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#### **Data structure**

#### Fenwick tree

```
template<typename T>
struct fenwick_tree {
       /* can convert it to map
       * build what you need only
       * will be: memory O(q*logn) ,time O(logn*logn) */
       vector<T> BIT;
       int n;
       fenwick_tree(int n) :
              n(n), BIT(n + 1) {
       T getAccum(int idx) {
              T sum = 0;
              while (idx) {
                     sum += BIT[idx];
                     idx -= (idx \& -idx);
              }
              return sum;
       void add(int idx, T val) {
              assert(idx != 0);
              while (idx <= n) {</pre>
                     BIT[idx] += val;
                     idx += (idx & -idx);
       T getValue(int idx) {
              return getAccum(idx) - getAccum(idx - 1); }
       // ordered statistics tree
       // get index that has value >= accum
       // values must by positive
       int getIdx(T accum) {
              int start = 1, end = n, rt = -1;
              while (start <= end) {</pre>
                     int mid = start + end >> 1;
                     T val = getAccum(mid);
                     if (val >= accum)
                            rt = mid, end = mid - 1;
                     else
                            start = mid + 1;
              return rt;
       //need review (from topcoder)
       //first index less than or equal accum O(logn)
       int find(T accum) { //equal getIdx
              int i = 1, idx = 0;
              while ((1 << i) <= MAX)
                     i <<= 1;
              for (idx = 0; i > 0; i >>= 1) {
                     int tidx = idx + i;
                     if (tidx > MAX)
                            continue;
                     if (accum >= BIT[tidx]) {
                            idx = tidx;
                            accum -= BIT[tidx];
                     }
```

```
return idx;//idx+1 if you need first greater
       }
};
Fenwick tree 2d
template<typename T>
struct fenwick_tree_2d {
#define Lbit(x) (x\&-x)
       int n, m;
       vector<vector<T>> BIT;
       fenwick_tree_2d(int n, int m) :
              n(n), m(m), BIT(n + 1, vector < T > (m + 1)) {
       }
       T getAccum(int i, int j) {
              T sum = 0;
              for (; i; i -= Lbit(i))
                     for (int idx = j; idx > 0; idx -= Lbit(idx))
                            sum += BIT[i][idx];
              return sum;
       }
       void add(int i, int j, int val) {
              assert(i != 0 && j != 0);
              for (; i <= n; i += Lbit(i))</pre>
                     for (int idx = j; idx <= m; idx += Lbit(idx))</pre>
                            BIT[i][idx] += val;
       T getRectangeSum(int x1, int y1, int x2, int y2) {
              if (y1 > y2)
                     swap(y1, y2);
              if (x1 > x2)
                     swap(x1, x2);
              return getAccum(x2, y2) - getAccum(x1 - 1, y2) - getAccum(x2, y1 - 1)
                     + getAccum(x1 - 1, y1 - 1);
       }
};
Fenwick tree max
//fenwick tree for get maximum from 1 to idx
// update a[idx] = max(a[idx],val)
//can't remove values
template<typename T>
struct fenwick_tree {
       vector<T> BIT;
       int n;
       fenwick_tree(int n) :
              n(n), BIT(n + 1) {
       T getMax(int idx) {
              T mx = numeric_limits<T>::min();
              while (idx) {
                     mx = max(mx, BIT[idx]);
                     idx -= (idx & -idx);
              return mx;
       void add(int idx, T val) {
              assert(idx != 0);
              while (idx <= n) {
                     BIT[idx] = max(BIT[idx], val);
                     idx += (idx \& -idx);
              }
       }
```

**}**;

### Fenwick tree update range

```
/*
x[i] = a[i] - a[i-1] //a is original array
y[i] = x[i]*(i-1)
 sum(1,3) = a[1] + a[2] + a[3] = (x[1]) + (x[2] + x[1]) + (x[3] + x[2] + x[1])
 = 3*(x[1] + x[2] + x[3]) - 0*x[1] - 1*x[2] - 2*x[3] //same equation but more complex
 = sumX(1,3) * 3 - sumY(1,3)
 so sum(1,n) = sumX(1,n)*n - sumY(1,n)
update:
x[1] += val, x[r+1] -= val
y[1] += val *(1-1), y[r+1] -= r*val
template<typename T>
class fenwick_tree {
       int n;
       vector<T> x, y;
       T getAccum(vector<T>& BIT, int idx) {
              T sum = 0;
              while (idx) {
                     sum += BIT[idx];
                     idx -= (idx & -idx);
              }
              return sum;
       void add(vector<T>& BIT, int idx, T val) {
              assert(idx != 0);
              while (idx <= n) {
                     BIT[idx] += val;
                     idx += (idx \& -idx);
              }
       }
       T prefix_sum(int idx) {
              return getAccum(x, idx) * idx - getAccum(y, idx);
       }
public:
       fenwick_tree(int n) :
              n(n), x(n + 1), y(n + 1) {
       void update_range(int 1, int r, T val) {
              add(x, 1, val);
              add(x, r + 1, -val);
              add(y, 1, val * (1 - 1));
              add(y, r + 1, -val * r);
       }
       T range_sum(int 1, int r) {
              return prefix_sum(r) - prefix_sum(1 - 1);
       }
};
```

