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#### Data structures

#### Fenwick tree

```
template<typename T> struct fenwick tree {
      /* can convert it to map, build what you need only
       * will be: memory O(q*logn) ,time O(logn*logn) */
      vector<T> BIT;
      int n;
      fenwick_tree(int n) : n(n), BIT(n + 1) {}
      T getAccum(int idx) {
            T sum = 0;
            while (idx) {
                  sum += BIT[idx];
                  idx -= (idx \& -idx);
            return sum;
      }
      void add(int idx, T val) {
            assert(idx != 0);
            while (idx <= n) {</pre>
                  BIT[idx] += val;
                  idx += (idx \& -idx);
            }
      }
      T getValue(int idx) {
            return getAccum(idx) - getAccum(idx - 1);
      // ordered statistics tree // get index that has value >= accum
      // values must by positive
      int getIdx(T accum) {
            int start = 1, end = n, rt = -1;
            while (start <= end) {</pre>
                  int mid = start + end >> 1;
                  T val = getAccum(mid);
                  if (val >= accum)
                         rt = mid, end = mid - 1;
                  else start = mid + 1;
            return rt;
      //not tested (from topcoder)
      //first index less than or equal accum O(logn) (same as getIdx)
      int find(T accum) {
            int i = 1, idx = 0;
            while ((1 << i) <= n) i <<= 1;
            for (; i > 0; i >>= 1) {
                  int tidx = idx + i;
                  if (tidx > n) continue;
                  if (accum >= BIT[tidx]) {
                         idx = tidx; accum -= BIT[tidx];
                  }
            return idx;
      }
};
```

#### Fenwick tree 2d

```
template<typename T>
struct fenwick_tree_2d {
#define Lbit(x) (x\&-x)
      int n, m;
      vector<vector<T>> BIT;
      fenwick_tree_2d(int n, int m) :
            n(n), m(m), BIT(n + 1, vector < T > (m + 1)) {
      }
      T getAccum(int i, int j) {
            T sum = 0;
            for (; i; i -= Lbit(i))
                  for (int idx = j; idx > 0; idx -= Lbit(idx))
                        sum += BIT[i][idx];
            return sum;
      void add(int i, int j, int val) {
            assert(i != 0 && j != 0);
            for (; i <= n; i += Lbit(i))
                  for (int idx = j; idx <= m; idx += Lbit(idx))</pre>
                        BIT[i][idx] += val;
      }
      T getRectangeSum(int x1, int y1, int x2, int y2) {
            if (y1 > y2)
                  swap(y1, y2);
            if (x1 > x2)
                  swap(x1, x2);
            return getAccum(x2, y2) - getAccum(x1 - 1, y2) - getAccum(x2, y1 - 1)
                  + getAccum(x1 - 1, y1 - 1);
      }
};
```

```
Fenwick tree update range
/*
x[i] = a[i] - a[i-1] //a is original array
 y[i] = x[i]*(i-1)
 sum(1,3) = a[1] + a[2] + a[3] = (x[1]) + (x[2] + x[1]) + (x[3] + x[2] + x[1])
 = 3*(x[1] + x[2] + x[3]) - 0*x[1] - 1*x[2] - 2*x[3] //same equation but more complex
 = sumX(1,3) * 3 - sumY(1,3)
 so sum(1,n) = sumX(1,n)*n - sumY(1,n)
 update:
 x[1] += val, x[r+1] -= val
 y[1] += val *(1-1), y[r+1] -= r*val
 */
template<typename T>
class fenwick_tree {
      int n;
      vector<T> x, y;
      T getAccum(vector<T>& BIT, int idx) {
            T sum = 0;
            while (idx) {
                  sum += BIT[idx];
                  idx -= (idx \& -idx);
            return sum;
      }
      void add(vector<T>& BIT, int idx, T val) {
            assert(idx != 0);
            while (idx <= n) {</pre>
                  BIT[idx] += val;
                  idx += (idx \& -idx);
            }
      }
      T prefix_sum(int idx) {
            return getAccum(x, idx) * idx - getAccum(y, idx);
      }
public:
      fenwick tree(int n) :
            n(n), x(n + 1), y(n + 1) {
      void update_range(int 1, int r, T val) {
            add(x, 1, val);
```

}

}

add(x, r + 1, -val); add(y, l, val \* (l - 1)); add(y, r + 1, -val \* r);

return prefix\_sum(r) - prefix\_sum(1 - 1);

T range sum(int 1, int r) {

# Segment tree for efficient memory (2\*n) #define LEFT (idx+1) #define MID ((start+end)>>1) #define RIGHT (idx+((MID-start+1)<<1))</pre> \*/ template<typename T> class segment\_tree {//1-based #define LEFT (idx<<1)</pre> #define RIGHT (idx<<1|1)</pre> #define MID ((start+end)>>1) int n; vector<T> tree, lazy; T merge(const T& left, const T& right) {} inline void pushdown(int idx, int start, int end) { if (lazy[idx] == 0) return; //update tree[idx] with lazy[idx] tree[idx] += lazy[idx]; if (start != end) { lazy[LEFT] += lazy[idx]; lazy[RIGHT] += lazy[idx]; lazy[idx] = 0; //clear lazy inline void pushup(int idx) { tree[idx] = merge(tree[LEFT], tree[RIGHT]); } void build(int idx, int start, int end) { if (start == end) return; build(LEFT, start, MID); build(RIGHT, MID + 1, end); pushup(idx); void build(int idx, int start, int end, const vector<T>& arr) { if (start == end) { tree[idx] = arr[start]; return; build(LEFT, start, MID, arr); build(RIGHT, MID + 1, end, arr); pushup(idx); T query(int idx, int start, int end, int from, int to) { pushdown(idx, start, end); if (from <= start && end <= to)</pre> return tree[idx]; if (to <= MID)</pre> return query(LEFT, start, MID, from, to); if (MID < from)</pre> return query(RIGHT, MID + 1, end, from, to); return merge(query(LEFT, start, MID, from, to), query(RIGHT, MID + 1, end, from, to));

}

```
void update(int idx, int start, int end, int lq, int rq, const T& val) {
             pushdown(idx, start, end);
             if (rq < start || end < lq)</pre>
                   return;
             if (lq <= start && end <= rq) {</pre>
                   lazy[idx] += val;//update lazy
                   pushdown(idx, start, end);
                   return;
             update(LEFT, start, MID, lq, rq, val);
             update(RIGHT, MID + 1, end, lq, rq, val);
             pushup(idx);
public:
      segment_tree(int n) :n(n), tree(n << 2), lazy(n << 2) \{\}
      segment_tree(const vector<T>& v) {
             n = v.size() - 1;
             tree = vector\langle T \rangle(n \langle \langle 2 \rangle;
             lazy = vector\langle T \rangle(n \langle < 2 \rangle;
             build(1, 1, n, v);
      }
      T query(int 1, int r) {
             return query(1, 1, n, 1, r);
      void update(int 1, int r, const T& val) {
             update(1, 1, n, l, r, val);
      }
#undef LEFT
#undef RIGHT
#undef MID
};
Max sum range node
struct MSR Node {
      11 left, right, mid, sum;
      MSR_Node(const 11& val) {//be careful from the empty subarray
             left = right = mid = sum = val;
      MSR Node(const MSR Node& a, const MSR Node& b) {
             left = max(a.left, a.sum + b.left);
             right = max(b.right, b.sum + a.right);
             mid = max({ a.mid, b.mid, a.right + b.left });
             sum = a.sum + b.sum;
      11 getMax() {
             return max({ left, right, mid, sum });
      }
};
```

```
Extended Segment tree
struct segtree {
      segtree *left = nullptr, *right = nullptr;
      int mx = 0;
      segtree(int val = 0) :
                  mx(val) {
      }
      void extend() {
            if (left == nullptr) {
                  left = new segtree();
                  right = new segtree();
            }
      }
      void pushup() {
            mx = max(left->mx, right->mx);
      ~segment_tree() {
            if (left == nullptr)return;
            delete left;
            delete right;
      }
};
class extend segment tree {
#define MID ((start+end)>>1)
      void update(segtree *root, int start, int end, int pos, int val) {
            if (pos < start | end < pos)</pre>
                  return;
            if (start == end) {
                  root->mx = max(root->mx, val);
                  return;
            }
            root->extend();
            update(root->left, start, MID, pos, val);
            update(root->right, MID + 1, end, pos, val);
            root->pushup();
      }
      int query(segtree *root, int start, int end, int 1, int r) {
            if (root == nullptr || r < start || end < 1)</pre>
                  return 0;
            if (1 <= start && end <= r)</pre>
                  return root->mx;
            return max(query(root->left, start, MID, 1, r),
                         query(root->right, MID + 1, end, 1, r));
public:
      int start, end;
      segtree *root;
      extened_segment_tree() {
      ~extened_segment_tree() {
            delete root;
      extened_segment_tree(int start, int end) : start(start), end(end) {
            root = new segtree();
      }
```

```
void update(int pos, int val) {
            update(root, start, end, pos, val);
      }
      int query(int 1, int r) {
            return query(root, start, end, 1, r);
      }
#undef MID
};
Persistent segment tree
struct segtree {
    static segtree *sentinel;
    segtree *left, *right;
    bool dirty = false;
    11 \text{ sum} = 0, \text{ lazy} = 0;
    segtree(ll val = 0) : sum(val) {
        left = right = this;
    }
    segtree(segtree *left, segtree *right) : left(left), right(right) {
        sum = left->sum + right->sum;
    }
};
segtree *segtree::sentinel = new segtree();
class persistent_segment_tree {
#define MID ((start+end)>>1)
    segtree* apply(segtree *root, int start, int end, ll val) {
        segtree *rt = new segtree(*root);
        rt->dirty = true;
        rt->sum += (end - start + 1) * val;
        rt->lazy += val;
        return rt;
    }
    void pushdown(segtree *root, int start, int end) {
        if (root->dirty == false || start == end)
            return:
        root->left = apply(root->left, start, MID, root->lazy);
        root->right = apply(root->right, MID + 1, end, root->lazy);
        root->lazy = 0;
        root->dirty = 0;
    }
    segtree* build(int start, int end, const vector<int> &v) {
        if (start == end)
            return new segtree(v[start]);
        return new segtree(build(start, MID, v), build(MID + 1, end, v));
    }
    segtree* Set(segtree *root, int start, int end, int pos, ll new_val) {
        pushdown(root, start, end);
        if (pos < start || end < pos)</pre>
            return root;
        if (pos <= start && end <= pos)</pre>
            return new segtree(new_val);
        return new segtree(Set(root->left, start, MID, pos, new_val),
                Set(root->right, MID + 1, end, pos, new val));
    }
```

```
segtree* update(segtree *root, int start, int end, int 1, int r, 11 val) {
        pushdown(root, start, end);
        if (r < start || end < 1)
            return root;
        if (1 <= start && end <= r)</pre>
            return apply(root, start, end, val);
        return new segtree(update(root->left, start, MID, 1, r, val),
                update(root->right, MID + 1, end, 1, r, val));
    }
    11 query(segtree *root, int start, int end, int 1, int r) {
        pushdown(root, start, end);
        if (r < start || end < 1)
            return 0;
        if (1 <= start && end <= r)
            return root->sum;
        return query(root->left, start, MID, 1, r)
                + query(root->right, MID + 1, end, 1, r);
public:
    int start, end;
    vector<segtree*> versions;
    persistent_segment_tree(int start, int end) :
            start(start), end(end) {
        versions.push back(segtree::sentinel);
    }
    persistent_segment_tree(const vector<int> &v) :
            start(0), end(v.size() - 1) {
        versions.push_back(build(start, end, v));
    }
    void update(int 1, int r, 11 val) {
        versions.push back(update(versions.back(), start, end, 1, r, val));
    }
    11 query(int time, int 1, int r) {
        return query(versions[time], start, end, 1, r);
    }
#undef MID
};
Ordered set
#include<bits/stdc++.h>
#include<ext/pb ds/assoc container.hpp>
#include<ext/pb_ds/tree_policy.hpp>
using namespace std;
using namespace __gnu_pbds;
template<typename key>
using ordered_set = tree<key, null_type, less<key>, rb_tree_tag,
tree_order_statistics_node_update>;
/*
 find_by_order(k) :
 It returns to an iterator to the k-th element (counting from zero) in the set in O(logn)
time.
 To find the first element k must be zero.
 order of key(k):
 It returns to the number of items that are strictly smaller than our item k in O(logn)
time. */
```

## **Quad Tree**

```
//set NIL with defult value
template<typename T>
struct node {
    node<T> *child[4];
    T val;
    node(T val = NIL) : val(val) {
        memset(child, 0, sizeof child);
    void push_up() {//merge the 4 childs
        val = NIL;
        for (int i = 0; i < 4; i++)
            if (child[i] != nullptr) {}
    }
    ~node() {
        for (int i = 0; i < 4; i++)
            if (child[i] != nullptr)
                delete child[i];
    }
};
template<typename T>
void update(node<T> *&root, int r1, int r2, int c1, int c2, int x, int y, T val) {
    if (x < r1 || x > r2 || y < c1 || y > c2)
        return;
    if (root == nullptr)
        root = new node<T>();
    if (r1 == r2 && c1 == c2) {
        //update
        return;
    int rmid = (r1 + r2) / 2, cmid = (c1 + c2) / 2;
    update(root->child[0], r1, rmid, c1, cmid, x, y, val);
    update(root->child[1], r1, rmid, cmid + 1, c2, x, y, val);
    update(root->child[2], rmid + 1, r2, c1, cmid, x, y, val);
    update(root->child[3], rmid + 1, r2, cmid + 1, c2, x, y, val);
    root->push up();
}
template<typename T>
T query(node<T> *root, int r1, int r2, int c1, int c2, int x, int y) {
    if (root == nullptr || x < r1 || x > r2 || y < c1 || y > c2)
        return NIL;
    if (r1 == r2 \&\& c1 == c2)
        return root->val;
    int rmid = (r1 + r2) / 2, cmid = (c1 + c2) / 2;
    query(root->child[0], r1, rmid, c1, cmid, x, y);
    query(root->child[1], r1, rmid, cmid + 1, c2, x, y);
    query(root->child[2], rmid + 1, r2, c1, cmid, x, y);
    query(root->child[3], rmid + 1, r2, cmid + 1, c2, x, y);
}
node<T> *seg = new node<T>();
```

## Sparse table

```
template<typename T>
struct sparse_table {
      vector<vector<T>> sparseTable;
      using F = function<T(T, T)>;
      F merge;
      static int LOG2(int x) { //floor(log2(x))
            return 31 - __builtin_clz(x);
      }
      sparse table(vector<T>& v, F merge) :
            merge(merge) {
            int n = v.size();
            int logN = LOG2(n);
            sparseTable = vector<vector<T>>(logN + 1);
            sparseTable[0] = v;
            for (int k = 1, len = 1; k <= logN; k++, len <<= 1) {
                  sparseTable[k].resize(n);
                  for (int i = 0; i + len < n; i++)
                         sparseTable[k][i] = merge(sparseTable[k - 1][i],
                               sparseTable[k - 1][i + len]);
            }
      }
      T query(int 1, int r) {
            int k = LOG2(r - l + 1); // max k ==> 2^k <= length of range
            //check first 2<sup>k</sup> from left and last 2<sup>k</sup> from right //overlap
            return merge(sparseTable[k][1], sparseTable[k][r - (1 << k) + 1]);</pre>
      }
      T query shifting(int 1, int r) {
            T res;
            bool first = true;
            for (int i = (int)sparseTable.size() - 1; i >= 0; i--)
                  if (1 + (1 << i) - 1 <= r) {</pre>
                         if (first)
                               res = sparseTable[i][1];
                         else
                               res = merge(res, sparseTable[i][1]);
                         first = false;
                         1 += (1 << i);
            return res;
      }
};
```

