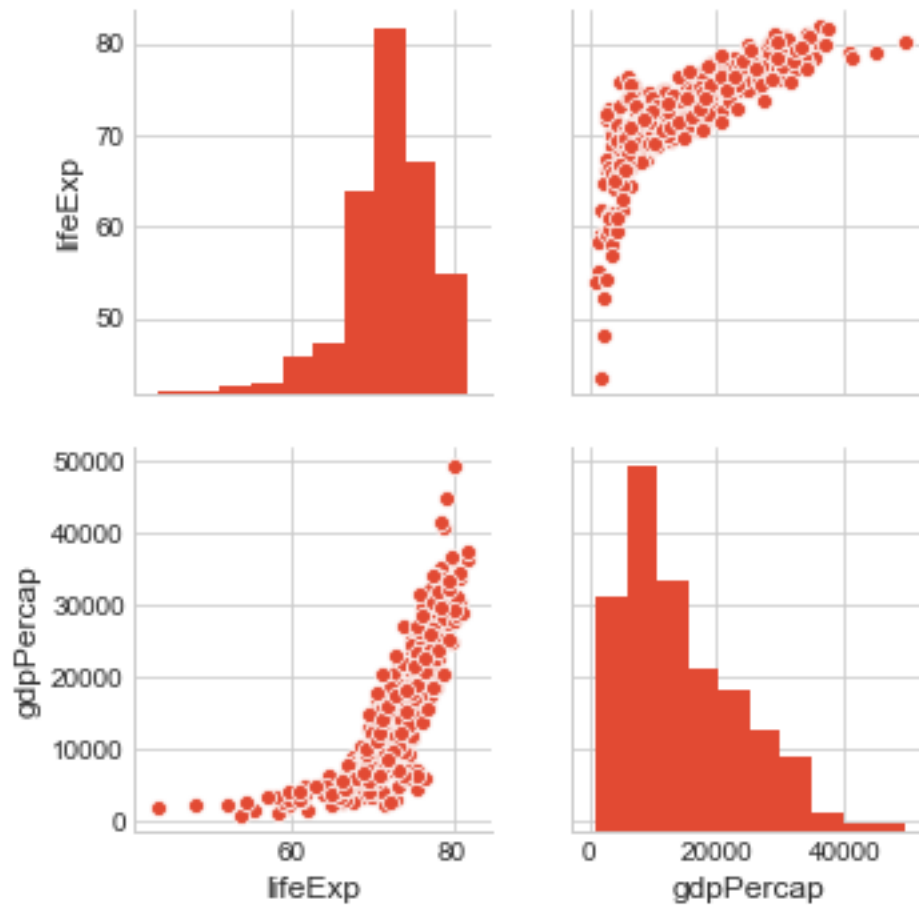


10.3 Violin Plots

```
In [109]: plt.figure(figsize=[15,5])
data['before_1990'] = data.year>2000
sns.violinplot( "continent", "gdpPercap", hue='before_1990', data=data, split=True);
plt.ylim([-10000, 60000]);
```



```
In [112]: sns.pairplot(data.loc[data.continent=='Europe'], ['lifeExp', 'gdpPercap']);
```



11 Plotting Maps with folium

- leaflet.js is a great javascript library for web based map visualizations
- folium let's you leverage python's flexibility with leaflet's visualization strengths

```
In [ ]: !pip install folium
```

```
In [204]: import folium
          m = folium.Map(location=[52.545195, 13.354670], zoom_start=16)
          m
```

```
Out[204]: <folium.folium.Map at 0x1a407be4a8>
```

```
In [205]: folium.Marker(
          location=[52.545195, 13.354670], popup='Where we are.',
          icon=folium.Icon(icon='cloud')
        ).add_to(m)

        folium.Marker(
          location=[52.543941, 13.355539], popup='Where the ponies live.',
          icon=folium.Icon(icon='cloud')
        ).add_to(m)
        m
```

```
Out[205]: <folium.folium.Map at 0x1a407be4a8>
```

12 Exercises

- In each exercise you will plot some data.
- The resulting plots should be saved to a file and handed in.
- Solutions will be evaluated based on the figures and the code.