## Segment tree

```
for efficient memory (2*n)
#define LEFT (idx+1)
 #define MID ((start+end)>>1)
 #define RIGHT (idx+((MID-start+1)<<1))</pre>
template<typename node> class segment tree {
#define LEFT (idx<<1)</pre>
#define RIGHT (idx<<1|1)</pre>
#define MID ((start+end)>>1)
       int left_range, right_range;
       vector<node> tree;
       inline void pushup(int idx) {
              tree[idx] = node(tree[LEFT], tree[RIGHT]);
       inline void pushdown(int idx, int start, int end) {
              if (!tree[idx].have_lazy || start == end)
                     return;
              tree[LEFT].apply(start, MID, tree[idx].lazy_value);
              tree[RIGHT].apply(MID + 1, end, tree[idx].lazy_value);
              tree[idx].clear_lazy();
       }
       void build(int idx, int start, int end) {
              if (start == end)
                     return;
              build(LEFT, start, MID);
              build(RIGHT, MID + 1, end);
              pushup(idx);
       template<typename T>
       void build(int idx, int start, int end, const vector<T>& arr) {
              if (start == end) {
                     tree[idx] = arr[start];
                     return;
              build(LEFT, start, MID, arr);
              build(RIGHT, MID + 1, end, arr);
              pushup(idx);
       }
       node query(int idx, int start, int end, int from, int to) {
              if (from <= start && end <= to)</pre>
                     return tree[idx];
              pushdown(idx, start, end);
              if (to <= MID)</pre>
                     return query(LEFT, start, MID, from, to);
              if (MID < from)</pre>
                     return query(RIGHT, MID + 1, end, from, to);
              return node(query(LEFT, start, MID, from, to),
                     query(RIGHT, MID + 1, end, from, to));
       }
       template<typename ... T>
       void update(int idx, int start, int end, int from, int to,const T&... val) {
              if (to < start || end < from)</pre>
                     return;
              if (from <= start && end <= to) {</pre>
                     tree[idx].apply(start, end, val...);
                     return;
              }
```

```
pushdown(idx, start, end);
              update(LEFT, start, MID, from, to, val...);
              update(RIGHT, MID + 1, end, from, to, val...);
              pushup(idx);
       void init(int 1, int r) {
              left_range = 1;
              right_range = r;
              tree = vector < node >((r - 1 + 1) << 2);
public:
       segment_tree(int 1, int r) {
              init(1, r);
              build(1, 1, r);
       template<typename T>
       segment_tree(int 1, int r, const vector<T>& v) {
              init(1, r);
              build(1, 1, r, v);
       }
       node query(int 1, int r) {
              assert(left_range <= 1 && 1 <= r && r <= right_range);</pre>
              return query(1, left_range, right_range, 1, r);
       template<typename ... T>
       void update(int 1, int r, const T&... val) {
              assert(left_range <= 1 && 1 <= r && r <= right_range);</pre>
              update(1, left_range, right_range, l, r, val...);
#undef LEFT
#undef RIGHT
#undef MID
};
Iterative Segment tree
struct node {
       node() { //set Default value
       node(const node& a, const node& b) {}
       void apply(int val) {}
struct segment_tree {
       int n; //0 to n-1
       vector<node> tree;
       segment_tree(int n) {
              resize(n);
              build();
       }
       template<typename T>
       segment_tree(const vector<T>& arr) {
              resize(arr.size());
              for (int i = 0; i < arr.size(); i++)</pre>
                     tree[n + i] = arr[i];
              build();
       void resize(int n) {
              int p = 1;
              while (p < n)
                     p <<= 1;
              this->n = p;
              tree = vector < node >(p << 1);
       void build() {
              for (int i = n - 1; i > 0; i--)
```

```
tree[i] = node(tree[i << 1], tree[i << 1 | 1]);</pre>
       }
       template<typename T>
       void update(int p, const T& value) {
              tree[p += n].apply(value);
              for (int i = p / 2; i > 0; i >>= 1)
                     tree[i] = node(tree[i << 1], tree[i << 1 | 1]);</pre>
       node query(int 1, int r) { //[1, r]
              node resl, resr; //set default value in node
              for (1 += n, r += n + 1; 1 < r; 1 >>= 1, r >>= 1) {
                      if (1 & 1) {
                             resl = node(resl, tree[1]);
                      if (r & 1) {
                             r--;
                             resr = node(tree[r], resr);
                      }
              return node(resl, resr);
       int kth_one(int k, int i = 1) {
              if (k > tree[i])
                      return -1;
              if (i >= n)
                      return i - n;
              if (tree[i << 1] >= k)
                      return kth_one(k, i << 1);</pre>
              return kth_one(k - tree[i << 1], i << 1 | 1);</pre>
       }
};
Max sum range node
struct MSR_Node {
       11 left, right, mid, sum;
       MSR_Node(const 11& val) {
              left = right = mid = sum = val;
       MSR_Node(const MSR_Node& a, const MSR_Node& b) {
              left = max(a.left, a.sum + b.left);
              right = max(b.right, b.sum + a.right);
              mid = max({ a.mid, b.mid, a.right + b.left });
              sum = a.sum + b.sum;
       }
       11 getMax() {
              return max({ left, right, mid, sum });
       }
};
Persistent segment tree
struct segtree {
  static segtree *sentinel;
  segtree *left, *right;
  bool dirty = false;
  11 \text{ sum} = 0;
  11 \text{ lazy} = 0;
```

```
segtree(11 val = 0):
        sum(val) {
     left = right = this;
  segtree(segtree *left, segtree *right) :
       left(left), right(right) {
     sum = left->sum + right->sum;
  }
};
segtree *segtree::sentinel = new segtree();
class persistent_segment_tree {
#define MID ((start+end)>>1)
  segtree* apply(segtree *root, int start, int end, ll val) {
     segtree *rt = new segtree(*root);
     rt->dirty = true;
     rt->sum += (end - start + 1) * val;
     rt->lazy += val;
     return rt;
  void pushdown(segtree *root, int start, int end) {
     if (root->dirty == false || start == end)
       return;
     root->left = apply(root->left, start, MID, root->lazy);
     root->right = apply(root->right, MID + 1, end, root->lazy);
     root->lazy = 0;
     root->dirty = 0;
  segtree* build(int start, int end, const vector<int> &v) {
     if (start == end)
       return new segtree(v[start]);
     return new segtree(build(start, MID, v), build(MID + 1, end, v));
  segtree* Set(segtree *root, int start, int end, int pos, ll new_val) {
     pushdown(root, start, end);
     if (pos < start || end < pos)
       return root;
     if (pos \le start & end \le pos)
       return new segtree(new_val);
     return new segtree(Set(root->left, start, MID, pos, new_val),
          Set(root->right, MID + 1, end, pos, new_val));
  segtree* update(segtree *root, int start, int end, int l, int r, ll val) {
     pushdown(root, start, end);
     if (r < start || end < 1)
       return root;
     if (1 \le \text{start \&\& end} \le r)
        return apply(root, start, end, val);
     return new segtree(update(root->left, start, MID, l, r, val),
          update(root->right, MID + 1, end, l, r, val));
  }
```

```
ll query(segtree *root, int start, int end, int l, int r) {
     pushdown(root, start, end);
     if (r < start || end < l)
       return 0;
     if (1 \le \text{start \&\& end} \le r)
       return root->sum;
     return query(root->left, start, MID, l, r)
          + query(root->right, MID + 1, end, l, r);
  }
public:
  int start, end;
  vector<segtree*> versions;
  persistent_segment_tree(int start, int end) :
        start(start), end(end) {
     versions.push_back(segtree::sentinel);
  persistent_segment_tree(const vector<int> &v):
        start(0), end(v.size() - 1) {
     versions.push_back(build(start, end, v));
  void update(int l, int r, ll val) {
     versions.push_back(update(versions.back(), start, end, l, r, val));
  1l query(int time, int l, int r) {
     return query(versions[time], start, end, l, r);
#undef MID
};
Extended Segment tree
struct segtree {
  segtree *left = nullptr, *right = nullptr;
  int mx = 0;
  segtree(int val = 0):
       mx(val) {
  }
  void extend() {
     if (left == NULL) {
       left = new segtree();
       right = new segtree();
  }
  void pushup() {
     mx = max(left->mx, right->mx);
  }
};
class extened segment tree {
#define MID ((start+end)>>1)
  void update(segtree *root, int start, int end, int pos, int val) {
     if (pos < start || end < pos)
       return;
```

```
if (start == end) {
       root->mx = max(root->mx, val);
       return:
     }
     root->extend();
     update(root->left, start, MID, pos, val);
     update(root->right, MID + 1, end, pos, val);
     root->pushup();
  int query(segtree *root, int start, int end, int l, int r) {
     if (root == nullptr || r < start || end < l)
       return 0;
     if (1 \le \text{start \&\& end} \le r)
       return root->mx;
     return max(query(root->left, start, MID, 1, r),
          query(root->right, MID + 1, end, l, r));
public:
  int start, end;
  segtree *root;
  extened_segment_tree() {
  extened_segment_tree(int start, int end) :
       start(start), end(end) {
     root = new segtree();
  void update(int pos, int val) {
     update(root, start, end, pos, val);
  int query(int 1, int r) {
     return query(root, start, end, l, r);
#undef MID
};
Ordered set
#include<bits/stdc++.h>
#include<ext/pb ds/assoc container.hpp>
#include<ext/pb_ds/tree_policy.hpp>
using namespace std;
using namespace gnu pbds;
template<typename key>
using ordered_set = tree<key, null_type, less<key>, rb_tree_tag, tree_order_statistics_node_update>;
find by order(k):
 It returns to an iterator to the k-th element (counting from zero) in the set in O(logn) time.
 To find the first element k must be zero.
order of key(k):
 It returns to the number of items that are strictly smaller than our item k in O(logn) time.
Sparse table
template<typename T>
struct sparse_table {
       vector<vector<T>> sparseTable;
```

```
using F = function<T(T, T)>;
       F merge;
       static int LOG2(int x) { //floor(log2(x))
              return 31 - __builtin_clz(x);
       }
       sparse table(vector<T>& v, F merge) :
              merge(merge) {
              int n = v.size();
              int logN = LOG2(n);
              sparseTable = vector<vector<T>>(logN + 1);
              sparseTable[0] = v;
              for (int k = 1, len = 1; k \leftarrow logN; k++, len \leftarrow = 1) {
                     sparseTable[k].resize(n);
                     for (int i = 0; i + len < n; i++)</pre>
                             sparseTable[k][i] = merge(sparseTable[k - 1][i],
                                    sparseTable[k - 1][i + len]);
              }
       T query(int 1, int r) {
              int k = LOG2(r - 1 + 1); // max k ==> 2^k <= length of range
              //check first 2^k from left and last 2^k from right //overlap
              return merge(sparseTable[k][1], sparseTable[k][r - (1 << k) + 1]);</pre>
       T query_shifting(int 1, int r) {
              T res;
              bool first = true;
              for (int i = (int)sparseTable.size() - 1; i >= 0; i--)
                     if (1 + (1 << i) - 1 <= r) {</pre>
                            if (first)
                                    res = sparseTable[i][1];
                             else
                                   res = merge(res, sparseTable[i][1]);
                            first = false;
                             l += (1 << i);
              return res;
       }
};
SQRT Decomposition
//zero based SQRT Decomposition with lazy propagation
template<typename update_type, typename query_type>
class SQRT_Decomposition {
       struct Bucket {
              int 1, r;
              update_type lazy;
              Bucket(int 1, int r) :
                     1(1), r(r) {
                     //set default value to lazy
                     //build bucket for the first time
              }
              void build() {
                     //update all bucket with lazy if have
                     //rebuild the bucket
                     //clear lazy
              }
              //update all bucket
              void update(const update_type& val) {
                     //just update lazy
              }
```

```
//update range in bucket
              void update(int start, int end, const update_type& val) {
                     if (start == 1 && end == r) {
                            update(val);
                            return;
                     //update bucket
                     //rebuild the bucket if need
              //query about all bucket
              query_type query() {
                     //calc with lazy
              //query about range in bucket
              query type query(int start, int end) {
                     if (start == 1 && end == r)
                            return query();
                     //push lazy if have
                     //calc
              }
       };
       int n, sqrtN;
       vector<Bucket> bucket;
       int begin(int idx) {
              return idx * sqrtN;
       int end(int idx) {
              return min(sqrtN * (idx + 1), n) - 1;
       int which_block(int idx) {
              return idx / sqrtN;
public:
       SQRT_Decomposition(int n) {
              this->n = n;
              sqrtN = sqrt(n);
              for (int i = 0; i < n; i += sqrtN)</pre>
                     bucket.push_back(Bucket(i, min(i + sqrtN, n) - 1));
       }
       void update(int left, int right, update_type val) {
              int st = which block(left), ed = which block(right);
              bucket[st].update(left, min(bucket[st].r, right), val);
              for (int i = st + 1; i < ed; i++)</pre>
                     bucket[i].update(val);
              if (st != ed)
                     bucket[ed].update(bucket[ed].l, right, val);
       }
       query_type query(int left, int right) {
              int st = which block(left), ed = which block(right);
              query_type rt = bucket[st].query(left, min(bucket[st].r, right));
              for (int i = st + 1; i < ed; i++)
                     rt += bucket[i].query();
              if (st != ed)
                     rt += bucket[ed].query(bucket[ed].1, right);
              return rt;
       }
```

```
};
```

```
Implicit treap
enum DIR {
       L, R
};
template<typename T>
struct cartesian_tree {
       static cartesian_tree<T>* sentinel;
       T key;
       int priority = 0, size = 0;
       bool reverse = false;
       cartesian_tree* child[2];
       cartesian_tree() {
              key = T();
              priority = 0;
              child[L] = child[R] = this;
       cartesian_tree(const T& x, int y) :
              key(x), priority(y) {
              size = 1;
              child[L] = child[R] = sentinel;
       }
       void push_down() {
              if (!reverse)
                     return;
              reverse = 0;
              child[L]->doRevese();
              child[R]->doRevese();
       void doReverse() {
              reverse ^= 1;
              swap(child[L], child[R]);
       void push_up() {
              size = child[L]->size + child[R]->size + 1;
       }
};
template<typename T>
cartesian tree<T>* cartesian tree<T>::sentinel = new cartesian tree<T>();
template<typename T, template<typename > class cartesian_tree>
class implicit_treap { //1 based
       typedef cartesian_tree<T> node;
       typedef cartesian_tree<T>* nodeptr;
#define emptyNode cartesian_tree<T>::sentinel
       nodeptr root;
       void split(nodeptr root, nodeptr& 1, nodeptr& r, int firstXElment) {
              if (root == emptyNode) {
                     1 = r = emptyNode;
                     return;
              root->push_down();
              if (firstXElment <= root->child[L]->size) {
                     split(root->child[L], 1, root->child[L], firstXElment);
                     r = root;
              }
              else {
                     split(root->child[R], root->child[R], r,
```

```
firstXElment - root->child[L]->size - 1);
                     1 = root;
              root->push_up();
       }
       nodeptr merge(nodeptr 1, nodeptr r) {
              1->push_down();
              r->push down();
              if (1 == emptyNode | | r == emptyNode)
                     return (1 == emptyNode ? r : 1);
              if (1->priority > r->priority) {
                     1->child[R] = merge(1->child[R], r);
                     1->push up();
                     return 1;
              r->child[L] = merge(1, r->child[L]);
              r->push_up();
              return r;
       }
       vector<nodeptr> split_range(int s, int e) { // [x<s,s<=x<=e,e<x]</pre>
              nodeptr 1, m, r, tmp;
              split(root, 1, tmp, s - 1);
              split(tmp, m, r, e - s + 1);
              return { 1,m,r };
       }
public:
       implicit_treap() :
              root(emptyNode) {
       int size() {
              return root->size;
       void insert(int pos, const T& key) {
              nodeptr tmp = new node(key, rand());
              nodeptr 1, r;
              split(root, l, r, pos - 1);
              root = merge(merge(1, tmp), r);
       }
       void push_back(const T& value) {
              root = merge(root, new node(value, rand()));
       T getByIndex(int pos) {
              vector<nodeptr> tmp = split range(pos, pos);
              nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
              Trt = m->key;
              root = merge(merge(1, m), r);
              return rt;
       void erase(int pos) {
              vector<nodeptr> tmp = split range(pos, pos);
              nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
              delete m;
              root = merge(1, r);
       void cyclic_shift(int s, int e) { //to the right
              vector<nodeptr> tmp = split range(s, e);
              nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
              nodeptr first, second;
              split(m, first, second, e - s);
              root = merge(merge(merge(1, second), first), r);
       void reverse_range(int s, int e) {
              vector<nodeptr> tmp = split_range(s, e);
```

```
nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
              m->reverse ^= 1;
              root = merge(merge(1, m), r);
       }
       node range_query(int s, int e) {
              vector<nodeptr> tmp = split_range(s, e);
              nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
              node rt = *m;
              root = merge(merge(1, m), r);
              return rt;
       }
};
Ordered multiset
enum DIR {
       L, R
};
template<typename T>
struct cartesian_tree {
       static cartesian_tree<T>* sentinel;
       int priority = 0, frequency = 0, size = 0;
       cartesian_tree* child[2];
       cartesian_tree() {
              key = T();
              priority = 0;
              child[L] = child[R] = this;
       cartesian_tree(const T& x, int y) :
              key(x), priority(y) {
              size = frequency = 1;
              child[L] = child[R] = sentinel;
       void push_down() {
       void push_up() {
              size = child[L]->size + child[R]->size + frequency;
       }
};
template<typename T>
cartesian_tree<T>* cartesian_tree<T>::sentinel = new cartesian_tree<T>();
template<typename T>
void split(cartesian_tree<T>* root, T key, cartesian_tree<T>*& 1,
       cartesian_tree<T>*& r) {
       if (root == cartesian_tree<T>::sentinel) {
              1 = r = cartesian_tree<T>::sentinel;
              return;
       }
       root->push_down();
       if (root->key <= key) {</pre>
              split(root->child[R], key, root->child[R], r);
              1 = root;
       else {
              split(root->child[L], key, 1, root->child[L]);
              r = root;
       root->push_up();
}
```

```
template<typename T>
cartesian_tree<T>* merge(cartesian_tree<T>* 1, cartesian_tree<T>* r) {
       1->push_down();
       r->push down();
       if (1 == cartesian_tree<T>::sentinel || r == cartesian_tree<T>::sentinel)
              return (1 == cartesian_tree<T>::sentinel ? r : 1);
       if (1->priority > r->priority) {
              1->child[R] = merge(1->child[R], r);
              1->push_up();
              return 1;
       r->child[L] = merge(1, r->child[L]);
       r->push_up();
       return r;
}
template<typename T, template<typename > class cartesian_tree>
class treap {
       typedef cartesian_tree<T> node;
       typedef node* nodeptr;
#define emptyNode node::sentinel
       nodeptr root;
       void insert(nodeptr& root, nodeptr it) {
              if (root == emptyNode) {
                     root = it;
              else if (it->priority > root->priority) {
                     split(root, it->key, it->child[L], it->child[R]);
                     root = it;
              }
              else
                     insert(root->child[root->key < it->key], it);
              root->push_up();
       bool increment(nodeptr root, const T& key) {
              if (root == emptyNode)
                     return 0;
              if (root->key == key) {
                     root->frequency++;
                     root->push up();
                     return root;
              bool rt = increment(root->child[root->key < key], key);</pre>
              root->push up();
              return rt;
       nodeptr find(nodeptr root, const T& key) {
              if (root == emptyNode | root->key == key)
                     return root;
              return find(root->child[root->key < key], key);</pre>
       void erase(nodeptr& root, const T& key) {
              if (root == emptyNode)
                     return;
              if (root->key == key) {
                     if (--(root->frequency) == 0)
                            root = merge(root->child[L], root->child[R]);
              else
```

```
erase(root->child[root->key < key], key);</pre>
              root->push up();
       }
       T kth(nodeptr root, int k) {
              if (root->child[L]->size >= k)
                     return kth(root->child[L], k);
              k -= root->child[L]->size;
              if (k <= root->frequency)
                     return root->key;
              return kth(root->child[R], k - root->frequency);
       int order_of_key(nodeptr root, const T& key) {
              if (root == emptyNode)
                     return 0;
              if (key < root->key)
                     return order_of_key(root->child[L], key);
              if (key == root->key)
                     return root->child[L]->size;
              return root->child[L]->size + root->frequency
                     + order_of_key(root->child[R], key);
       }
public:
       treap() :
              root(emptyNode) {
       void insert(const T& x) {
              if (increment(root, x)) //change it to find(x) to make it as a set
              insert(root, new node(x, rand()));
       void erase(const T& x) {
              erase(root, x);
       bool find(const T& x) {
              return (find(root, x) != emptyNode);
       int get kth number(int k) {
              assert(1 <= k && k <= size());
              return kth(root, k);
       int order_of_key(const T& x) {
              return order_of_key(root, x);
       int size() {
              return root->size;
       }
};
BST
class BST {
       struct node {
              int key;
              node* left, * right, * parent;
              node() {
                     key = 0;
                     left = right = parent = NULL;
              node(int key, node* left = NULL, node* right = NULL, node* parent = NULL) :
                     key(key), left(left), right(right), parent(parent) {
              }
       };
```

```
typedef node* nodeptr;
nodeptr minimum(nodeptr root) {
       if (root->left == NULL)
              return root;
       return minimum(root->left);
}
nodeptr maximum(nodeptr root) {
       if (root->right == NULL)
              return root;
       return maximum(root->right);
nodeptr successor(nodeptr cur) { //smallest key larger than cur
       if (cur->right != NULL)
              return minimum(cur->right);
       nodeptr tmp = cur->parent;
       while (tmp != NULL && tmp->right == cur)
              cur = tmp, tmp = tmp->parent;
       return tmp;
nodeptr bredecessor(nodeptr cur) { //biggest key less than cur
       if (cur->left != NULL)
              return maximum(cur->left);
       nodeptr tmp = cur->parent;
       while (tmp != NULL && tmp->left == cur)
              cur = tmp, tmp = tmp->parent;
       return tmp;
}
nodeptr find(nodeptr root, int key) {
       if (root == NULL)
              return NULL;
       if (key == root->key)
              return root;
       if (key < root->key)
              return find(root->left, key);
       return find(root->right, key);
nodeptr insert(nodeptr root, int key) {
       if (root == NULL)
              root = new node(key);
       else if (key < root->key) {
              root->left = insert(root->left, key);
              root->left->parent = root;
       else if (key > root->key) {
              root->right = insert(root->right, key);
              root->right->parent = root;
       return root;
nodeptr erase(nodeptr root, int key) {
       if (root == NULL)
              return root;
       if (key < root->key) {
              root->left = erase(root->left, key);
              root->left->parent = root;
       else if (key > root->key) {
              root->right = erase(root->right, key);
              root->right->parent = root;
      else {
              nodeptr tmp;
              if (root->left == NULL || root->right == NULL) {
                     if (root->left == NULL)
```

```
tmp = root->right;
                             else
                                    tmp = root->left;
                             free(root);
                             return tmp;
                     }
                     else {
                             tmp = successor(root);
                             root->key = tmp->key;
                             root->right = erase(root->right, tmp->key);
                             root->right->parent = root;
                     }
              }
              return root;
       }
public:
       nodeptr root;
       BST():
              root(NULL) {
       }
       nodeptr find(int key) {
              return find(root, key);
       void insert(int key) {
              root = insert(root, key);
       void erase(int key) {
              root = erase(root, key);
       }
};
void inorder(nodeptr root) {
       if (root == NULL)
              return;
       inorder(root->left);
       cout << root->key << ' ';</pre>
       inorder(root->right);
}
void preorder(nodeptr root) {
       if (root == NULL)
              return;
       cout << root->key << ' ';</pre>
       preorder(root->left);
       preorder(root->right);
}
void postorder(nodeptr root) {
       if (root == NULL)
              return;
       postorder(root->left);
       postorder(root->right);
       cout << root->key << ' ';</pre>
}
AVL
struct AVLnode {
       int key, height;
       AVLnode* left, * right, * parent;
       static AVLnode* sentinel;
       AVLnode() {
              parent = left = right = sentinel;
              height = 0;
       }
```

```
AVLnode(int key) : key(key) {
              parent = left = right = sentinel;
              height = 0;
       }
       void updateHeight() {
              height = 1 + max(left->height, right->height);
       int balanceFactor() {
              return left->height - right->height;
       }
};
AVLnode* AVLnode::sentinel = new AVLnode();
class AVL : public BST {
       typedef AVLnode* nodeptr;
public:
       nodeptr root;
       AVL() : root(NULL) {}
       void insert(int key) { root = insert(root, key); }
private:
       nodeptr rightRotation(nodeptr Q) {
              nodeptr P = Q->left;
              Q->left = P->right;
              Q->left->parent = Q;
              P->right = Q;
              P->parent = Q->parent;
              Q->parent = P;
              Q->updateHeight();
              P->updateHeight();
              return P;
       nodeptr leftRotation(nodeptr P) {
              nodeptr Q = P->right;
              P->right = Q->left;
              P->right->parent = P;
              Q \rightarrow left = P;
              Q->parent = P->parent;
              P->parent = Q;
              Q->updateHeight();
              P->updateHeight();
              return Q;
       }
       nodeptr balance(nodeptr root) {
              if (root->balanceFactor() == 2) {
                     if (root->left->balanceFactor() == -1)
                            root->left = leftRotation(root->left);
                     root = rightRotation(root);
              }
              else if (root->balanceFactor() == -2) {
                     if (root->right->balanceFactor() == 1)
                            root->right = rightRotation(root->right);
                     root = leftRotation(root);
              }
              return root;
       nodeptr insert(nodeptr root, int key) {
              if (root == AVLnode::sentinel)
                     return root = new AVLnode(key);
              if (key < root->key) {
                     root->left = insert(root->left, key);
                     root->left->parent = root;
              }
```

```
else if (key > root->key) {
                     root->right = insert(root->right, key);
                     root->right->parent = root;
              root->updateHeight();
              root = balance(root);
              return root;
       }
};
Heap
template<class T, class cmp = less<T>>
class heap {
       vector<T> v;
       void check() const {
              assert(size() > 0);
       int parent(const int& node) const {
              return (node == 0 ? -1 : (node - 1) / 2);
       int right(const int& node) const {
              int r = 2 * node + 2;
              return (r < size() ? r : -1);</pre>
       int left(const int& node) const {
              int 1 = 2 * node + 1;
              return (1 < size() ? 1 : -1);</pre>
       void reheapUp(const int& node) {
              if (node == 0 || cmp()(v[parent(node)], v[node]))
                     return;
              swap(v[node], v[parent(node)]);
              reheapUp(parent(node));
       }
       void reheapDown(const int& node) {
              int child = left(node);
              if (child == -1)
                     return;
              int rightChild = right(node);
              if (rightChild != -1 && cmp()(v[rightChild], v[child]))
                     child = rightChild;
              if (cmp()(v[node], v[child]))
                     return;
              swap(v[node], v[child]);
              reheapDown(child);
       }
public:
       int size() const {
              return v.size();
       void push(const int& val) {
              v.push back(val);
              reheapUp((int)v.size() - 1);
       const T& top() const {
              check();
              return v[0];
       void pop() {
              check();
              v[0] = v.back();
              v.pop_back();
              reheapDown(0);
```

```
};
```

}

```
Big Integer
class BigInt {
private:
#define CUR (*this)
  const int BASE = 1000000000;//1e9
  vector<int> v;
public:
  BigInt() {
  BigInt(const long long &val) {
    CUR = val;
  BigInt(const string &val) {
    CUR = val;
  int size() const {
    return v.size();
  bool zero() const {
    return v.empty();
  BigInt& operator =(long long val) {
    v.clear();
    while (val) {
      v.push_back(val % BASE);
      val /= BASE;
    return CUR;
  BigInt& operator =(const BigInt &a) {
    v = a.v;
    return CUR;
  BigInt& operator=(const string &s) {
    CUR = 0;
    for (const char &ch : s)
      CUR = CUR * 10 + (ch - '0');
    return CUR;
  }
  bool operator <(const BigInt &a) const {
    if (a.size() != size())
      return size() < a.size();</pre>
```

```
for (int i = size() - 1; i >= 0; i--) {
    if (v[i] != a.v[i])
      return v[i] < a.v[i];
  }
  return false;
}
bool operator >(const BigInt &a) const {
  return a < CUR;
}
bool operator ==(const BigInt &a) const {
  return (!(CUR < a) && !(a < CUR));
bool operator <=(const BigInt &a) const {
  return ((CUR < a) || !(a < CUR));
}
BigInt operator +(const BigInt &a) const {
  BigInt res = CUR;
  int idx = 0, carry = 0;
  while (idx < a.size() \parallel carry) {
    if (idx < a.size())
      carry += a.v[idx];
    if (idx == res.size())
      res.v.push_back(0);
    res.v[idx] += carry;
    carry = res.v[idx] / BASE;
    res.v[idx] \% = BASE;
    idx++;
  }
  return res;
BigInt& operator +=(const BigInt &a) {
  CUR = CUR + a;
  return CUR;
}
BigInt operator *(const BigInt &a) const {
  BigInt res;
  if (CUR.zero() || a.zero())
    return res;
  res.v.resize(size() + a.size());
  for (int i = 0; i < size(); i++) {
    if(v[i] == 0)
      continue;
    long long carry = 0;
    for (int j = 0; carry || j < a.size(); j++) {
      carry += 1LL * v[i] * (j < a.size() ? a.v[i] : 0);
      while (i + j \ge res.size())
        res.v.push_back(0);
```

```
carry += res.v[i + j];
        res.v[i + j] = carry \% BASE;
        carry /= BASE;
      }
    while (!res.v.empty() && res.v.back() == 0)
      res.v.pop_back();
    return res;
  }
  BigInt& operator *=(const BigInt &a) {
    CUR = CUR * a;
    return CUR;
  BigInt& operator /=(const int &a) {
    11 \text{ carry} = 0;
    for (int i = (int) \text{ v.size}() - 1; i >= 0; i--) {
      ll cur = v[i] + carry * BASE;
      v[i] = cur / a;
      carry = cur % a;
    while (!v.empty() && v.back() == 0)
      v.pop_back();
    return CUR;
  friend ostream& operator<<(ostream &out, const BigInt &a) {
    out << (a.zero() ? 0 : a.v.back());
    for (int i = (int) a.v.size() - 2; i >= 0; i--)
      out \ll setfill(0) \ll setw(9) \ll a.v[i];
    return out;
  }
#undef CUR
};
Graph
Graph Data structures
DSU
struct DSU {
      vector<int> rank, parent, size;
      vector<vector<int>> component;
      int forsets;
      DSU(int n) {
             size = rank = parent = vector<int>(n + 1, 1);
             component = vector<vector<int>>(n + 1);
             forsets = n;
             for (int i = 0; i <= n; i++) {
                   parent[i] = i;
                   component[i].push_back(i);
             }
```