## **SQRT Decomposition**

```
//zero based SQRT Decomposition with lazy propagation
template<typename update_type, typename query_type>
class SQRT Decomposition {
      struct Bucket {
            int 1, r;
            update_type lazy;
            Bucket(int l, int r) : l(l), r(r) {
                  //set default value to lazy
                  //build bucket for the first time
            void build() {
                  //update all bucket with lazy if have
                  //rebuild the bucket
                  //clear lazy
            //update all bucket
            //just update lazy
            void update(const update_type& val) {}
            //update range in bucket
            void update(int start, int end, const update_type& val) {
                  if (start == 1 && end == r) {
                        update(val);
                        return;
                  }
                  //update bucket
                  //rebuild the bucket if need
            //query about all bucket
            //calc with lazy
            query_type query() {}
            //query about range in bucket
            query_type query(int start, int end) {
                  if (start == 1 && end == r)
                        return query();
                  //push lazy if have
                  //calc
            }
      };
      int n, sqrtN;
      vector<Bucket> bucket;
      int begin(int idx) {
            return idx * sqrtN;
      }
      int end(int idx) {
            return min(sqrtN * (idx + 1), n) - 1;
      int which_block(int idx) {
            return idx / sqrtN;
      }
```

```
public:
      SQRT_Decomposition(int n) {
            this->n = n;
            sqrtN = sqrt(n);
            for (int i = 0; i < n; i += sqrtN)</pre>
                  bucket.push back(Bucket(i, min(i + sqrtN, n) - 1));
      }
      void update(int left, int right, update_type val) {
            int st = which block(left), ed = which block(right);
            bucket[st].update(left, min(bucket[st].r, right), val);
            for (int i = st + 1; i < ed; i++)
                  bucket[i].update(val);
            if (st != ed) bucket[ed].update(bucket[ed].l, right, val);
      }
      query_type query(int left, int right) {
            int st = which_block(left), ed = which_block(right);
            query type rt = bucket[st].query(left, min(bucket[st].r, right));
            for (int i = st + 1; i < ed; i++)
                  rt += bucket[i].query();
            if (st != ed) rt += bucket[ed].query(bucket[ed].1, right);
            return rt;
      }
};
Treap
Implicit Treap
enum DIR { L, R };
template<typename T> struct cartesian tree {
      static cartesian_tree<T>* sentinel;
      T \text{ key} = T();
      int priority = 0, size = 0, reverse = false;
      cartesian_tree* child[2];
      cartesian tree() {
            child[L] = child[R] = this;
      }
      cartesian_tree(const T& x, int y) : key(x), priority(y) {
            size = 1;
            child[L] = child[R] = sentinel;
      }
      void push_down() {
            if (!reverse) return;
            reverse = 0;
            child[L]->doRevese();
            child[R]->doRevese();
      void doReverse() {
            reverse ^= 1;
            swap(child[L], child[R]);
      void push up() {
            size = child[L]->size + child[R]->size + 1;
      }
};
```

```
template<typename T>
cartesian tree<T>* cartesian tree<T>::sentinel = new cartesian tree<T>();
template<typename T, template<typename > class cartesian tree>
class implicit_treap { //1 based
      typedef cartesian_tree<T> node;
      typedef cartesian tree<T>* nodeptr;
#define emptyNode cartesian tree<T>::sentinel
      nodeptr root;
      void split(nodeptr root, nodeptr& 1, nodeptr& r, int firstXElment) {
            if (root == emptyNode) {
                  1 = r = emptyNode;
                  return;
            }
            root->push_down();
            if (firstXElment <= root->child[L]->size) {
                  split(root->child[L], 1, root->child[L], firstXElment);
                  r = root;
            }
            else {
                  split(root->child[R], root->child[R], r,
                        firstXElment - root->child[L]->size - 1);
                  1 = root;
            }
            root->push up();
      }
      nodeptr merge(nodeptr 1, nodeptr r) {
            1->push down();
            r->push down();
            if (1 == emptyNode | | r == emptyNode)
                  return (1 == emptyNode ? r : 1);
            if (1->priority > r->priority) {
                  1->child[R] = merge(1->child[R], r);
                  1->push_up();
                  return 1;
            r->child[L] = merge(1, r->child[L]);
            r->push_up();
            return r;
      }
      vector<nodeptr> split_range(int s, int e) { // [x<s,s<=x<=e,e<x]</pre>
            nodeptr 1, m, r, tmp;
            split(root, 1, tmp, s - 1);
            split(tmp, m, r, e - s + 1);
            return { 1,m,r };
      }
public:
      implicit_treap() : root(emptyNode) {}
      int size() {
            return root->size;
      }
```

```
void insert(int pos, const T& key) {
            nodeptr tmp = new node(key, rand());
            nodeptr 1, r;
            split(root, l, r, pos - 1);
            root = merge(merge(1, tmp), r);
      }
      void push back(const T& value) {
            root = merge(root, new node(value, rand()));
      }
      T getByIndex(int pos) {
            vector<nodeptr> tmp = split_range(pos, pos);
            nodeptr 1 = tmp[0], m = tmp[1], r = tmp[2];
            T rt = m->key;
            root = merge(merge(1, m), r);
            return rt;
      }
      void erase(int pos) {
            vector<nodeptr> tmp = split_range(pos, pos);
            nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
            delete m;
            root = merge(1, r);
      void cyclic_shift(int s, int e) { //to the right
            vector<nodeptr> tmp = split range(s, e);
            nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
            nodeptr first, second;
            split(m, first, second, e - s);
            root = merge(merge(merge(1, second), first), r);
      }
      void reverse range(int s, int e) {
            vector<nodeptr> tmp = split_range(s, e);
            nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
            m->reverse ^= 1;
            root = merge(merge(1, m), r);
      }
      node range_query(int s, int e) {
            vector<nodeptr> tmp = split range(s, e);
            nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
            node rt = *m;
            root = merge(merge(1, m), r);
            return rt;
      }
Ordered multiset
enum DIR { L, R };
template<typename T>
struct cartesian tree {
      static cartesian_tree<T>* sentinel;
      T \text{ key} = T();
      int priority = 0, frequency = 0, size = 0;
      cartesian_tree* child[2];
      cartesian tree() {
            child[L] = child[R] = this;
      }
```

```
cartesian tree(const T& x, int y) : key(x), priority(y) {
            size = frequency = 1;
            child[L] = child[R] = sentinel;
      void push_down() {
      void push_up() {
            size = child[L]->size + child[R]->size + frequency;
};
template<typename T> //be
cartesian tree<T>* cartesian tree<T>::sentinel = new cartesian tree<T>();
template<typename T>
void split(cartesian_tree<T>* root, T key, cartesian_tree<T>*& 1,
      cartesian_tree<T>*& r) {
      if (root == cartesian tree<T>::sentinel) {
            1 = r = cartesian tree<T>::sentinel;
            return;
      }
      root->push down();
      if (root->key <= key) {</pre>
            split(root->child[R], key, root->child[R], r);
            1 = root;
      }
      else {
            split(root->child[L], key, 1, root->child[L]);
            r = root;
      root->push up();
}
template<typename T>
cartesian tree<T>* merge(cartesian tree<T>* 1, cartesian tree<T>* r) {
      1->push down();
      r->push down();
      if (1 == cartesian tree<T>::sentinel || r == cartesian tree<T>::sentinel)
            return (1 == cartesian_tree<T>::sentinel ? r : 1);
      if (1->priority > r->priority) {
            1->child[R] = merge(1->child[R], r);
            1->push_up();
            return 1:
      r->child[L] = merge(1, r->child[L]);
      r->push up();
      return r;
}
template<typename T, template<typename > class cartesian tree>
class treap {
      typedef cartesian_tree<T> node;
      typedef node* nodeptr;
#define emptyNode node::sentinel
      nodeptr root;
```

```
void insert(nodeptr& root, nodeptr it) {
      if (root == emptyNode) {
            root = it;
      else if (it->priority > root->priority) {
            split(root, it->key, it->child[L], it->child[R]);
            root = it;
      }
      else
            insert(root->child[root->key < it->key], it);
      root->push_up();
bool increment(nodeptr root, const T& key) {
      if (root == emptyNode)
            return 0;
      if (root->key == key) {
            root->frequency++;
            root->push_up();
            return root;
      }
      bool rt = increment(root->child[root->key < key], key);</pre>
      root->push_up();
      return rt;
}
nodeptr find(nodeptr root, const T& key) {
      if (root == emptyNode || root->key == key)
            return root;
      return find(root->child[root->key < key], key);</pre>
void erase(nodeptr& root, const T& key) {
      if (root == emptyNode)
            return;
      if (root->key == key) {
            if (--(root->frequency) == 0)
                  root = merge(root->child[L], root->child[R]);
      }
      else
            erase(root->child[root->key < key], key);</pre>
      root->push_up();
}
T kth(nodeptr root, int k) {
      if (root->child[L]->size >= k)
            return kth(root->child[L], k);
      k -= root->child[L]->size;
      if (k <= root->frequency)
            return root->key;
      return kth(root->child[R], k - root->frequency);
}
```

```
int order_of_key(nodeptr root, const T& key) {
            if (root == emptyNode)
                  return 0;
            if (key < root->key)
                  return order_of_key(root->child[L], key);
            if (key == root->key)
                  return root->child[L]->size;
            return root->child[L]->size + root->frequency
                  + order_of_key(root->child[R], key);
      }
public:
      treap() : root(emptyNode) {}
      void insert(const T& x) {
            if (increment(root, x)) //change it to find(x) to make it as a set
                  return;
            insert(root, new node(x, rand()));
      void erase(const T& x) {
            erase(root, x);
      bool find(const T& x) {
            return (find(root, x) != emptyNode);
      int get_kth_number(int k) {
            assert(1 <= k && k <= size());
            return kth(root, k);
      int order_of_key(const T& x) {
            return order_of_key(root, x);
      }
      int size() {
            return root->size;
      }
};
Big Integer
class BigInt {
private:
#define CUR (*this)
    const int BASE = 1000000000;//1e9
    vector<int> v;
public:
    BigInt(const long long &val = 0) {
        CUR = val;
    }
    BigInt(const string &val) {
        CUR = val;
    }
    int size() const {
        return v.size();
    bool zero() const {
        return v.empty();
    }
```

```
BigInt& operator =(long long val) {
   v.clear();
   while (val) {
       v.push_back(val % BASE);
       val /= BASE;
   }
   return CUR;
BigInt& operator =(const BigInt &a) {
   v = a.v;
   return CUR;
BigInt& operator=(const string &s) {
   CUR = 0;
   for (const char &ch : s)
       CUR = CUR * 10 + (ch - '0');
   return CUR;
bool operator <(const BigInt &a) const {</pre>
   if (a.size() != size())
       return size() < a.size();</pre>
   for (int i = size() - 1; i >= 0; i--) {
       if (v[i] != a.v[i])
           return v[i] < a.v[i];</pre>
   return false;
}
BigInt operator +(const BigInt &a) const {
   BigInt res = CUR;
   int idx = 0, carry = 0;
   while (idx < a.size() || carry) {</pre>
       if (idx < a.size())</pre>
           carry += a.v[idx];
       if (idx == res.size())
           res.v.push_back(0);
       res.v[idx] += carry;
       carry = res.v[idx] / BASE;
       res.v[idx] %= BASE;
       idx++;
   }
   return res;
BigInt& operator +=(const BigInt &a) {
   CUR = CUR + a;
   return CUR;
}
```

```
BigInt operator *(const BigInt &a) const {
       BigInt res;
       if (CUR.zero() || a.zero())
          return res;
       res.v.resize(size() + a.size());
       for (int i = 0; i < size(); i++) {
          if (v[i] == 0)
              continue;
          long long carry = 0;
          for (int j = 0; carry || j < a.size(); j++) {</pre>
              carry += 1LL * v[i] * (j < a.size() ? a.v[j] : 0);
              while (i + j >= res.size())
                 res.v.push_back(0);
              carry += res.v[i + j];
              res.v[i + j] = carry % BASE;
              carry /= BASE;
          }
       }
       while (!res.v.empty() && res.v.back() == 0)
          res.v.pop_back();
       return res;
   BigInt& operator *=(const BigInt &a) {
       CUR = CUR * a;
       return CUR;
   BigInt& operator /=(const int &a) {
       11 \text{ carry } = 0;
       for (int i = (int) v.size() - 1; i >= 0; i--) {
          ll cur = v[i] + carry * BASE;
          v[i] = cur / a;
          carry = cur % a;
       while (!v.empty() && v.back() == 0)
          v.pop back();
       return CUR;
   }
   friend ostream& operator<<(ostream &out, const BigInt &a) {</pre>
       out << (a.zero() ? 0 : a.v.back());
       for (int i = (int) a.v.size() - 2; i >= 0; i--)
          out << setfill('0') << setw(9) << a.v[i];
       return out;
#undef CUR
```

### **Mod int**

```
struct modint {
#define CUR (*this)
      static const int MOD = 1e9 + 7;
      int val;
      modint(const long long& a = 0) {
            val = a \% MOD;
            if (val < 0) val += MOD;</pre>
      }
      modint& operator+=(const modint& a) {
            if ((val += a.val) >= MOD) val -= MOD;
            return CUR;
      }
      modint operator+(const modint& a) const {
            modint c = CUR;
            c += a;
            return c;
      modint& operator-=(const modint& a) {
            if ((val -= a.val) < 0) val += MOD;</pre>
            return CUR;
      }
      modint operator-(const modint& a) const {
            modint c = CUR;
            c -= a;
            return c;
      }
      modint operator*(const modint& a) const {
            return modint((1LL * this->val * a.val) % MOD);
      }
      modint& operator*=(const modint& a) {
            CUR = CUR * a;
            return CUR;
      modint operator/(const modint& a) {
            return CUR * power(a, MOD - 2);
      modint& operator/=(const modint& a) {
            CUR = CUR / a;
            return CUR;
      }
      static modint power(modint x, long long y) {
            modint res = 1;
            while (y > 0) {
                  if (y & 1) res *= x;
                  x *= x; y >>= 1;
            return res;
      friend ostream& operator<<(ostream& out, const modint& a) {</pre>
            out << a.val;
            return out;
#undef CUR
};
```

## Graph

## **Graph Data structures**

```
DSU
struct DSU {
      vector<int> rank, parent, size;
      vector<vector<int>> component;
      int forsets;
      DSU(int n) {
            size = rank = parent = vector<int>(n + 1, 1);
            component = vector<vector<int>>(n + 1);
            forsets = n;
            for (int i = 0; i <= n; i++) {
                  parent[i] = i;
                  component[i].push_back(i);
            }
      }
      int find_set(int v) {
            if (v == parent[v])
                  return v;
            return parent[v] = find_set(parent[v]);
      }
      void link(int par, int node) {
            parent[node] = par;
            size[par] += size[node];
            for (const int& it : component[node])
                  component[par].push_back(it);
            component[node].clear();
            if (rank[par] == rank[node])
                  rank[par]++;
            forsets--;
      }
      bool union_sets(int v, int u) {
            v = find_set(v), u = find_set(u);
            if (v != u) {
                  if (rank[v] < rank[u])</pre>
                        swap(v, u);
                  link(v, u);
            return v != u;
      bool same_set(int v, int u) {
            return find_set(v) == find_set(u);
      int size set(int v) {
            return size[find_set(v)];
      }
};
DSU bipartiteness
struct DSU_bipartiteness {
      vector<int> bipartite, rank;
      vector<pair<int, int>> parent;
```

```
DSU_bipartiteness(int n) {
            bipartite = rank = vector<int>(n + 1, 1);
            parent = vector<pair<int, int>>(n + 1);
            for (int i = 0; i <= n; i++)
                  parent[i] = { i, 0 };
      }
      pair<int, int> find_set(int x) {
            if (x == parent[x].first)
                  return parent[x];
            int parity = parent[x].second;
            parent[x] = find set(parent[x].first);
            parent[x].second ^= parity;
            return parent[x];
      }
      void union_sets(int x, int y) {
            pair<int, int> p = find_set(x);
            x = p.first;
            int paX = p.second;
            p = find_set(y);
            y = p.first;
            int paY = p.second;
            if (x == y) {
                  if (paX == paY)
                        bipartite[x] = false;
            }
            else {
                  if (rank[x] < rank[y])</pre>
                        swap(x, y);
                  parent[y] = { x, paX ^ paY ^ 1 };
                  bipartite[x] &= bipartite[y];
                  if (rank[x] == rank[y])
                        rank[x]++;
            }
      }
      bool is_bipartite(int x) {
            return bipartite[find_set(x).first];
      }
};
DSU rollback
struct dsu_save {
    int v, rnkv, u, rnku;
    dsu_save() {}
    dsu save(int v, int rnkv, int u, int rnku)
        : v(_v), rnkv(_rnkv), u(_u), rnku(_rnku) {}
};
struct dsu_with_rollbacks {
    vector<int> p, rnk;
    int comps;
    stack<dsu_save> op;
```

```
dsu_with_rollbacks() {}
dsu with rollbacks(int n) {
    p.resize(n + 1);
    rnk.resize(n + 1);
    for (int i = 1; i <= n; i++) {
        p[i] = i;
        rnk[i] = 0;
    }
    comps = n;
}
int find_set(int v) {
    return (v == p[v]) ? v : find_set(p[v]);
}
bool same_group(int v, int u) {
    v = find_set(v);
    u = find_set(u);
    if (v == u)
        return false;
    comps--;
    if (rnk[v] > rnk[u])
        swap(v, u);
    op.push(dsu_save(v, rnk[v], u, rnk[u]));
    p[v] = u;
    if (rnk[u] == rnk[v])
        rnk[u]++;
    return true;
void snapshot() {
    // this function save the current trees (merged) and don't rollback them any more
    while (!op.empty())
        op.pop();
void rollback() {
    // you can erase the while loop if you want to rollback just the last merge
    while (!op.empty()) {
        dsu_save x = op.top();
        op.pop();
        comps++;
        p[x.v] = x.v;
        rnk[x.v] = x.rnkv;
        p[x.u] = x.u;
        rnk[x.u] = x.rnku;
    }
}
```

```
LCA
class LCA {
    int n, logN, root = 1;
    vector<int> depth;
    vector<vector<int>> adj, lca;
    void dfs(int node, int parent) {
        lca[node][0] = parent;
        depth[node] = (~parent ? depth[parent] + 1 : 0);
        for (int k = 1; k <= logN; k++) {
            int up_parent = lca[node][k - 1];
            if (~up parent)
            lca[node][k] = lca[up_parent][k - 1];
        for (int child : adj[node])
            if (child != parent)
            dfs(child, node);
    }
public:
    LCA(const vector<vector<int>> & adj, int root = 1) : root(root), adj(_adj) {
        adj = adj;
        n = adj.size() - 1;
        logN = log2(n);
        lca = vector<vector<int>>(n + 1, vector<int>(logN + 1, -1));
        depth = vector<int>(n + 1);
        dfs(root, -1);
    int get_LCA(int x, int y) {
        if (depth[x] < depth[y])</pre>
            swap(x, y);
        for (int k = logN; k >= 0; k--)
            if (depth[x] - (1 << k) >= depth[y])
                x = lca[x][k];
        if(x == y)
            return x;
        for (int k = logN; k >= 0; k--) {
            if (lca[x][k] != lca[y][k]) {
                x = lca[x][k], y = lca[y][k];
            }
        return lca[x][0];
    }
    int get_distance(int u, int v) {
        return depth[u] + depth[v] - 2 * depth[get_LCA(u, v)];
    int shifting(int node, int dist) {
        for (int i = logN; i >= 0 && ~node; i--)
            if (dist & (1 << i))</pre>
                node = lca[node][i];
        return node;
    }
```

