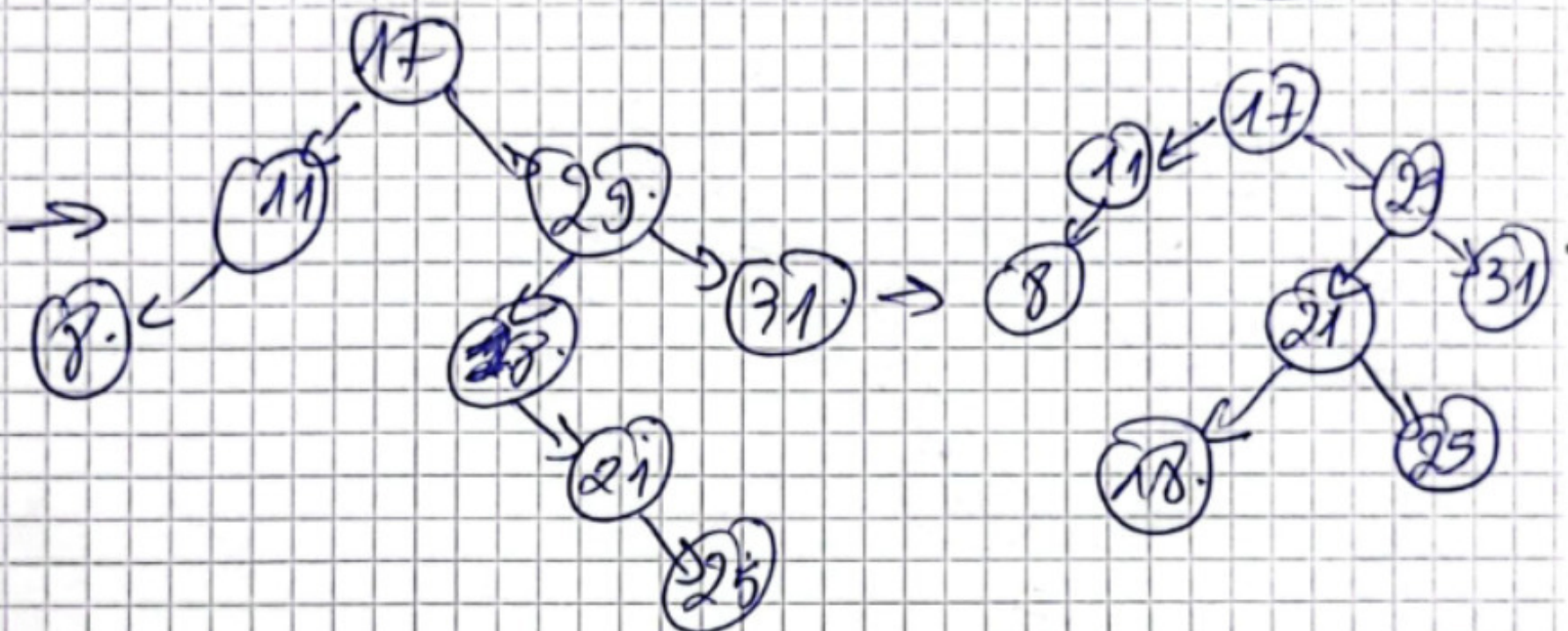