}

```
int find_set(int v) {
              if (v == parent[v])
                     return v;
              return parent[v] = find_set(parent[v]);
       }
       void link(int par, int node) {
              parent[node] = par;
              size[par] += size[node];
              for (const int& it : component[node])
                     component[par].push_back(it);
              component[node].clear();
              if (rank[par] == rank[node])
                     rank[par]++;
              forsets--;
       bool union_sets(int v, int u) {
              v = find_set(v), u = find_set(u);
              if (v != u) {
                     if (rank[v] < rank[u])</pre>
                            swap(v, u);
                     link(v, u);
              }
              return v != u;
       bool same_set(int v, int u) {
              return find_set(v) == find_set(u);
       int size_set(int v) {
              return size[find_set(v)];
       }
};
DSU apps
void Painting_subarrays() {
       struct Query {
              int 1, r, c;
              Query(int 1, int r, int c):
                     1(1), r(r), c(c) {
              }
       };
       int n, q;
       cin >> n >> q;
       DSU uf(n);
       vector<int> ans(n + 1);
       vector<Query> query(q);
       for (int i = 0; i < q; i++)
              cin >> query[i].l >> query[i].r >> query[i].c;
       reverse(query.begin(), query.end());
       for (auto q : query) {
              int 1 = q.1, r = q.r, c = q.c;
              for (int cur = uf.find_set(1); cur <= r; cur = uf.find_set(cur)) {</pre>
                     uf.parent[cur] = cur + 1;
                     ans[cur] = c;
              }
       }
}
void RMQ() {
       struct Query {
              int 1, r, idx;
              Query(int 1, int r, int idx):
                     l(1), r(r), idx(idx) {
              }
       };
```

```
int n, q;
       cin \gg n \gg q;
       vector<int> v(n);
       vector < vector < Query >> query(n);
       vector<int> ans(q);
       DSU uf(n);
       for (auto& a : v)
              cin >> a;
       for (int i = 0; i < q; i++) {
              int 1, r;
              cin \gg l \gg r;
              query[r].push_back(Query(l, r, i));
       }
       stack<int> st;
       for (int i = 0; i < n; i++) {</pre>
              while (!st.empty() && v[st.top()] > v[i]) {
                     uf.parent[st.top()] = i;
                     st.pop();
              }
              st.push(i);
              for (auto q : query[i])
                     ans[q.idx] = v[uf.find_set(q.1)];
       }
}
DSU bipartiteness
struct DSU_bipartiteness {
       vector<int> bipartite, rank;
       vector<pair<int, int>> parent;
       DSU_bipartiteness(int n) {
              bipartite = rank = vector<int>(n + 1, 1);
              parent = vector<pair<int, int>>(n + 1);
              for (int i = 0; i <= n; i++)</pre>
                     parent[i] = { i, 0 };
       }
       pair<int, int> find_set(int x) {
              if (x == parent[x].first)
                     return parent[x];
              int parity = parent[x].second;
              parent[x] = find_set(parent[x].first);
              parent[x].second ^= parity;
              return parent[x];
       }
       void union_sets(int x, int y) {
              pair<int, int> p = find_set(x);
              x = p.first;
              int paX = p.second;
              p = find_set(y);
              y = p.first;
              int paY = p.second;
              if (x == y) {
                     if (paX == paY)
                            bipartite[x] = false;
              }
              else {
                     if (rank[x] < rank[y])</pre>
                            swap(x, y);
                     parent[y] = { x, paX ^ paY ^ 1 };
                     bipartite[x] &= bipartite[y];
                     if (rank[x] == rank[y])
                            rank[x]++;
              }
       }
```

```
bool is_bipartite(int x) {
                return bipartite[find set(x).first];
        }
};
LCA
class LCA {
  int n, log N, root = 1;
  vector<int> depth;
  vector<vector<int>> adj, lca;
  void dfs(int node, int parent) {
     lca[node][0] = parent;
     depth[node] = (\sim parent ? depth[parent] + 1 : 0);
     for (int k = 1; k \le \log N; k++) {
       int up\_parent = lca[node][k - 1];
       if (~up_parent)
          lca[node][k] = lca[up\_parent][k - 1];
     for (int child : adj[node])
       if (child != parent)
          dfs(child, node);
  }
public:
  LCA(const vector<vector<int>> &_adj, int root = 1):
       root(root), adj(_adj) {
     adi = adi;
     n = adj.size() - 1;
     logN = log2(n);
     lca = vector < vector < int > (n + 1, vector < int > (logN + 1, -1));
     depth = vector < int > (n + 1);
     dfs(root, -1);
  int get_LCA(int x, int y) {
     if (depth[x] < depth[y])
        swap(x, y);
     for (int k = log N; k >= 0; k--)
       if (depth[x] - (1 << k) >= depth[y])
          x = lca[x][k];
     if(x == y)
       return x;
     for (int k = log N; k >= 0; k -- ) {
       if (lca[x][k] != lca[y][k]) {
          x = lca[x][k], y = lca[y][k];
        }
     return lca[x][0];
  int get_distance(int u, int v) {
     return depth[u] + depth[v] - 2 * depth[get_LCA(u, v)];
  int shifting(int node, int dist) {
     for (int i = log N; i >= 0 && ~node; i--)
```

```
if (dist & (1 << i))
          node = lca[node][i];
     return node;
  }
  edge get_path(int u, int LCA) {
     edge rt;
     for (int k = log N; k >= 0; k--)
       if (depth[u] - (1 \ll k) >= depth[LCA]) {
          rt = merge(rt, lca[u][k]);
          u = lca[u][k].to;
       }
     return rt;
};
Heavy light decomposition
class heavy_light_decomposition { //1-based,if value in node,just update it after build chains
  int n, is_value_in_edge;
  vector<int> parent, depth, heavy, root, pos_in_array, pos_to_node, size;
  const static int merge(int a, int b); //implement it
  struct array_ds { //implement it
     int n;
     array_ds(int n):
          n(n) {
     void update(int pos, int value);
     int query(int l, int r);
  } seg;
  struct TREE {
     int cnt_edges = 1;
     vector<vector<int>> adj;
     //need for value in edges
     vector<vector<int>> edge idx;
     //edge_to need for undirected tree //end of edge in directed tree
     vector<int> edge_to, edge_cost;
     TREE(int n):
          adj(n + 1), edge\_idx(n + 1), edge\_to(n + 1), edge\_cost(n + 1) {
     void add_edge(int u, int v, int c) {
       adj[u].push_back(v);
       adj[v].push_back(u);
       edge_idx[u].push_back(cnt_edges);
       edge_idx[v].push_back(cnt_edges);
       edge_cost[cnt_edges] = c;
       cnt_edges++;
  } tree;
  int dfs_hld(int node) {
     int size = 1, max sub tree = 0;
     for (int i = 0; i < (int) tree.adj[node].size(); i++) {
       int ch = tree.adj[node][i], edge_idx = tree.edge_idx[node][i];
       if (ch != parent[node]) {
```

```
tree.edge to [edge idx] = ch;
          parent[ch] = node;
          depth[ch] = depth[node] + 1;
          int child_size = dfs_hld(ch);
          if (child_size > max_sub_tree)
            heavy[node] = ch, max_sub_tree = child_size;
          size += child size;
       }
     }
     return size;
  vector<tuple<int, int, bool>> get_path(int u, int v) { //l,r,must_reverse?
     vector<pair<int, int>> tmp[2];
     bool idx = 1;
     while (root[u] != root[v]) {
       if (depth[root[u]] > depth[root[v]]) {
          swap(u, v);
          idx = !idx;
       //if value in edges ,you need value of root[v] also (connecter edge)
       tmp[idx].push_back( { pos_in_array[root[v]], pos_in_array[v] });
       v = parent[root[v]];
     if (depth[u] > depth[v]) {
       swap(u, v);
       idx = !idx;
     if (!is_value_in_edge || u != v)
       tmp[idx].push_back( { pos_in_array[u] + is_value_in_edge,
            pos_in_array[v] });
     reverse(all(tmp[1]));
     vector<tuple<int, int, bool>> rt;
     for (int i = 0; i < 2; i++)
       for (auto &it : tmp[i])
          rt.emplace_back(it.first, it.second, i == 0);
     return rt; //u is LCA
  }
public:
  heavy_light_decomposition(int n, bool is_value_in_edge):
       n(n), is_value_in_edge(is_value_in_edge), seg(n + 1), tree(n + 1) {
     heavy = vector<int>(n + 1, -1);
     parent = depth = root = pos_in_array = pos_to_node = size = vector<int>(
          n + 1);
  void add_edge(int u, int v, int c = 0) {
     tree.add_edge(u, v, c);
  void build_chains(int src = 1) {
     parent[src] = -1;
     dfs_hld(src);
     for (int chain_root = 1, pos = 1; chain_root <= n; chain_root++) {
       if (parent[chain_root] == -1
```

```
|| heavy[parent[chain_root]] != chain_root)
          for (int j = \text{chain\_root}; j != -1; j = \text{heavy}[j]) {
             root[i] = chain_root;
            pos_in_array[j] = pos++;
            pos_to_node[pos_in_array[j]] = j;
     }
     if (is_value_in_edge)
       for (int i = 1; i < n; i++)
          update_edge(i, tree.edge_cost[i]);
  void update_node(int node, int value) {
     seg.update(pos_in_array[node], value);
  void update_edge(int edge_idx, int value) {
     update node(tree.edge to[edge idx], value);
  void update_path(int u, int v, ll c) {
     vector<tuple<int, int, bool>> intervals = get_path(u, v);
     for (auto &it: intervals)
        seg.update(get<0>(it), get<1>(it), c);
  node query_in_path(int u, int v) {
     vector<tuple<int, int, bool>> intervals = get path(u, v);
     //initial value,check if handling u == v
     node query res = 0;
     for (auto &it : intervals) {
       int l, r;
       bool rev;
       tie(1, r, rev) = it;
       node cur = seg.query(l, r);
       if (rev)
          cur.reverse();
       query_res = node(query_res, cur);
     return query_res;
};
centroid decomposition
class centroid decomposition {
  vector<br/>bool> centroidMarked;
  vector<int> size;
  void dfsSize(int node, int par) {
     size[node] = 1;
     for (int ch : adj[node])
       if (ch != par && !centroidMarked[ch]) {
          dfsSize(ch, node);
          size[node] += size[ch];
        }
  int getCenter(int node, int par, int size_of_tree) {
```

```
bool is centroid = true;
  int heaviest\_child = -1;
  for (int ch : adi[node])
     if (ch != par && !centroidMarked[ch]) {
       if (size[ch] > size_of_tree / 2)
          is centroid = false;
       if (heaviest_child == -1 || size[ch] > size[heaviest_child])
          heaviest_child = ch;
  if (is_centroid && size_of_tree - size[node] <= size_of_tree / 2)
     return node;
  assert(heaviest_child != -1);
  return getCenter(heaviest_child, node, size_of_tree);
int getCentroid(int src) {
  dfsSize(src, -1);
  int centroid = getCenter(src, -1, size[src]);
  centroidMarked[centroid] = true; //need to mark it after solve?
  return centroid;
int decomposeTree(int root) {
  root = getCentroid(root);
  solve(root);
  for (int ch : adj[root]) {
    if (centroidMarked[ch])
       continue;
    int centroid_of_subtree = decomposeTree(ch);
    //note: root and centroid_of_subtree probably not have a direct edge in adj
     centroidTree[root].push back(centroid of subtree);
     centroidParent[centroid_of_subtree] = root;
  }
  return root;
void calc(int node, int par) {
  //TO-DO
  for (int ch : adj[node])
    if (ch != par && !centroidMarked[ch])
       calc(ch, node);
}
void add(int node, int par) {
  //TO-DO
  for (int ch : adj[node])
    if (ch != par && !centroidMarked[ch])
       add(ch, node);
void remove(int node, int par) {
  //TO-DO
  for (int ch : adj[node])
     if (ch != par && !centroidMarked[ch])
       remove(ch, node);
void solve(int root) {
```

```
//add root
    for (int ch : adj[root])
       if (!centroidMarked[ch]) {
         calc(ch, root);
         add(ch, root);
       }
    //remove root
    for (int ch : adj[root])
       if (!centroidMarked[ch])
         remove(ch, root);
public:
  int n, root;
  vector<vector<int>> adj, centroidTree;
  vector<int> centroidParent;
  centroid decomposition(vector<vector<int>> &adj):
       adj(adj) {
    n = (int) adj.size() - 1;
    size = vector < int > (n + 1);
    centroidTree = vector<vector<int>>(n + 1);
    centroidParent = vector<int>(n + 1, -1);
    centroidMarked = vector < bool > (n + 1);
    root = decomposeTree(1);
  }
};
shortest path algorithms
Dijkstra
struct edge {
       int from, to, weight;
       edge() {
              from = to = weight = 0;
       }
       edge(int from, int to, int weight) :
              from(from), to(to), weight(weight) {
       bool operator <(const edge& other) const {</pre>
              return weight > other.weight;
       }
};
vector<vector<edge>> adj;
//0(E*log(v))
void dijkstra(int src, int dest = -1) {
       priority_queue<edge> q;
       vector<int> dis(adj.size(), INT_MAX), prev(adj.size(), -1);
       q.push(edge(-1, src, 0));
       dis[src] = 0;
       while (!q.empty()) {
               edge e = q.top();
              q.pop();
               if (e.weight > dis[e.to])
                      continue;
              prev[e.to] = e.from;
               if (e.to == dest)
                      break;
```

```
for (edge ne : adj[e.to])
                     if (dis[ne.to] > dis[e.to] + ne.weight) {
                            ne.weight = dis[ne.to] = dis[e.to] + ne.weight;
                            q.push(ne);
                     }
       vector<int> path;
       while (dest != -1) {
              path.push_back(dest);
              dest = prev[dest];
       reverse(path.begin(), path.end());
}
Bellmanford
vector<edge> edgeList;
//0(V*E)
void bellmanford(int n, int src, int dest = -1) {
       vector\langle int \rangle dis(n + 1, oo), prev(n + 1, -1);
       dis[src] = 0;
       bool negativeCycle = false;
       int last = -1, tmp = n;
       while (tmp--) {
              last = -1;
              for (edge e : edgeList)
                     if (dis[e.to] > dis[e.from] + e.weight) {
                            dis[e.to] = dis[e.from] + e.weight;
                            prev[e.to] = e.from;
                            last = e.to;
                     }
              if (last == -1)
                     break;
              if (tmp == 0)
                     negativeCycle = true;
       if (last != -1) {
              for (int i = 0; i < n; i++)</pre>
                     last = prev[last];
              vector<int> cycle;
              for (int cur = last; cur != last || cycle.size() > 1; cur = prev[cur])
                     cycle.push_back(cur);
              reverse(cycle.begin(), cycle.end());
       }
       vector<int> path;
       while (dest != -1) {
              path.push_back(dest);
              dest = prev[dest];
       }
       reverse(path.begin(), path.end());
}
Difference constraints
void difference_constraints() {
       int m;
       cin >> m;
       int cnt = 1;
       while (m--) {
              string x1, x2;
              int w; // x1 - x2 <= w
              cin >> x1 >> x2 >> w;
              map<string, int> id;
              if (id.find(x1) == id.end())
                     id[x1] = cnt++;
```

```
if (id.find(x2) == id.end())
                      id[x2] = cnt++;
              edgeList.emplace_back(id[x2], id[x1], w);
       }
       for (int i = 1; i < cnt; i++)
               edgeList.emplace_back(cnt, i, 0);
       bellmanford(cnt, cnt);
}
Floyed
vector<vector<int>> adj, par;
// adj[i][j] = oo , adj[i][i] = 0 , par[i][j] = i
void init(int n) {
       par = adj = vector<vector<int>>(n + 1, vector<int>(n + 1, oo));
       for (int i = 1; i <= n; i++)
              adj[i][i] = 0;
       for (int i = 1; i <= n; i++)
              for (int j = 1; j <= n; j++)
                      par[i][j] = i;
void floyd() {
       for (int k = 1; k < adj.size(); k++)</pre>
              for (int i = 1; i < adj.size(); i++)</pre>
                      for (int j = 1; j < adj.size(); j++)</pre>
                             if (adj[i][j] > adj[i][k] + adj[k][j]) {
                                     adj[i][j] = adj[i][k] + adj[k][j];
                                     par[i][j] = par[k][j];
                             }
}
void buildPath(int src, int dest) {
       vector<int> path;
       while (src != dest) {
               path.push_back(dest);
              dest = par[src][dest];
       path.push_back(src);
       reverse(path.begin(), path.end());
}
SPFA
vector<vector<edge>> adj;
void spfa(int src) {
  enum visit {
    finished, in_queue, not_visited
  };
  int n = adj.size();
  vector<int> dis(n, INF), prev(n, -1), state(n, not_visited);
  dis[src] = 0;
  deque<int> q;
  q.push_back(src);
  while (!q.empty()) {
    int u = q.front();
    q.pop_front();
    state[u] = finished;
    for (auto &e : adj[u]) {
       if (dis[e.to] > dis[e.from] + e.cost) {
         dis[e.to] = dis[e.from] + e.cost;
         prev[e.to] = e.from;
         if (state[e.to] == not_visited)
```

```
q.push_back(e.to);
         else if (state[e.to] == finished)
            q.push_front(e.to);
         state[e.to] = in_queue;
       }
    }
  }
MST
Kruskal
struct edge {
       int from, to;
       11 weight;
       edge() {
              from = to = weight = 0;
       edge(int from, int to, ll weight) :
              from(from), to(to), weight(weight) {
       bool operator <(const edge& other) const {</pre>
              return weight < other.weight;</pre>
       }
};
vector<edge> edgeList;
pair<int, vector<edge>> MST_Kruskal(int n) {//0(edges*log(edges))
       DSU uf(n);
       vector < edge > edges;
       int mstCost = 0;
       sort(edgeList.begin(), edgeList.end());
       for (auto e : edgeList)
              if (uf.union_sets(e.from, e.to)) {
                     mstCost += e.weight;
                     edges.push_back(e);
       if (edges.size() != n - 1)
              return { INT_MAX, vector<edge>() };
       return { mstCost,edges };
int miniMax(int src, int dest, int n) {
       int max = INT_MIN;
       DSU uf(n);
       sort(edgeList.begin(), edgeList.end());
       for (auto e : edgeList) {
              if (uf.same_set(src, dest))
                     return max;
              uf.union_sets(e.from, e.to);
              max = e.weight;
       }
       return max;
//O(edges*log(edges) + nodes*nodes)
pair<int, vector<edge>> SMST_Kruskal(int n) {
       DSU uf(n);
       sort(edgeList.begin(), edgeList.end());
       vector<edge> take, leave;
       int mstCost = 0;
       for (auto e : edgeList)
              if (uf.union_sets(e.from, e.to)) {
```

```
mstCost += e.weight;
                     take.push back(e);
              }
              else leave.push_back(e);
       pair<int, vector<edge>> ret = { INT_MAX, vector<edge>() };
       for (int i = 0; i < take.size(); i++) {</pre>
              uf = DSU(n);
              vector < edge > edges;
              mstCost = 0;
              for (int j = 0; j < take.size(); j++) {</pre>
                     if (i == j)
                            continue;
                     uf.union_sets(take[j].from, take[j].to);
                     mstCost += take[j].weight;
                     edges.push back(take[j]);
              for (edge e : leave) {
                     if (uf.union_sets(e.from, e.to)) {
                            mstCost += e.weight;
                            edges.push_back(e);
                             break;
                     }
              if (edges.size() == n - 1 && ret.first < mstCost)</pre>
                     ret = { mstCost, edges };
       }
       return ret;
}
Prim
struct edge {
       int from, to, weight;
       edge() {
              from = to = weight = 0;
       edge(int from, int to, int weight) :
              from(from), to(to), weight(weight) {
       bool operator <(const edge& other) const {</pre>
              return weight > other.weight;
       }
};
vector<vector<edge>> adj;
vector<edge> prim(int node) {
       vector<bool> vis(adj.size());
       priority queue<edge> q;
       vector<edge> edges;
       q.push(edge(-1, node, 0));
       while (!q.empty()) {
              edge e = q.top();
              q.pop();
              if (vis[e.to])
                     continue;
              vis[e.to] = true;
              if (e.from != -1)
                     edges.push back(e);
              for (edge ch : adj[e.to])
                     if (!vis[ch.to])
                            q.push(ch);
       return edges;//check it connected or not
}
```

```
SMST
```

```
struct edge {
       int from, to;
       11 weight;
       edge() {
              from = to = weight = 0;
       edge(int from, int to, ll weight) :
              from(from), to(to), weight(weight) {
       bool operator <(const edge& other) const {</pre>
              return weight < other.weight;</pre>
       }
};
int MST_Kruskal(int n, vector<edge> edgeList, vector<edge>& take,
       vector<edge>& leave) {
       DSU uf(n);
       vector<edge> edges;
       sort(edgeList.begin(), edgeList.end());
       int mst_cost = 0;
       for (auto e : edgeList)
              if (uf.union_sets(e.from, e.to)) {
                     take.push_back(e);
                     mst_cost += e.weight;
              }
              else leave.push_back(e);
       return mst_cost;
}
struct LCA {
#define INIT { -1, -2 }
       struct data {
              int lca = -1;
              pair<int, int> max_edges = INIT; //first max,second max (distinct)
       pair<int, int> merge(pair<int, int> a, pair<int, int> b) {
              if (a.first < b.first)</pre>
                     swap(a, b);
              if (b.first == a.first)
                     a.second = max(a.second, b.second);
              else if (b.first > a.second)
                     a.second = b.first;
              return a;
       }
       int logN;
       vector<vector<data>> lca;
       vector<vector<edge>> adj;
       vector<int> depth;
       void dfs(int node, int par) {
              for (edge e : adj[node])
                     if (e.to != par) {
                            depth[e.to] = depth[node] + 1;
                            lca[e.to][0].max_edges.first = e.weight;
                            lca[e.to][0].lca = node;
                            dfs(e.to, node);
                     }
       LCA(int n, vector<edge>& edges) :
              adj(n + 1) {
              for (auto& e : edges) {
```

```
adj[e.from].push_back(e);
                     adj[e.to].push_back(edge(e.to, e.from, e.weight));
              logN = log2(n);
              depth = vector<int>(n + 1);
              lca = vector<vector<data>>(n + 1, vector<data>(logN + 1));
              dfs(1, -1);
              for (int k = 1; k <= logN; k++)</pre>
                     for (int node = 1; node <= n; node++) {</pre>
                             int par = lca[node][k - 1].lca;
                             if (~par) {
                                    lca[node][k].lca = lca[par][k - 1].lca;
                                    lca[node][k].max_edges = merge(lca[node][k - 1].max_edges,
                                           lca[par][k - 1].max_edges);
                             }
                     }
       }
       pair<int, int> max_two_edges(int u, int v) {
              pair<int, int> ans = INIT;
              if (depth[u] < depth[v])</pre>
                     swap(u, v);
              for (int i = logN; i >= 0; i--)
                     if (depth[u] - (1 << i) >= depth[v]) {
                             ans = merge(ans, lca[u][i].max_edges);
                             u = lca[u][i].lca;
                     }
              if (u == v)
                     return ans;
              for (int i = logN; i >= 0; i--)
                     if (lca[u][i].lca != lca[v][i].lca) {
                             ans = merge(ans, lca[u][i].max_edges);
                             ans = merge(ans, lca[v][i].max_edges);
                             u = lca[u][i].lca;
                             v = lca[v][i].lca;
                     }
              ans = merge(ans, lca[u][0].max_edges);
              ans = merge(ans, lca[v][0].max_edges);
              return ans;
       }
};
int main() {
       run();
       int t;
       cin >> t;
       for (int I = 1; I <= t; I++) {
              int n, e;
              cin >> n >> e;
              vector<edge> edgeList(e);
              for (auto& it : edgeList)
                     cin >> it.from >> it.to >> it.weight;
              vector<edge> take, leave;
              int mst_cost = MST_Kruskal(n, edgeList, take, leave);
              if (take.size() != n - 1) {
                     cout << "No way\n";</pre>
                     continue;
              LCA tree(n, take);
              11 \text{ rt} = INF;
              for (edge e : leave) {
                     pair<int, int> p = tree.max_two_edges(e.from, e.to);
                     rt = min(rt, mst_cost - p.first + e.weight);
              if (rt == INF)
                     cout << "No second way\n";</pre>
```

```
else
                     cout << rt << endl;</pre>
       }
}
Tarjan
SCC
vector<vector<int>> adj, scc;
vector<set<int>> dag;
vector<int> dfs_num, dfs_low, compId;
vector<bool> inStack;
stack<int> stk;
int timer;
void dfs(int node) {
       dfs_num[node] = dfs_low[node] = ++timer;
       stk.push(node);
       inStack[node] = 1;
       for (int child : adj[node])
              if (!dfs_num[child]) {
                     dfs(child);
                     dfs_low[node] = min(dfs_low[node], dfs_low[child]);
              else if (inStack[child])
                     dfs_low[node] = min(dfs_low[node], dfs_num[child]);
       //can be dfs_low[node] = min(dfs_low[node], dfs_low[child]);
       if (dfs_low[node] == dfs_num[node]) {
              scc.push_back(vector<int>());
              int v = -1;
              while (v != node) {
                     v = stk.top();
                     stk.pop();
                     inStack[v] = 0;
                     scc.back().push_back(v);
                     compId[v] = scc.size() - 1;
              }
       }
}
void SCC() {
       timer = 0;
       dfs_num = dfs_low = compId = vector<int>(adj.size());
       inStack = vector<bool>(adj.size());
       scc = vector<vector<int>>();
       for (int i = 1; i < adj.size(); i++)</pre>
              if (!dfs num[i])
                     dfs(i);
}
void DAG() {
       dag = vector<set<int>>(scc.size());
       for (int i = 1; i < adj.size(); i++)</pre>
              for (int j : adj[i])
                     if (compId[i] != compId[j])
                            dag[compId[i]].insert(compId[j]);
}
Articulation points and bridges
vector<vector<int>> adj;
```