### **Heavy light decomposition**

```
//1-based, if value in node, just update it after build chains
//don't forget to call build chains after add edges.
class heavy light decomposition {
    int n, is value in edge;
    vector<int> parent, depth, heavy, root, pos_in_array, pos_to_node, size;
    const static int merge(int a, int b); //implement it
    struct array_ds { //implement it
        int n;
        array_ds(int n) : n(n) {}
    } seg;
    struct TREE {
        int cnt_edges = 1;
        vector<vector<int>> adj;
        //need for value in edges
        vector<vector<int>> edge_idx;
        //edge to need for undirected tree //end of edge in directed tree
        vector<int> edge_to, edge_cost;
        TREE(int n): adj(n + 1), edge_idx(n + 1), edge_to(n + 1), edge_cost(n + 1) {
        void add_edge(int u, int v, int c) {
            adj[u].push back(v);
            adj[v].push back(u);
            edge_idx[u].push_back(cnt_edges);
            edge_idx[v].push_back(cnt_edges);
            edge_cost[cnt_edges] = c;
            cnt_edges++;
        }
    } tree;
    int dfs_hld(int node) {
        int size = 1, max sub tree = 0;
        for (int i = 0; i < (int) tree.adj[node].size(); i++) {</pre>
            int ch = tree.adj[node][i], edge_idx = tree.edge_idx[node][i];
            if (ch != parent[node]) {
                tree.edge_to[edge_idx] = ch;
                parent[ch] = node;
                depth[ch] = depth[node] + 1;
                int child size = dfs hld(ch);
                if (child size > max sub tree)
                    heavy[node] = ch, max sub tree = child size;
                size += child_size;
            }
        }
        return size;
    }
    vector<tuple<int, int, bool>> get_path(int u, int v) { //l,r,must_reverse?
        vector<pair<int, int>> tmp[2];
        bool idx = 1;
        while (root[u] != root[v]) {
            if (depth[root[u]] > depth[root[v]]) {
                swap(u, v);
                idx = !idx;
            }
```

```
//if value in edges ,you need value of root[v] also (connecter edge)
            tmp[idx].push_back( { pos_in_array[root[v]], pos_in_array[v] });
            v = parent[root[v]];
        if (depth[u] > depth[v]) {
            swap(u, v);
            idx = !idx;
        if (!is_value_in_edge || u != v)
            tmp[idx].push_back( { pos_in_array[u] + is_value_in_edge, pos_in_array[v] });
        reverse(all(tmp[1]));
        vector<tuple<int, int, bool>> rt;
        for (int i = 0; i < 2; i++)
            for (auto &it : tmp[i])
                rt.emplace_back(it.first, it.second, i == 0);
        return rt; //u is LCA
public:
    heavy_light_decomposition(int n, bool is_value_in_edge) :
            n(n), is value in edge(is value in edge), seg(n + 1), tree(n + 1) {
        heavy = vector<int>(n + 1, -1);
        parent = depth = root = pos_in_array = pos_to_node = size = vector<int>(n + 1);
    }
    void add_edge(int u, int v, int c = 0) {
        tree.add_edge(u, v, c);
    }
    void build_chains(int src = 1) {
        parent[src] = -1;
        dfs hld(src);
        for (int chain_root = 1, pos = 1; chain_root <= n; chain_root++) {</pre>
            if (parent[chain_root] == -1 || heavy[parent[chain_root]] != chain_root)
                for (int j = chain_root; j != -1; j = heavy[j]) {
                    root[j] = chain_root;
                    pos_in_array[j] = pos++;
                    pos to node[pos in array[j]] = j;
                }
        if (is value in edge)
            for (int i = 1; i < n; i++)
                update_edge(i, tree.edge_cost[i]);
    }
    void update node(int node, int value) {
        seg.update(pos_in_array[node], value);
    }
    void update edge(int edge idx, int value) {
        update_node(tree.edge_to[edge_idx], value);
    }
    void update_path(int u, int v, ll c) {
        vector<tuple<int, int, bool>> intervals = get_path(u, v);
        for (auto &it : intervals)
            seg.update(get<0>(it), get<1>(it), c);
    }
```

```
node query in path(int u, int v) {
        vector<tuple<int, int, bool>> intervals = get_path(u, v);
        //initial value,check if handling u == v
        node query res = 0;
        for (auto &it : intervals) {
            int 1, r;
            bool rev;
            tie(l, r, rev) = it;
            node cur = seg.query(1, r);
            if (rev) cur.reverse();
            query_res = node(query_res, cur);
        return query res;
    }
};
Centroid decomposition
class centroid decomposition {
      vector<bool> centroidMarked;
      vector<int> size;
      void dfsSize(int node, int par) {
            size[node] = 1;
            for (int ch : adj[node])
                  if (ch != par && !centroidMarked[ch]) {
                        dfsSize(ch, node);
                        size[node] += size[ch];
                  }
      int getCenter(int node, int par, int size_of_tree) {
            for (int ch : adj[node]) {
                  if (ch == par || centroidMarked[ch]) continue;
                  if (size[ch] * 2 > size_of_tree)
                        return getCenter(ch, node, size of tree);
            return node;
      int getCentroid(int src) {
            dfsSize(src, -1);
            int centroid = getCenter(src, -1, size[src]);
            centroidMarked[centroid] = true;
            return centroid;
      }
      int decomposeTree(int root) {
            root = getCentroid(root);
            solve(root);
            for (int ch : adj[root]) {
                  if (centroidMarked[ch])
                        continue:
                  int centroid_of_subtree = decomposeTree(ch);
            //note: root and centroid of subtree probably not have a direct edge in adj
                  centroidTree[root].push_back(centroid_of_subtree);
                  centroidParent[centroid_of_subtree] = root;
            return root;
      }
```

```
void calc(int node, int par) {
            //TO-DO
            for (int ch : adj[node]) if (ch != par && !centroidMarked[ch])
                  calc(ch, node);
      }
      void add(int node, int par) {
            //T0-D0
            for (int ch : adj[node]) if (ch != par && !centroidMarked[ch])
                  add(ch, node);
      }
      void remove(int node, int par) {
            //T0-D0
            for (int ch : adj[node]) if (ch != par && !centroidMarked[ch])
                  remove(ch, node);
      }
      void solve(int root) {
            //add root
            for (int ch : adj[root])
                  if (!centroidMarked[ch]) {
                        calc(ch, root);
                        add(ch, root);
            //TO-DO //remove root
            for (int ch : adj[root])
                  if (!centroidMarked[ch])
                        remove(ch, root);
      }
public:
      int n, root;
      vector<vector<int>> adj, centroidTree;
      vector<int> centroidParent;
      centroid_decomposition(vector<vector<int>> &adj) : adj(adj) {
            n = (int) adj.size() - 1;
            size = vector<int>(n + 1);
            centroidTree = vector<vector<int>>(n + 1);
            centroidParent = vector<int>(n + 1, -1);
            centroidMarked = vector<bool>(n + 1);
            root = decomposeTree(1);
      }
};
Shortest path algorithms
Dijkstra
struct edge {
      int from, to, weight;
      edge() { from = to = weight = 0;}
      edge(int from, int to, int weight) :
            from(from), to(to), weight(weight) {
      bool operator <(const edge& other) const {</pre>
            return weight > other.weight;
      }
};
```

```
vector<vector<edge>> adj;
//0(E*log(v))
void dijkstra(int src, int dest = -1) {
      priority_queue<edge> q;
      vector<int> dis(adj.size(), INT_MAX), prev(adj.size(), -1);
      q.push(edge(-1, src, 0));
      dis[src] = 0;
      while (!q.empty()) {
            edge e = q.top();
            q.pop();
            if (e.weight > dis[e.to])
                  continue;
            prev[e.to] = e.from;
            if (e.to == dest)
                  break;
            for (edge ne : adj[e.to])
                  if (dis[ne.to] > dis[e.to] + ne.weight) {
                         ne.weight = dis[ne.to] = dis[e.to] + ne.weight;
                         q.push(ne);
                  }
      }
      vector<int> path;
      while (dest != -1) {
            path.push_back(dest);
            dest = prev[dest];
      reverse(path.begin(), path.end());
}
Bellmanford
vector<edge> edgeList;
//0(V*E)
void bellmanford(int n, int src, int dest = -1) {
      vector\langle int \rangle dis(n + 1, oo), prev(n + 1, -1);
      dis[src] = 0;
      bool negativeCycle = false;
      int last = -1, tmp = n;
      while (tmp--) {
            last = -1;
            for (edge e : edgeList)
                  if (dis[e.to] > dis[e.from] + e.weight) {
                        dis[e.to] = dis[e.from] + e.weight;
                        prev[e.to] = e.from;
                        last = e.to;
                  }
            if (last == -1)
                  break;
            if (tmp == 0)
                  negativeCycle = true;
      if (last != -1) {
            for (int i = 0; i < n; i++)
                  last = prev[last];
            vector<int> cycle;
```

```
for (int cur = last; cur != last || cycle.size() > 1; cur = prev[cur])
                  cycle.push back(cur);
            reverse(cycle.begin(), cycle.end());
      }
      vector<int> path;
      while (dest != -1) {
            path.push back(dest);
            dest = prev[dest];
      reverse(path.begin(), path.end());
}
Difference constraints
void difference_constraints() {
      int m;
      cin >> m;
      int cnt = 1;
      while (m--) {
            string x1, x2;
            int w; // x1 - x2 <= w
            cin >> x1 >> x2 >> w;
            map<string, int> id;
            if (id.find(x1) == id.end())
                  id[x1] = cnt++;
            if (id.find(x2) == id.end())
                  id[x2] = cnt++;
            edgeList.emplace_back(id[x2], id[x1], w);
      for (int i = 1; i < cnt; i++)</pre>
            edgeList.emplace_back(cnt, i, 0);
      bellmanford(cnt, cnt);
}
Floyed
vector<vector<int>> adj, par;
// adj[i][j] = oo , adj[i][i] = 0 , par[i][j] = i
void init(int n) {
      par = adj = vector<vector<int>>(n + 1, vector<int>(n + 1, oo));
      for (int i = 1; i <= n; i++)
            adj[i][i] = 0;
      for (int i = 1; i <= n; i++)
            for (int j = 1; j <= n; j++)
                  par[i][j] = i;
void floyd() {
      for (int k = 1; k < adj.size(); k++)</pre>
            for (int i = 1; i < adj.size(); i++)</pre>
                  for (int j = 1; j < adj.size(); j++)</pre>
                         if (adj[i][j] > adj[i][k] + adj[k][j]) {
                               adj[i][j] = adj[i][k] + adj[k][j];
                               par[i][j] = par[k][j];
                         }
}
```

```
void buildPath(int src, int dest) {
      vector<int> path;
      while (src != dest) {
            path.push back(dest);
            dest = par[src][dest];
      }
      path.push back(src);
      reverse(path.begin(), path.end());
}
SPFA
vector<vector<edge>> adj;
enum visit {finished, in_queue, not_visited };
void spfa(int src) {
      int n = adj.size();
      vector<int> dis(n, INF), prev(n, -1), state(n, not_visited);
      dis[src] = 0;
      deque<int> q;
      q.push_back(src);
      while (!q.empty()) {
            int u = q.front();
            q.pop_front();
            state[u] = finished;
            for (auto &e : adj[u]) {
                  if (dis[e.to] > dis[e.from] + e.cost) {
                         dis[e.to] = dis[e.from] + e.cost;
                         prev[e.to] = e.from;
                         if (state[e.to] == not_visited) {
                               q.push_back(e.to);
                         } else if (state[e.to] == finished) {
                               q.push_front(e.to);
                        state[e.to] = in_queue;
                  }
            }
      }
}
MST
Kruskal
struct edge {
      int from, to;
      11 weight;
      edge() {
            from = to = weight = 0;
      edge(int from, int to, 11 weight) :
            from(from), to(to), weight(weight) {
      bool operator <(const edge& other) const {</pre>
            return weight < other.weight;</pre>
      }
};
```

```
vector<edge> edgeList;
pair<int, vector<edge>> MST_Kruskal(int n) {//O(edges*log(edges))
      DSU uf(n);
      vector < edge > edges;
      int mstCost = 0;
      sort(edgeList.begin(), edgeList.end());
      for (auto e : edgeList)
            if (uf.union_sets(e.from, e.to)) {
                  mstCost += e.weight;
                  edges.push_back(e);
            }
      if (edges.size() != n - 1)
            return { INT MAX, vector < edge > () };
      return { mstCost,edges };
int miniMax(int src, int dest, int n) {
      int max = INT_MIN;
      DSU uf(n);
      sort(edgeList.begin(), edgeList.end());
      for (auto e : edgeList) {
            if (uf.same set(src, dest))
                  return max;
            uf.union_sets(e.from, e.to);
            max = e.weight;
      }
      return max;
//O(edges*log(edges) + nodes*nodes)
pair<int, vector<edge>> SMST_Kruskal(int n) {
      DSU uf(n);
      sort(edgeList.begin(), edgeList.end());
      vector<edge> take, leave;
      int mstCost = 0;
      for (auto e : edgeList)
            if (uf.union_sets(e.from, e.to)) {
                  mstCost += e.weight;
                  take.push back(e);
            }
            else leave.push_back(e);
      pair<int, vector<edge>> ret = { INT_MAX, vector<edge>() };
      for (int i = 0; i < take.size(); i++) {</pre>
            uf = DSU(n);
            vector <edge> edges;
            mstCost = 0;
            for (int j = 0; j < take.size(); j++) {</pre>
                  if (i == j)
                        continue;
                  uf.union_sets(take[j].from, take[j].to);
                  mstCost += take[j].weight;
                  edges.push_back(take[j]);
            }
```

```
for (edge e : leave) {
                  if (uf.union_sets(e.from, e.to)) {
                        mstCost += e.weight;
                        edges.push_back(e);
                        break;
                  }
            if (edges.size() == n - 1 && ret.first < mstCost)</pre>
                  ret = { mstCost, edges };
      return ret;
}
Prim
struct edge {
      int from, to, weight;
      edge() {
            from = to = weight = 0;
      }
      edge(int from, int to, int weight) : from(from), to(to), weight(weight) {}
      bool operator <(const edge& other) const {</pre>
            return weight > other.weight;
      }
};
vector<vector<edge>> adj;
vector<edge> prim(int node) {
      vector<bool> vis(adj.size());
      priority_queue<edge> q;
      vector<edge> edges;
      q.push(edge(-1, node, 0));
      while (!q.empty()) {
            edge e = q.top();
            q.pop();
            if (vis[e.to])
                  continue;
            vis[e.to] = true;
            if (e.from != -1)
                  edges.push_back(e);
            for (edge ch : adj[e.to])
                  if (!vis[ch.to])
                        q.push(ch);
      }
      return edges;//check it connected or not
}
SMST O(n * log(n))
struct edge {
      int from, to;
      11 weight;
      edge() {
            from = to = weight = 0;
      edge(int from, int to, 11 weight) :
            from(from), to(to), weight(weight) {
      }
```

```
bool operator <(const edge& other) const {</pre>
            return weight < other.weight;</pre>
      }
};
int MST_Kruskal(int n, vector<edge> edgeList, vector<edge>& take,
      vector<edge>& leave) {
      DSU uf(n);
      vector<edge> edges;
      sort(edgeList.begin(), edgeList.end());
      int mst_cost = 0;
      for (auto e : edgeList)
            if (uf.union sets(e.from, e.to)) {
                  take.push_back(e);
                  mst_cost += e.weight;
            }
            else leave.push_back(e);
      return mst_cost;
}
struct LCA {
#define INIT { -1, -2 }
      struct data {
            int lca = -1;
            pair<int, int> max edges = INIT; //first max,second max (distinct)
      };
      pair<int, int> merge(pair<int, int> a, pair<int, int> b) {
            if (a.first < b.first)</pre>
                  swap(a, b);
            if (b.first == a.first)
                  a.second = max(a.second, b.second);
            else if (b.first > a.second)
                  a.second = b.first;
            return a;
      }
      int logN;
      vector<vector<data>> lca;
      vector<vector<edge>> adj;
      vector<int> depth;
      void dfs(int node, int par) {
            for (edge e : adj[node])
                  if (e.to != par) {
                         depth[e.to] = depth[node] + 1;
                         lca[e.to][0].max_edges.first = e.weight;
                         lca[e.to][0].lca = node;
                         dfs(e.to, node);
                  }
      LCA(int n, vector<edge>& edges) :
            adj(n + 1) {
            for (auto& e : edges) {
                  adj[e.from].push_back(e);
                  adj[e.to].push_back(edge(e.to, e.from, e.weight));
            logN = log2(n);
            depth = vector<int>(n + 1);
```

```
lca = vector<vector<data>>(n + 1, vector<data>(logN + 1));
            dfs(1, -1);
            for (int k = 1; k <= logN; k++)</pre>
                  for (int node = 1; node <= n; node++) {</pre>
                         int par = lca[node][k - 1].lca;
                         if (~par) {
                               lca[node][k].lca = lca[par][k - 1].lca;
                               lca[node][k].max_edges = merge(lca[node][k - 1].max_edges,
                                      lca[par][k - 1].max_edges);
                         }
                  }
      }
      pair<int, int> max two edges(int u, int v) {
            pair<int, int> ans = INIT;
            if (depth[u] < depth[v]) swap(u, v);</pre>
            for (int i = logN; i >= 0; i--)
                  if (depth[u] - (1 << i) >= depth[v]) {
                         ans = merge(ans, lca[u][i].max edges);
                         u = lca[u][i].lca;
                  }
            if (u == v) return ans;
            for (int i = logN; i >= 0; i--)
                  if (lca[u][i].lca != lca[v][i].lca) {
                         ans = merge(ans, lca[u][i].max edges);
                         ans = merge(ans, lca[v][i].max_edges);
                         u = lca[u][i].lca;
                         \vee = lca[v][i].lca;
                  }
            ans = merge(ans, lca[u][0].max_edges);
            ans = merge(ans, lca[v][0].max edges);
            return ans;
      }
};
int main() {
      run();
      int t;
      cin >> t;
      for (int I = 1; I <= t; I++) {</pre>
            int n, e;
            cin >> n >> e;
            vector<edge> edgeList(e);
            for (auto& it : edgeList)
                  cin >> it.from >> it.to >> it.weight;
            vector<edge> take, leave;
            int mst_cost = MST_Kruskal(n, edgeList, take, leave);
            if (take.size() != n - 1) {
                  cout << "No way\n";</pre>
                  continue;
            LCA tree(n, take);
            11 \text{ rt} = INF;
            for (edge e : leave) {
                  pair<int, int> p = tree.max two edges(e.from, e.to);
                  rt = min(rt, mst cost - p.first + e.weight);
            }
```

```
if (rt == INF)
                  cout << "No second way\n";</pre>
            else
                  cout << rt << endl;</pre>
      }
}
Tarjan
SCC
vector<vector<int>> adj, scc;
vector<set<int>> dag;
vector<int> dfs_num, dfs_low, compId;
vector<bool> inStack;
stack<int> stk;
int timer;
void dfs(int node) {
      dfs_num[node] = dfs_low[node] = ++timer;
      stk.push(node);
      inStack[node] = 1;
      for (int child : adj[node])
            if (!dfs_num[child]) {
                  dfs(child);
                  dfs_low[node] = min(dfs_low[node], dfs_low[child]);
            else if (inStack[child])
                  dfs_low[node] = min(dfs_low[node], dfs_num[child]);
      //can be dfs_low[node] = min(dfs_low[node], dfs_low[child]);
      if (dfs low[node] == dfs num[node]) {
            scc.push_back(vector<int>());
            int v = -1;
            while (v != node) {
                  v = stk.top();
                  stk.pop();
                  inStack[v] = 0;
                  scc.back().push_back(v);
                  compId[v] = scc.size() - 1;
            }
      }
}
void SCC() {
      timer = 0;
      dfs_num = dfs_low = compId = vector<int>(adj.size());
      inStack = vector<bool>(adj.size());
      scc = vector<vector<int>>();
      for (int i = 1; i < adj.size(); i++)</pre>
            if (!dfs_num[i]) dfs(i);
}
void DAG() {
      dag = vector<set<int>>(scc.size());
      for (int i = 1; i < adj.size(); i++)</pre>
            for (int j : adj[i])
                  if (compId[i] != compId[j])
                         dag[compId[i]].insert(compId[j]);
}
```

```
Articulation points and bridges
vector<vector<int>> adi;
vector<int> dfs num, dfs low;
vector<bool> articulation_point;
vector<pair<int, int>> bridge;
stack<pair<int, int>> edges;
vector<vector<pair<int, int>>> BCC; //biconnected components
int timer, cntChild;
void dfs(int node, int par) {
      dfs num[node] = dfs_low[node] = ++timer;
      for (int child : adj[node]) {
            if (par != child && dfs num[child] < dfs num[node])</pre>
                  edges.push({ node, child });
            if (!dfs_num[child]) {
                  if (par == -1)
                        cntChild++;
                  dfs(child, node);
                  if (dfs_low[child] >= dfs_num[node]) {
                        articulation point[node] = 1;
                        //get biconnected component
                        BCC.push_back(vector<pair<int, int>>());
                        pair<int, int> edge;
                        do {
                              edge = edges.top();
                              BCC.back().push_back(edge);
                              edges.pop();
                        } while (edge.first != node || edge.second != child);
                  }
                  //can be (dfs_low[child] == dfs_num[child])
                  if (dfs_low[child] > dfs_num[node])
                        bridge.push_back({ node, child });
                  dfs low[node] = min(dfs low[node], dfs low[child]);
            else if (child != par)
                  dfs_low[node] = min(dfs_low[node], dfs_num[child]);
      }
}
void articulation points and bridges() {
      timer = 0;
      dfs num = dfs_low = vector<int>(adj.size());
      articulation_point = vector<bool>(adj.size());
      bridge = vector<pair<int, int>>();
      for (int i = 1; i < adj.size(); i++)</pre>
            if (!dfs num[i]) {
                  cntChild = 0;
                  dfs(i, -1);
                  articulation_point[i] = cntChild > 1;
            }
}
```

```
Edge classification
vector<vector<int>> adj;
vector<int> start, finish;
int timer;
void dfsEdgeClassification(int node) {
      start[node] = timer++;
      for (int child : adj[node]) {
            if (start[child] == -1)
                  dfsEdgeClassification(child);
            else {
                  if (finish[child] == -1)
                         ; // Back Edge
                  else if (start[node] < start[child])</pre>
                         ; // Forward Edge
                  else; // Cross Edge
            }
      }
      finish[node] = timer++;
}
2-SAT
int n;
int Not(int x) {
      return (x > n ? x - n : x + n);
}
void addEdge(int a, int b) {
      adj[Not(a)].push_back(b);
      adj[Not(b)].push_back(a);
}
void add_xor_edge(int a, int b) {
      addEdge(Not(a), Not(b));
      addEdge(a, b);
}
bool 2SAT(vector<int>& value) {
      SCC();
      for (int i = 1; i <= n; i++)
            if (compId[i] == compId[Not(i)])
                  return false;
      vector<int> assign(scc.size(), -1);
      for (int i = 0; i < scc.size(); i++)</pre>
            if (assign[i] == -1) {
                  assign[i] = true;
                  assign[compId[Not(scc[i].back())]] = false;
      for (int i = 1; i <= n; i++)</pre>
            value[i] = assign[compId[i]];
      return true;
```