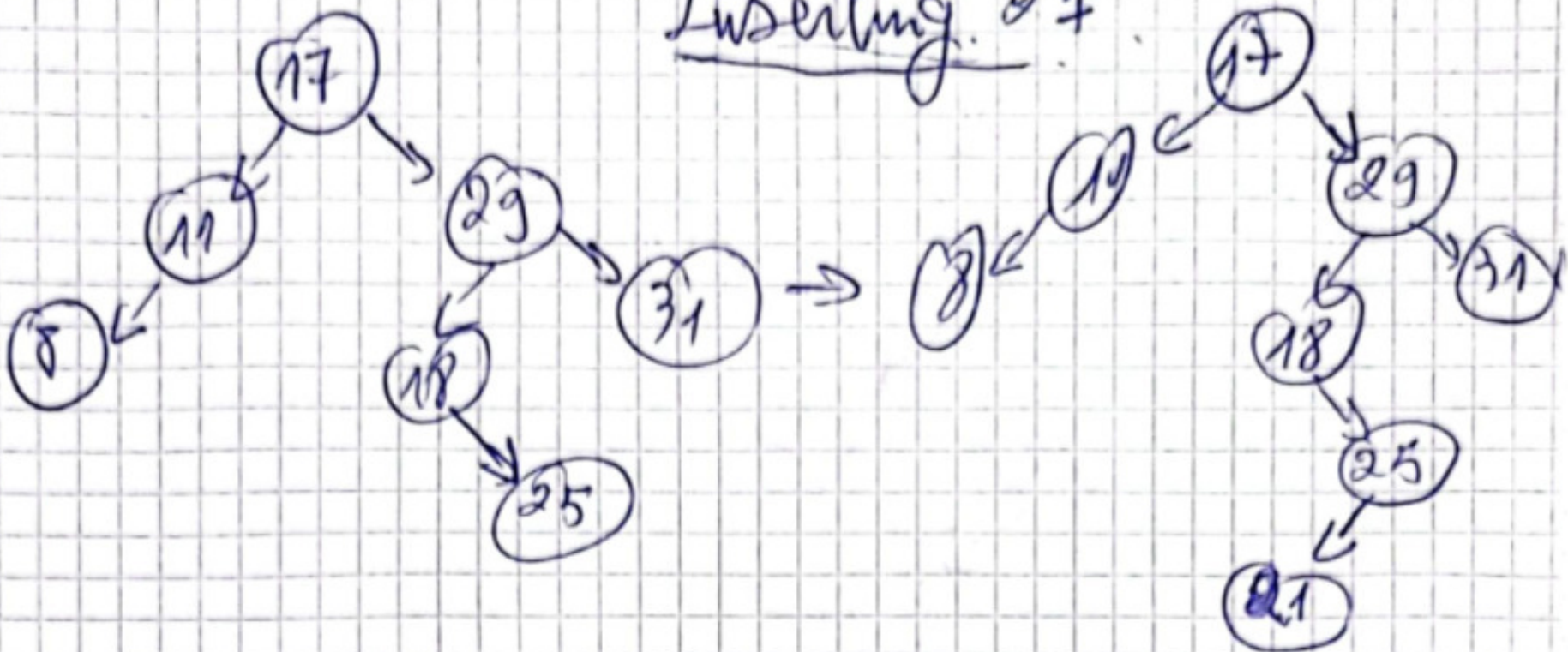
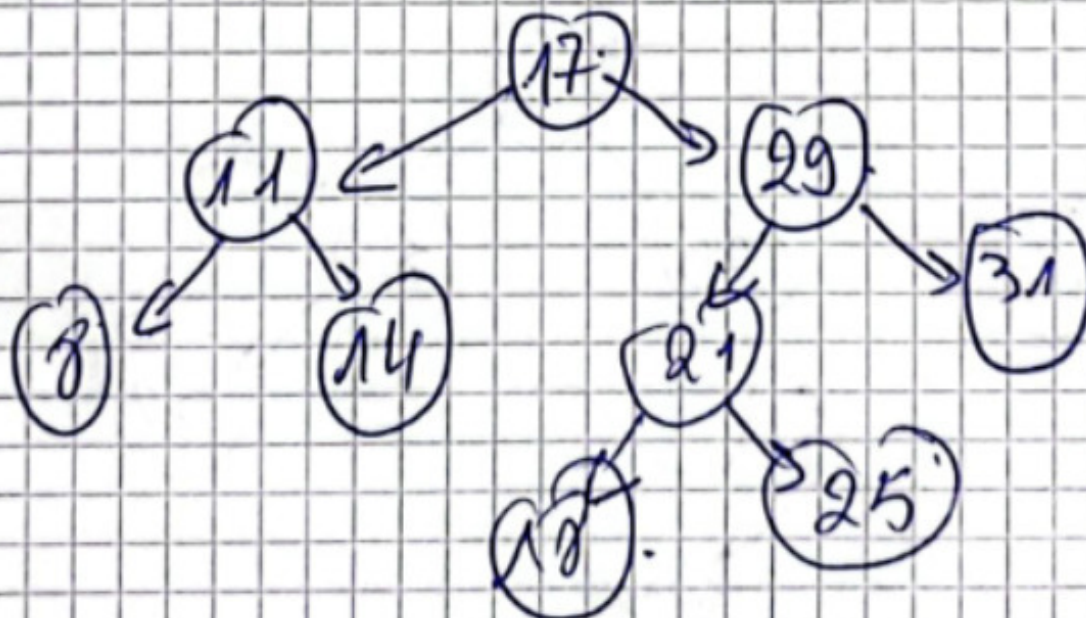