vector<int> dfs\_num, dfs\_low;

```
vector<bool> articulation_point;
vector<pair<int, int>> bridge;
stack<pair<int, int>> edges;
vector<vector<pair<int, int>>> BCC; //biconnected components
int timer, cntChild;
void dfs(int node, int par) {
       dfs_num[node] = dfs_low[node] = ++timer;
       for (int child : adj[node]) {
              if (par != child && dfs_num[child] < dfs_num[node])</pre>
                     edges.push({ node, child });
              if (!dfs_num[child]) {
                     if (par == -1)
                            cntChild++;
                     dfs(child, node);
                     if (dfs_low[child] >= dfs_num[node]) {
                            articulation_point[node] = 1;
                            //get biconnected component
                            BCC.push_back(vector<pair<int, int>>());
                            pair<int, int> edge;
                            do {
                                   edge = edges.top();
                                   BCC.back().push_back(edge);
                                   edges.pop();
                            } while (edge.first != node || edge.second != child);
                     if (dfs_low[child] > dfs_num[node]) //can be (dfs_low[child] == dfs_num[child])
                            bridge.push_back({ node, child });
                     dfs_low[node] = min(dfs_low[node], dfs_low[child]);
              else if (child != par)
                     dfs_low[node] = min(dfs_low[node], dfs_num[child]);
       }
}
void articulation_points_and_bridges() {
       timer = 0;
       dfs num = dfs low = vector<int>(adj.size());
       articulation_point = vector<bool>(adj.size());
       bridge = vector<pair<int, int>>();
       for (int i = 1; i < adj.size(); i++)</pre>
              if (!dfs_num[i]) {
                     cntChild = 0;
                     dfs(i, -1);
                     articulation_point[i] = cntChild > 1;
              }
}
Edge classification
vector<vector<int>> adj;
vector<int> start, finish;
int timer;
void dfsEdgeClassification(int node) {
       start[node] = timer++;
       for (int child : adj[node]) {
              if (start[child] == -1)
                     dfsEdgeClassification(child);
              else {
                     if (finish[child] == -1)
                            ; // Back Edge
                     else if (start[node] < start[child])</pre>
                            ; // Forward Edge
```

```
else; // Cross Edge
       finish[node] = timer++;
}
2-SAT
#include"..\strongly connected component.h"
int n;
int Not(int x) {
       return (x > n ? x - n : x + n);
void addEdge(int a, int b) {
       adj[Not(a)].push_back(b);
       adj[Not(b)].push_back(a);
}
void add_xor_edge(int a, int b) {
       addEdge(Not(a), Not(b));
       addEdge(a, b);
}
bool _2SAT(vector<int>& value) {
       SCC();
       for (int i = 1; i <= n; i++)
              if (compId[i] == compId[Not(i)])
                     return false;
       vector<int> assign(scc.size(), -1);
       for (int i = 0; i < scc.size(); i++)</pre>
              if (assign[i] == -1) {
                     assign[i] = true;
                     assign[compId[Not(scc[i].back())]] = false;
              }
       for (int i = 1; i <= n; i++)
             value[i] = assign[compId[i]];
       return true;
}
Flows
Maximum bipartite matching
vector<vector<int>> adj;
vector<int> rowAssign, colAssign, vis;
int test_id;
bool canMatch(int i) {
       for (int j : adj[i]) {
              if (vis[j] == test_id)
                     continue;
              vis[j] = test_id;
              if (colAssign[j] == -1 || canMatch(colAssign[j])) {
                     colAssign[j] = i;
                     rowAssign[i] = j;
                     return true;
              }
       }
       return false;
// O(rows * edges) //number of operation could by strictly less than order (1e5*1e5->AC)
int maximum_bipartite_matching(int rows, int cols) {
       int maxFlow = 0;
       rowAssign = vector<int>(rows, -1);
```

```
colAssign = vector<int>(cols, -1);
       vis = vector<int>(cols);
       for (int i = 0; i < rows; i++) {</pre>
               test_id++;
               if (canMatch(i))
                      maxFlow++;
       }
       vector<pair<int, int>> matches;
       for (int j = 0; j < cols; j++)</pre>
               if (~colAssign[j])
                      matches.push_back({ colAssign[j], j });
       return maxFlow;
}
Edmonds Karp
//O( V * E * E)
#define INF 0x3f3f3f3f3f3f3f3f3f1LL
int n:
int capacity[101][101];
int getPath(int src, int dest, vector<int> &parent) {
  parent = vector<int>(n + 1, -1);
  queue<pair<int, int>> q;
  q.push( { src, INF });
  while (q.size()) {
     int cur = q.front().first, flow = q.front().second;
     q.pop();
     if (cur == dest)
       return flow;
     for (int i = 1; i \le n; i++)
       if (parent[i] == -1 && capacity[cur][i]) {
          parent[i] = cur;
          q.push( { i, min(flow, capacity[cur][i]) });
          if (i == dest) return q.back().second;
  }
  return 0;
int Edmonds_Karp(int source, int sink) {
  int max_flow = 0;
  int new_flow = 0;
  vector<int> parent(n + 1, -1);
  while (new_flow = getPath(source, sink, parent)) {
     max_flow += new_flow;
     int cur = sink;
     while (cur != source) {
       int prev = parent[cur];
       capacity[prev][cur] -= new_flow;
       capacity[cur][prev] += new_flow;
       cur = prev;
     };
  }
  return max_flow;
```