}

#### **Flows**

```
Maximum bipartite matching
vector<vector<int>> adj;
vector<int> rowAssign, colAssign, vis;//make vis array instance of vector
int test_id;
bool canMatch(int i) {
      if (vis[i] == test_id) return false;
      vis[i] = test_id;
      for (int j : adj[i])
            if (colAssign[j] == -1) {
                  colAssign[j] = i;
                  rowAssign[i] = j;
                  return true;
      for (int j : adj[i])
            if (canMatch(colAssign[j])) {
                  colAssign[j] = i;
                  rowAssign[i] = j;
                  return true;
      return false;
}
// O(rows * edges) //number of operation could by strictly less than order (1e5*1e5->AC)
int maximum_bipartite_matching(int rows, int cols) {
      int maxFlow = 0;
      rowAssign = vector<int>(rows, -1);
      colAssign = vector<int>(cols, -1);
      vis = vector<int>(rows);
      for (int i = 0; i < rows; i++) {</pre>
            test id++;
            if (canMatch(i)) maxFlow++;
      vector<pair<int, int>> matches;
      for (int j = 0; j < cols; j++)</pre>
            if (~colAssign[j]) matches.push_back( { colAssign[j], j });
      return maxFlow;
}
Hopcroft Karp for bipartite matching
//0(sqrt(V) * E)
struct Hopcroft_Karp {//1-based
#define NIL 0
#define INF INT_MAX
      int n, m;
      vector<vector<int>> adj;
      vector<int> rowAssign, colAssign, dist;
      bool bfs() {
            queue<int> q;
            dist = vector<int>(adj.size(), INF);
            for (int i = 1; i <= n; i++)
                  if (rowAssign[i] == NIL) {
                        dist[i] = 0;
                        q.push(i);
                  }
```

```
while (!q.empty()) {
                  int cur = q.front();
                  q.pop();
                  if (dist[cur] >= dist[NIL])break;
                  for (auto& nxt : adj[cur]) {
                        if (dist[colAssign[nxt]] == INF) {
                              dist[colAssign[nxt]] = dist[cur] + 1;
                              q.push(colAssign[nxt]);
                        }
                  }
            return dist[NIL] != INF;
      bool dfs(int i) {
            if (i == NIL)
                  return true;
            for (int j : adj[i]) {
                  if (dist[colAssign[j]] == dist[i] + 1 && dfs(colAssign[j])) {
                        colAssign[j] = i;
                        rowAssign[i] = j;
                        return true;
                  }
            dist[i] = INF;
            return false;
      }
      Hopcroft_Karp(int n, int m)
            :n(n), m(m), adj(n + 1), rowAssign(n + 1), colAssign(m + 1) {
      void addEdge(int u, int v) {
            adj[u].push_back(v);
      }
      int maximum_bipartite_matching() {
            int rt = 0;
            while (bfs()) {
                  for (int i = 1; i <= n; i++)
                        if (rowAssign[i] == NIL && dfs(i))
                              rt++;
            }
            return rt;
      }
Edmonds Karp
//0(V*E*E)
#define INF 0x3f3f3f3f3f3f3f3f1LL
int n;
int capacity[101][101];
int getPath(int src, int dest, vector<int> &parent) {
    parent = vector<int>(n + 1, -1);
    queue<pair<int, int>> q;
    q.push( { src, INF });
    while (q.size()) {
        int cur = q.front().first, flow = q.front().second;
        q.pop();
```

**}**;

```
if (cur == dest) return flow;
        for (int i = 1; i <= n; i++)
            if (parent[i] == -1 && capacity[cur][i]) {
                parent[i] = cur;
                q.push( { i, min(flow, capacity[cur][i]) });
                if (i == dest) return q.back().second;
            }
    return 0;
}
int Edmonds_Karp(int source, int sink) {
    int max flow = 0;
    int new flow = 0;
    vector<int> parent(n + 1, -1);
    while (new_flow = getPath(source, sink, parent)) {
        max_flow += new_flow;
        int cur = sink;
        while (cur != source) {
            int prev = parent[cur];
            capacity[prev][cur] -= new_flow;
            capacity[cur][prev] += new_flow;
            cur = prev;
        };
    }
    return max_flow;
}
Dinic
//O(V*V*E) more faster
struct Dinic { //0-based
    struct flowEdge {
        int from, to;
        ll cap, flow = 0;
        flowEdge(int from, int to, 11 cap) :
                from(from), to(to), cap(cap) {
        }
    };
    vector<flowEdge> edges;
    int n, m = 0, source, sink;
    vector<vector<int>> adj;
    vector<int> level, ptr;
    Dinic(int n, int source, int sink) :
            n(n), source(source), sink(sink), adj(n), level(n), ptr(n) {
    void addEdge(int u, int v, ll cap) {
        edges.emplace_back(u, v, cap);
        edges.emplace_back(v, u, 0);
        adj[u].push back(m);
        adj[v].push_back(m + 1);
        m += 2;
    }
```

```
bool bfs() {
        queue<int> q;
        level = vector<int>(n, -1);
        level[source] = 0;
        q.push(source);
        while (!q.empty()) {
            int cur = q.front();
            q.pop();
            for (auto &id : adj[cur]) {
                 if (edges[id].cap - edges[id].flow <= 0)</pre>
                     continue;
                 int nxt = edges[id].to;
                 if (level[nxt] != -1)
                     continue;
                level[nxt] = level[cur] + 1;
                 q.push(nxt);
            }
        return level[sink] != -1;
    11 dfs(int node, 11 cur flow) {
        if (cur_flow == 0 || node == sink)
            return cur_flow;
        for (int &cid = ptr[node]; cid < adj[node].size(); cid++) {</pre>
            int id = adj[node][cid];
            int nxt = edges[id].to;
            if (level[node] + 1 != level[nxt] || edges[id].cap - edges[id].flow <= 0)</pre>
                 continue;
            11 tmp = dfs(nxt, min(cur_flow, edges[id].cap - edges[id].flow));
            if (tmp == 0)
                  continue;
            edges[id].flow += tmp;
            edges[id ^ 1].flow -= tmp;
            return tmp;
        return 0;
    11 flow() {
        11 \text{ max\_flow} = 0;
        while (bfs()) {
            fill(ptr.begin(), ptr.end(), 0);
            while (ll pushed = dfs(source, INF))
                 max flow += pushed;
        return max_flow;
    }
Min cost Max flow
struct MCMF { //0-based
    struct edge {
        int from, to, cost, cap, flow, backEdge;
        edge() {
            from = to = cost = cap = flow = backEdge = 0;
        }
```

**}**;

```
edge(int from, int to, int cost, int cap, int flow, int backEdge) :
            from(from), to(to), cost(cost), cap(cap), flow(flow), backEdge(
                    backEdge) {
    bool operator <(const edge &other) const {</pre>
        return cost < other.cost;</pre>
    }
};
int n, src, dest;
vector<vector<edge>> adj;
const int 00 = 1e9;
MCMF(int n, int src, int dest) : n(n), src(src), dest(dest), adj(n) {}
void addEdge(int u, int v, int cost, int cap) {
    edge e1 = edge(u, v, cost, cap, 0, adj[v].size());
    edge e2 = edge(v, u, -cost, 0, 0, adj[u].size());
    adj[u].push_back(e1);
    adj[v].push_back(e2);
}
pair<int, int> minCostMaxFlow() {
    int maxFlow = 0, cost = 0;
    while (true) {
        vector<pair<int, int>> path = spfa();
        if (path.empty())
            break;
        int new_flow = 00;
        for (auto &it : path) {
            edge &e = adj[it.first][it.second];
            new_flow = min(new_flow, e.cap - e.flow);
        for (auto &it : path) {
            edge &e = adj[it.first][it.second];
            e.flow += new_flow;
            cost += new_flow * e.cost;
            adj[e.to][e.backEdge].flow -= new_flow;
        maxFlow += new flow;
    return {maxFlow,cost};
enum visit { finished, in_queue, not_visited };
vector<pair<int, int>> spfa() {
    vector<int> dis(n, 00), prev(n, -1), from_edge(n), state(n,
            not_visited);
    deque<int> q;
    dis[src] = 0;
    q.push_back(src);
    while (!q.empty()) {
        int u = q.front();
        q.pop_front();
        state[u] = finished;
        for (int i = 0; i < adj[u].size(); i++) {</pre>
            edge e = adj[u][i];
            if (e.flow >= e.cap || dis[e.to] <= dis[u] + e.cost)</pre>
                continue;
```

```
dis[e.to] = dis[u] + e.cost;
                prev[e.to] = u;
                from_edge[e.to] = i;
                if (state[e.to] == in_queue) continue;
                if (state[e.to] == finished
                         || (!q.empty() && dis[q.front()] > dis[e.to]))
                    q.push front(e.to);
                else
                    q.push_back(e.to);
                state[e.to] = in_queue;
            }
        if (dis[dest] == 00)
            return {};
        vector<pair<int, int>> path;
        int cur = dest;
        while (cur != src) {
            path.push_back( { prev[cur], from_edge[cur] });
            cur = prev[cur];
        reverse(path.begin(), path.end());
        return path;
    }
};
Hungarian
// nodes are 0-based
/* There are n workers and n tasks.
You know exactly how much you need to pay each worker to perform one or another task.
You also know that every worker can only perform one task.
Your goal is to assign each worker some a task,
while minimizing your expenses.
*/
// fill vector a with costs
// if you want maximizie final cost then you will multiply edges cost with -1
// this algorithm works only on bipartite graph
// the maximum matching must equal to n
template<typename T>
class hungarian {
public:
    int n;
    int m;
    vector< vector<T> > a;
    vector<T> u;
    vector<T> v;
    vector<int> pa;
    vector<int> pb;
    vector<int> way;
    vector<T> minv;
    vector<bool> used;
    T inf;
    hungarian(int _n, int _m) : n(_n), m(_m) {
        assert(n <= m);</pre>
        a = vector< vector<T> >(n, vector<T>(m));
        u = vector < T > (n + 1);
```

```
v = vector < T > (m + 1);
    pa = vector<int>(n + 1, -1);
    pb = vector < int > (m + 1, -1);
    way = vector<int>(m, -1);
    minv = vector<T>(m);
    used = vector<bool>(m + 1);
    inf = numeric limits<T>::max();
inline void add_row(int i) {
    fill(minv.begin(), minv.end(), inf);
    fill(used.begin(), used.end(), false);
    pb[m] = i;
    pa[i] = m;
    int j0 = m;
    do {
        used[j0] = true;
        int i0 = pb[j0];
        T delta = inf;
        int j1 = -1;
        for (int j = 0; j < m; j++) {
            if (!used[j]) {
                 T cur = a[i0][j] - u[i0] - v[j];
                 if (cur < minv[j]) {</pre>
                     minv[j] = cur;
                     way[j] = j0;
                 if (minv[j] < delta) {</pre>
                     delta = minv[j];
                     j1 = j;
                 }
            }
        }
        for (int j = 0; j <= m; j++) {
            if (used[j]) {
                 u[pb[j]] += delta;
                 v[j] -= delta;
            }
            else {
                minv[j] -= delta;
            }
        j0 = j1;
    } while (pb[j0] != -1);
    do {
        int j1 = way[j0];
        pb[j0] = pb[j1];
        pa[pb[j0]] = j0;
        j0 = j1;
    } while (j0 != m);
}
inline T current_score() {
    return -v[m];
}
```

```
inline T solve() {
        for (int i = 0; i < n; i++) {
            add_row(i);
        return current_score();
    }
};
String
Hashing
struct hashing {
      int MOD, BASE;
      vector<int> Hash, modInv;
      hashing(string s, int MOD, int BASE, char first_char = 'a') :
            MOD(MOD), BASE(BASE), Hash(sz(s) + 1), modInv(sz(s) + 1) {
            modInv[0] = 1;
            11 \text{ base} = 1;
            for (int i = 1; i <= sz(s); i++) {
                  Hash[i] = (Hash[i - 1] + (s[i - 1] - first_char + 1) * base) % MOD;
                  modInv[i] = power(base, MOD - 2, MOD);
                  base = (base * BASE) % MOD;
            }
      }
      int getHash(int 1, int r) { //1-based
            return (1LL * (Hash[r] - Hash[l - 1] + MOD) % MOD * modInv[l]) % MOD;
      }
};
//MOD = 1e9 + 9 , BASE = 31
//MOD = 2000000011 ,BASE = 53 ->careful of overflow
//********
//MOD = 998634293, BASE = 953
//MOD = 986464091, BASE = 1013
KMP
struct KMP {
      string pattern;
      vector<int> longestPrefix;
      KMP(string& str) :pattern(str) {
            failure_function();
      }
      int fail(int k, char nxt) {
            while (k > 0 && pattern[k] != nxt)
                  k = longestPrefix[k - 1];
            if (nxt == pattern[k]) k++;
            return k;
      }
      void failure function() {
            int n = pattern.size();
            longestPrefix = vector<int>(n);
            for (int i = 1, k = 0; i < n; i++)
                  longestPrefix[i] = k = fail(k, pattern[i]);
      }
```

```
void match(const string& str) {
            int n = str.size();
            int m = pattern.size();
            for (int i = 0, k = 0; i < n; i++) {
                  k = fail(k, str[i]);
                  if (k == m) {
                        cout << i - m + 1 << endl; //0-based</pre>
                        k = longestPrefix[k - 1]; // if you want next match
                  }
            }
      }
};
vector<bool> suffix pal(string s) { //[i..n-1] pal?
      string r = s;
      reverse(all(r));
      vector<bool> v(s.size());
      v[0] = (s == r);
      string pattern = r + "#" + s;
      int n = pattern.size();
      vector<int> longestPrefix(n);
      int k = 0;
      for (int i = 1; i < n; i++) {
            while (k > 0 && pattern[k] != pattern[i])
                  k = longestPrefix[k - 1];
            if (pattern[i] == pattern[k]) k++;
            longestPrefix[i] = k;
      }
      while (k > 0) {
            v[s.size() - k] = true;
            k = longestPrefix[k - 1];
      }
      return v;
}
vector<bool> prefix_pal(string s) { // [0..i] pal?
      string r = s;
      reverse(all(r));
      vector<bool> v(s.size());
      v.back() = (s == r);
      string pattern = s + "#" + r;
      int n = pattern.size();
      vector<int> longestPrefix(n);
      int k = 0;
      for (int i = 1; i < n; i++) {
            while (k > 0 && pattern[k] != pattern[i])
                  k = longestPrefix[k - 1];
            if (pattern[i] == pattern[k])
                  k++;
            longestPrefix[i] = k;
      }
      while (k > 0) {
            v[k - 1] = true;
            k = longestPrefix[k - 1];
      }
      return v;
}
```

```
//frq[i] = number of occur s[0..i] in s
vector<int> build_fre_prefix(const string& s) {
      KMP kmp(s);
      kmp.failure_function();
      vector<int> f = kmp.longestPrefix;
      int n = sz(s);
      vector<int> frq(n);
      for (int i = n - 1; i >= 0; i--)
            if (f[i]) frq[f[i] - 1] += frq[i] + 1;
      for (auto& it : frq)it++;
      return frq;
}
Trie
class trie {
    struct trie_node {
        bool is_leaf = false;
        map<char, int> next;
        bool have_next(char ch) {
            return next.find(ch) != next.end();
        int& operator[](char ch) {
            return next[ch];
        }
    };
    vector<trie_node> t;
public:
    trie() {
        t.push_back(trie_node());
    void insert(const string &s) {
        int root = 0;
        for (const char &ch : s) {
            if (!t[root].have_next(ch)) {
                t.push_back(trie_node());
                t[root][ch] = t.size() - 1;
            }
            root = t[root][ch];
        t[root].is_leaf = true;
    bool find(const string &s) {
        int root = 0;
        for (const char &ch : s) {
            if (!t[root].have_next(ch))
                return false;
            root = t[root][ch];
        return t[root].is_leaf;
    }
};
```

#### **Aho Corasick**

```
struct aho corasick {
    struct trie_node {
        vector<int> pIdxs; //probably take memory limit
        map<char, int> next;
        int fail;
        trie node() : fail(0) {}
        bool have_next(char ch) {
            return next.find(ch) != next.end();
        int& operator[](char ch) {
            return next[ch];
        }
    };
    vector<trie_node> t;
    vector<string> patterns;
    vector<int> end of pattern;
    vector<vector<int>> adj;
    int insert(const string &s, int patternIdx) {
        int root = 0;
        for (const char &ch : s) {
            if (!t[root].have_next(ch)) {
                t.push_back(trie_node());
                t[root][ch] = t.size() - 1;
            root = t[root][ch];
        }
        t[root].pIdxs.push back(patternIdx);
        return root;
    }
    int next_state(int cur, char ch) {
        while (cur > 0 && !t[cur].have_next(ch))
            cur = t[cur].fail;
        if (t[cur].have next(ch))
            return t[cur][ch];
        return 0;
    }
    void buildAhoTree() {
        queue<int> q;
        for (auto &child : t[0].next)
            q.push(child.second);
        while (!q.empty()) {
            int cur = q.front();
            q.pop();
            for (auto &child : t[cur].next) {
                int k = next_state(t[cur].fail, child.first);
                t[child.second].fail = k;
                vector<int> &idxs = t[child.second].pIdxs;
                //dp[child.second] = max(dp[child.second],dp[k]);
                idxs.insert(idxs.end(), all(t[k].pIdxs));
                q.push(child.second);
            }
        }
    }
```

```
void buildFailureTree() {
        adj = vector<vector<int>>(t.size());
        for (int i = 1; i < t.size(); i++)</pre>
            adj[t[i].fail].push_back(i);
    aho_corasick(const vector<string> &_patterns) {
        t.push_back(trie_node());
        patterns = _patterns;
        end_of_pattern = vector<int>(patterns.size());
        for (int i = 0; i < patterns.size(); i++)</pre>
            end_of_pattern[i] = insert(patterns[i], i);
        buildAhoTree();
        //buildFailureTree();
    }
    vector<vector<int>> match(const string &str) {
        int k = 0;
        vector<vector<int>> rt(patterns.size());
        for (int i = 0; i < str.size(); i++) {</pre>
            k = next_state(k, str[i]);
            for (auto &it : t[k].pIdxs)
                rt[it].push_back(i);
        return rt;
    }
};
```