Exercise 1.

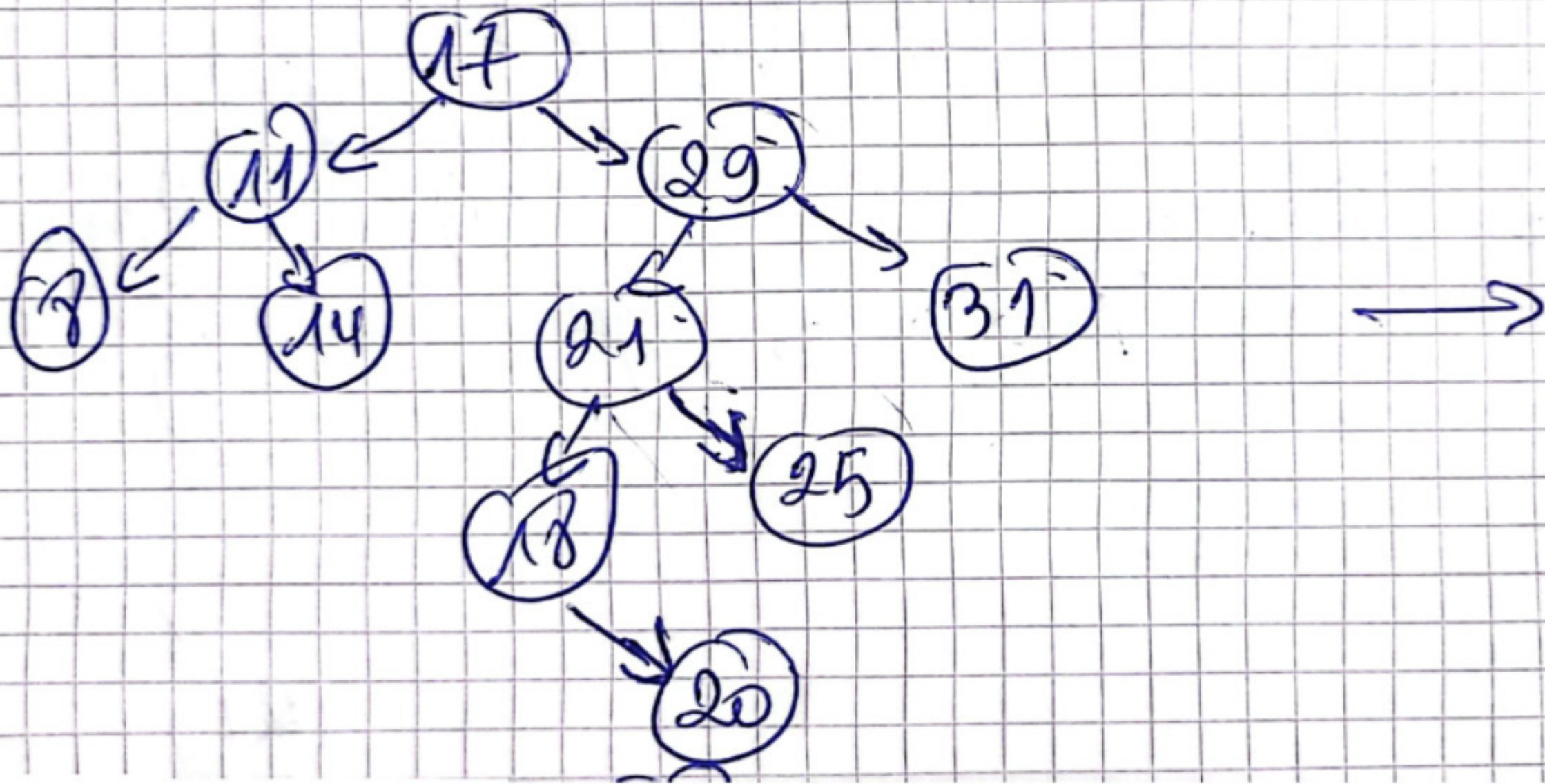
