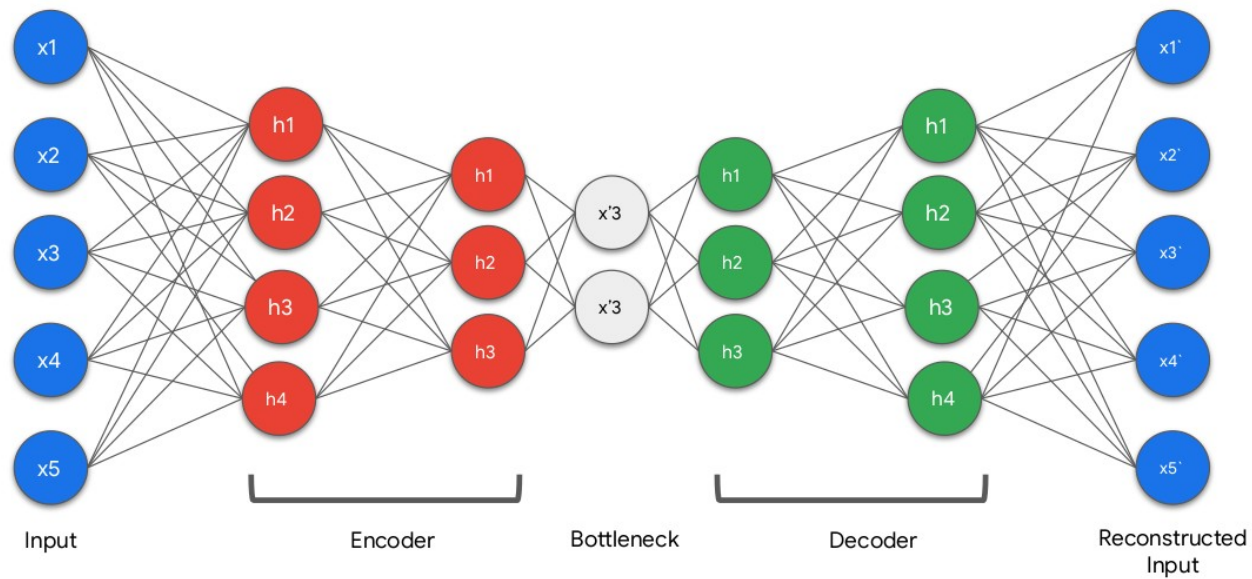


# Variational autoencoder

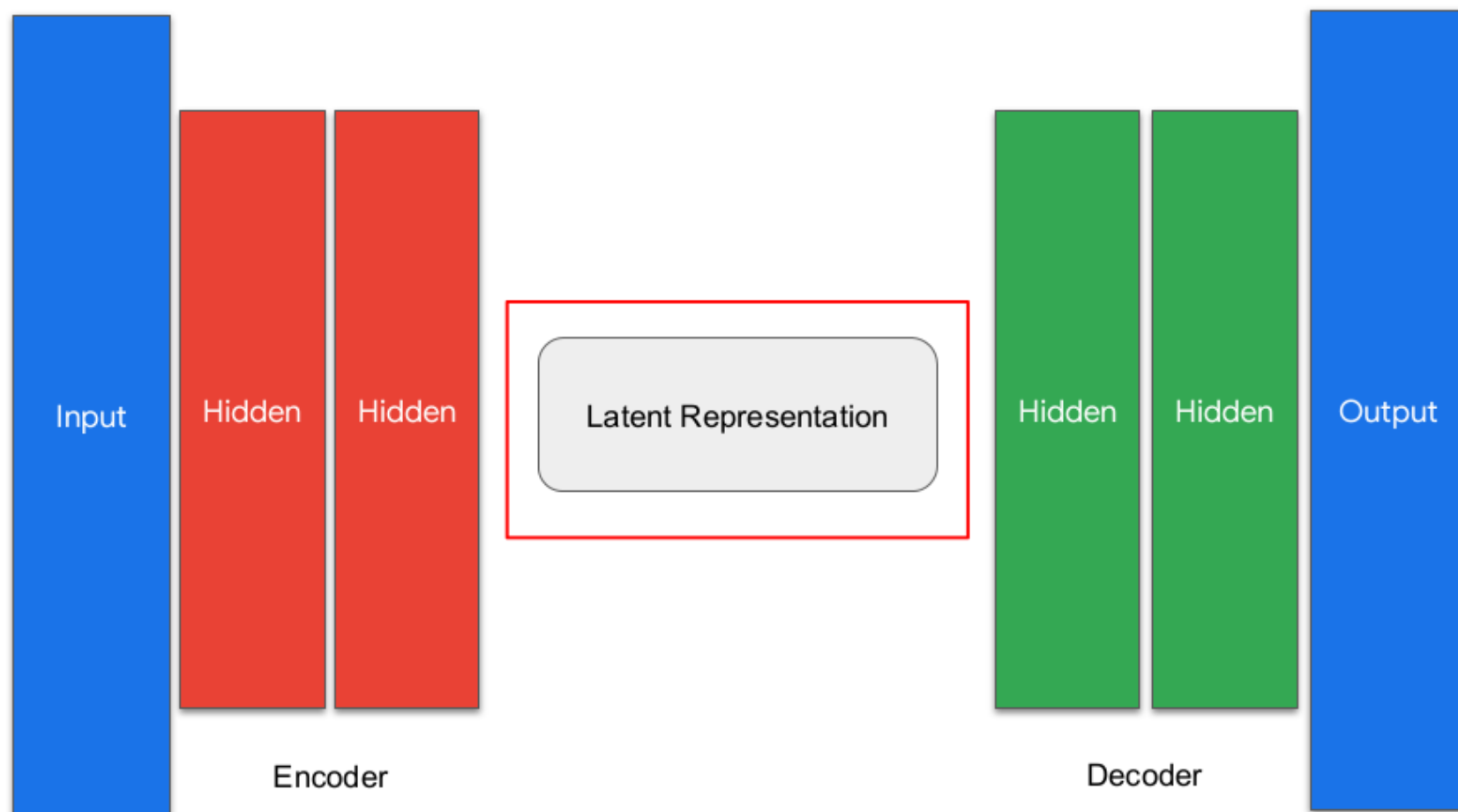
By eng.Ahmed Hisham

# Recap autoencoders

## Stacked Auto-Encoders