# **Suffix Automaton**

```
struct suffix automaton {
    struct state {
        int len, link = 0, cnt = 0;
        bool terminal = false, is clone = false;
        map<char, int> next;
        state(int len = 0) : len(len) {}
        bool have_next(char ch) {
            return next.find(ch) != next.end();
        void clone(const state &other, int nlen) {
            len = nlen;
            next = other.next;
            link = other.link;
            is_clone = true;
        }
    };
    vector<state> st;
    int last = 0;
    suffix_automaton() {
        st.push_back(state());
        st[0].link = -1;
    }
    suffix_automaton(const string &s) : suffix_automaton() {
        for (char ch : s) extend(ch);
        for (int cur = last; cur > 0; cur = st[cur].link)
            st[cur].terminal = true;
    }
    void extend(char c) {
        int cur = st.size();
        st.push_back(state(st[last].len + 1));
        st[cur].cnt = 1;
        int p = last;
        last = cur;
        while (p != -1 && !st[p].have_next(c)) {
            st[p].next[c] = cur;
            p = st[p].link;
        }
        if (p == -1) return;
        int q = st[p].next[c];
        if (st[p].len + 1 == st[q].len) {
            st[cur].link = q;
            return;
        }
        int clone = st.size();
        st.push_back(state());
        st[clone].clone(st[q], st[p].len + 1);
        while (p != -1 \&\& st[p].next[c] == q) {
            st[p].next[c] = clone;
            p = st[p].link;
        st[q].link = st[cur].link = clone;
    }
```

```
void calc_number_of_occurrences() {
    vector<vector<int>> lvl(st[last].len + 1);
    for (int i = 1; i < st.size(); i++)</pre>
        lvl[st[i].len].push_back(i);
    for (int i = st[last].len; i >= 0; i--)
        for (auto cur : lvl[i])
            st[st[cur].link].cnt += st[cur].cnt;
}
vector<11> dp;
11 Count(int cur) { //count number of paths
    11 &rt = dp[cur];
    if (rt) return rt;
    rt = 1;
    for (auto ch : st[cur].next)
        rt += Count(ch.second);
    return rt;
}
string kth_substring(ll k) { //1-based,different substring,0 = ""
    assert(k <= Count(0));</pre>
    string rt;
    int cur = 0;
    while (k > 0) {
        for (auto ch : st[cur].next) {
            if (Count(ch.second) < k)</pre>
                k -= Count(ch.second);
            else {
                 rt += ch.first;
                cur = ch.second;
                k--;
                break;
            }
        }
    }
    return rt;
string longest common substring(const string &t) {
    int cur = 0, 1 = 0, mx = 0, idx = 0;
    for (int i = 0; i < t.size(); i++) {</pre>
        while (cur > 0 && !st[cur].have_next(t[i])) {
            cur = st[cur].link;
            1 = st[cur].len;
        }
        if (st[cur].have_next(t[i])) {
            cur = st[cur].next[t[i]];
            1++;
        if (1 > mx) {
            mx = 1;
            idx = i;
        }
    return t.substr(idx - mx + 1, mx);
}
```

**}**;

```
Suffix array
```

```
class suffix array {
    int getOrder(int a) const {
        return (a < (int) order.size() ? order[a] : 0);</pre>
    void radix_sort(int k) {
        vector<int> frq(n), tmp(n);
        for (auto &it : suf)
            frq[getOrder(it + k)]++;
        for (int i = 1; i < n; i++)
            frq[i] += frq[i - 1];
        for (int i = n - 1; i >= 0; i--)
            tmp[--frq[getOrder(suf[i] + k)]] = suf[i];
        suf = tmp;
    }
public:
    int n;
    string s;
    vector<int> suf, lcp, order; // order store position of suffix i in suf array
    suffix_array(const string &s) :
            n(s.size() + 1), s(s) {
        suf = order = vector<int>(n);
        vector<int> newOrder(n);
        for (int i = 0; i < n; i++)
            suf[i] = i;
        { //sort according to first character
            vector<int> tmp(n);
            for (int i = 0; i < n; i++)</pre>
                 tmp[i] = s[i];
            sort(all(tmp));
            for (int i = 0; i < n; i++)</pre>
                 order[i] = (lower_bound(all(tmp), s[i]) - tmp.begin());
        for (int len = 1; newOrder.back() != n - 1; len <<= 1) {</pre>
            auto cmp = [&](const int &a, const int &b) {
                 if (order[a] != order[b])
                     return order[a] < order[b];</pre>
                 return getOrder(a + len) < getOrder(b + len);</pre>
            };
            //sort(all(suf), cmp); //run in 576ms (n<=4e5)</pre>
            radix_sort(len); //sort second part
            radix sort(0); //sort first part
            newOrder[0] = 0;
            for (int i = 1; i < n; i++)</pre>
                 newOrder[i] = newOrder[i - 1] + cmp(suf[i - 1], suf[i]);
            for (int i = 0; i < n; i++)
                 order[suf[i]] = newOrder[i];
        buildLCP();
    }
```

```
* longest common prefix
 * lcp[i] = lcp(suf[i],suf[i-1])
void buildLCP() {
    lcp = vector<int>(n);
    int k = 0;
    for (int i = 0; i < n - 1; i++) {
        int pos = order[i];
        int j = suf[pos - 1];
        while (s[i + k] == s[j + k])
        lcp[pos] = k;
        if (k)
            k--;
    }
int LCP by order(int a, int b) {
    if (a > b) swap(a, b);
    int mn = n - suf[a] - 1;
    for (int k = a + 1; k \le b; k++)
        mn = min(mn, lcp[k]);
    return mn; }
//LCP(i,j) : longest common prefix between suffix i and suffix j
int LCP(int i, int j) {
    //return LCP_by_order(order[i],order[j]);
    if (order[j] < order[i])</pre>
        swap(i, j);
    int mn = n - i - 1;
    for (int k = order[i] + 1; k <= order[j]; k++)</pre>
        mn = min(mn, lcp[k]);
    return mn;
}
//compare s[a.first..a.second] with s[b.first..b.second]
//-1:a<b ,0:a==b,1:a>b
int compare substrings(pair<int, int> a, pair<int, int> b) {
    int lcp = min({ LCP(a.first, b.first), a.second - a.first + 1,
                      b.second - b.first + 1 });
    a.first += lcp;
    b.first += lcp;
    if (a.first <= a.second) {</pre>
        if (b.first <= b.second) {</pre>
            if (s[a.first] == s[b.first])
                 return 0;
            return (s[a.first] < s[b.first] ? -1 : 1);</pre>
        }
        return 1;
    return (b.first <= b.second ? -1 : 0);</pre>
}
```

```
pair<int, int> find string(const string &x) {
        int st = 0, ed = n;
        for (int i = 0; i < sz(x) && st < ed; i++) {
            auto cmp = [&](int a, int b) {
                if (a == -1)
                    return x[i] < s[b + i];
                return s[a + i] < x[i];
            };
            st = lower_bound(suf.begin() + st, suf.begin() + ed, -1, cmp)
                    - suf.begin();
            ed = upper_bound(suf.begin() + st, suf.begin() + ed, -1, cmp)
                    - suf.begin();
        return {st,ed-1};
    }
};
11 number_of_different_substrings(string s) {
    int n = s.size();
    suffix array sa(s);
    11 cnt = 0;
    for (int i = 0; i <= n; i++)
        cnt += n - sa.suf[i] - sa.lcp[i];
    return cnt;
}
string longest_common_substring(const string &s1, const string &s2) {
    suffix_array sa(s1 + "#" + s2);
    vector<int> suf = sa.suf, lcp = sa.lcp;
    auto type = [&](int idx) {
        return idx <= s1.size();</pre>
    };
    int mx = 0, idx = 0;
    int len = s1.size() + 1 + s2.size();
    for (int i = 1; i <= len; i++)</pre>
        if (type(suf[i - 1]) != type(suf[i]) && lcp[i] > mx) {
            mx = lcp[i];
            idx = min(suf[i - 1], suf[i]);
        }
    return s1.substr(idx, mx);
}
int longest_common_substring(const vector<string> &v) {
    int n = v.size();
    int len = n - 1;
    for (auto &it : v)
        len += it.size();
    string s(len, '.');
    vector<int> type(len + 1, n), frq(n + 1);
    for (int i = 0, j = 0; i < v.size(); i++) {</pre>
        if (i) s[j] = 'z' + i; //review this
        for (char ch : v[i]) {
            s[j] = ch;
            type[j] = i;
            j++;
        }
    suffix_array sa(s);
```

```
vector<int> suf = sa.suf, lcp = sa.lcp;
    monoqueue q;
    int st = 0, ed = 0, cnt = 0, mx = 0;
    while (st <= s.size()) {</pre>
        while (ed <= s.size() && cnt < v.size()) {</pre>
            q.push(lcp[ed], ed);
            if (++frq[type[suf[ed]]] == 1)
                cnt++;
            ed++;
        }
        q.pop(st);
        if (cnt == v.size()) mx = max(mx, q.getMin()); //st+1,ed
        if (--frq[type[suf[st]]] == 0) cnt--;
        st++;
    }
    return mx;
}
string kth substring(string s, int k) { //1-based, repated
    int n = s.size();
    suffix_array sa(s);
    vector<int> suf = sa.suf, lcp = sa.lcp;
    for (int i = 1; i <= n; i++) {
        int len = n - suf[i];
        int cnt = 0;
        for (int l = 1; l <= len; l++) {
            cnt++;
            int st = i + 1, ed = n, ans = i;
            while (st <= ed) {
                int md = st + ed >> 1;
                if (sa.LCP by order(i, md) >= 1)
                    st = md + 1, ans = md;
                else
                      ed = md - 1;
            }
            cnt += ans - i;
            if (cnt >= k) return s.substr(suf[i], 1);
        k -= len;
    }
    assert(0);
}
Suffix array Faster
class suffix_array {
    const static int alpha = 128;
    int getOrder(int a) const {
        return (a < (int) order.size() ? order[a] : 0);</pre>
public:
    int n;
    string s;
    vector<int> suf, order, lcp; // order store position of suffix i in suf array
    suffix_array(const string &s) : n(s.size() + 1), s(s) {
        suf = order = lcp = vector<int>(n);
        vector<int> bucket idx(n), newOrder(n), newsuff(n);
        vector<int> prev(n), head(alpha, -1);
```

```
for (int i = 0; i < n; i++) {
            prev[i] = head[s[i]];
            head[s[i]] = i;
        int buc = -1, idx = 0;
        for (int i = 0; i < alpha; i++) {</pre>
            if (head[i] == -1) continue;
            bucket_idx[++buc] = idx;
            for (int j = head[i]; ~j; j = prev[j])
                suf[idx++] = j, order[j] = buc;
        }
        int len = 1;
        do {
            auto cmp = [&](int a, int b) {
                if (order[a] != order[b])
                     return order[a] < order[b];</pre>
                return getOrder(a + len) < getOrder(b + len);</pre>
            };
            for (int i = 0; i < n; i++) {
                int j = suf[i] - len;
                if (j < 0)
                     continue;
                newsuff[bucket_idx[order[j]]++] = j;
            for (int i = 1; i < n; i++) {
                suf[i] = newsuff[i];
                bool cmpres = cmp(suf[i - 1], suf[i]);
                newOrder[suf[i]] = newOrder[suf[i - 1]] + cmpres;
                if (cmpres)
                     bucket idx[newOrder[suf[i]]] = i;
            }
            order = newOrder;
            len <<= 1;
        } while (order[suf[n - 1]] != n - 1);
    }
};
Z algorithm
/* z[i] equal the length of the longest substring starting from s[i]
   which is also a prefix of s */
vector<int> z_algo(string s) {
    int n = s.size();
    vector<int> z(n);
    z[0] = n;
    for (int i = 1, L = 1, R = 1; i < n; i++) {
        int k = i - L;
        if (z[k] + i >= R) {
            L = i;
            R = max(R, i);
            while (R < n \&\& s[R - L] == s[R]) R++;
            z[i] = R - L;
        } else z[i] = z[k];
    }
    return z;
}
```

## Math

### **Primes**

```
Sieve
const int N = 1e8;
bool isPrime[N + 1];
vector<int> prime;
void sieve() {
      memset(isPrime, true, sizeof(isPrime));
      isPrime[0] = isPrime[1] = false;
      for (int i = 4; i <= N; i += 2)
            isPrime[i] = false;
      for (int i = 3; i * i <= N; i += 2)
            if (isPrime[i])
                  for (int j = i * i; j <= N; j += i + i)
                        isPrime[j] = false;
      for (int i = 1; i <= N; i++)
            if (isPrime[i])
                  prime.push back(i);
}
Linear Sieve
const int N = 1e7;
int lpf[N + 1];
vector<int> prime;
void sieve() {
      for (int i = 2; i <= N; i++) {
            if (lpf[i] == 0) {
                  lpf[i] = i;
                  prime.push back(i);
            for (int j : prime) {
                  if (j > lpf[i] || 1LL * i * j > N)break;
                  lpf[i * j] = j;
            }
      }
}
Miller Rabin Primality Test
const int ITER = 4;
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
bool millerTest(ll n, ll d) {
    11 a = uniform int distribution<11>(2, n - 2)(rng);
    a = fpow(a, d, n);
    if (a == 1 || a == n - 1)
        return true;
    d <<= 1;
    while (d != n - 1) {
        a = a * a % n;
        if (a == 1) return false;
        if (a == n - 1) return true;
        d <<= 1;
    }
```

```
return false;
}
bool isPrime(ll n) {
    if (n <= 1) return false;</pre>
    if (n <= 3) return true;</pre>
    if (!(n & 1)) return false;
    11 d = n - 1;
    while (!(d & 1))
        d >>= 1;
    for (int i = 0; i < ITER; i++)
        if (!millerTest(n, d))
            return false;
    return true;
}
bool isPrimeSquare(ll n) {
    11 sq = round(sqrt(n));
    if (sq * sq < n) {
        sq++;
        if (sq * sq != n)return false;
    return isPrime(n);
}
int countDivisors(ll n) {
    // ans will contain total number of distinct
    // divisors
    int ans = 1;
    // Loop for counting factors of n
    for (int i = 2; 1LL * i * i * i <= n; i++) {
        // Calculating power of i in n.
        int cnt = 1; // cnt is power of prime i in n.
        while (n \% i == 0) // if i is a factor of n
        {
            n = n / i;
            cnt = cnt + 1; // incrementing power
        }
        // Calculating the number of divisors
        // If n = a^p * b^q then total divisors of n
        // are (p+1)*(q+1)
        ans = ans * cnt;
    }
    // If i is greater than cube root of n
    // First case
    if (isPrime(n))
        ans = ans << 1;
        // Second case
    else if (isPrimeSquare(n))
        ans = ans * 3;
        // Third case
    else if (n != 1)
        ans = ans << 2;
    return ans; // Total divisors
}
```

```
Prime Factors
```

```
// return number of Divisors(n) using prime factorization
11 numOfDivisors(primeFactors mp) {
      11 cnt = 1;
      for (auto it : mp) cnt *= (it.second + 1);
      return cnt;
}
// return sum of Divisors(n) using prime factorization
11 sumOfDivisors(primeFactors mp) {
      11 \text{ sum} = 1;
      for (auto it : mp) sum *= sumPower(it.first, it.second);
      return sum;
}
Phi function
11 phi function(ll n) {
      11 \text{ result} = n;
      primeFactors pf = prime_factors(n);
      for (auto &it : pf) {
            11 p = it.first;
            result -= (result / p);
      }
      return result;
}
void phi 1 to n(int n) {
      for (int i = 0; i <= n; i++)
            phi[i] = i;
      for (int i = 2; i <= n; i++)
            if (phi[i] == i)
                  for (int j = i; j <= n; j += i)
                         phi[j] -= phi[j] / i;
}
Moebius function
char mob[N];
bool prime[N];
void moebius() {
      memset(mob, 1, sizeof mob);
      memset(prime + 2, 1, sizeof(prime) - 2);
      \mathsf{mob}[0] = 0;
      mob[2] = -1;
      for (int i = 4; i < N; i += 2) {
            mob[i] *= (i & 3) ? -1 : 0;
            prime[i] = 0;
      }
      for (int i = 3; i < N; i += 2)
            if (prime[i]) {
                  mob[i] = -1;
                  for (int j = 2 * i; j < N; j += i) {</pre>
                         mob[j] *= j % (1LL * i * i) ? -1 : 0;
                         prime[j] = 0;
                  }
            }
}
```

```
Extended Euclidean
```

```
11 egcd(l1 a, l1 b, l1& x, l1& y) {
      if (a < 0) {
            auto g = egcd(-a, b, x, y);
            x *= -1;
            return g;
      if (b < 0) {
            auto g = egcd(a, -b, x, y);
            v *= -1;
            return g;
      }
      if (!b) {
            x = 1;
            y = 0;
            return a;
      }
      11 x1, y1;
      ll g = egcd(b, a % b, x1, y1);
      x = y1, y = x1 - y1 * (a / b);
      return g;
}
Linear Diophantine Equation
// return false if there is no solution
// return true if there exist a solution
// x, y are the solutions and g is the gcd between a and b
bool Diophantine_Solution(ll a, ll b, ll c, ll& x, ll& y, ll& g) {
      if (!a && !b) {
            if (c) return false;
            x = y = g = 0;
            return true;
      }
      g = egcd(a, b, x, y);
      if (c % g) return false;
      x *= c / g;
      y *= c / g;
      return true;
}
void shift_solution(11& x, 11& y, 11 a, 11 b, 11 cnt) {
      x += b * cnt;
      y -= a * cnt;
}
// find all number of solutions of ax + by = c
// x in range {minx, maxx}
// y in range {miny, maxy}
11 Diophantine_Solutions(11 a, 11 b, 11 c, 11 minx, 11 maxx, 11 miny, 11 maxy) {
      if (minx > maxx || miny > maxy) return 0;
      if (!a && !b && !c)
            return (maxx - minx + 1) * (maxy - miny + 1);
      if (!a && !b) return 0;
```

```
if (!a) {
      if (c % b) return 0;
      11 \text{ num} = c / b;
      return (num >= miny && num <= maxy) * (maxx - minx + 1);</pre>
if (!b) {
      if (c % a) return 0;
      11 \text{ num} = c / a;
      return (num >= minx && num <= maxx) * (maxy - miny + 1);</pre>
}
11 x, y, g;
if (!Diophantine Solution(a, b, c, x, y, g))
      return 0;
11 lx1, lx2, rx1, rx2;
// a * x + b * y = c
// (a / g) * x + (b / g) * y = c / g
a /= g, b /= g, c /= g;
g = 1;
int sign_a = (a > 0 ? 1 : -1);
int sign_b = (b > 0 ? 1 : -1);
// x + k * b >= minx
// k * b >= minx - x
// k >= (minx - x) / b
// k >= ceil((minx - x) / b)
shift_solution(x, y, a, b, (minx - x) / b);
// if x is less than minx so we need to increase it by one step only
// from the upove equation x + k * b >= minx
// if b is positive so choose k equal to 1 to increase x one
// if b is negattive so choose k equal to -1 because -1 * -1 = 1 ans also increase x
if (x < minx)
      shift_solution(x, y, a, b, sign_b);
if (x > maxx) return 0;
1x1 = x;
// x + k * b <= maxx
// k * b <= maxx - x
// k \le (maxx - x) / b
shift_solution(x, y, a, b, (maxx - x) / b);
if(x > maxx)
      shift_solution(x, y, a, b, -sign_b);
rx1 = x;
// y - k * a >= miny
// y - miny >= k * a
// k * a <= y - miny
// k <= (y - miny) / a
shift_solution(x, y, a, b, (y - miny) / a);
if (y < miny)</pre>
      shift_solution(x, y, a, b, -sign_a);
if (y > maxy) return 0;
1x2 = x;
// y - k * a <= maxy
// y - maxy <= k * a
// k * a >= y - maxy
// k >= (y - maxy) / a
shift_solution(x, y, a, b, (y - maxy) / a);
```

```
if (y > maxy)
            shift_solution(x, y, a, b, sign_a);
      if (1x2 > rx2) swap(1x2, rx2);
      // becuase we calculate the equations lx2, rx2 from shifting y
      // not from shifting x directly
      11 1x = max(1x1, 1x2);
      11 \text{ rx} = \min(\text{rx1}, \text{rx2});
      if (1x > rx) return 0;
      return (rx - lx) / abs(b) + 1;
}
Extended Euclidean for n variables
//O(n * log(m)) Memory & Time; coefficients.size() <= n, coefficients[i] <= m</pre>
// 0-based implementation
template<typename T>
T extended euclidean(const deque<T>& cof, deque<T>& var) {
      int n = cof.size();
      if (!cof.back()) {
            int cnt = 0, id = 0;
            for (int i = 0; i < n; i++)
                  if (!cof[i]) {
                         cnt++;
                         var[i] = 0;
                  }
                  else id = i;
            if (cnt >= n - 1) {
                  var[id] = 1;
                  return cof[id];
            deque<T> new cof, new var;
            for (int i = 0; i < n; i++)
                  if (cof[i]) {
                         new cof.push back(cof[i]);
                         new_var.push_back(var[i]);
                  }
            T g = extended euclidean(new cof, new var);
            for (int i = 0; !new_var.empty(); i++)
                  if (cof[i]) {
                         var[i] = new var.front();
                         new_var.pop_front();
            return g;
      deque<T> new_cof = cof;
      for (int i = 0; i < n - 1; i++)
            new_cof[i] %= new_cof.back();
      new cof.push front(new cof.back());
      new cof.pop back();
      var.push_front(var.back());
      var.pop_back();
      T g = extended_euclidean(new_cof, var);
      var.push back(var.front());
      var.pop front();
```

```
for (int i = 0; i < n - 1; i++)
            var.back() -= cof[i] / cof.back() * var[i];
      return g;
template<typename T>
vector<T> find any solution(const vector<T>& cof, T rhs) {
      int n = cof.size();
      if (!n)
            return vector<T>();
      deque<T> deque_cof(cof.begin(), cof.end()), deque_var(n);
      T g = extended_euclidean(deque_cof, deque_var);
      if (g && rhs % g)
            return vector<T>();
      vector<T> var(deque_var.begin(), deque_var.end());
      if (g) {
            rhs /= g;
            for (auto& it : var)
                  it *= rhs;
      }
      return var;
}
Sum Sequence
//return sum of sequence a, a+x , a+2x .... b
11 sumSequence(11 a, 11 b, 11 x) {
      a = ((a + x - 1) / x) * x;
      b = (b / x) * x;
      return (b + a) * (b - a + x) / (2 * x);
}
Sum Range Divisors
// return sum of divisors for all number from 1 to n //O(n)
11 sumRangeDivisors(int n) {
      11 \text{ ans} = 0;
      for (int x = 1; x <= n; x++)
            ans += (n / x) * x;
      return ans;
}
// calc 1e9 in 42ms, can calc more but need big integer
11 sumRangeDivisors(11 x) {
      11 ans = 0, left = 1, right;
      for (; left <= x; left = right + 1) {</pre>
            right = \times / (\times / left);
            ans += (x / left) * (left + right) * (right - left + 1) / 2;
      }
      return ans;
}
```