Inserting 04

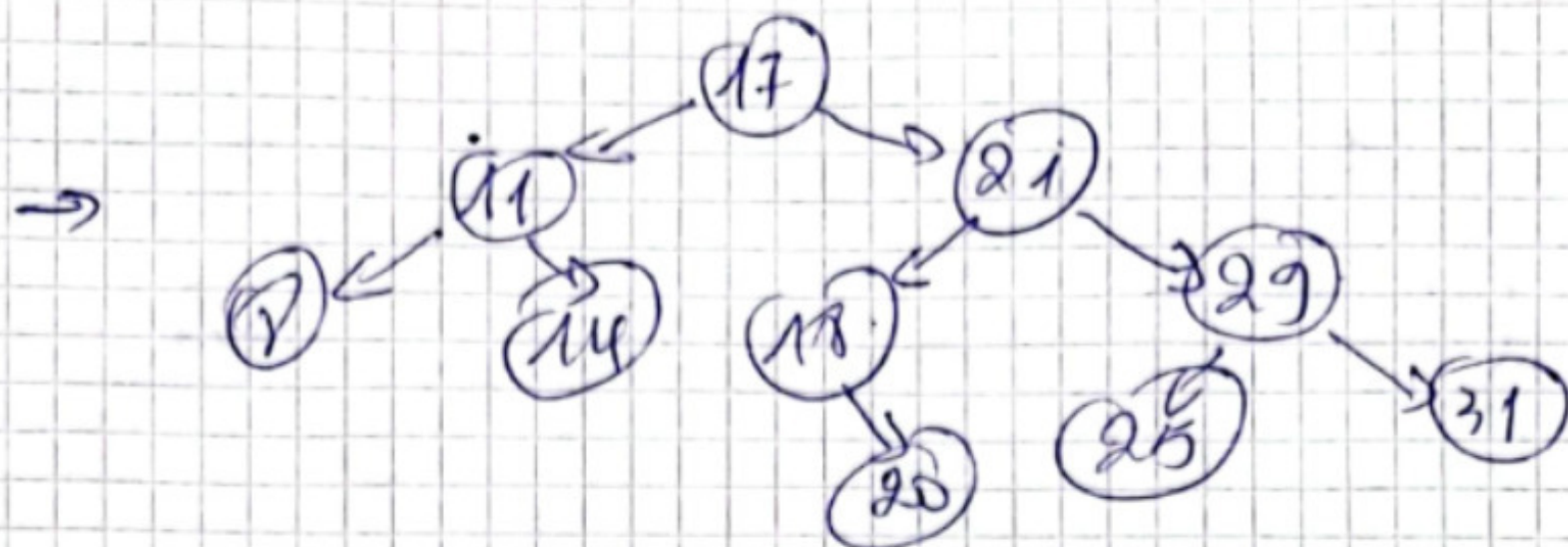