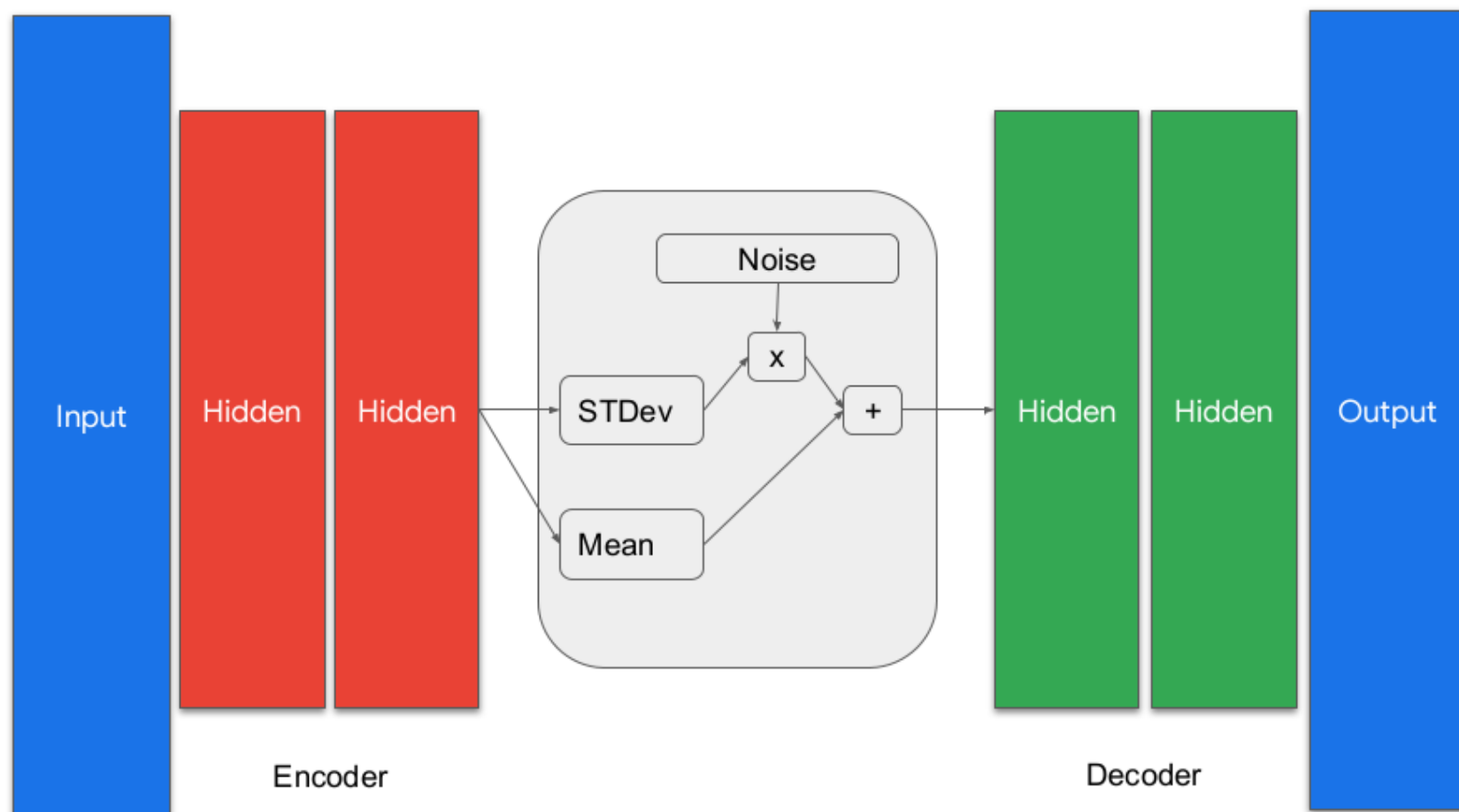
# Variational autoencoder



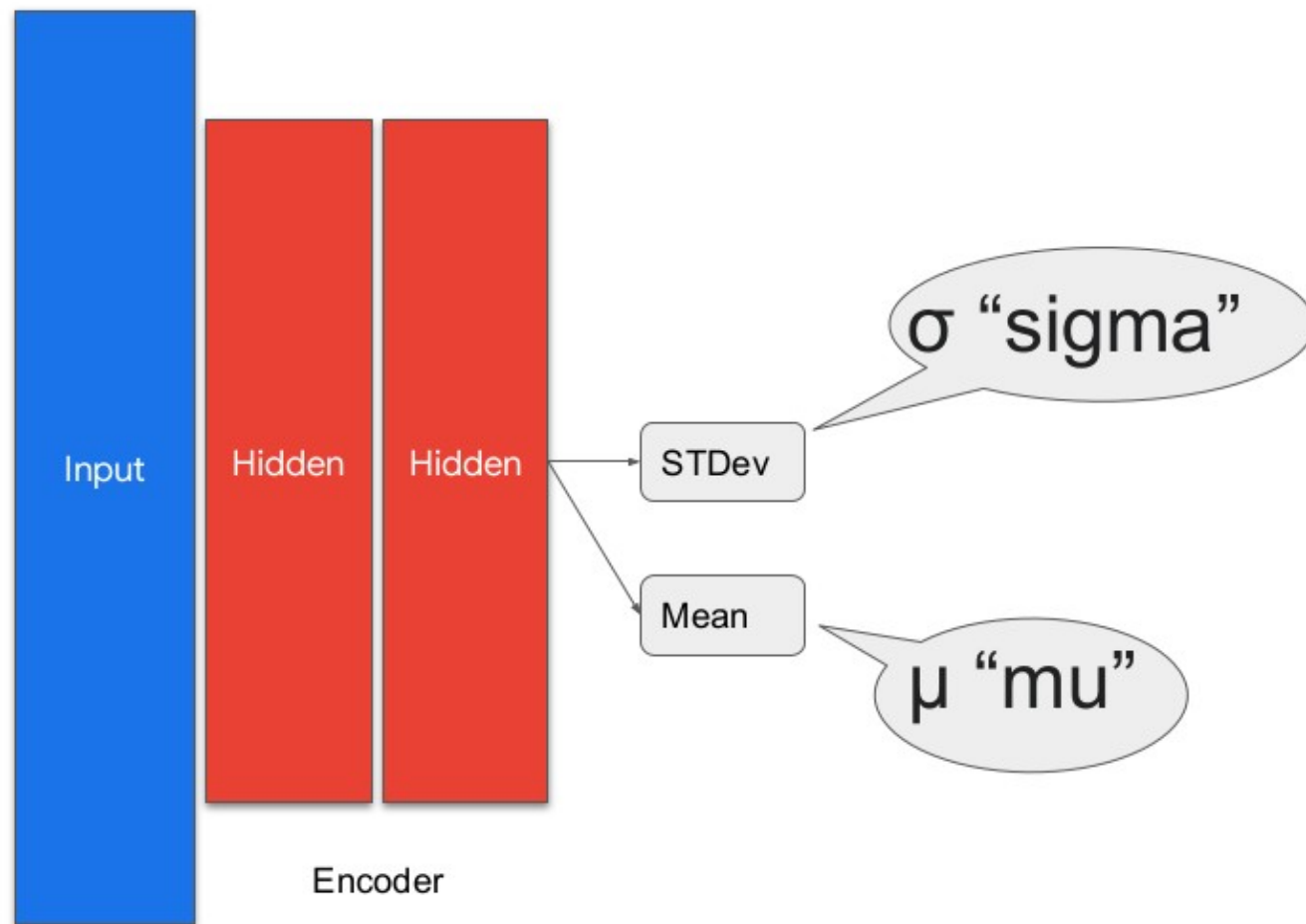
# Key difference

**This model tends to deal with statistical computations rather than bottle neck layer (downsampling)**

# VAE latent layer



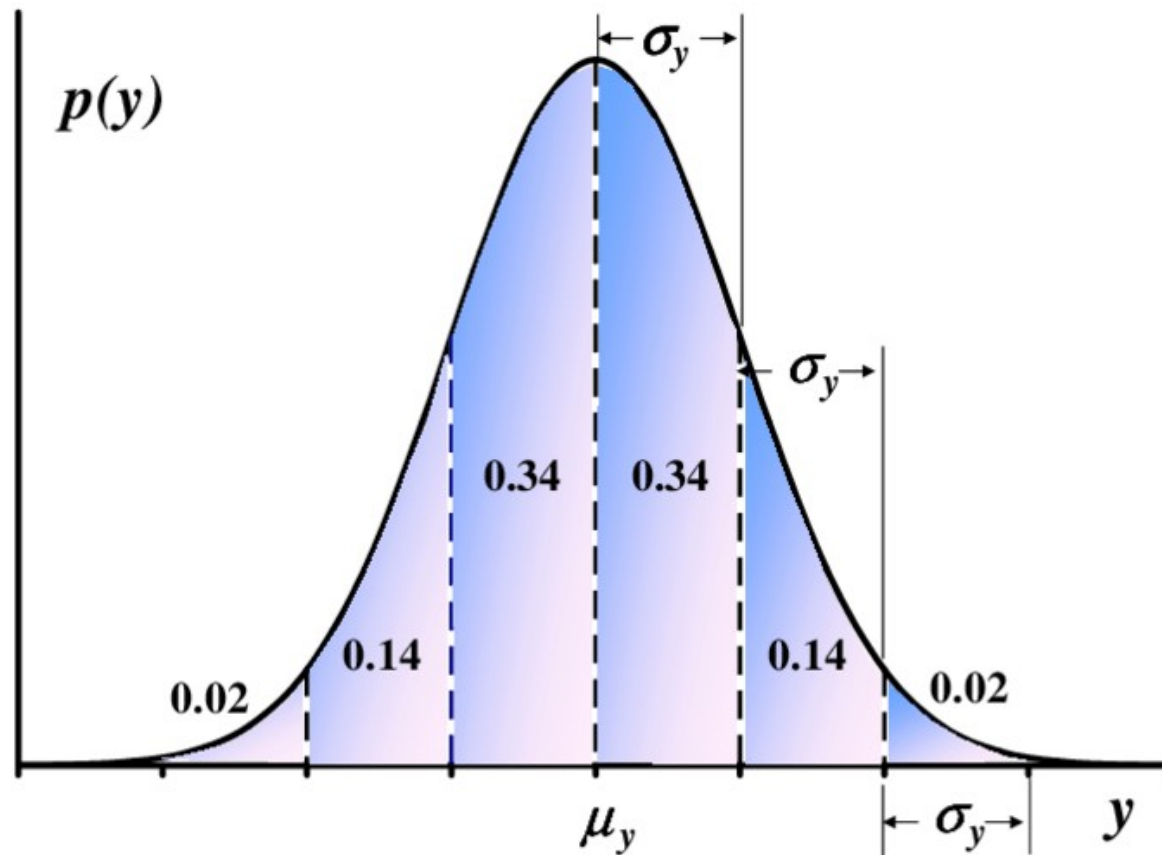
# Encoder + latent layer



# Sigma and Mu

**Sigma and Mu usually are linked to a probability density function → Normal distribution or what is known as Gaussian density probability function**

# Gaussian distribution





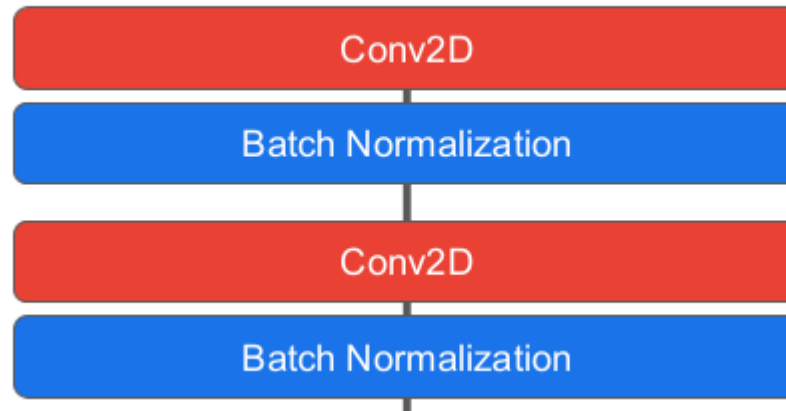
# Terminology

**Mu** → if we looked at the distribution, we notice that at the middle of the curve there is a function named  $\mu(y)$ , since it's at the middle exactly, → **Mu** → mean value of the curve

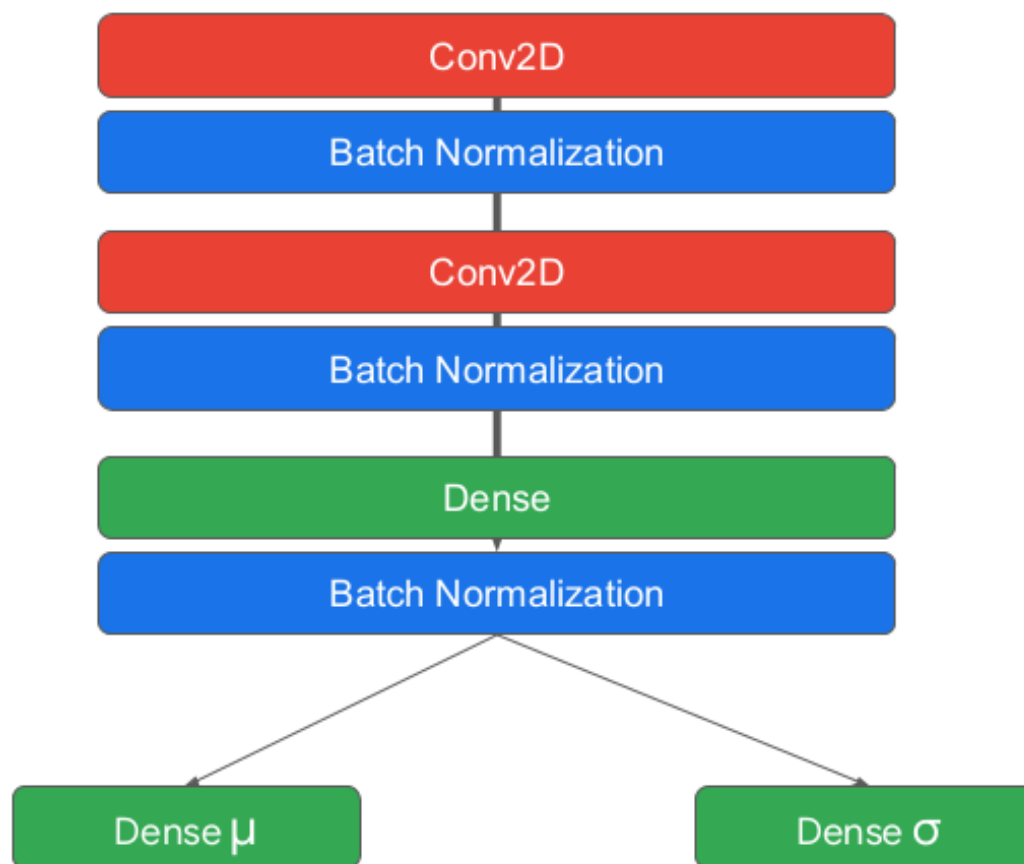
**Sigma**(y) → if we looked to the curve slopping up and down, taking a slope of a deviating curve, therefore it's known as the standard deviation of the curve

# Encoder

**No maxpooling here why ?**



# Full encoder architecture



# Important notes

**The encoder function here**

**Must take 2 parameters ( input shape and latent dimension )**

**Recall latent\_dimension is the sigma and Mu**

**must return the following**

**Mu, Sigma and the flattened batch shape of the last conv2d layer ( no maxpooling return)**

# Latent layer

## Sampling layer ( $\mu$ and $\sigma$ )

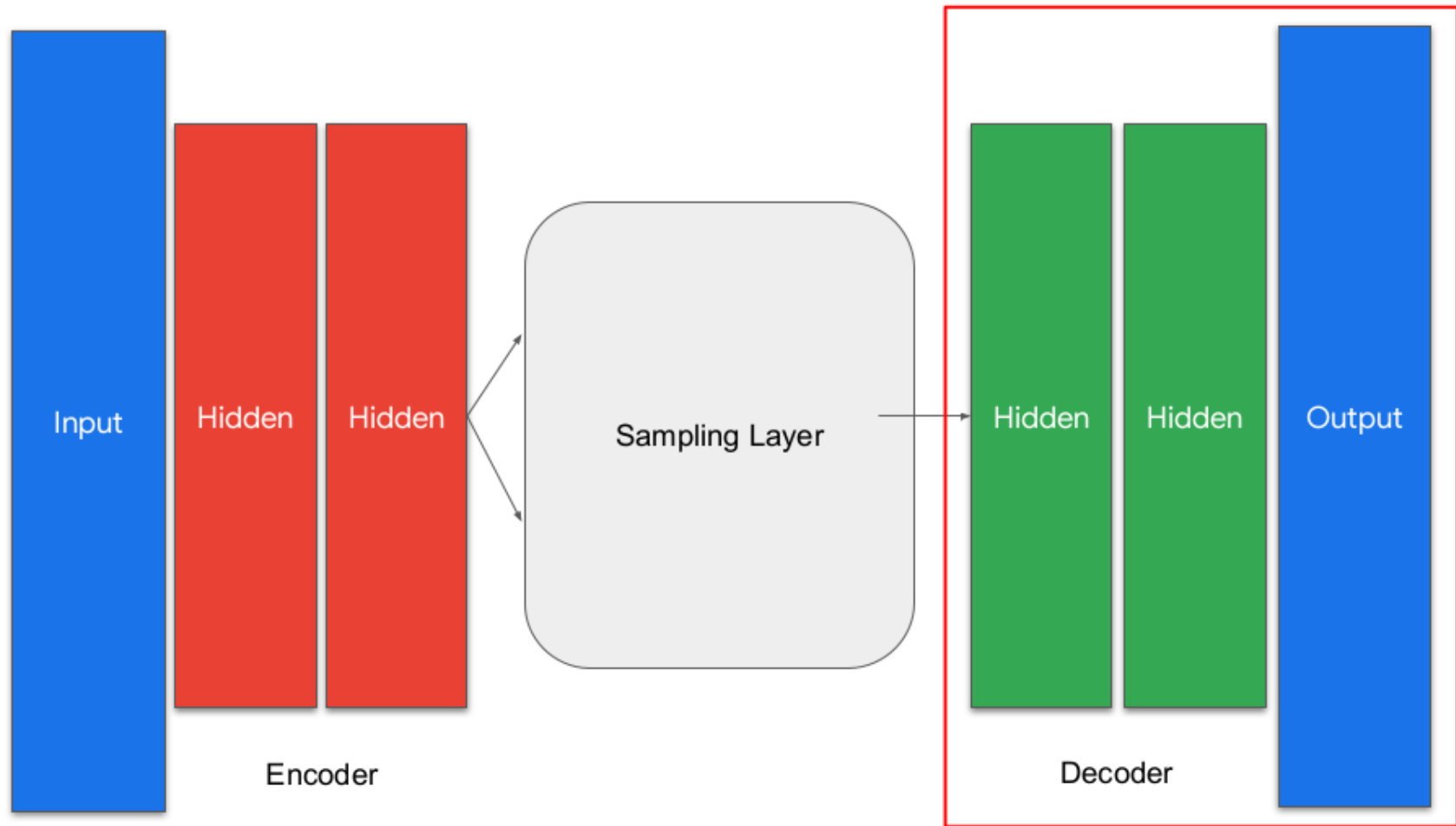
**1<sup>st</sup> output of the encoder  $\rightarrow \mu$  and  $\sigma$**

**2<sup>nd</sup> get the size and dimensions of the batch**

**3<sup>rd</sup> generate a random tensor ( generated from  $\mu$  and  $\sigma$  , using gaussian distribution)**

**4<sup>th</sup> combine the inputs and noise**

# Decoder



# Decoder

**Traditional decoder except it uses conv2D transpose in its layers**

# Loss Kullback leiber loss

## Kullback Leibler divergence

- $P$  = true distribution;
- $Q$  = alternative distribution that is used to encode data
- KL divergence is the expected extra message length per datum that must be transmitted using  $Q$

$$\begin{aligned} D_{KL}(P \parallel Q) &= \sum_i P(x_i) \log (P(x_i)/Q(x_i)) \\ &= \sum_i P(x_i) \log P(x_i) - \sum_i P(x_i) \log Q(x_i) \\ &= H(P, Q) - H(P) \\ &= \text{Cross-entropy} - \text{entropy} \end{aligned}$$

- Measures how different the two distributions are



## To simplify KLD

**$-1/2 * \text{mean of } (1 + \sigma - (\mu)^2 - \exp(\sigma))$**