### **Combinatorics**

```
* nCr = n!/((n-r)! * r!)
 * nCr(n,r) = nCr(n,n-r)
 * nPr = n!/(n-r)!
 * nPr(circle) = nPr/r
 * nCr(n,r) = pascal[n][r]
 * catalan[n] = nCr(2n,n)/(n+1)
ull nCr(int n, int r) {
      if(r > n)
            return 0;
      r = max(r, n - r);
      ull ans = 1, div = 1, i = r + 1;
      while (i <= n) {
            ans *= i++;
            ans /= div++;
      }
      return ans;
}
ull nPr(int n, int r) {
      if (r > n)
            return 0;
      ull p = 1, i = n - r + 1;
      while (i <= n)</pre>
            p *= i++;
      return p;
}
// return catalan number n-th using dp O(n^2)//max = 35 then overflow
vector<ull> catalanNumber(int n) {
      vector<ull> catalan(n + 1);
      catalan[0] = catalan[1] = 1;
      for (int i = 2; i <= n; i++) {
            ull& rt = catalan[i];
            for (int j = 0; j < n; j++)
                  rt += catalan[j] * catalan[n - j - 1];
      return catalan;
}
// count number of paths in matrix n*m
// go to right or down only
ull countNumberOfPaths(int n, int m) {
      return nCr(n + m - 2, n - 1);
}
nCr pre calculation
const int N = 1e5 + 100;
const int mod = 1e9 + 7;
11 fact[N];
11 inv[N]; //mod inverse for i
11 invfact[N]; //mod inverse for i!
```

```
void factInverse() {
      fact[0] = inv[1] = fact[1] = invfact[0] = invfact[1] = 1;
      for (long long i = 2; i < N; i++) {</pre>
            fact[i] = (fact[i - 1] * i) % mod;
            inv[i] = mod - (inv[mod % i] * (mod / i) % mod);
            invfact[i] = (inv[i] * invfact[i - 1]) % mod;
      }
}
11 nCr(int n, int r) {
      if (r > n) return 0;
      return (((fact[n] * invfact[r]) % mod) * invfact[n - r]) % mod;
}
Matrices
typedef vector<int> row;
typedef vector<row> matrix;
matrix initial(int n, int m, int val = 0) {
      return matrix(n, row(m, val));
}
matrix identity(int n) {
      matrix rt = initial(n, n);
      for (int i = 0; i < n; i++)rt[i][i] = 1;
      return rt;
}
matrix addIdentity(const matrix& a) {
      matrix rt = a;
      for (int i = 0; i < sz(a); i++)rt[i][i] += 1;
      return rt;
}
matrix add(const matrix& a, const matrix& b) {
      matrix rt = initial(sz(a), sz(a[0]));
      for (int i = 0; i < sz(a); i++)for (int j = 0; j < sz(a[0]); j++)
            rt[i][j] = a[i][j] + b[i][j];
      return rt;
matrix multiply(const matrix& a, const matrix& b) {
      matrix rt = initial(sz(a), sz(b[0]));
      for (int i = 0; i < sz(a); i++) for (int k = 0; k < sz(a[0]); k++) {
            if (a[i][k] == 0)continue;
            for (int j = 0; j < sz(b[0]); j++)
                  rt[i][j] += a[i][k] * b[k][j];
      }
      return rt;
}
matrix power(const matrix& a, 11 k) {
      if (k == 0)return identity(sz(a));
      if (k & 1)return multiply(a, power(a, k - 1));
      return power(multiply(a, a), k >> 1);
}
```

```
matrix power_itr(matrix a, 11 k) {
      matrix rt = identity(sz(a));
      while (k) {
            if (k & 1)rt = multiply(rt, a);
            a = multiply(a, a); k >>= 1;
      }
      return rt;
}
matrix sumPower(const matrix& a, 11 k) {
      if (k == 0)return initial(sz(a), sz(a));
      if (k & 1)return multiply(a, addIdentity(sumPower(a, k - 1)));
      return multiply(sumPower(a, k >> 1), addIdentity(power(a, k >> 1)));
}
/* return matrix contains
    a^k
a^1+a^2.. a^k
                Τ
*/
matrix sumPowerV2(const matrix& a, 11 k) {
      int n = sz(a);
      matrix rt = initial(2 * n, 2 * n);
      for (int i = 0; i < 2 * n; i++)
            for (int j = 0; j < n; j++)</pre>
                  rt[i][j] = a[i % n][j];
      for (int i = n; i < 2 * n; i++)rt[i][i] = 1;
      return power(rt, k);
}
Matrix class
struct matrix {
      using T = int;
      using row = vector<T>;
      vector<vector<T>> v;
      matrix() {}
      matrix(int n, int m, T val = 0) : v(n, row(m, val)) {
      int size() const {
            return v.size();
      int cols() const {
            return v[0].size();
      }
      matrix operator*(T a) const {
            matrix rt = *this;
            REP(i, rt.size())
                  REP(j, rt.cols())
                  rt.v[i][j] *= a;
            return rt;
      }
      friend matrix operator*(T a, const matrix& b) {
            return (b * a);
      }
```

```
friend matrix operator+(const matrix& a, const matrix& b) {
            assert(a.size() == b.size() && a.cols() == b.cols());
            matrix rt(a.size(), a.cols());
            REP(i, rt.size()) REP(j, rt.cols())
                  rt.v[i][j] = a.v[i][j] + b.v[i][j];
            return rt;
      friend matrix operator*(const matrix& a, const matrix& b) {
            assert(a.cols() == b.size());
            matrix rt(a.size(), b.cols());
            REP(i, rt.size()) REP(k, a.cols()) {
                  if (a.v[i][k] == 0) continue;
                  REP(j, rt.cols()) rt.v[i][j] += a.v[i][k] * b.v[k][j];
            return rt;
      }
};
matrix identity(int n) {
      matrix r(n, n);
      for (int i = 0; i < n; i++)
            r.v[i][i] = 1;
      return r;
}
matrix addIdentity(const matrix& a) {
      matrix rt = a;
      REP(i, a.size()) rt.v[i][i]++;
      return rt;
matrix power(matrix a, long long y) {
      assert(y >= 0 && a.size() == a.cols());
      matrix rt = identity(a.size());
      while (y > 0) {
            if (y & 1)
                  rt = rt * a;
            a = a * a;
            ∨ >>= 1;
      }
      return rt;
}
matrix sumPower(const matrix& a, 11 k) {
      if (k == 0)
            return matrix(sz(a), sz(a));
      if (k & 1)
            return a * addIdentity(sumPower(a, k - 1));
      return (sumPower(a, k >> 1) * addIdentity(power(a, k >> 1)));
}
/* return matrix contains
    a^k
                0
a^1+a^2.. a^k
                Ι
*/
```

```
matrix sumPowerV2(const matrix& a, 11 k) {
      int n = sz(a);
      matrix rt(2 * n, 2 * n);
      REP(i, n) REP(j, n) {
            rt.v[i][j] = a.v[i][j];
            rt.v[i + n][j] = a.v[i][j];
      for (int i = n; i < 2 * n; i++)</pre>
            rt.v[i][i] = 1;
      return power(rt, k);
}
Mod
Fast power
11 power(ll x, ll y, int mod) {
    if (y == 0) return 1;
    if (y == 1) return x % mod;
    ll r = power(x, y \gg 1, mod);
    return (((r * r) % mod) * power(x, y & 1, mod)) % mod;
}
Sum of powers
// return a ^ 1 + a ^ 2 + a ^ 3 + .... a ^ k
11 sumPower(11 a, 11 k, int mod) {
      if (k == 1) return a % mod;
      11 half = sumPower(a, k / 2, mod);
      11 p = half * power(a, k / 2, mod) % mod;
      p = (p + half) \% mod;
      if (k & 1) p = (p + power(a, k, mod)) % mod;
      return p;
}
Mod Inverse
11 modInverse(11 b, 11 mod) { // if mod is Prime
    return power(b, mod - 2, mod);
11 modInverse(ll b, ll mod) { // if mod is not Prime,gcd(a,b) must be equal 1
    return power(b, phi_function(mod) - 1, mod);
}
```

```
(a^n)%p=result, return n
// (a^n)%p=result, return minimum n
int getPower(int a, int result, int mod) {
      int sq = sqrt(mod);
      map<int, int> mp;
      11 r = 1;
      for (int i = 0; i < sq; i++) {
            if (mp.find(r) == mp.end())
                  mp[r] = i;
            r = (r * a) \% mod;
      }
      11 tmp = modInverse(r, mod);
      11 cur = result;
      for (int i = 0; i <= mod; i += sq) {</pre>
            if (mp.find(cur) != mp.end())
                  return i + mp[cur];
            cur = (cur * tmp) % mod;//val/(a^sq)
      }
      return INF;
}
// Returns minimum x for which a ^x % m = b % m.
// a,m not not coprime
int getPower(int a, int b, int m) {
      a \%= m, b \%= m;
      int k = 1, add = 0, g;
      while ((g = \_gcd(a, m)) > 1) {
            if (b == k)
                  return add;
            if (b % g)
                  return -1;
            b /= g, m /= g, ++add;
            k = (k * 111 * a / g) % m;
      }
      int n = sqrt(m) + 1;
      int an = 1;
      for (int i = 0; i < n; ++i)</pre>
            an = (an * 111 * a) % m;
      unordered map<int, int> vals;
      for (int q = 0, cur = b; q <= n; ++q) {
            vals[cur] = q;
            cur = (cur * 1ll * a) % m;
      }
      for (int p = 1, cur = k; p <= n; ++p) {</pre>
            cur = (cur * 111 * an) % m;
            if (vals.count(cur)) {
                  int ans = n * p - vals[cur] + add;
                  return ans;
            }
      }
      return -1;
}
```

```
CRT
11 C
```

```
11 CRT(vector<11>& a, vector<11>& m){
      11 lcm = m[0], rem = a[0];
      int n = a.size();
      for(int i = 1; i < n; i++){</pre>
            11 x, y;
            11 gcd = extended_euclidean(lcm, m[i], x, y);
            if((a[i] - rem) % gcd) return -1;
            11 tmp = m[i] / gcd, f = (a[i] - rem) / gcd;
            x = ((x \% tmp) * (f \% tmp)) \% tmp;
            rem += 1cm * x;
            lcm = lcm * m[i] / gcd;
            rem = (rem % lcm + lcm) % lcm;
      }
      return rem;
}
FFT
typedef valarray<complex<double>> polynomial;
vector<complex<double>> CM1[3][LGN + 1];
const double PI = acos(-1);
void prepare() {
      for (int sign = -1; sign <= 1; sign += 2) {
            for (int i = 0; i <= LGN; i++) {
                  int N = 1 \ll i;
                  double theta = sign * 2 * PI / N;
                  complex<double> cm1 = 1;
                  complex<double> cm2(cos(theta), sin(theta));
                  for (int j = 0; j < N / 2; j++) {
                        CM1[sign + 1][i].push_back(cm1);
                        cm1 *= cm2;
                  }
            }
      }
}
void fft(polynomial &a, int sign = -1) {
      int N = a.size();
      int lgn = log2(N);
      for (int m = N; m >= 2; m >>= 1, lgn--) {
            int mh = m >> 1;
            for (int i = 0; i < mh; i++) {</pre>
                  const complex<double> &w = CM1[sign + 1][lgn][i];
                  for (int j = i; j < N; j += m) {
                        int k = j + mh;
                        complex<double> x = a[j] - a[k];
                        a[j] += a[k];
                        a[k] = w * x;
                  }
            }
      }
```

```
int i = 0;
      for (int j = 1; j < N - 1; j++) {
            for (int k = N >> 1; k > (i ^= k); k >>= 1)
            if(j < i)
                   swap(a[i], a[j]);
      }
}
void inv_fft(polynomial &a) {
      complex<double> N = a.size();
      fft(a, 1);
      a /= N;
valarray<int> mul(const valarray<int> &a, const valarray<int> &b) {
      int adeg = (int) a.size() - 1, bdeg = (int) b.size() - 1;
      int N = 1;
      while (N <= adeg + bdeg)</pre>
            N <<= 1;
      polynomial A(N), B(N);
      for (int i = 0; i < a.size(); i++)</pre>
            A[i] = a[i];
      for (int i = 0; i < b.size(); i++)</pre>
            B[i] = b[i];
      fft(A);
      fft(B);
      polynomial m = A * B;
      inv fft(m);
      valarray<int> rt(N);
      for (int i = 0; i < N; i++)</pre>
            rt[i] = round(m[i].real());
      return rt;
}
NTT
typedef valarray<modint> polynomial;
vector<modint> CM1[2][LGN + 1];
bool validRoot(modint root) {
      modint rootinv = modint(1) / root;
      for (int invert = 0; invert <= 1; invert++) {</pre>
            for (int i = 1; i <= LGN; i++) {
                   int N = 1 \ll i;
                   assert((MOD - 1) % N == 0);
                   int C = (MOD - 1) / N;
                   modint cm2 = modint::power(invert ? root : rootinv, C);
                   if (cm2.val <= 1) return false;</pre>
            }
      }
      return true;
}
```

```
void prepare() {
      modint root = 2;
      while (!validRoot(root)) root += 1;
      modint rootinv = modint(1) / root;
      for (int invert = 0; invert <= 1; invert++) {</pre>
            for (int i = 0; i <= LGN; i++) {</pre>
                   int N = 1 \ll i;
                   int C = (MOD - 1) / N;
                   modint cm2 = modint::power(invert ? root : rootinv, C);
                   modint cm1 = 1;
                   set<int> st;
                   for (int j = 0; j < N / 2; j++) {
                         CM1[invert][i].push_back(cm1);
                         cm1 *= cm2;
                   }
            }
      }
void fft(polynomial& a, bool invert = 0) {
      int N = a.size();
      int lgn = log2(N);
      for (int m = N; m >= 2; m >>= 1, lgn--) {
            int mh = m >> 1;
            for (int i = 0; i < mh; i++) {</pre>
                   const modint& w = CM1[invert][lgn][i];
                   for (int j = i; j < N; j += m) {
                         int k = j + mh;
                         modint x = a[j] - a[k];
                         a[j] += a[k];
                         a[k] = w * x;
                   }
            }
      }
      int i = 0;
      for (int j = 1; j < N - 1; j++) {
            for (int k = N \gg 1; k \gg (i ^= k); k \gg 1) continue;
            if (j < i)swap(a[i], a[j]);</pre>
      }
}
void inv_fft(polynomial& a) {
      int N = a.size();
      fft(a, 1);
      a /= N;
valarray<modint> mul(const polynomial& a, const polynomial& b) {
      int adeg = (int)a.size() - 1, bdeg = (int)b.size() - 1;
      int N = 1;
      while (N <= adeg + bdeg)</pre>
            N <<= 1;
      polynomial A(N), B(N);
      for (int i = 0; i < a.size(); i++)</pre>
            A[i] = a[i];
      for (int i = 0; i < b.size(); i++)</pre>
            B[i] = b[i];
```

```
fft(A);
      fft(B);
      polynomial rt = A * B;
      inv_fft(rt);
      return rt;
}
Misc
Bitmask
bool getBit(ll num, int ind) {
      return ((num >> ind) & 1);
}
11 setBit(ll num, int ind, bool val) {
      return val ? (num | (1LL << ind)) : (num & ~(1LL << ind));</pre>
}
11 flipBit(ll num, int ind) {
      return (num ^ (1LL << ind));</pre>
}
11 leastBit(ll num) {
      return (num & -num);
}
template<class Int>
Int turnOnLastZero(Int num) {
      return num | num + 1;
}
template<class Int>
Int turnOnLastConsecutiveZeroes(Int num) {
      return num | num - 1;
}
template<class Int>
Int turnOffLastBit(Int num) {
      return num & num - 1;
}
template<class Int>
Int turnOffLastConsecutiveBits(Int num) {
      return num & num + 1;
//num%mod, mod is a power of 2
11 Mod(11 num, 11 mod) {
      return (num & mod - 1);
}
bool isPowerOfTwo(11 num) {
      return (num & num - 1) == 0;
}
void genAllSubmask(int mask) {
      for (int subMask = mask;; subMask = (subMask - 1) & mask) {
            //code
            if (subMask == 0)
                  break;
      }
```

}

```
/*
     builtin functions:
      builtin popcount -> used to count the number of one's
     builtin clz -> used to count the leading zeros of the integer
      builtin ctz -> used to count the trailing zeros of the integer
int LOG2(int x) { //floor(log2(x))
      return 31 - __builtin_clz(x);
}
int LOG2(long long x) { //floor(log2(x))
      return 63 - __builtin_clzll(x);
}
Coordinate Compress
void coordinateCompress(vector<int>& axes, vector<int>& iToV,
      map<int, int> vToI, int start = 2, int step = 2) {
      for (auto& it : axes) vToI[it] = 0;
      iToV.resize(start + step * vToI.size());
      int idx = 0;
      for (auto& it : vToI) {
            it.second = start + step * idx++;
            iToV[it.second] = it.first;
      }
}
Random numbers
#include <chrono>
#include <random>
//write this line once in top
mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count()* ((uint64_t) new char
1));
// use this instead of rand()
template<typename T> T Rand(T low, T high) {
      return uniform_int_distribution<T>(low, high)(rng);
}
Custom hash
struct custom hash {
      static uint64_t splitmix64(uint64_t x) {
            x += 0x9e3779b97f4a7c15;
            x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
            x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
            return \times ^ (\times >> 31);
      }
      size_t operator()(pair<uint64_t, uint64_t> x) const {
            static const uint64_t FIXED_RANDOM =
chrono::steady clock::now().time since epoch().count();
            return splitmix64(x.first + FIXED_RANDOM) ^ (splitmix64(x.second +
FIXED RANDOM) >> 1);
      size_t operator()(uint64_t x) const {
            static const uint64 t FIXED RANDOM =
chrono::steady_clock::now().time_since_epoch().count();
            return splitmix64(x + FIXED_RANDOM);
      }
};
```

## Max histogram area

```
int maxHistogramArea(vector<int> v) {
      stack<int> st;
      int maxArea = 0, area = 0, i = 0;
      while (i < sz(v)) {
            if (st.empty() || v[st.top()] <= v[i])</pre>
                  st.push(i++);
            else {
                  int top = st.top(); st.pop();
                  if (st.empty()) area = v[top] * i;
                  else area = v[top] * (i - st.top() - 1);
                  maxArea = max(maxArea, area);
            }
      }
      while (!st.empty()) {
            int top = st.top(); st.pop();
            if (st.empty())
                  area = v[top] * i;
            else area = v[top] * (i - st.top() - 1);
            maxArea = max(maxArea, area);
      }
      return maxArea;
}
```

## **Sorting**

```
long long cnt = 0;
vector<int> v, temp;
// e the first index not have in range array
// like end()
template<class T = less<int>>
void merge_sort(int s, int e, T cmp = less<int>()) {
      if (s + 1 >= e) return;
      int m = s + (e - s >> 1);
      merge_sort(s, m, cmp);
      merge_sort(m, e, cmp);
      for (int i = s; i < e; i++)
            temp[i] = v[i];
      int i = s, j = m, k = s;
      while (i < m && j < e)
            if (cmp(temp[i], temp[j]))
                  v[k++] = temp[i++];
            else
                  v[k++] = temp[j++], cnt += j - k;
      while (i < m)
            v[k++] = temp[i++];
      while (j < e)
            v[k++] = temp[j++];
}
// O(n*log(n)/log(base))
// O(n + base) memory
void radix_sort(vector<int>& v, int base) {
      vector<int> tmp(v.size());
      for (int it = 0, p = 1; it < 10; it++, p *= base) {
            vector<int> frq(base);
            for (auto& it : v)
                  frq[(it / p) % base]++;
            for (int i = 1; i < base; i++)</pre>
                  frq[i] += frq[i - 1];
            for (int i = v.size() - 1; i >= 0; i--)
                  tmp[--frq[(v[i] / p) \% base]] = v[i];
            \vee = tmp;
      }
}
void quick_sort(int s, int e) {
      if (s >= e) return;
      int j = rand() \% (e - s + 1) + s;
      swap(v[s], v[j]);
      j = s;
      int pivot = v[s];
      for (int i = s + 1; i <= e; i++)
            if (v[i] <= pivot)</pre>
                  swap(v[i], v[++j]);
      swap(v[s], v[j]);
      quick_sort(s, j - 1);
      quick_sort(j + 1, e);
}
```

## LIS binary Search

```
/* without build
 * make upper_bound if can take equal elements */
int LIS(const vector<int>& v) {
      vector<int> lis(v.size());//put value less than zero if needed
      int 1 = 0;
      for (int i = 0; i < sz(v); i++) {
            int idx = lower_bound(lis.begin(), lis.begin() + 1, v[i]) - lis.begin();
            if (idx == 1)
                  1++;
            lis[idx] = v[i];
      }
      return 1;
}
void LIS_binarySearch(vector<int> v) {
      int n = v.size();
      vector<int> last(n), prev(n, -1);
      int length = 0;
      auto BS = [&](int val) {
            int st = 1, ed = length, md, rt = length;
            while (st <= ed) {</pre>
                  md = st + ed \gg 1;
                  if (v[last[md]] >= val)
                         ed = md - 1, rt = md;
                  else st = md + 1;
            return rt;
      };
      for (int i = 1; i < n; i++) {
            if (v[i] < v[last[0]])</pre>
                  last[0] = i;
            else if (v[i] > v[last[length]]) {
                  prev[i] = last[length];
                  last[++length] = i;
            }
            else {
                  int index = BS(v[i]);
                  prev[i] = last[index - 1];
                  last[index] = i;
            }
      }
      cout << length + 1 << "\n";</pre>
      vector<int> out;
      for (int i = last[length]; i >= 0; i = prev[i])
            out.push back(v[i]);
      reverse(out.begin(), out.end());
      for (auto it : out)
            cout << it << endl;</pre>
}
```

```
Mo algorithm
int sqrtN; //use a constent value
struct query {
      int 1, r, qIdx, block;
      query(int 1, int r, int qIdx) : 1(1), r(r), qIdx(qIdx), block(1 / sqrtN) {}
      bool operator <(const query& o) const {</pre>
            if (block != o.block) return block < o.block;</pre>
            return (block % 2 == 0 ? r < o.r : r > o.r);
      }
};
int curL, curR, ans;
vector<query> q;
void add(int index);
void remove(int index);
void solve(int 1, int r) {
      while (curL > 1) add(--curL);
      while (curR < r) add(++curR);</pre>
      while (curL < 1) remove(curL++);</pre>
      while (curR > r) remove(curR--);
}
vector<int> MO(int n) {
      vector<int> rt(q.size());
      ans = curL = curR = 0;
      add(0);
      sort(q.begin(), q.end());
      for (auto it : q) {
            solve(it.l, it.r);
            rt[it.qIdx] = ans;
      return rt;
}
floyd cycle detection algorithm
template<class IntFunction>
pair<int, int> find_cycle_floyd(IntFunction f, int x0) {
      int tortoise = f(x0), hare = f(f(x0));
      while (tortoise != hare) {
            tortoise = f(tortoise);
            hare = f(f(hare));
      int start = 0;
      tortoise = x0;
      while (tortoise != hare) {
            tortoise = f(tortoise);
            hare = f(hare);
            start++;
      int length = 1;
      hare = f(tortoise);
      while (tortoise != hare) {
            hare = f(hare);
            length++;
      }
      return make_pair(start, length);
}
```

# **Convex Hull Trick (Line Container)** struct Line { 11 m, c; mutable ll p; //p is intersection between cur and next bool operator<(const Line &o) const {</pre> //change to (m>o.m,c < o.c) to get min</pre> **if** (m != o.m) return m < o.m;</pre> return c > o.c; } bool operator<(11 x) const {</pre> return p < x;</pre> } **}**; struct LineContainer: multiset<Line, less<>>> { // (for doubles, use inf = INFINITY, div(a,b) = a/b) static const 11 inf = LLONG\_MAX; 11 div(11 a, 11 b) { // floored division return a / b - ((a ^ b) < 0 && a % b); bool isect(iterator x, iterator y) { if (y == end())return x->p = inf, 0; if (x->m == y->m)x->p = inf;else x->p = div(y->c - x->c, x->m - y->m);return x->p >= y->p; } void add(ll m, ll c) { auto z = insert( { m, c, 0 }), y = z++, x = y; while (isect(y, z)) z = erase(z);if (x != begin() && isect(--x, y)) isect(x, y = erase(y)); while ((y = x) != begin() && (--x)->p >= y->p)isect(x, erase(y)); 11 query(11 x) { assert(!empty()); auto 1 = \*lower bound(x);return 1.m \* x + 1.c;} }; **Iava Scanner** static class MScanner { StringTokenizer st; BufferedReader br; public MScanner(InputStream system) {

br = new BufferedReader(new InputStreamReader(system));

}

```
public MScanner(String file) throws Exception {
      br = new BufferedReader(new FileReader(file));
}
public String next() throws IOException {
     while (st == null !st.hasMoreTokens())
            st = new StringTokenizer(br.readLine());
     return st.nextToken();
}
public String nextLine() throws IOException {
     return br.readLine();
public int nextInt() throws IOException {
      return Integer.parseInt(next());
}
public double nextDouble() throws IOException {
     return Double.parseDouble(next());
public char nextChar() throws IOException {
     return next().charAt(0);
public long nextLong() throws IOException {
      return Long.parseLong(next());
public int[] intArr(int n) throws IOException {
      int[]in = new int[n]; for (int i = 0; in; i++)in[i] = nextInt();
     return in;
public long[] longArr(int n) throws IOException {
      long[]in = new long[n]; for (int i = 0; in; i++)in[i] = nextLong();
     return in;
public int[] intSortedArr(int n) throws IOException {
      int[]in = new int[n]; for (int i = 0; in; i++)in[i] = nextInt();
      shuffle(in);
     Arrays.sort(in);
     return in;
}
public long[] longSortedArr(int n) throws IOException {
      long[]in = new long[n]; for (int i = 0; in; i++)in[i] = nextLong();
      shuffle(in);
     Arrays.sort(in);
     return in;
}
static void shuffle(int[]in) {
      for (int i = 0; iin.length; i++) {
            int idx = (int)(Math.random()in.length);
            int tmp = in[i];
            in[i] = in[idx];
            in[idx] = tmp;
      }
}
static void shuffle(long[]in) {
     for (int i = 0; iin.length; i++) {
            int idx = (int)(Math.random()in.length);
            long tmp = in[i];
```

```
in[i] = in[idx];
                  in[idx] = tmp;
            }
     }
      public Integer[] IntegerArr(int n) throws IOException {
            Integer[]in = new Integer[n]; for (int i = 0; in; i++)in[i] = nextInt();
            return in;
      }
     public Long[] LongArr(int n) throws IOException {
            Long[]in = new Long[n]; for (int i = 0; in; i++)in[i] = nextLong();
            return in;
     }
      public boolean ready() throws IOException {
            return br.ready();
      }
      public void waitForInput() throws InterruptedException {
            Thread.sleep(3000);
     }
}
```

## **Geometry**

point

```
#define 11 long long
typedef long double ld;
typedef complex<double> point; // it can be long long not double
template<class T>
istream& operator>>(istream& is, complex<T>& p) {
      T value;
      is >> value:
      p.real(value);
      is >> value;
      p.imag(value);
      return is;
#define PI acos(-1.0)
#define EPS 1e-8
#define X real()
#define Y imag()
#define angle(a) (atan2((a).imag(), (a).real())) // angle with orignial
#define length(a) (hypot((a).imag(), (a).real()))
#define vec(a,b) ((b)-(a))
#define dp(a,b)
                  ( (conj(a)*(b)).real() )
#define cp(a,b)
                  ( (conj(a)*(b)).imag() ) product = area of parllelogram
#define normalize(a)
                        (a)/length(a)
// norm(a) // return x^2 + y^2 //a is point //can use dp(a,a)
bool same(point p1, point p2) {// check to points same or not
      return dp(vec(p1, p2), vec(p1, p2)) < EPS;
}
rotate
point rotate(point p, double angle, point around = point(0, 0)) {
      p -= around;
      return (p * exp(point(0, angle))) + around;
}
reflect
// Refelect v around m and origin
point reflect0(point v, point m) {
      return conj(v / m) * m;
}
// Refelect point p around 11-12
point reflect(point p, point 11, point 12) {
      point z = p - 11, w = 12 - 11;
      return conj(z / w) * w + 11;
}
```

```
Triangles
/*
 sin(A)/a = sin(B)/b = sin(C)/c
 a^2 = b^2 + c^2 - 2b*c*cos(A)
 sin(A+B) = sin(A) * cos(B) + sin(B) * cos(A)
 sin(A-B) = sin(A) * cos(B) - sin(B) * cos(A)
 cos(A+B) = cos(A) * cos(B) - sin(A) * sin(B)
 cos(A-B) = cos(A) * cos(B) + sin(A) * sin(B)
 tan(A+B) = (tan(A) + tan(B))/(1 - tan(A) * tan(B))
 tan(A-B) = (tan(A) - tan(B))/(1 - tan(A) * tan(B))
 */
Get Angles/Sides
double fixAngle(double A) {
      return A > 1 ? 1 : (A < -1 ? -1 : A);
// return min angle: aOb / bOa
// dp(v1, v2) = |v1|*|v2|*cos(theta)
double angleO(point a, point 0, point b) {
      point v1(a - 0), v2(b - 0);
      return acos(fixAngle(dp(v1, v2) / dist(v1) / dist(v2)));
}
double getSide_a_bAB(double b, double A, double B) {
      return (sin(A) * b) / sin(B);
}
double getAngle_A_abB(double a, double b, double B) {
      return asin(fixAngle((a * sin(B)) / b));
}
// give me wrong answer in team formation :D
double getAngle_A_abc(double a, double b, double c) {
      return acos(fixAngle((b * b + c * c - a * a) / (2 * b * c)));
}
double triangleArea(double a, double b, double c) {
      double s = (a + b + c) / 2.0;
      return sqrt((s - a) * (s - b) * (s - c) * s);
double triangleArea(point p0, point p1, point p2) {
      double a = length(vec(p1, p0)), b = length(vec(p2, p0)), c = length(
                  vec(p2, p1));
      return triangleArea(a, b, c);
}
Point In Triangle
bool pointInTriangle(point a, point b, point c, point pt) {
      11 s1 = fabs(cp(vec(a,b), vec(a,c)));
      11 s2 = fabs(cp(vec(pt,a), vec(pt,b))) + fabs(cp(vec(pt, b), vec(pt, c)))
                  + fabs(cp(vec(pt, a), vec(pt, c)));
      return s1 == s2;
}
```

```
Get largest Circle Inside the triangle
//A triangle with area A and semi-perimeter s has an inscribed circle (incircle) with
//radius r = A/s
bool circleInTriangle(point a, point b, point c, point& ctr, double& r) {
    double ab = length(a - b), bc = length(b - c),
```

}

}

}

}

}

Lines

**IsCollinear** 

//else not

**isPointOnRay** 

//else not

**isPointOnSegment** 

//o = anlge(a) - angle(b)

//o = anlge(a) - angle(b)
//if o = 0 isPointOnRay a->b

//if o = 0 || o = 180 isCollinear

bool isCollinear(point a, point b, point c) {

bool isPointOnRay(point a, point b, point c) {

bool isPointOnRay(point a, point b, point c) {

if (length(vec(a, c)) < EPS) return true;</pre>

bool isPointOnSegment(point a, point b, point c) {

bool isPointOnSegment(point a, point b, point c) {

return dcmp(acb - (ac + cb), 0) == 0;

double distToLine(point p0, point p1, point p2) {

if (!isCollinear(a, b, c))
 return false;

return fabs(cp(vec(a, b), vec(a, c))) < EPS;</pre>

return dcmp(dp(vec(a, b), vec(a, c)), 0) == 1;

return same(normalize(vec(a, b)), normalize(vec(a, c)));

return isPointOnRay(a, b, c) && isPointOnRay(b, a, c);

return fabs(cp(vec(p0, p1), vec(p0, p2)) / length(vec(p1, p0)));

double acb = length(vec(b, a)), ac = length(vec(c, a)), cb = length(vec(c, b));

ca = length(c - a);
double s = 0.5 \* (ab + bc + ca);
r = triangleArea(ab, bc, ca) / s;

if (fabs(r) < EPS) return 0; // no inCircle center</pre>

point p1 = b + (vec(b, c) \* (ratio / (1 + ratio)));

point p2 = a + (vec(a, c) \* (ratio / (1 + ratio)));

return intersectSegments(a, p1, b, p2, ctr); // get their intersection point

double ratio = length(a - b) / length(a - c);

ratio = length(b - a) / length(b - c);

distToLine

// dist point p2 to line p0-p1

```
distToSegment
//minimum distance from point p2 to segment p0-p1
double distToSegment(point p0, point p1, point p2) {
      double d1, d2;
      point v1 = p1 - p0, v2 = p2 - p0;
      if ((d1 = dp(v1, v2)) \le 0) return length(vec(p0, p2));
      if ((d2 = dp(v1, v1)) \leftarrow d1) return length(vec(p1, p2));
      double t = d1 / d2;
      return length(vec((p0 + v1 * t), p2));
}
pointToSegment
// minimum point in segment po-p1 to point p2
point pointToSegment(point p0, point p1, point p2) {
      double d1, d2;
      point v1 = p1 - p0, v2 = p2 - p0;
      if ((d1 = dp(v1, v2)) \le 0) return p0;
      if ((d2 = dp(v1, v1)) <= d1) return p1;</pre>
      double t = d1 / d2;
      return (p0 + v1 * t);
}
intersectSegments
// return point intersect in line a-b with c-d using parametric equations
bool intersectSegments(point a, point b, point c, point d, point& intersect) {
      double d1 = cp(vec(b, a), vec(c, d)), d2 = cp(vec(c, a), vec(c, d)), d3 = cp(vec(b, a))
a), vec(c, a));
      if (fabs(d1) < EPS)</pre>
            return false; // Parllel || identical
      double t1 = d2 / d1, t2 = d3 / d1;
      intersect = a + (b - a) * t1;
      if (t1 < -EPS || t2 < -EPS || t2 > 1 + EPS)
            return false; //e.g ab is ray, cd is segment ... change to whatever
      return true;
}
CCW
// return 1 if point c is counter-clockwise about segment a-b
// -1 if point c is clockwise about segment a-b
// 0 if c is isCollinear about a-b
int ccw(point a, point b, point c) {
      point v1(b - a), v2(c - a);
      double t = cp(v1, v2);
      if (t > EPS)
            return 1;
      if (t < -EPS)</pre>
            return -1;
      if (v1.X * v2.X < -EPS || v1.Y * v2.Y < -EPS)
            return -1;
      if (norm(v1) < norm(v2) - EPS)
            return 1;
      return 0;
```

}

```
Find circle passes with 3 points
// 2 points has infinite circles
// Find circle passes with 3 points, some times, there is no circle! (in case colinear)
// Draw two perpendicular lines and intersect them
pair<double, point> findCircle(point a, point b, point c) {
      //create median, vector, its prependicular
      point m1 = (b + a) * 0.5, v1 = b - a, pv1 = point(v1.Y, -v1.X);
      point m2 = (b + c) * 0.5, v2 = b - c, pv2 = point(v2.Y, -v2.X);
      point end1 = m1 + pv1, end2 = m2 + pv2, center;
      intersectSegments(m1, end1, m2, end2, center);
      return make pair(length(vec(center, a)), center);
}
intersectLineCircle
// If line intersect cirlce at point p, and p = p0 + t(p1-p0)
// Then (p-c)(p-c) = r^2 substitute p and rearrange
//(p1-p0)(p1-p0)t^2 + 2(p1-p0)(p0-C)t + (p0-C)(p0-C) = r*r; -> Quadratic
vector<point> intersectLineCircle(point p0, point p1, point C, double r) {
      double a = dp(vec(p0, p1), vec(p0, p1)), b = 2 * dp(vec(p0, p1), vec(C, p0)),
            c = dp(vec(C, p0), vec(C, p0)) - r * r;
      double f = b * b - 4 * a * c;
      vector<point> v;
      if (dcmp(f, 0) >= 0) {
            if (dcmp(f, 0) == 0)
                                 f = 0;
            double t1 = (-b + sqrt(f)) / (2 * a);
            double t2 = (-b - sqrt(f)) / (2 * a);
           v.push_back(p0 + t1 * (p1 - p0));
            if (dcmp(f, 0) != 0) v.push back(p0 + t2 * (p1 - p0));
      }
      return v;
}
Circle Circle Intersection
vector<point> intersectCircleCircle(point c1, double r1, point c2, double r2) {
      // Handle infinity case first: same center/radius and r > 0
      if (same(c1, c2) \&\& dcmp(r1, r2) == 0 \&\& dcmp(r1, 0) > 0)
            return vector<point>(3, c1); // infinity 2 same circles (not points)
        // Compute 2 intersection case and handle 0, 1, 2 cases
      double ang1 = angle(vec(c1, c2)), ang2 = getAngle_A_abc(r2, r1, length(vec(c1, c2)));
      if (::isnan(ang2)) ang2 = 0; // if r1 or d = 0 => nan in getAngle_A_abc (/0)
      vector<point> v(1, polar(r1, ang1 + ang2) + c1);
      // if point NOT on the 2 circles = no intersection
      if (dcmp(dp(vec(c1, v[0]), vec(c1, v[0])), r1 * r1) != 0 | |
            dcmp(dp(vec(c2, v[0]), vec(c2, v[0])), r2 * r2) != 0)
            return vector<point>();
      v.push back(polar(r1, ang1 - ang2) + c1);
      if (same(v[0], v[1])) // if same, then 1 intersection only
            v.pop_back();
      return v;
}
```

#### **Circle Circle Intersection Area**

```
ld circleCircleIntersectionArea(point cen1, ld r1, point cen2, ld r2) {
      ld dis = hypot(cen1.X - cen2.X, cen1.Y - cen2.Y);
      if (dis > r1 + r2) return 0;
      if (dis <= fabs(r2 - r1) && r1 >= r2)
            return PI * r2 * r2;
      if (dis <= fabs(r2 - r1) && r1 < r2)</pre>
            return PI * r1 * r1;
      1d \ a = r1 * r1, b = r2 * r2;
      ld ang1 = acos((a + dis * dis - b) / (2 * r1 * dis)) * 2;
      1d ang2 = acos((b + dis * dis - a) / (2 * r2 * dis)) * 2;
      1d ret1 = .5 * b * (ang2 - sin(ang2));
      ld ret2 = .5 * a * (ang1 - sin(ang1));
      return ret1 + ret2;
}
Check if polygon is convex
// CCW function must return 0 if the 3 points are collinear
bool isConvex(vector<point>& v) {
      int n = v.size(), m = n, sum = 0;
      v.push_back(v[0]);
      v.push_back(v[1]);
      char tmp;
      for (int i = 0; i < n; i++) {
            tmp = ccw(v[i], v[i + 1], v[i + 2]);
            if (tmp) sum += tmp;
            else m--;
      }
      v.pop_back();
      v.pop_back();
      return abs(sum) == m;
}
Convex hull
bool cmp(point a, point b) {
      return a.X < b.X || (a.X == b.X && a.Y < b.Y);</pre>
bool cw(point a, point b, point c) {
      return cp(vec(a, b), vec(b, c)) < 0;
bool ccw(point a, point b, point c) {
      return cp(vec(a, b), vec(b, c)) > 0;
}
```

```
vector<point> convex_hull(vector<point>& p) {
      if (p.size() == 1) return p;
      sort(p.begin(), p.end(), &cmp);
      point p1 = p[0], p2 = p.back();
      vector<point> up, down;
      up.push back(p1);
      down.push back(p1);
      for (int i = 1; i < (int)p.size(); i++) {</pre>
            if (i == p.size() - 1 || cw(p1, p[i], p2)) {
                  while (up.size() >= 2
                        && !cw(up[up.size() - 2], up[up.size() - 1], p[i]))
                        up.pop back();
                  up.push back(p[i]);
            if (i == p.size() - 1 || ccw(p1, p[i], p2)) {
                  while (down.size() >= 2
                        && !ccw(down[down.size() - 2], down[down.size() - 1], p[i]))
                        down.pop back();
                  down.push back(p[i]);
            }
      }
      vector<point> convex;
      for (int i = 0; i < (int)down.size(); i++)</pre>
            convex.push back(down[i]);
      for (int i = up.size() - 2; i > 0; i--)
            convex.push_back(up[i]);
      return convex;
}
Point in polygon O(log(n))
void prepare(vector<point>& polygon) {
      int pos = 0;
      for (int i = 0; i < sz(polygon); i++) {</pre>
            if (make_pair(polygon[i].X, polygon[i].Y)
                  < make pair(polygon[pos].X, polygon[pos].Y))</pre>
                  pos = i;
      }
      rotate(polygon.begin(), polygon.begin() + pos, polygon.end());
int dcmp(double x, double y) {
      if (fabs(x - y) \le EPS)
            return 0;
      return (x < y ? -1 : 1);
11 cross(point a, point b, point c) {
      return cp(vec(a, b), vec(a, c));
bool isPointOnSegment(point a, point b, point c) {
      double acb = length(a - b), ac = length(a - c), cb = length(b - c);
      return dcmp(acb - (ac + cb), 0) == 0;
}
```

```
//call prepare(polygon) before start
bool pointInConvexPolygon(const vector<point>& polygon, point pt) {
      if (isPointOnSegment(polygon[0], polygon.back(), pt))
            return true;
      if (cross(polygon[0], polygon.back(), pt) > 0)
            return false;
      if (cross(polygon[0], polygon[1], pt) < 0)</pre>
            return false;
      if (polygon.size() == 2)
            return false;
      int st = 2, ed = sz(polygon) - 2, ans = 1;
      while (st <= ed) {</pre>
            int md = st + ed >> 1;
            if (cross(polygon[0], polygon[md], pt) >= 0)
                   st = md + 1, ans = md;
            else
                   ed = md - 1;
      return cross(polygon[ans], polygon[ans + 1], pt) >= 0;
}
line sweep for lines intersections
struct segment {
      point p, q;
      int idx;
      segment() {
      segment(point a, point b, int idx) :
            p(a), q(b), idx(idx) {
      }
      double CY(int x) const {
            if (p.X == q.X)
                   return p.Y;
            double t = 1.0 * (x - p.X) / (q.X - p.X);
            return p.Y + (q.Y - p.Y) * t;
      bool operator<(const segment& o) const {</pre>
            if (p == 0.p \&\& q == 0.q)
                   return idx < o.idx;</pre>
            int maxX = max(p.X, o.p.X);
            int res = dcmp(CY(maxX), o.CY(maxX));
            if (res == 0)
                   return idx < o.idx;</pre>
            return res < 0;</pre>
      }
};
struct event {
      bool entry;
      point p;
      int idx;
      event(point p, bool entry, int idx) :
            p(p), entry(entry), idx(idx) {
      }
```

```
bool operator<(const event& o) const {</pre>
            if (p.X != o.p.X)
                  return p.X < o.p.X;</pre>
            if (entry != o.entry)
                  return entry > o.entry;
            return idx < o.idx;</pre>
      }
};
int ccw(point a, point b, point c) {
      point v1(b - a), v2(c - a);
      double t = cp(v1, v2);
      if (t > EPS)
            return 1;
      if (t < -EPS)</pre>
            return -1;
      if (v1.X * v2.X < -EPS || v1.Y * v2.Y < -EPS)
            return -1;
      if (norm(v1) < norm(v2) - EPS)
            return 1;
      return 0;
}
bool intersect(point p1, point p2, point p3, point p4) {
      // special case handling if a segment is just a point
      bool x = (p1 == p2), y = (p3 == p4);
      if (x && y) return p1 == p3;
      if (x) return ccw(p3, p4, p1) == 0;
      if (y) return ccw(p1, p2, p3) == 0;
      return ccw(p1, p2, p3) * ccw(p1, p2, p4) <= 0
            && ccw(p3, p4, p1) * ccw(p3, p4, p2) <= 0;
}
pair<int, int> solve(vector<segment> v) {
      int n = v.size();
      vector<event> events;
      for (int i = 0; i < n; i++) {
            point& p = v[i].p;
            point& q = \sqrt{i}.q;
            if (q.X < p.X \mid | (q.X == p.X && q.Y < p.Y))
                  swap(p, q);
            events.push_back(event(p, true, i));
            events.push_back(event(q, false, i));
      sort(all(events));
      set<segment> st;
      auto before = [&](set<segment>::iterator it) {
            if (it == st.begin())
                  return st.end();
            return --it;
      };
      auto check = [&](set<segment>::iterator x,
            set<segment>::iterator y) -> bool {
                  if (x == st.end() || y == st.end())
                         return false;
                  return intersect(x->p, x->q, y->p, y->q);
      };
```

```
for (auto& cur : events) {
            if (cur.entry) {
                  auto it = st.insert(v[cur.idx]).first;
                  auto below = before(it);
                  auto above = next(it);
                  if (check(below, it)) return { below->idx,it->idx };
                  if (check(above, it)) return { above->idx,it->idx };
            }
            else {
                  auto it = st.find(v[cur.idx]);
                  auto below = before(it);
                  auto above = next(it);
                  if (check(below, above)) return { below->idx,above->idx };
                  st.erase(it);
            }
      }
      return { -1,-1 };
}
Pyramid Volume
ld pyramidVolume(ld ab, ld ac, ld ad, ld bc, ld bd, ld cd) {
      ld w = ab, v = ac, u = ad, U = bc, V = bd, W = cd;
      1d A = (W - U + V) * (U + V + W);
      1d x = (U - V + W) * (V - W + U);
      1d B = (u - V + w) * (V + w + u);
      1d y = (V - w + u) * (w - u + V);
      1d Z = (v - W + u) * (W + u + v);
      1d z = (W - u + v) * (u - v + W);
      ld a = sqrt(x * B * Z);
      ld b = sqrt(A * y * Z);
      ld c = sqrt(A * B * z);
      1d d = sqrt(x * y * z);
      1d volume = -a + b + c + d;
      volume *= a - b + c + d;
      volume *= a + b - c + d;
      volume *= a + b + c - d;
      volume = sqrt(volume) / (192.0 * u * v * w);
      return volume;
}
Suffix Automaton
class SuffixAutomaton {
private:
      class SNode {
      public:
            int len, link, firstpos, is_clone;
            map<char, int> next;
            int endpos;
            vi inv_next;
            SNode() {
                  len = 0, link = firstpos = -1;
                  endpos = 1;
                  is clone = 0;
            }
```

```
SNode(const SNode& other) :SNode() {
                  len = other.len;
                  link = other.link;
                  next = other.next;
                  firstpos = other.firstpos;
                  endpos = other.endpos;
                  is_clone = other.is_clone;
            }
      };
public:
      int n, last, cur;
      string str;
      vector<SNode> nodes;
      vector<ll> dist_substr;
      vi sz_link_tree;
      SuffixAutomaton(string s) {
            str = s;
            n = sz(str);
            nodes.resize(2 * n);
            dist_substr = vector<ll>(2 * n, -1);
            sz link_tree = vi(2 * n);
            last = 0, cur = 1;
            for (auto& it : str)
                  add char(it);
            build_endpos();
            build_distinct_substrings(0);
            build inv next();
            dfs_linktree(0);
      }
      void add char(char ch) {
            int newNode = cur++;
            nodes[newNode].len = nodes[last].len + 1;
            nodes[newNode].firstpos = nodes[newNode].len - 1;
            int p = last;
            last = newNode;
            for (; p != -1 && nodes[p].next.find(ch) == nodes[p].next.end(); p =
nodes[p].link)
                  nodes[p].next[ch] = newNode;
            if (p == -1) {
                  nodes[newNode].link = 0;
                  return;
            int q = nodes[p].next[ch];
            if (nodes[p].len + 1 == nodes[q].len) {
                  nodes[newNode].link = q;
                  return;
            }
            int clone = cur++;
            nodes[clone] = SNode(nodes[q]);
            nodes[clone].len = nodes[p].len + 1;
            nodes[clone].endpos = 0;
            nodes[clone].is clone = true;
            nodes[q].link = clone;
            nodes[newNode].link = clone;
```

```
for (; p != -1 && nodes[p].next.find(ch) != nodes[p].next.end() &&
nodes[p].next[ch] == q; p = nodes[p].link)
                  nodes[p].next[ch] = clone;
      void build_endpos() {
            vi tmp(cur - 1);
            iota(all(tmp), 1);
            sort(all(tmp), [&](int a, int b) {return nodes[a].len > nodes[b].len; });
            for (auto& it : tmp)
                  nodes[nodes[it].link].endpos += nodes[it].endpos;
            nodes[0].endpos = 0;
      }
      void build distinct substrings(int u) {
            11& ret = dist_substr[u];
            if (ret != -1) return;
            ret = u > 0;
            for (auto& it : nodes[u].next) {
                  build_distinct_substrings(it.second);
                  ret += dist substr[it.second];
            }
      }
      void build_inv_next() {
// be attention this order is important to make occurrences sorted in increasing order
            for (int i = 1; i < cur; i++)
                  nodes[nodes[i].link].inv_next.push_back(i);
      void dfs_linktree(int u) {
            sz_link_tree[u] = !nodes[u].is_clone;
            for (auto& v : nodes[u].inv next) {
                  dfs linktree(v);
                  sz link tree[u] += sz link tree[v];
            }
      string lcs(const string& p) {
            int u = 0, l = 0, best = 0, bestpos = 0;
            for (int i = 0; i < sz(p); i++) {
                  while (u && nodes[u].next.find(p[i]) == nodes[u].next.end()) {
                        u = nodes[u].link;
                        1 = nodes[u].len;
                  if (nodes[u].next.find(p[i]) != nodes[u].next.end()) {
                        u = nodes[u].next[p[i]];
                  if (1 > best) {
                        best = 1;
                        bestpos = i;
                  }
            return p.substr(bestpos - best + 1, best);
      }
```

```
int match(const string& p) {
      int u = 0, idx = 0;
      while (idx < sz(p) && nodes[u].next.find(p[idx]) != nodes[u].next.end())</pre>
            u = nodes[u].next[p[idx]], idx++;
      if (idx != sz(p))
            return 0;
      return u;
}
vi all_occurrences_of_pattern(int u, int p_len) {
      vi ret; // 0 based all indices of p in automaton
      queue<int> q;
      q.push(u);
     while (!q.empty()) {
            int cur = q.front();
            q.pop();
            if (!nodes[cur].is_clone)
                  ret.push_back(nodes[cur].firstpos - p_len + 1);
            for (auto& v : nodes[cur].inv next)
                  q.push(v);
      return ret;
vi get_occurrences_of_pattern(const string& p) {
      int u = match(p);
      if (!u) return vi();
      return all_occurrences_of_pattern(u, sz(p));
int get_cnt_occurrences_of_pattern(const string& p) {
      int u = match(p);
      if (!u) return 0;
      return sz_link_tree[u];
}
void kth_distinct(int u, 11 k, string& ret) {
      if (u) k--;
      if (!k) return;
      for (auto& it : nodes[u].next) {
            if (dist substr[it.second] >= k) {
                  ret.push_back(it.first);
                  kth_distinct(it.second, k, str);
                  return;
            k -= dist substr[it.second];
      }
}
string get_kth_distinct(ll k) {
      if (k > dist substr[0]) return "-1";
      string ret = "";
      kth_distinct(0, k, ret);
      return ret;
}
```

**}**;