#### **Dinic**

```
//O(V*V*E) more faster
struct Dinic { //0-based
  struct flowEdge {
     int from, to;
     11 \text{ cap, flow} = 0;
     flowEdge(int from, int to, ll cap):
          from(from), to(to), cap(cap) {
     }
  };
  vector<flowEdge> edges;
  int n, m = 0, source, sink;
  vector<vector<int>> adj;
  vector<int> level, ptr;
  Dinic(int n, int source, int sink):
       n(n), source(source), sink(sink), adj(n), level(n), ptr(n) {
  void addEdge(int u, int v, ll cap) {
     edges.emplace_back(u, v, cap);
     edges.emplace_back(v, u, 0);
     adj[u].push_back(m);
     adj[v].push_back(m + 1);
     m += 2;
  bool bfs() {
     queue<int> q;
     level = vector < int > (n, -1);
     level[source] = 0;
     q.push(source);
     while (!q.empty()) {
       int cur = q.front();
       q.pop();
       for (auto &id : adj[cur]) {
          if (edges[id].cap - edges[id].flow <= 0)</pre>
             continue;
          int nxt = edges[id].to;
          if (level[nxt] != -1)
             continue;
          level[nxt] = level[cur] + 1;
          q.push(nxt);
     return level[sink] != -1;
  ll dfs(int node, ll cur_flow) {
     if (cur\_flow == 0 || node == sink)
```

```
return cur flow;
     for (int &cid = ptr[node]; cid < adj[node].size(); cid++) {</pre>
       int id = adj[node][cid];
       int nxt = edges[id].to;
       if (level[node] + 1 != level[nxt]
             \parallel edges[id].cap - edges[id].flow <= 0)
          continue;
       ll tmp = dfs(nxt, min(cur_flow, edges[id].cap - edges[id].flow));
       if (tmp == 0)
          continue;
       edges[id].flow += tmp;
       edges[id ^ 1].flow -= tmp;
       return tmp;
     }
     return 0;
  ll flow() {
     11 \text{ max\_flow} = 0;
     while (bfs()) {
       fill(ptr.begin(), ptr.end(), 0);
        while (ll pushed = dfs(source, INF))
          max_flow += pushed;
     return max flow;
};
Min cost Max flow
struct MCMF { //0-based
  struct edge {
     int from, to, cost, cap, flow, backEdge;
     edge() {
       from = to = cost = cap = flow = backEdge = 0;
     edge(int from, int to, int cost, int cap, int flow, int backEdge):
          from(from), to(to), cost(cost), cap(cap), flow(flow), backEdge(
               backEdge) {
     bool operator <(const edge &other) const {
       return cost < other.cost:
     }
  };
  int n, src, dest;
  vector<vector<edge>> adj;
  const int OO = 1e9;
  MCMF(int n, int src, int dest):
       n(n), src(src), dest(dest), adj(n) {
  void addEdge(int u, int v, int cost, int cap) {
     edge e1 = edge(u, v, cost, cap, 0, adj[v].size());
     edge e2 = edge(v, u, -cost, 0, 0, adj[u].size());
```

```
adj[u].push_back(e1);
  adj[v].push_back(e2);
pair<int, int> minCostMaxFlow() {
  int maxFlow = 0, cost = 0;
  while (true) {
     vector<pair<int, int>> path = spfa();
     if (path.empty())
       break:
     int new_flow = OO;
     for (auto &it : path) {
       edge &e = adj[it.first][it.second];
       new_flow = min(new_flow, e.cap - e.flow);
     for (auto &it : path) {
       edge &e = adj[it.first][it.second];
       e.flow += new_flow;
       cost += new_flow * e.cost;
       adj[e.to][e.backEdge].flow -= new_flow;
     maxFlow += new_flow;
  return {maxFlow,cost};
enum visit {
  finished, in_queue, not_visited
};
vector<pair<int, int>> spfa() {
  vector<int> dis(n, OO), prev(n, -1), from_edge(n), state(n,
       not_visited);
  deque<int>q;
  dis[src] = 0;
  q.push_back(src);
  while (!q.empty()) {
     int u = q.front();
     q.pop_front();
     state[u] = finished;
     for (int i = 0; i < adj[u].size(); i++) {
       edge e = adi[u][i];
       if (e.flow \ge e.cap || dis[e.to] \le dis[u] + e.cost)
          continue;
       dis[e.to] = dis[u] + e.cost;
       prev[e.to] = u;
       from\_edge[e.to] = i;
       if (state[e.to] == in_queue)
          continue;
       if (state[e.to] == finished
            \parallel (!q.empty() \&\& dis[q.front()] > dis[e.to]))
          q.push_front(e.to);
       else
          q.push_back(e.to);
       state[e.to] = in_queue;
```

```
if (dis[dest] == OO)
       return { };
    vector<pair<int, int>> path;
    int cur = dest;
    while (cur != src) {
       path.push_back( { prev[cur], from_edge[cur] });
       cur = prev[cur];
    reverse(path.begin(), path.end());
    return path;
  }
};
String
Hashing
struct hashing {
       int MOD, BASE;
       vector<int> Hash, modInv;
       hashing(string s, int MOD, int BASE, char first_char = 'a') :
              MOD(MOD), BASE(BASE), Hash(sz(s) + 1), modInv(sz(s) + 1) {
              modInv[0] = 1;
              11 \text{ base} = 1;
              for (int i = 1; i \le sz(s); i++) {
                     Hash[i] = (Hash[i - 1] + (s[i - 1] - first\_char + 1) * base) % MOD;
                     modInv[i] = power(base, MOD - 2, MOD);
                     base = (base * BASE) % MOD;
              }
       int getHash(int 1, int r) { //1-based
              return ((Hash[r] - Hash[l - 1] + MOD) % MOD * modInv[l]) % MOD;
       }
//MOD = 1e9 + 9 , BASE = 31
//MOD = 2000000011 ,BASE = 53 ->careful of overflow
//MOD = 998634293, BASE = 953
//MOD = 986464091, BASE = 1013
KMP
string pattern;
vector<int> longestPrefix;
int fail(int k, char nxt) {
       while (k > 0 && pattern[k] != nxt)
              k = longestPrefix[k - 1];
       if (nxt == pattern[k])
              k++;
       return k;
void failure function() {
       int n = pattern.size();
       longestPrefix = vector<int>(n);
       for (int i = 1, k = 0; i < n; i++)</pre>
              longestPrefix[i] = k = fail(k, pattern[i]);
```

}

```
void KMP(const string& str) {
       int n = str.size();
       int m = pattern.size();
       for (int i = 0, k = 0; i < n; i++) {
               k = fail(k, str[i]);
               if (k == m) {
                       cout << i - m + 1 << endl; //0-based</pre>
                       k = longestPrefix[k - 1]; // if you want next match
               }
       }
}
Trie tree
class trie {
  struct trie_node {
     bool is_leaf = false;
     map<char, int> next;
     bool have_next(char ch) {
       return next.find(ch) != next.end();
     int& operator[](char ch) {
       return next[ch];
     }
  };
  vector<trie_node> t;
public:
  trie() {
     t.push_back(trie_node());
  void insert(const string &s) {
     int root = 0;
     for (const char &ch: s) {
       if (!t[root].have_next(ch)) {
          t.push_back(trie_node());
          t[root][ch] = t.size() - 1;
          //t[root][ch] = add_node();doesn't work if next is array
       }
       root = t[root][ch];
     t[root].is_leaf = true;
  bool find(const string &s) {
     int root = 0;
     for (const char &ch: s) {
       if (!t[root].have_next(ch))
          return false;
       root = t[root][ch];
     return t[root].is_leaf;
};
```

### **Aho Corasick**

```
struct aho_corasick {
  struct trie_node {
     vector<int> pIdxs; //probably take memory limit
     map<char, int> next;
     int fail;
     trie node():
          fail(-1) {
     bool have_next(char ch) {
       return next.find(ch) != next.end();
     int& operator[](char ch) {
       return next[ch];
  };
  vector<trie_node> t;
  vector<string> patterns;
  vector<int> end_of_pattern;
  vector<vector<int>> adj;
  int insert(const string &s, int patternIdx) {
     int root = 0;
     for (const char &ch: s) {
       if (!t[root].have_next(ch)) {
          t.push_back(trie_node());
          t[root][ch] = t.size() - 1;
        }
       root = t[root][ch];
     t[root].pIdxs.push_back(patternIdx);
     return root;
  int next_state(int cur, char ch) {
     while (cur > 0 && !t[cur].have_next(ch))
       cur = t[cur].fail;
     if (t[cur].have_next(ch))
       return t[cur][ch];
     return 0;
  }
  void buildAhoTree() {
     queue<int>q;
     for (auto &child : t[0].next) {
       q.push(child.second);
       t[child.second].fail = 0;
     while (!q.empty()) {
       int cur = q.front();
       q.pop();
       for (auto &child : t[cur].next) {
          int k = next_state(t[cur].fail, child.first);
          t[child.second].fail = k;
```

```
vector<int> &idxs = t[child.second].pIdxs;
          //dp[child.second] = max(dp[child.second],dp[k]);
          idxs.insert(idxs.end(), all(t[k].pIdxs));
          q.push(child.second);
        }
     }
  }
  void buildFailureTree() {
     adj = vector<vector<int>>(t.size());
     for (int i = 1; i < t.size(); i++)
        adj[t[i].fail].push_back(i);
  aho_corasick(const vector<string> &_patterns) {
     t.push_back(trie_node());
     patterns = _patterns;
     end_of_pattern = vector<int>(patterns.size());
     for (int i = 0; i < patterns.size(); i++)
       end_of_pattern[i] = insert(patterns[i], i);
     buildAhoTree();
     buildFailureTree();
  vector<vector<int>> match(const string &str) {
     int k = 0;
     vector<vector<int>> rt(patterns.size());
     for (int i = 0; i < str.size(); i++) {
       k = next state(k, str[i]);
       for (auto &it : t[k].pIdxs)
          rt[it].push_back(i);
     return rt;
  }
}:
Suffix Automaton
struct suffix_automaton {
  struct state {
     int len, link = 0, cnt = 0;
     bool terminal = false, is_clone = false;
     map<char, int> next;
     state(int len = 0):
          len(len) {
     bool have_next(char ch) {
       return next.find(ch) != next.end();
     void clone(const state &other, int nlen) {
       len = nlen;
       next = other.next;
       link = other.link;
       is_clone = true;
     }
  };
```

```
vector<state> st;
int last = 0;
suffix_automaton() {
  st.push_back(state());
  st[0].link = -1;
}
suffix automaton(const string &s):
     suffix_automaton() {
  for (char ch : s)
     extend(ch);
  mark_terminals();
void mark_terminals() {
  for (int cur = last; cur > 0; cur = st[cur].link)
     st[cur].terminal = true;
}
void extend(char c) {
  int cur = st.size();
  st.push_back(state(st[last].len + 1));
  st[cur].cnt = 1;
  int p = last;
  last = cur;
  while (p != -1 \&\& !st[p].have_next(c)) {
     st[p].next[c] = cur;
     p = st[p].link;
  if (p == -1)
     return;
  int q = st[p].next[c];
  if (st[p].len + 1 == st[q].len) {
     st[cur].link = q;
     return;
   }
  int clone = st.size();
  st.push_back(state());
  st[clone].clone(st[q], st[p].len + 1);
  while (p != -1 \&\& st[p].next[c] == q) {
     st[p].next[c] = clone;
     p = st[p].link;
  st[q].link = st[cur].link = clone;
void calc_number_of_occurrences() {
  vector<vector<int>> lvl(st[last].len + 1);
  for (int i = 1; i < st.size(); i++)
     lvl[st[i].len].push_back(i);
  for (int i = st[last].len; i >= 0; i--)
     for (auto cur : lvl[i])
        st[st[cur].link].cnt += st[cur].cnt;
}
vector<ll> dp;
```

```
11 Count(int cur) { //count number of paths
     ll &rt = dp[cur];
     if (rt)
       return rt;
     rt = 1;
     for (auto ch : st[cur].next)
        rt += Count(ch.second);
     return rt;
  }
  string kth_substring(ll k) { //1-based,different substring,0 = ""
     assert(k \le Count(0));
     string rt;
     int cur = 0;
     while (k > 0) {
       for (auto ch : st[cur].next) {
          if (Count(ch.second) < k)</pre>
             k -= Count(ch.second);
          else {
             rt += ch.first;
             cur = ch.second;
             k--;
             break;
     return rt;
  string longest_common_substring(const string &t) {
     int cur = 0, l = 0, mx = 0, idx = 0;
     for (int i = 0; i < t.size(); i++) {
        while (cur > 0 \&\& !st[cur].have_next(t[i]))  {
          cur = st[cur].link;
          1 = st[cur].len;
       if (st[cur].have_next(t[i])) {
          cur = st[cur].next[t[i]];
          1++;
       if (l > mx) {
          mx = 1;
          idx = i;
        }
     return t.substr(idx - mx + 1, mx);
};
```

### **Suffix array**

```
class suffix_array {
  int getOrder(int a) const {
     return (a < (int) order.size() ? order[a] : 0);
  void radix_sort(int k) {
     vector < int > frq(n), tmp(n);
     for (auto &it : suf)
        frq[getOrder(it + k)]++;
     for (int i = 1; i < n; i++)
       frq[i] += frq[i - 1];
     for (int i = n - 1; i >= 0; i--)
        tmp[--frq[getOrder(suf[i] + k)]] = suf[i];
     suf = tmp;
public:
  int n;
  string s;
  vector<int> suf, lcp, order; // order store position of suffix i in suf array
  suffix_array(const string &s):
        n(s.size() + 1), s(s) {
     suf = order = vector < int > (n);
     vector<int> newOrder(n);
     for (int i = 0; i < n; i++)
        suf[i] = i;
     { //sort according to first character
        vector < int > tmp(n);
       for (int i = 0; i < n; i++)
          tmp[i] = s[i];
        sort(all(tmp));
       for (int i = 0; i < n; i++)
          order[i] = (lower_bound(all(tmp), s[i]) - tmp.begin());
     for (int len = 1; newOrder.back() != n - 1; len <<= 1) {
        auto cmp = [\&](const int &a, const int &b) {
          if (order[a] != order[b])
             return order[a] < order[b];</pre>
          return getOrder(a + len) < getOrder(b + len);
       //sort(all(suf), cmp); //run in 576ms (n<=4e5)
        radix sort(len); //sort second part
       radix_sort(0); //sort first part
        newOrder[0] = 0;
       for (int i = 1; i < n; i++)
          newOrder[i] = newOrder[i - 1] + cmp(suf[i - 1], suf[i]);
       for (int i = 0; i < n; i++)
          order[suf[i]] = newOrder[i];
     buildLCP();
```

```
/*
* longest common prefix
* O(n)
* lcp[i] = lcp(suf[i], suf[i-1])
void buildLCP() {
  lcp = vector < int > (n);
  int k = 0;
  for (int i = 0; i < n - 1; i++) {
     int pos = order[i];
     int j = suf[pos - 1];
     while (s[i+k] == s[j+k])
        k++;
     lcp[pos] = k;
     if (k)
        k--;
   }
}
int LCP_by_order(int a, int b) {
  if(a > b)
     swap(a, b);
  int mn = n - suf[a] - 1;
  for (int k = a + 1; k \le b; k++)
     mn = min(mn, lcp[k]);
  return mn;
//LCP(i,j): longest common prefix between suffix i and suffix j
int LCP(int i, int j) {
  //return LCP_by_order(order[i],order[j]);
  if (order[i] < order[i])</pre>
     swap(i, j);
  int mn = n - i - 1;
  for (int k = order[i] + 1; k \le order[j]; k++)
     mn = min(mn, lcp[k]);
  return mn;
//compare s[a.first..a.second] with s[b.first..b.second]
//-1:a < b, 0:a == b, 1:a > b
int compare_substrings(pair<int, int> a, pair<int, int> b) {
  int lcp = min({ LCP(a.first, b.first), a.second - a.first + 1, b.second - b.first + 1 });
  a.first += lcp;
  b.first += lcp;
  if (a.first <= a.second) {</pre>
     if (b.first <= b.second) {
        if(s[a.first] == s[b.first])
          return 0;
        return (s[a.first] < s[b.first] ? -1 : 1);
     }
     return 1;
  return (b.first <= b.second ? -1 : 0);
```

```
pair<int, int> find_string(const string &x) {
     int st = 0, ed = n;
     for (int i = 0; i < sz(x) && st < ed; i++) {
        auto cmp = [\&](int a, int b) {
          if (a == -1)
             return x[i] < s[b+i];
          return s[a + i] < x[i];
        };
        st = lower\_bound(suf.begin() + st, suf.begin() + ed, -1, cmp)
             - suf.begin();
        ed = upper_bound(suf.begin() + st, suf.begin() + ed, -1, cmp)
             - suf.begin();
     return {st,ed-1};
};
ll number_of_different_substrings(string s) {
  int n = s.size();
  suffix_array sa(s);
  11 \text{ cnt} = 0;
  for (int i = 0; i \le n; i++)
     cnt += n - sa.suf[i] - sa.lcp[i];
  return cnt;
}
string longest_common_substring(const string &s1, const string &s2) {
  suffix_array sa(s1 + "#" + s2);
  vector<int> suf = sa.suf, lcp = sa.lcp;
  auto type = [\&](int idx) {
     return idx <= s1.size();
  };
  int mx = 0, idx = 0;
  int len = s1.size() + 1 + s2.size();
  for (int i = 1; i \le len; i++)
     if (type(suf[i-1]) != type(suf[i]) && lcp[i] > mx) {
        mx = lcp[i];
        idx = min(suf[i - 1], suf[i]);
  return s1.substr(idx, mx);
}
int longest_common_substring(const vector<string> &v) {
  int n = v.size();
  int len = n - 1;
  for (auto &it: v)
     len += it.size();
  string s(len, '.');
  vector<int> type(len + 1, n), frq(n + 1);
  for (int i = 0, j = 0; i < v.size(); i++) {
     if (i)
        s[i] = 'z' + i;
```

```
for (char ch : v[i]) {
        s[j] = ch;
        type[j] = i;
       j++;
     }
  }
  suffix_array sa(s);
  vector<int> suf = sa.suf, lcp = sa.lcp;
  monoqueue q;
  int st = 0, ed = 0, cnt = 0, mx = 0;
  while (st \le s.size()) {
     while (ed <= s.size() && cnt < v.size()) {
        q.push(lcp[ed], ed);
       if (++frq[type[suf[ed]]] == 1)
          cnt++;
        ed++;
     }
     q.pop(st);
     if (cnt == v.size())
        mx = max(mx, q.getMin()); //st+1,ed
     if (--frq[type[suf[st]]] == 0)
       cnt--;
     st++;
  }
  return mx;
string kth_substring(string s, int k) { //1-based,repated
  int n = s.size();
  suffix_array sa(s);
  vector<int> suf = sa.suf, lcp = sa.lcp;
  for (int i = 1; i \le n; i++) {
     int len = n - suf[i];
     int cnt = 0;
     for (int l = 1; l \le len; l++) {
        cnt++;
       int st = i + 1, ed = n, ans = i;
        while (st \leq ed) {
          int md = st + ed \gg 1;
          if (sa.LCP_by_order(i, md) >= 1)
             st = md + 1, ans = md;
          else
             ed = md - 1;
       cnt += ans - i;
       if (cnt >= k)
          return s.substr(suf[i], l);
     k = len;
  assert(0);
```