12.1 Assignment 01

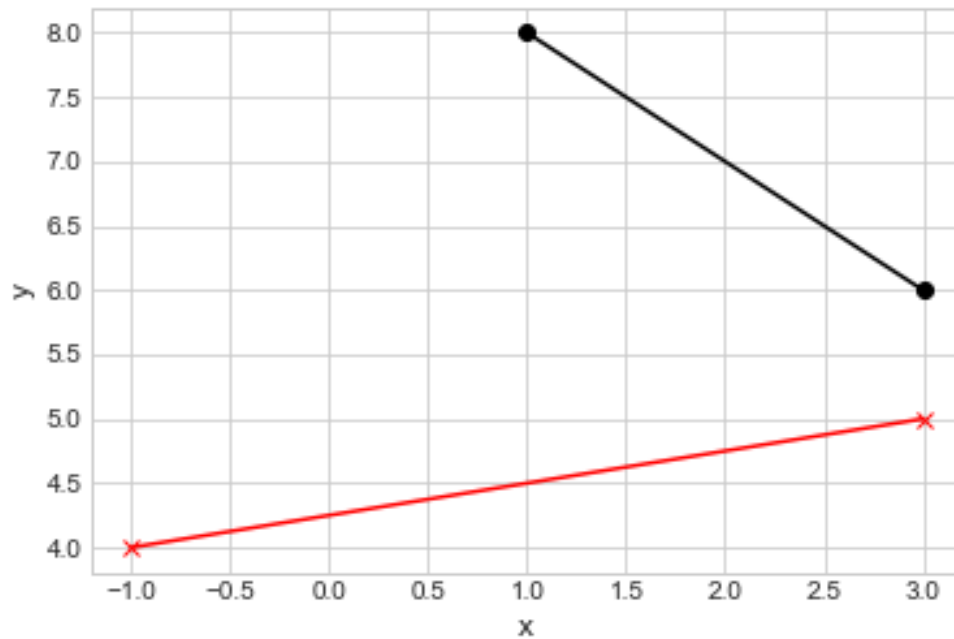
Plot some lines

Write a function `assignment_05_01` that draws a line from the point `[-1,4]` to the point `[3,5]` with line style `'r-x'` and another line from `[3,6]` to `[1,8]` with line style `'k-o'`.

```
def assignment_05_01():
    x = [-1,3]
    y = [4,5]
    ...
    plt.xlabel('x')
    plt.ylabel('y')
    plt.savefig("assignment_05_01.png")
```

```
In [118]: from IPython.display import Image
          Image("assignment_05_01.png")
```

Out[118]:



12.2 Assignment 02

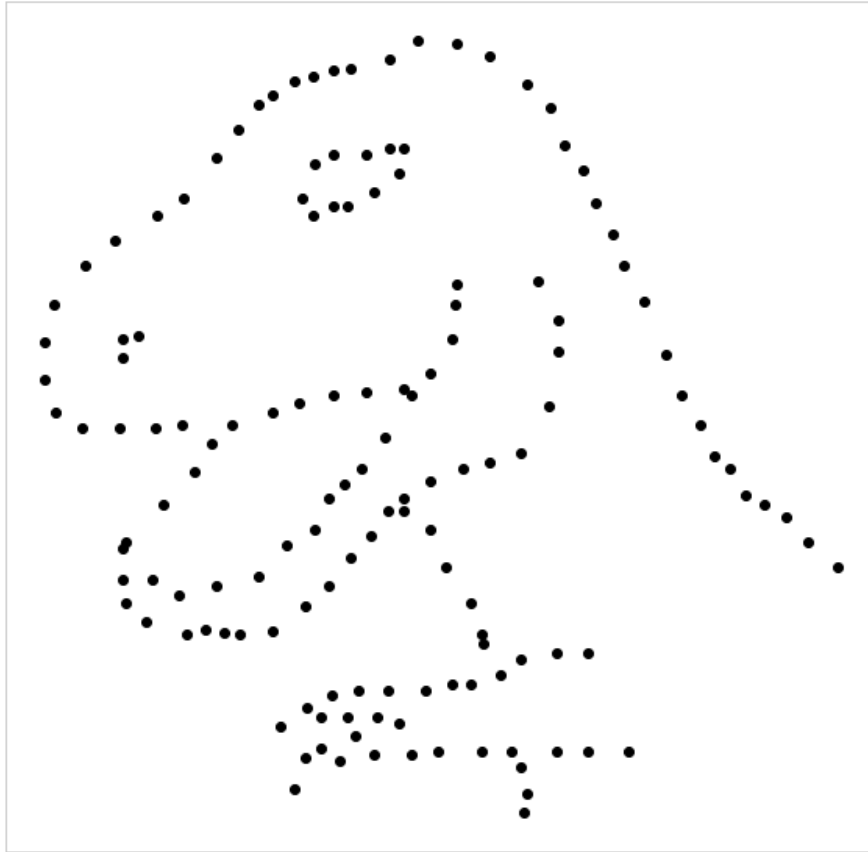
Plot a dinosaur

Write a function `assignment_05_02` that draws the data set 'dino' from the tab-separated file `data/DatasaurusDozen.tsv`.

```
def assignment_05_02():
    ds = pd.read_csv('data/DatasaurusDozen.tsv', sep='\t')
    plt.figure(figsize=[10,10])
    ...
    plt.xticks([])
    plt.yticks([])
    plt.savefig("assignment_05_02.png")
```

```
In [131]: from IPython.display import Image
          Image("assignment_05_02.png")
```

Out[131]:



12.3 Assignment 03

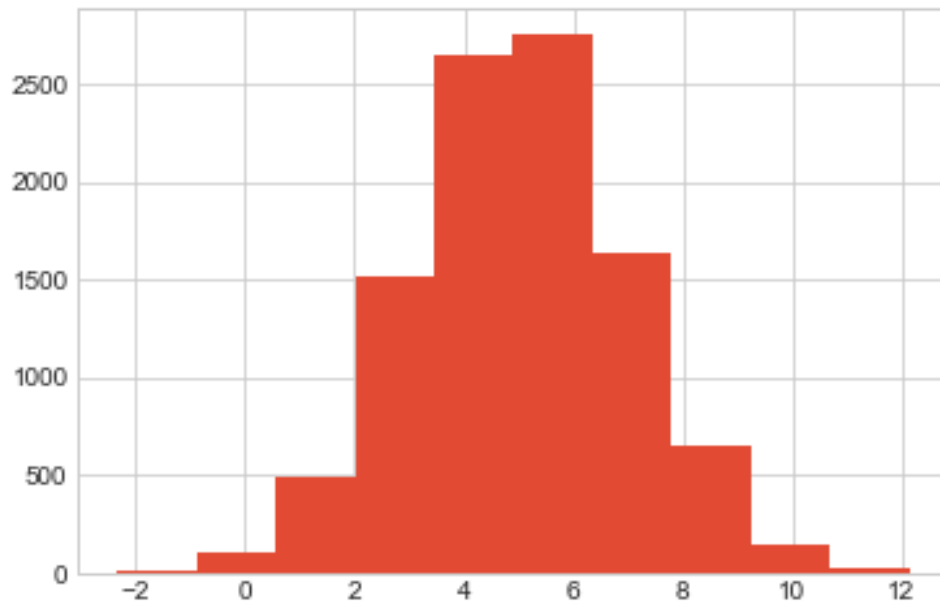
Plot some histograms

Write a function `assignment_05_03` creates a normally distributed variable with mean 5 and standard deviation 2. Plot the histogram and save the file as `assignment_05_03.png`.

```
def assignment_05_03():  
    ...  
    plt.savefig("assignment_05_03.png")
```

```
In [186]: from IPython.display import Image  
          Image("assignment_05_03.png")
```

Out[186]:



12.4 Assignment 04

Plot some 2D Kernel Density Estimates

Write a function `assignment_05_04` that creates a 2D normally distributed variable with mean $[0,0]$ and covariance matrix $\begin{bmatrix} 5 & 2 \\ 2 & 2 \end{bmatrix}$. Plot the joint kernel density estimate and save the file as `assignment_05_04.png`.

```
def assignment_05_04():
    import seaborn as sns
    ...
    normal_data = pd.DataFrame(data, columns=['x', 'y'])
    sns.jointplot("x", "y", normal_data, kind='kde');
    plt.savefig("assignment_05_04.png")
```

```
In [197]: from IPython.display import Image
          Image("assignment_05_04.png")
```

Out[197]:

