

Parallel Backtracking Method: Classic backtracking approach

1. Identify an empty cell
2. Try each digit (1-9) that can legally be placed
3. For each valid digit, recursively solve the resulting board.
4. Continue until all cells are filled or no valid moves remain

OpenMP Tasks in Practice

- After entering a parallel region, I used a `#pragma omp single` to start backtracking in just one thread
- Inside the backtracking function, each valid digit triggers a new task. This allows multiple branches of the solution space to be processed simultaneously on multi-core CPUs.
- `Taskwait` ensures that the parent function waits for all sub-branches to complete at the current level before moving on

Shared State and Synchronization

- I used a global flag (`solutionFound`) to indicate when a valid solution was discovered. Once it is set, other tasks can return early, saving time.
- To prevent data races when setting the solution, I used a critical section to ensure that only one task writes the final solution at a time.

Local Board Copies

- Each parallel branch needs its own copy of the board. This avoids the complexity of locking. Instead, each task effectively explores its own partial solution without overwriting another's changes.

Benefits and Overheads

- Benefit: When the puzzle is difficult or the search space is large, parallel tasks significantly reduce total solve time by distributing work
- Overhead: The cost of task creation for smaller puzzles can offset the gain.