# **Suffix array Faster** class suffix\_array { const static int alpha = 128; int getOrder(int a) const { return (a < (int) order.size() ? order[a] : 0); public: int n; string s; vector<int> suf, order, lcp; // order store position of suffix i in suf array suffix\_array(const string &s): n(s.size() + 1), s(s) { suf = order = lcp = vector < int > (n);vector<int> bucket\_idx(n), newOrder(n), newsuff(n); vector<int> prev(n), head(alpha, -1); for (int i = 0; i < n; i++) { prev[i] = head[s[i]];head[s[i]] = i;int buc = -1, idx = 0; for (int i = 0; i < alpha; i++) { if (head[i] == -1)continue: bucket idx[++buc] = idx; for (int j = head[i]; $\sim j$ ; j = prev[j]) suf[idx++] = i, order[i] = buc; int len = 1;do { auto cmp = [&](int a, int b) { if (order[a] != order[b]) return order[a] < order[b];</pre> return getOrder(a + len) < getOrder(b + len);**}**; for (int i = 0; i < n; i++) { int j = suf[i] - len;if (j < 0)continue: newsuff[bucket\_idx[order[j]]++] = j; for (int i = 1; i < n; i++) { suf[i] = newsuff[i]; bool cmpres = cmp(suf[i - 1], suf[i]); newOrder[suf[i]] = newOrder[suf[i - 1]] + cmpres; if (cmpres) bucket\_idx[newOrder[suf[i]]] = i; order = newOrder; len <<= 1; $\}$ while (order[suf[n - 1]] != n - 1); } **}**;

# Z algorithm

```
/*
   z[i] equal the length of the longest substring starting from s[i]
    which is also a prefix of s
vector<int> z_algo(string s) {
  int n = s.size();
  vector\langle int \rangle z(n);
  z[0] = n;
  for (int i = 1, L = 1, R = 1; i < n; i++) {
     int k = i - L;
     if(z[k] + i >= R) 
        L = i;
        R = max(R, i);
        while (R < n \&\& s[R - L] == s[R])
           R++;
        z[i] = R - L;
     } else
        z[i] = z[k];
  }
  return z;
}
```

## Math

### **Combinatorics**

```
* nCr = n!/((n-r)! * r!)
 * nCr(n,r) = nCr(n,n-r)
 * nPr = n!/(n-r)!
 * nPr(circle) = nPr/r
 * nCr(n,r) = pascal[n][r]
 * catalan[n] = nCr(2n,n)/(n+1)
ull nCr(int n, int r) {
       if(r > n)
              return 0;
       r = max(r, n - r);
       ull ans = 1, div = 1, i = r + 1;
       while (i \lt = n) {
              ans *= i++;
              ans /= div++;
       return ans;
}
ull nPr(int n, int r) {
       if (r > n)
             return 0;
       ull p = 1, i = n - r + 1;
       while (i <= n)
              p *= i++;
       return p;
vector<vector<ull>>> pascalTriangle(int n) {
```

```
vector<vector<ull>>> pascal(n + 1, vector<ull>(n + 1));
       for (int i = 0; i <= n; i++) {
              pascal[i][i] = pascal[i][0] = 1;
              for (int j = 1; j < n; j++)
                     pascal[i][j] = pascal[i - 1][j] + pascal[i - 1][j - 1];
       return pascal;
}
// return catalan number n-th using dp O(n^2)//max = 35 then overflow
vector<ull> catalanNumber(int n) {
       vector<ull> catalan(n + 1);
       catalan[0] = catalan[1] = 1;
       for (int i = 2; i <= n; i++) {
              ull& rt = catalan[i];
              for (int j = 0; j < n; j++)
                    rt += catalan[j] * catalan[n - j - 1];
       return catalan;
}
// count number of paths in matrix n*m
// go to right or down only
ull countNumberOfPaths(int n, int m) {
       return nCr(n + m - 2, n - 1);
}
NCR pre calculation
const int N = 1e5 + 100;
const int mod = 1e9 + 7;
11 fact[N];
11 inv[N]; //mod inverse for i
11 invfact[N]; //mod inverse for i!
void factInverse() {
       fact[0] = inv[1] = fact[1] = invfact[0] = invfact[1] = 1;
       for (long long i = 2; i < N; i++) {
              fact[i] = (fact[i - 1] * i) % mod;
              inv[i] = mod - (inv[mod % i] * (mod / i) % mod);
              invfact[i] = (inv[i] * invfact[i - 1]) % mod;
       }
11 nCr(int n, int r) {
       if (r > n)
              return 0;
       return (((fact[n] * invfact[r]) % mod) * invfact[n - r]) % mod;
}
Matrices
typedef vector<int> row;
typedef vector<row> matrix;
matrix initial(int n, int m, int val = 0) {
       return matrix(n, row(m, val));
}
matrix identity(int n) {
       matrix rt = initial(n, n);
       for (int i = 0; i < n; i++)rt[i][i] = 1;
       return rt;
}
matrix addIdentity(const matrix& a) {
       matrix rt = a;
```

```
for (int i = 0; i < sz(a); i++)rt[i][i] += 1;
       return rt;
}
matrix add(const matrix& a, const matrix& b) {
       matrix rt = initial(sz(a), sz(a[0]));
       for (int i = 0; i < sz(a); i++)for (int j = 0; j < sz(a[0]); j++)
              rt[i][j] = a[i][j] + b[i][j];
       return rt;
}
matrix multiply(const matrix& a, const matrix& b) {
       matrix rt = initial(sz(a), sz(b[0]));
       for (int i = 0; i < sz(a); i++) for (int k = 0; k < sz(a[0]); k++) {
              if (a[i][k] == 0)continue;
              for (int j = 0; j < sz(b[0]); j++)
                     rt[i][j] += a[i][k] * b[k][j];
       return rt;
}
matrix power(const matrix& a, 11 k) {
       if (k == 0)return identity(sz(a));
       if (k & 1)return multiply(a, power(a, k - 1));
       return power(multiply(a, a), k >> 1);
}
matrix power_itr(matrix a, 11 k) {
       matrix rt = identity(sz(a));
       while (k) {
              if (k & 1)rt = multiply(rt, a);
              a = multiply(a, a); k >>= 1;
       }
       return rt;
}
matrix sumPower(const matrix& a, 11 k) {
       if (k == 0)return initial(sz(a), sz(a));
       if (k & 1)return multiply(a, addIdentity(sumPower(a, k - 1)));
       return multiply(sumPower(a, k >> 1), addIdentity(power(a, k >> 1)));
}
matrix sumPowerV2(const matrix& a, 11 k) {
       int n = sz(a);
       matrix rt = initial(2 * n, 2 * n);
       for (int i = 0; i < 2 * n; i++)
              for (int j = 0; j < n; j++)
                     rt[i][j] = a[i % n][j];
       for (int i = n; i < 2 * n; i++)rt[i][i] = 1;
       return power(rt, k);
}
Matrix class
struct matrix {
       using T = int;
       using row = vector<T>;
       vector<vector<T>> v;
       matrix() {}
       matrix(int n, int m, T val = 0) : v(n, row(m, val)) {
       int size() const {
              return v.size();
       int cols() const {
              return v[0].size();
```

```
}
       matrix operator*(T a) const {
              matrix rt = *this;
              REP(i, rt.size())
                     REP(j, rt.cols())
                     rt.v[i][j] *= a;
              return rt;
       friend matrix operator*(T a, const matrix& b) {
              return (b * a);
       friend matrix operator+(const matrix& a, const matrix& b) {
              assert(a.size() == b.size() && a.cols() == b.cols());
              matrix rt(a.size(), a.cols());
              REP(i, rt.size())
                     REP(j, rt.cols())
                     rt.v[i][j] = a.v[i][j] + b.v[i][j];
              return rt;
       friend matrix operator*(const matrix& a, const matrix& b) {
              assert(a.cols() == b.size());
              matrix rt(a.size(), b.cols());
              REP(i, rt.size())
                     REP(k, a.cols())
                     if (a.v[i][k] == 0)
                            continue;
                     REP(j, rt.cols())
                            rt.v[i][j] += a.v[i][k] * b.v[k][j];
              return rt;
       }
};
matrix identity(int n) {
       matrix r(n, n);
       for (int i = 0; i < n; i++)</pre>
              r.v[i][i] = 1;
       return r;
}
matrix power(matrix a, long long y) {
       assert(y >= 0 && a.size() == a.cols());
       matrix rt = identity(a.size());
       while (y > 0) {
              if (y & 1)
                     rt = rt * a;
              a = a * a;
              y >>= 1;
       }
       return rt;
}
matrix addIdentity(const matrix& a) {
       matrix rt = a;
       REP(i, a.size())
              rt.v[i][i]++;
       return rt;
}
matrix sumPower(const matrix& a, 11 k) {
       if (k == 0)
              return matrix(sz(a), sz(a));
       if (k & 1)
```

```
return a * addIdentity(sumPower(a, k - 1));
       return (sumPower(a, k >> 1) * addIdentity(power(a, k >> 1)));
}
matrix sumPowerV2(const matrix& a, 11 k) {
       int n = sz(a);
       matrix rt(2 * n, 2 * n);
       REP(i, n)
               REP(j, n)
       {
               rt.v[i][j] = a.v[i][j];
               rt.v[i + n][j] = a.v[i][j];
       for (int i = n; i < 2 * n; i++)
               rt.v[i][i] = 1;
       return power(rt, k);
}
Mod inverse
ll power(ll x, ll y, int mod) {
  if (y == 0)
     return 1:
  if (y == 1)
     return x % mod;
  ll r = power(x, y \gg 1, mod);
  return (((r * r) \% \text{ mod}) * power(x, y & 1, mod)) % mod;
ll modInverse(ll b, ll mod) { // if mod is Prime
  return power(b, mod - 2, mod);
Il modInverse(ll b, ll mod) { // if mod is not Prime,g(a,b) must be equal 1
  return power(b, phi_function(mod) - 1, mod);
}
//ax + by = gcd(a, b)
int gcdExtended(int a, int b, int &x, int &y) {
  if (a == 0) {
     x = 0;
    y = 1;
     return b;
  int x1, y1;
  int g = gcdExtended(b \% a, a, x1, y1);
  x = y1 - (b/a) * x1;
  y = x1;
  return g;
int modInverse(int a, int mod) {
  int x, y;
  int g = gcdExtended(a, mod, x, y);
  assert(g == 1);
  x = (x \% mod + mod) \% mod;
  return x;
```

```
template<typename T>
T inverse(T a, T m) { //tourist code
  T u = 0, v = 1;
  while (a != 0) \{
    T t = m / a;
    m = t * a;
    swap(a, m);
    u = t * v;
    swap(u, v);
  }
  assert(m == 1);
  return u;
}
(a^n)%p=result, return n
// (a^n)%p=result,return minimum n
int getPower(int a, int result, int mod) {
       int sq = sqrt(mod);
       map<int, int> mp;
       11 r = 1;
       for (int i = 0; i < sq; i++) {</pre>
              if (mp.find(r) == mp.end())
                      mp[r] = i;
              r = (r * a) \% mod;
       11 tmp = modInverse(r, mod);
       11 cur = result;
       for (int i = 0; i <= mod; i += sq) {</pre>
              if (mp.find(cur) != mp.end())
                      return i + mp[cur];
              cur = (cur * tmp) % mod;//val/(a^sq)
       return INF;
}
// Returns minimum x for which a ^ x % m = b % m.
// a,m not not coprime
int getPower(int a, int b, int m) {
       a \%= m, b \%= m;
       int k = 1, add = 0, g;
       while ((g = \underline{\underline{gcd}(a, m)}) > 1) {
              if (b == k)
                      return add;
              if (b % g)
                      return -1;
              b /= g, m /= g, ++add;
              k = (k * 111 * a / g) % m;
       }
       int n = sqrt(m) + 1;
       int an = 1;
       for (int i = 0; i < n; ++i)</pre>
              an = (an * 111 * a) % m;
       unordered_map<int, int> vals;
       for (int q = 0, cur = b; q <= n; ++q) {</pre>
              vals[cur] = q;
               cur = (cur * 111 * a) % m;
       }
       for (int p = 1, cur = k; p <= n; ++p) {</pre>
               cur = (cur * 1ll * an) % m;
```

```
if (vals.count(cur)) {
                     int ans = n * p - vals[cur] + add;
                     return ans;
              }
       }
       return -1;
}
Primes
typedef vector<pair<11, int>> primeFactors;
const int N = 1e8;
bool isPrime[N + 1];
vector<int> prime;
void sieve() {
       memset(isPrime, true, sizeof(isPrime));
       isPrime[0] = isPrime[1] = false;
       for (int i = 4; i <= N; i += 2)
              isPrime[i] = false;
       for (int i = 3; i * i <= N; i += 2)
              if (isPrime[i])
                     for (int j = i * i; j <= N; j += i + i)
                             isPrime[j] = false;
       for (int i = 1; i <= N; i++)
              if (isPrime[i])
                     prime.push_back(i);
}
// generate prime divisors in n
// n = p1^x1 * p2^x2 .... pn^xn
// O(sqrt(n)) // max = 1e16
primeFactors prime_factors(11 n) {
       primeFactors p;
       int idx = 0;
       while (!(n <= N && isPrime[n]) && idx < prime.size()</pre>
              && 1LL * prime[idx] * prime[idx] <= n) {
              int cnt = 0;
              while (n % prime[idx] == 0)
                     n /= prime[idx], cnt++;
                     p.push_back({ prime[idx], cnt });
              idx++;
       if (n > 1)
              p.push_back({ n, 1 });
       return p;
// return number of Divisors(n) using prime factorization
11 numOfDivisors(primeFactors mp) {
       11 \text{ cnt} = 1;
       for (auto it : mp)
              cnt *= (it.second + 1);
       return cnt;
}
// return sum of Divisors(n) using prime factorization
11 sumOfDivisors(primeFactors mp) {
       11 \text{ sum} = 1;
       for (auto it : mp)
              sum *= sumPower(it.first, it.second);
       return sum;
11 phi function(11 n) {
       11 \text{ result} = n;
```

```
primeFactors pf = prime_factors(n);
       for (auto& it : pf) {
              11 p = it.first;
              result -= (result / p);
       return result;
}
Summations
#define numOfDigit(x) 1+(int)(floor(log10(x)))
#define numOfBits(x) 1+(int)(floor(log2(x)))
//return sum of sequence a, a+x , a+2x .... b
11 sumSequence(11 a, 11 b, 11 x) {
       a = ((a + x - 1) / x) * x;
       b = (b / x) * x;
       return (b + a) * (b - a + x) / (2 * x);
11 sumPower(11 x, 11 y) { //x^0 + x^1 + x^2 ... x^y
       return (power(x, y + 1) - 1) / (x - 1);
// return sum of divisors for all number from 1 to n
//0(n)
11 sumRangeDivisors(int n) {
       11 \text{ ans} = 0;
       for (int x = 1; x <= n; x++)
              ans += (n / x) * x;
       return ans;
}
// return sum of divisors for all number from 1 to n
// calc 1e9 in 42ms, can calc more but need big integer
11 sumRangeDivisors(11 x) {
       11 ans = 0, left = 1, right;
       for (; left <= x; left = right + 1) {</pre>
              right = \times / (\times / left);
               ans += (x / left) * (left + right) * (right - left + 1) / 2;
       return ans;
}
* sum of q^0 + q^1 + q^2 \dots q^N = 1/q if (0 < q < 1)
Calculator
bool delim(char c) {
  return c == ' ';
bool is_op(char c) {
  return c == '+' || c == '-' || c == '*' || c == '/';
bool is_unary(char c) {
  return c == '+' || c=='-';
int priority (char op) {
  if (op < 0) // unary operator
    return 3;
  if (op == '+' || op == '-')
    return 1;
  if (op == '*' || op == '/')
    return 2;
  return -1;
```

```
}
void process_op(stack<int>& st, char op) {
  if (op < 0) {
     int 1 = st.top(); st.pop();
     switch (-op) {
        case '+': st.push(l); break;
        case '-': st.push(-l); break;
   } else {
     int r = st.top(); st.pop();
     int l = st.top(); st.pop();
     switch (op) {
        case '+': st.push(l + r); break;
        case '-': st.push(l - r); break;
        case '*': st.push(1 * r); break;
        case '/': st.push(1 / r); break;
     }
   }
}
int evaluate(string& s) {
  stack<int> st;
  stack<char> op;
  bool may_be_unary = true;
  for (int i = 0; i < (int)s.size(); i++) {
     if (delim(s[i]))
        continue;
     if(s[i] == '(') {
        op.push('(');
        may_be_unary = true;
     else\ if\ (s[i] == ')') {
        while (op.top() != '(') {
           process_op(st, op.top());
           op.pop();
        }
        op.pop();
        may_be_unary = false;
     } else if (is_op(s[i])) {
        char cur_op = s[i];
        if (may_be_unary && is_unary(cur_op))
           cur_op = -cur_op;
        while (!op.empty() && (
              (\operatorname{cur\_op} >= 0 \&\& \operatorname{priority}(\operatorname{op.top}()) >= \operatorname{priority}(\operatorname{cur\_op})) \parallel
              (cur_op < 0 && priority(op.top()) > priority(cur_op))
           )) {
           process_op(st, op.top());
           op.pop();
        op.push(cur_op);
        may_be_unary = true;
      } else {
        int number = 0;
        while (i < (int)s.size() && isalnum(s[i]))
```

```
number = number * 10 + s[i++] - '0';
       --i;
       st.push(number);
       may_be_unary = false;
     }
  }
  while (!op.empty()) {
    process_op(st, op.top());
    op.pop();
  return st.top();
Misc
Bitmask
bool getBit(ll num, int ind) {
       return ((num >> ind) & 1);
11 setBit(ll num, int ind, bool val) {
       return val ? (num | (1LL << ind)) : (num & ~(1LL << ind));</pre>
}
11 flipBit(ll num, int ind) {
       return (num ^ (1LL << ind));</pre>
11 leastBit(ll num) {
       return (num & -num);
}
template<class Int>
Int turnOnLastZero(Int num) {
       return num | num + 1;
template<class Int>
Int turnOnLastConsecutiveZeroes(Int num) {
       return num | num - 1;
template<class Int>
Int turnOffLastBit(Int num) {
       return num & num - 1;
}
template<class Int>
Int turnOffLastConsecutiveBits(Int num) {
       return num & num + 1;
}
//num%mod, mod is a power of 2
11 Mod(11 num, 11 mod) {
       return (num & mod - 1);
bool isPowerOfTwo(11 num) {
       return (num & num - 1) == 0;
void genAllSubmask(int mask) {
```

for (int subMask = mask;; subMask = (subMask - 1) & mask) {

}

//code

if (subMask == 0)
 break;

```
}
/*
    builtin functions:
     _builtin_popcount -> used to count the number of one's
     _builtin_clz -> used to count the leading zeros of the integer
     builtin ctz -> used to count the trailing zeros of the integer
int LOG2(int x) { //floor(log2(x))
       return 31 - __builtin_clz(x);
int LOG2(long long x) { //floor(log2(x))
       return 63 - __builtin_clzll(x);
}
coordinateCompress
void coordinateCompress(vector<int>& axes, vector<int>& iToV,
      map<int, int> vToI, int start = 2, int step = 2) {
       for (auto& it : axes)
              vToI[it] = 0;
       iToV.resize(start + step * vToI.size());
       int idx = 0;
       for (auto& it : vToI) {
              it.second = start + step * idx;
              iToV[it.second] = it.first;
             idx++;
      }
}
Random numbers
//write this line once in top
mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count()* ((uint64_t) new char | 1));
// use this instead of rand()
long long rnd = uniform int distribution<long long>(low, high)(rng);
Custom hash
struct custom hash {
       static uint64 t splitmix64(uint64 t x) {
             x += 0x9e3779b97f4a7c15;
             x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
             x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
             return \times ^ (\times >> 31);
      }
      // for pair
       size_t operator()(pair<uint64_t, uint64_t> x) const {
              static const uint64 t FIXED RANDOM = chrono::steady clock::now().time since epoch().count();
             return splitmix64(x.first + FIXED_RANDOM) ^ (splitmix64(x.second + FIXED_RANDOM) >> 1);
       // for single element
       size_t operator()(uint64_t x) const {
              static const uint64_t FIXED_RANDOM = chrono::steady_clock::now().time_since_epoch().count();
              return splitmix64(x + FIXED_RANDOM);
       }
};
Max histogram area
int maxHistogramArea(vector<int> v) {
       stack<int> st;
       int maxArea = 0, area = 0;
      int i = 0;
```

```
while (i < sz(v)) {
              if (st.empty() || v[st.top()] <= v[i])</pre>
                     st.push(i++);
              else {
                     int top = st.top(); st.pop();
                     if (st.empty())
                            area = v[top] * i;
                     else
                            area = v[top] * (i - st.top() - 1);
                     maxArea = max(maxArea, area);
              }
       while (!st.empty()) {
              int top = st.top(); st.pop();
              if (st.empty())
                     area = v[top] * i;
              else
                     area = v[top] * (i - st.top() - 1);
              maxArea = max(maxArea, area);
       }
       return maxArea;
}
Sorting
long long cnt = 0;
vector<int> v, temp;
// e the first index not have in range array
// like end()
template<class T = less<int>>
void merge_sort(int s, int e, T cmp = less<int>()) {
       if (s + 1 >= e)
              return;
       int m = s + (e - s >> 1);
       merge sort(s, m, cmp);
       merge_sort(m, e, cmp);
       for (int i = s; i < e; i++)
              temp[i] = v[i];
       int i = s, j = m, k = s;
       while (i < m && j < e)
              if (cmp(temp[i], temp[j]))
                     v[k++] = temp[i++];
              else
                     v[k++] = temp[j++], cnt += j - k;
       while (i < m)
              v[k++] = temp[i++];
       while (j < e)
              v[k++] = temp[j++];
}
// 0(n*log(n)/log(base))
// O(n + base) memory
void radix_sort(vector<int>& v, int base) {
       vector<int> tmp(v.size());
       for (int it = 0, p = 1; it < 10; it++, p *= base) {
              vector<int> frq(base);
              for (auto& it : v)
                     frq[(it / p) % base]++;
              for (int i = 1; i < base; i++)</pre>
                     frq[i] += frq[i - 1];
              for (int i = v.size() - 1; i >= 0; i--)
                     tmp[--frq[(v[i] / p) \% base]] = v[i];
              \vee = tmp;
```

```
}
}
void quick_sort(int s, int e) {
       if (s >= e)
              return;
       int j = rand() \% (e - s + 1) + s;
       swap(v[s], v[j]);
       j = s;
       int pivot = v[s];
       for (int i = s + 1; i <= e; i++)
              if (v[i] <= pivot)</pre>
                     swap(v[i], v[++j]);
       swap(v[s], v[j]);
       quick_sort(s, j - 1);
       quick_sort(j + 1, e);
}
LIS binary Search
/* without build
* make upper_bound if can take equal elements */
int LIS(const vector<int>& v) {
       vector<int> lis(v.size());//put value less than zero if needed
       int 1 = 0;
       for (int i = 0; i < sz(v); i++) {</pre>
              int idx = lower_bound(lis.begin(), lis.begin() + 1, v[i]) - lis.begin();
              if (idx == 1)
                     1++;
              lis[idx] = v[i];
       }
       return 1;
void LIS binarySearch(vector<int> v) {
       int n = v.size();
       vector<int> last(n), prev(n, -1);
       int length = 0;
       auto BS = [&](int val) {
              int st = 1, ed = length, md, rt = length;
              while (st <= ed) {
                     md = st + ed \gg 1;
                     if (v[last[md]] >= val)
                            ed = md - 1, rt = md;
                     else st = md + 1;
              }
              return rt;
       };
       for (int i = 1; i < n; i++) {
              if (v[i] < v[last[0]])</pre>
                     last[0] = i;
              else if (v[i] > v[last[length]]) {
                     prev[i] = last[length];
                     last[++length] = i;
              }
              else {
                     int index = BS(v[i]);
                     prev[i] = last[index - 1];
                     last[index] = i;
              }
       cout << length + 1 << "\n";</pre>
       vector<int> out;
       for (int i = last[length]; i >= 0; i = prev[i])
```

```
out.push_back(v[i]);
       reverse(out.begin(), out.end());
       for (auto it : out)
              cout << it << endl;</pre>
}
Mo algorithm
int sqrtN; //use a constent value
struct query {
       int l, r, qIdx, block;
       query(int 1, int r, int qIdx) :
              l(1), r(r), qIdx(qIdx), block(1 / sqrtN) {
       bool operator <(const query& o) const {</pre>
              if (block != o.block)
                     return block < o.block;</pre>
              return (block % 2 == 0 ? r < o.r : r > o.r);
       }
};
int curL, curR, ans;
vector<query> q;
void add(int index);
void remove(int index);
void solve(int 1, int r) {
       while (curL > 1)
              add(--curL);
       while (curR < r)</pre>
              add(++curR);
       while (curL < 1)</pre>
              remove(curL++);
       while (curR > r)
              remove(curR--);
}
vector<int> MO(int n) {
       vector<int> rt(q.size());
       ans = curL = curR = 0;
       add(0);
       sort(q.begin(), q.end());
       for (auto it : q) {
              solve(it.l, it.r);
              rt[it.qIdx] = ans;
       }
       return rt;
}
floyd cycle detection algorithm
template<class IntFunction>
pair<int, int> find_cycle_floyd(IntFunction f, int x0) {
       int tortoise = f(x0), hare = f(f(x0));
       while (tortoise != hare) {
              tortoise = f(tortoise);
              hare = f(f(hare));
       int start = 0;
       tortoise = x0;
       while (tortoise != hare) {
              tortoise = f(tortoise);
              hare = f(hare);
              start++;
       int length = 1;
```

```
hare = f(tortoise);
while (tortoise != hare) {
    hare = f(hare);
    length++;
}
return make_pair(start, length);
}
```

```
Convex Hull Trick
struct Line {
  ll m, c;
  mutable ll p; //p is intersection between cur and next
  bool operator<(const Line &o) const {
     //change to (m>o.m,c < o.c) to get min
     if (m != o.m)
        return m < o.m;
     return c > o.c;
  bool operator<(ll x) const {
     return p < x;
   }
};
struct LineContainer: multiset<Line, less<>> {
  // (for doubles, use \inf = 1/.0, \operatorname{div}(a,b) = a/b)
  static const ll inf = LLONG MAX;
  ll div(ll a, ll b) { // floored division
     return a / b - ((a \land b) < 0 \&\& a \% b);
  bool isect(iterator x, iterator y) {
     if (y == end())
        return x - p = \inf_{x \to 0} 0;
     if (x->m == y->m)
        x->p = inf;
     else
        x->p = div(y->c - x->c, x->m - y->m);
     return x->p>=y->p;
  void add(ll m, ll c) {
     auto z = insert( \{ m, c, 0 \}), y = z++, x = y;
     while (isect(y, z))
        z = erase(z);
     if (x != begin() && isect(--x, y))
        isect(x, y = erase(y));
     while ((y = x) != begin() && (--x)->p >= y->p)
       isect(x, erase(y));
  }
  ll query(ll x) {
     assert(!empty());
     auto l = *lower_bound(x);
     return 1.m * x + 1.c;
   }
```

## Geometry

```
typedef complex<long double> point;
#define sz(a) ((int)(a).size())
#define all(n) (n).begin(),(n).end()
#define EPS 1e-9
#define 00 1e9
#define PI acos(-1.0)
#define X real()
#define Y imag()
#define vec(a,b) ((b)-(a))
#define polar(r,t) ((r)*exp(point(0,(t))))
#define angle(v) (atan2((v).Y,(v).X))
#define length(v) ((long double)hypot((v).Y,(v).X))
#define lengthSqr(v) (dot(v,v))
#define dot(a,b) ((conj(a)*(b)).real())
#define cross(a,b) ((conj(a)*(b)).imag())
#define rotate(v,t) (polar(v,t))
#define rotateabout(v,t,a) (rotate(vec(a,v),t)+(a))
#define reflect(p,m) ((conj((p)/(m)))*(m))
#define normalize(p) ((p)/length(p))
#define same(a,b) (lengthSqr(vec(a,b))<EPS)</pre>
#define mid(a,b) (((a)+(b))/point(2,0))
#define perp(a) (point(-(a).Y,(a).X))
#define colliner pointOnLine
enum STATE {IN, OUT, BOUNDRY};
int dcmp(double x, double y) { return fabs(x - y) <= EPS ? 0 : x < y ? -1 : 1; }
double fixAngle(double A) { return A > 1 ? 1 : (A < -1 ? -1 : A);}</pre>
double fixMod(double a, double b) {return fmod(fmod(a, b) + b, b);}
pointOnLine
bool pointOnLine(const point& a, const point& b, const point& p) {
       return fabs(cross(vec(a, b), vec(a, p))) < EPS;</pre>
}
pointOnRay
inline bool pointOnRay(point a, point b, point p) {
       return dot(vec(a, b), vec(a, p)) > -EPS && pointOnLine(a, b, p);
}
pointOnSegment
inline bool pointOnSegment(point a, point b, point p) {
       return dot(vec(a, b), vec(a, p)) > -EPS && pointOnLine(a, b, p) && <math>dot(vec(b, a), vec(b, p)) > -
EPS;
}
return y of point on line given the line and x of this point
long double getYfromXforline(point a, point b, long double x) {
       if (a.X == b.X)return b.Y;
       long double m = (a.Y - b.Y) / (a.X - b.X);
       long double c = a.Y - m * a.X;
       return m * x + c;
}
```

```
return x of point on line given the line and y of this point
long double getXfromYforline(point a, point b, long double y) {
       if (a.X == b.X)return b.X;
       long double m = (a.Y - b.Y) / (a.X - b.X);
       long double c = a.Y - m * a.X;
       return (y - c) / m;
}
namespace std {
       bool operator <(const point& a, const point& b) {</pre>
              return a.X != b.X ? a.X < b.X : a.Y < b.Y;</pre>
       bool operator >(const point& a, const point& b) {
              return a.X != b.X ? a.X > b.X : a.Y > b.Y;
       // sortsegments butome up , note the point of 1 segment must be sorted
       // the functions that coled must be up of this poisition in code
       bool operator <(const vector<point>& a, const vector<point>& b) {
              point p(a[0].X, getYfromXforline(b[0], b[1], a[0].X));
              if (pointOnSegment(b[0], b[1], p))return a[0].Y < p.Y;</pre>
              p = point(a[1].X, getYfromXforline(b[0], b[1], a[1].X));
              if (pointOnSegment(b[0], b[1], p))return a[1] < p;</pre>
              p = point(b[0].X, getYfromXforline(a[0], a[1], b[0].X));
              if (pointOnSegment(a[0], a[1], p))return p < b[0];</pre>
              p = point(b[1].X, getYfromXforline(a[0], a[1], b[1].X));
              if (pointOnSegment(a[0], a[1], p))return p < b[1];</pre>
              return max(a[0].Y, a[1].Y) < max(b[0].Y, b[1].Y);</pre>
       }
}
return the y of a point that falling up segments untile it fall to ground (as water fall)
double waterFallOnsegments(vector< vector<point> > v, point p) {
       for (int i = (int)v.size() - 1; i >= 0; i--) {
              double x = p.X, y = getYfromXforline(v[i][0], v[i][1], p.X);
              if (y \le p.Y\&pointOnSegment(v[i][0], v[i][1], point(x, y))) {
                     if (v[i][0].Y < v[i][1].Y)p = v[i][0];
                     else p = v[i][1];
              }
       }
       return p.X;
point readpoint() { long double x, y; cin >> x >> y; return point(x, y); }
void printpoint(point P) { cout << P.X << " " << P.Y; }</pre>
// somtimes point is -0.0 it is ronge mmust be 0,0
void fixpoint(point &p) {
       if (p.X<EPS&&p.X>-EPS)p = point(0, p.Y);
       if (p.Y < EPS\&p.Y > -EPS)p = point(p.X, 0);
}
prependecularVecor
bool prependecularVec(const point &a, const point &b) {
       return dot(a, b) == 0;
}
paralelVector
bool paralelVec(const point &a, const point &b) {
       return cross(a, b) == 0;
}
check if a point inside the rectangle
bool pointInsidReqt(point LD, point RU, point P) {
       //note that ">= and <=" not "> and <" it based on your problem...</pre>
```

```
return P.X >= LD.X && P.X <= RU.X && P.Y >= LD.Y && P.Y <= RU.Y;
}
check if a point inside the circle
bool pointInsidCircle(point center, long double rad, point P) {
       long double d = length(vec(center, P));
       return d<rad;//note that " < " not " <= " it based on your problem......</pre>
}
check if a point inside the triangle
bool pointInsidTrian(point P1, point P2, point P3, point P) {
       long double A = fabs(cross(vec(P1, P2), vec(P1, P3)) / 2);
       long double A1 = fabs(cross(vec(P, P2), vec(P, P3)) / 2);
       long double A2 = fabs(cross(vec(P, P1), vec(P, P3)) / 2);
       long double A3 = fabs(cross(vec(P, P1), vec(P, P2)) / 2);
       //total area==areas of 3 triangles and the point is not in the porder =>>(A1>0 ,..)
       return fabs(A - A1 - A2 - A3) < EPS&&A1&&A2&&A3;</pre>
}
line using it's a, b, c
struct line {
       long double a, b, c;
       line(point p1, point p2) {
              if (abs(p1.X - p2.X) < EPS) \{ a = 1.0; b = 0.0; c = -p1.X; \}
                     a = -(long double)(p1.Y - p2.Y) / (p1.X - p2.X);
                     b = 1.0;
                     c = -(long double)(a * p1.X) - p1.Y;
              }
       }
};
Point To Segment
point pointToSegment(point p0, point p1, point p2) {
       ld d1, d2;
       point v1 = p1 - p0, v2 = p2 - p0;
       if ((d1 = dp(v1, v2)) <= 0) return p0;</pre>
       if ((d2 = dp(v1, v1)) <= d1) return p1;</pre>
       1d t = d1 / d2;
       return (p0 + v1 * t);
}
check if to lines are parallel
bool areParallel(line 11, line 12) {
       return abs(11.a - 12.a) < EPS && abs(11.b - 12.b) < EPS;
check if to lines are the same
bool areSame(line 11, line 12) {
       return areParallel(11, 12) && abs(11.c - 12.c) < EPS;</pre>
}
check if to lines are the same using points
bool samelLine(const point &a1, const point &b1,const point &a2, const point &b2)
{
    return paralelVec(vec(a1,b1),vec(a2,b2))&&pointOnLine(a1,b1,a2);
}
check if 2 lines are intersecting
int linIntersect(point a, point b, point p, point q, point &ret) {
```

```
line 11(a, b), 12(p, q);
       if (areParallel(11, 12)) return areSame(11, 12) ? 2 : 0;
                                                                          // no intersection
       // solve system of 2 linear algebraic equations with 2 unknowns
       double x, y;
      x = (12.b * 11.c - 11.b * 12.c) / (12.a * 11.b - 11.a * 12.b);
       // special case: test for vertical line to avoid division by zero
       if (abs(11.b) > EPS) y = -(11.a * x + 11.c);
       else y = -(12.a * x + 12.c);
       ret = point(x, y);
       return 1;}
get angle (AOB): in radian
double angl(point a, point o, point b) {
       point oa = vec(o, a), ob = vec(o, b);
       return acos(dot(oa, ob) / sqrt(norm sq(oa) * norm sq(ob)));
}
// wr answer in team formation :D
double getAngle_A_abc(double a, double b, double c) {
       return acos(fixAngle((b * b + c * c - a * a) / (2 * b * c)));
// \sin(A)/a = \sin(B)/b = \sin(C)/c
// a^2 = b^2 + c^2 - 2b*c*cos(A)
Triangle side given other side and angle
double getSide a bAB(double b, double A, double B) {
       return (sin(A) * b) / sin(B);
}
Triangle angel given other side and angle
double getAngle_A_abB(double a, double b, double B) {
       return asin(fixAngle((a * sin(B)) / b));
}
Line Inside Rectangle
bool lineInsideRectangle(double x1, double x2, double y1, double y2, point st, point ed) {
      if (x2 < x1) swap(x1, x2);
       if (y2 < y1) swap(y1, y2);
       double mnX = min(st.X, ed.X), mxX = max(st.X, ed.X),
             mnY = min(st.Y, ed.Y), mxY = (st.Y, ed.Y);
       return dcmp(x1, mnX) <= 0 && dcmp(x2, mxX) >= 0 && dcmp(y1, mnY) <= 0 && dcmp(y2, mxY) >= 0;
}
check if 2 segments intersect
bool segmentIntersect(point a, point b, point p, point q, point &ret) {
       int ans = linIntersect(a, b, p, q, ret);
       if (ans == 0)return 0;
       // if we check on ray we must use pointOnray() insted of pointOnSegment
       if (ans == 1)return pointOnSegment(a, b, ret) && pointOnSegment(p, q, ret);
      if (a > b)swap(a, b);
      if (p > q)swap(p, q);
      if (b < p | | q < a)return 0;
      ret = max(a, q); return 1;
}
check if a line intersects with a rectangle using its (left dawn) and (right up) points
bool linReqtIntersect(point LD, point RU, point a, point b) {
       point ret;
       point LU = point(LD.X, RU.Y);
       point RD = point(RU.X, LD.Y);
       if (pointInsidReqt(LD, RU, a))return 1;
```

```
if (pointInsidReqt(LD, RU, b))return 1;
      if (segmentIntersect(LU, RU, a, b, ret))return 1;
      if (segmentIntersect(LD, RD, a, b, ret))return 1;
      if (segmentIntersect(LD, LU, a, b, ret))return 1;
      if (segmentIntersect(RD, RU, a, b, ret))return 1;
      return 0;
}
double norm_sq(point v) { return v.X * v.X + v.Y * v.Y; }
convert the angle from degree to radian
double toRad(double d) { return (d * PI) / 180.0; }
convert the angle from radian to degree
double toDeg(double d) {
      if (d < 0) d += 2 * PI; return (d * 180 / PI);</pre>
find angle Anticlockwise from v1 to v2
double getAngle 2vec(point v1, point v2) {
      return toDeg(atan2(cross(v1, v2), dot(v1, v2)));
}
find angle p2p0p1, anti-clock p0p1 to p0p2
double getAngle_3points(point p0, point p1, point p2) {
      return getAngle_2vec(vec(p0, p1), vec(p0, p2));
}
get vector as a point from it length and angle
point getvec(double r, double ang) {
      //if the angle in degree
      ang = toRad(ang);
      double x = cos(ang)*r;
      double y = sin(ang)*r;
      return point(x, y);
}
point scale(point v, double r) {
      return point(v.X*r, v.Y*r);
}
get vector with length R according to a Ray ab
point getVectorWithLengthR(point a, point b, double r) {
      return scale(normalize(vec(a, b)), r); }
get triangle Area using 3 points
long double triangleArea3points(const point& a, const point& b, const point& c) {
      return fabs(cross(a, b) + cross(b, c) + cross(c, a)) / 2;
}
given the area of rectangle using 3 medians
double traingleArea_medians(double m1, double m2, double m3) {
      if (m1 <= 0.0 || m2 <= 0.0 || m3 <= 0.0)return -1; //impossipole
      double s = 0.5*(m1 + m2 + m3);
      double midian_area = (s*(s - m1)*(s - m2)*(s - m3));
      double area = 4.0 / 3.0*sqrt(midian_area);
      if (midian_area <= 0.0 || area <= 0.0)return -1;//impossipole</pre>
      return area;
}
check Overlapping Rectangles using (left down) and (right up) point for each
bool overlapReqt(point LD1, point RU1, point LD2, point RU2, point &LD3, point &RU3) {
```

```
long double x, y;
       x = max(LD1.X, LD2.X);
       y = max(LD1.Y, LD2.Y);
      LD3 = point(x, y); // the left down point for the new rectangle
       x = min(RU1.X, RU2.X);
       y = min(RU1.Y, RU2.Y);
       RU3 = point(x, y);// the left right up for the new rectangle
       return LD3.X < RU3.X&&LD3.Y < RU3.Y;</pre>
}
Given are the (x, y) coordinates of the endpoints of two adjacent sides of a parallelogram.
Find the (x, y) coordinates of the fourth point.
point getForthPoint(point a1, point a2, point b1, point b2) {
       if (same(a1, b1))return a2 + vec(b1, b2);
       if (same(a1, b2))return a2 + vec(b2, b1);
       if (same(a2, b1))return a1 + vec(b1, b2);
       return a1 + vec(b2, b1);
}
get all possible points that complete the parallelogram with another 3 points (triangle)
vector<point> getParalel Tria(point p1, point p2, point p3) {
      vector<point> v(3);
      v[0] = p3 + vec(p2, p1);
      v[1] = p1 + vec(p3, p2);
      v[2] = p3 + vec(p1, p2);
       return v;//each point from them can added to the old 3 points to get the paralelogram
}
check if a polygon with angles = A is regular polygon
bool isRegulPoleg_Angle(double A) {
       for (int i = 3; i < 400; i++)
             if (A == ((i - 2.0)*180.0) / i)return 1;
       return 0;
}
Check if 4 point create a Rectangle
// the order needed colocwise
bool isRect(point a, point b, point c, point d){
       return vec(a, b) = vec(d, c) & vec(a, d) = vec(b, c) & prependecular <math>vec(vec(a, b), vec(a, d));
Check if 4 point create a Square
// the order needed colocwise
bool isSquar(point a, point b, point c, point d){
       return vec(a, b) == vec(d, c) && vec(a, d) == vec(b, c)
             && lengthSqr(vec(a, d)) == lengthSqr(vec(a, b)) && prependecularVec(vec(a, b), vec(a, d));
}
Point distance to Line
double pointDistToLine(point p, point a, point b, point &c) {//line a,b
       // formula: c = a + u * ab
       point ap = vec(a, p), ab = vec(a, b);
       long double u = dot(ap, ab) / lengthSqr(ab);
       c = translate(a, scale(ab, u)); // translate a to c
       return dist(p, c); }
Point distance to segment
// dis p to ab
double pointDistToLineSegment(point p, point a, point b, point &c) {
       point ap = vec(a, p), ab = vec(a, b);
       long double u = dot(ap, ab) / lengthSqr(ab);
```

```
if (u < 0.0) {// closer to a
              c = point(a.X, a.Y); return dist(p, a);
       } // Euclidean distance between p and a
       if (u > 1.0) { // closer to b
              c = point(b.X, b.Y); return dist(p, b);
       } // Euclidean distance between p and b
       c = translate(a, scale(ab, u)); // translate a to c //between a,b
       return dist(p, c);
}
given 2 diagonal points for the square find the other two
void square_points(point p1, point p3, point& p2, point& p4) {
      // center point
       1d cx = (p1.X + p3.X) / 2.;
       1d cy = (p1.Y + p3.Y) / 2.;
       // half-diagonal
      1d dx = (p1.X - p3.X) / 2.;
      1d dy = (p1.Y - p3.Y) / 2.;
                                       // second corner
       1d x2 = cx - dy, y2 = cy + dx;
       1d x4 = cx + dy, y4 = cy - dx;
                                       // Fourth corner
       p2 = point(x2, y2);
      p4 = point(x4, y4);
       return;
}
Circle rad given 2 points and cen
bool circle2PtsRad(point p1, point p2, double r, point& c) {
       double d2 = (p1.X - p2.X) * (p1.X - p2.X) +
              (p1.Y - p2.Y) * (p1.Y - p2.Y);
       double det = r * r / d2 - 0.25;
       if (det < 0.0) return false;</pre>
      double h = sqrt(det);
       c.real((p1.X + p2.X) * 0.5 + (p1.Y - p2.Y) * h);
       c.imag((p1.Y + p2.Y) * 0.5 + (p2.X - p1.X) * h);
       return true;
       // to get the other center, reverse p1 and p2
}
circleCircleIntersectionArea
ld circleCircleIntersectionArea(point cen1, ld r1, point cen2, ld r2) {
       ld dis = hypot(cen1.X - cen2.X, cen1.Y - cen2.Y);
       if (dis > r1 + r2)return 0;
       if (dis <= fabs(r2 - r1) \&\& r1 >= r2)
             return PI * r2 * r2;
       if (dis <= fabs(r2 - r1) && r1 < r2)</pre>
             return PI * r1 * r1;
       1d = r1 * r1, b = r2 * r2;
       ld ang1 = acos((a + dis * dis - b) / (2 * r1 * dis)) * 2;
      1d \ ang2 = acos((b + dis * dis - a) / (2 * r2 * dis)) * 2;
       1d ret1 = .5 * b * (ang2 - sin(ang2));
      ld ret2 = .5 * a * (ang1 - sin(ang1));
       return ret1 + ret2;
}
distance between two points in arc
double calcArc(point p1, point p2, point cen) {
       double d = length(vec(p1, p2));
       double ang = (angle(vec(cen, p1)) - angle(vec(cen, p2))) * 180 / PI;
       if (ang < 0) ang += 360;
       ang = min(ang, 360 - ang);
       return r * ang * PI / 180;
}
```

```
Segment and Segment intersection
bool onSegment(point p, point q, point r) {
       if (q.X \le max(p.X, r.X) \&\& q.X \ge min(p.X, r.X) \&\&
              q.Y \leftarrow \max(p.Y, r.Y) \&\& q.Y > \min(p.Y, r.Y))
              return true:
       return false;
}
ld orientation(point p, point q, point r) {
       1d val = (q.Y - p.Y) * (r.X - q.X) - (q.X - p.X) * (r.Y - q.Y);
       if (val == 0) return 0;
       return (val > 0) ? 1 : 2;
bool doIntersect(point p1, point q1, point p2, point q2) {
       ld o1 = orientation(p1, q1, p2);
       ld o2 = orientation(p1, q1, q2);
       ld o3 = orientation(p2, q2, p1);
       ld o4 = orientation(p2, q2, q1);
       if (fabs(o1 - o2) > EPS && fabs(o3 - o4) > EPS)
              return true;
       if (o1 == 0 && onSegment(p1, p2, q1)) return true;
       if (o2 == 0 && onSegment(p1, q2, q1)) return true;
       if (o3 == 0 && onSegment(p2, p1, q2)) return true;
       if (o4 == 0 && onSegment(p2, q1, q2)) return true;
       return false;
}
3D geometry
// give the sperical distance between 2 points using 2 angels for each (long, lat)
double spherical_distance(double lat1, double lon1, double lat2, double lon2, double rad) {
       double dlon = lon2 - lon1;
       double dlat = lat2 - lat1;
       double a = pow((sin(dlat / 2)), 2) + cos(lat1) * cos(lat2) * pow(sin(dlon / 2), 2);
       double c = 2 * atan2(sqrt(a), sqrt(1 - a));
       return rad * c;
}
3D Point
struct point3D{
       long double x, y, z;
       point3D(){};
       point3D(long double x1, long double y1, long double z1){
              x = x1; y = y1; z = z1;
       bool read(){ if (cin >> x >> y >> z)return 1; return 0; }
       long double dis(point3D other){
              return sqrt(pow(x - other.x, 2) + pow(y - other.y, 2) + pow(z - other.z, 2));
       }
};
The volume of Triangular Pyramid
long double cosRule(long double a, long double b, long double c){
       // Handle denom = 0
       long double res = (b * b + a * a - c*c) / (2 * b *a);
       if (res > 1)
              res = 1;
       if (res < -1)
              res = -1;
       return res;
```

}

```
ld triangularPyramidVolume(ld AB, ld AC, ld BC, ld AD, ld BD, ld CD){
       ld cos1 = cosRule(AD, BD, AB),cos2 = cosRule(BD, CD, BC),cos3 = cosRule(CD, AD, AC);
       ld temp = sqrt(1 + 2 * cos1 * cos2 * cos3 - cos1*cos1 - cos2*cos2 - cos3*cos3);
       return AD * BD * CD * temp / 6;
}
long double pyramidVolume(long double ab, long double ac, long double ad,
       long double bc, long double bd, long double cd) {
       long double w = ab, v = ac, u = ad, U = bc, V = bd, W = cd;
       long double X = (w - U + v) * (U + v + w);
       long double x = (U - v + w) * (v - w + U);
       long double Y = (u - V + w) * (V + w + u);
       long double y = (V - w + u) * (w - u + V);
       long double Z = (v - W + u) * (W + u + v);
       long double z = (W - u + v) * (u - v + W);
       long double a = sqrt(x * Y * Z);
       long double b = sqrt(X * y * Z);
       long double c = sqrt(X * Y * z);
       long double d = sqrt(x * y * z);
       long double volume = -a + b + c + d;
       volume *= a - b + c + d;
       volume *= a + b - c + d;
       volume *= a + b + c - d;
       volume = sqrt(volume) / (192.0 * u * v * w);
       return volume;
}
```

## Java Scanner

```
static class MScanner {
   StringTokenizer st;
   BufferedReader br;
   public MScanner(InputStream system) {
      br = new BufferedReader(new InputStreamReader(system));
   }
   public MScanner(String file) throws Exception {
      br = new BufferedReader(new FileReader(file));
   }
   public String next() throws IOException {
      while (st == null !st.hasMoreTokens())
```

```
st = new StringTokenizer(br.readLine());
  return st.nextToken();
public String nextLine() throws IOException {
  return br.readLine();
}
public int nextInt() throws IOException {
  return Integer.parseInt(next());
}
public double nextDouble() throws IOException {
  return Double.parseDouble(next());
}
public char nextChar() throws IOException {
  return next().charAt(0);
public long nextLong() throws IOException {
  return Long.parseLong(next());
}
public int[] intArr(int n) throws IOException {
  int[]in=new int[n];for(int i=0;in;i++)in[i]=nextInt();
  return in;
}
public long[] longArr(int n) throws IOException {
  long[]in=new long[n];for(int i=0;in;i++)in[i]=nextLong();
  return in;
public int[] intSortedArr(int n) throws IOException {
  int[]in=new int[n];for(int i=0;in;i++)in[i]=nextInt();
  shuffle(in);
  Arrays.sort(in);
  return in:
public long[] longSortedArr(int n) throws IOException {
  long[]in=new long[n];for(int i=0;in;i++)in[i]=nextLong();
  shuffle(in);
  Arrays.sort(in);
  return in;
static void shuffle(int[]in) {
  for(int i=0;iin.length;i++) {
     int idx=(int)(Math.random()in.length);
     int tmp=in[i];
    in[i]=in[idx];
     in[idx]=tmp;
static void shuffle(long[]in) {
```

```
for(int i=0;iin.length;i++) {
     int idx=(int)(Math.random()in.length);
     long tmp=in[i];
    in[i]=in[idx];
     in[idx]=tmp;
}
public Integer[] IntegerArr(int n) throws IOException {
  Integer[]in=new Integer[n];for(int i=0;in;i++)in[i]=nextInt();
  return in;
public Long[] LongArr(int n) throws IOException {
  Long[]in=new Long[n];for(int i=0;in;i++)in[i]=nextLong();
  return in;
}
public boolean ready() throws IOException {
  return br.ready();
}
public void waitForInput() throws InterruptedException {
  Thread.sleep(3000);
}
```

}