Inserting 14

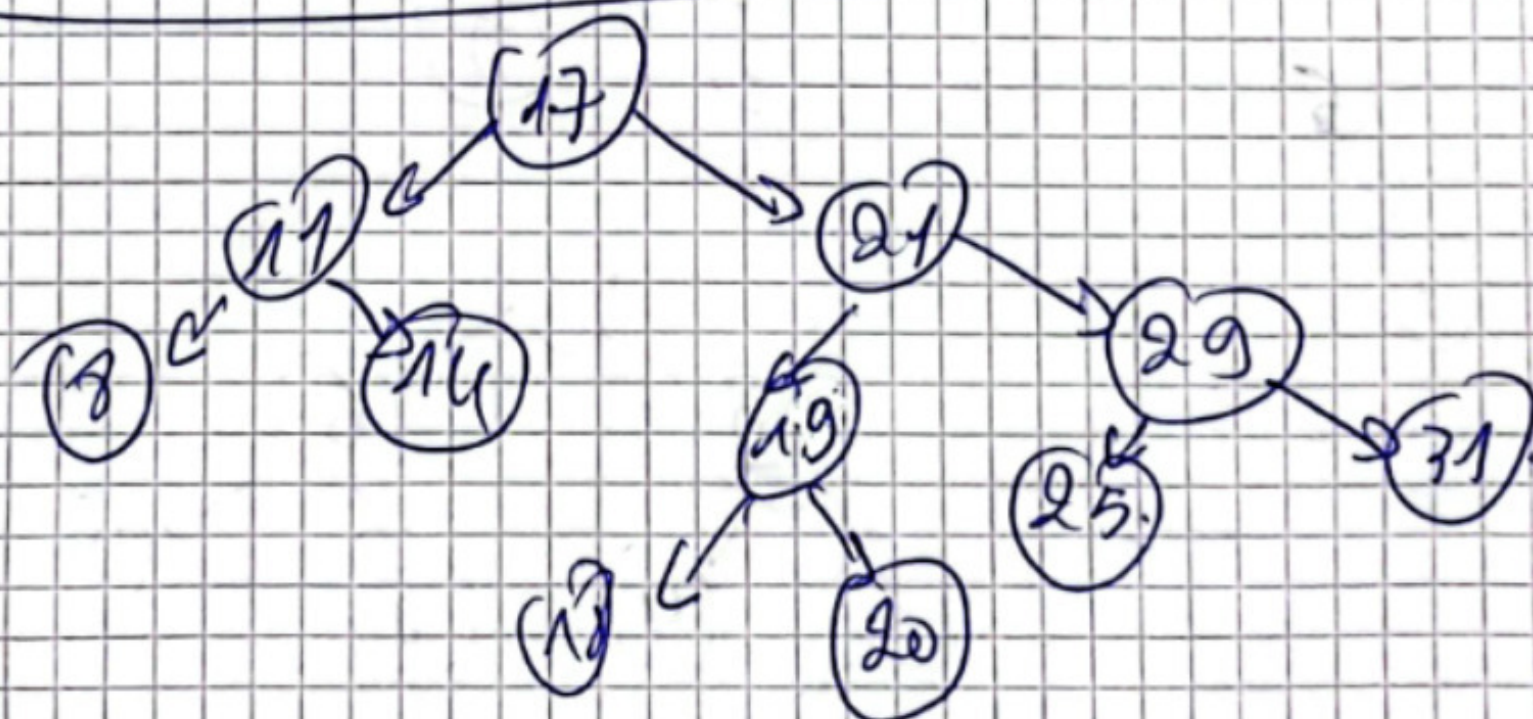
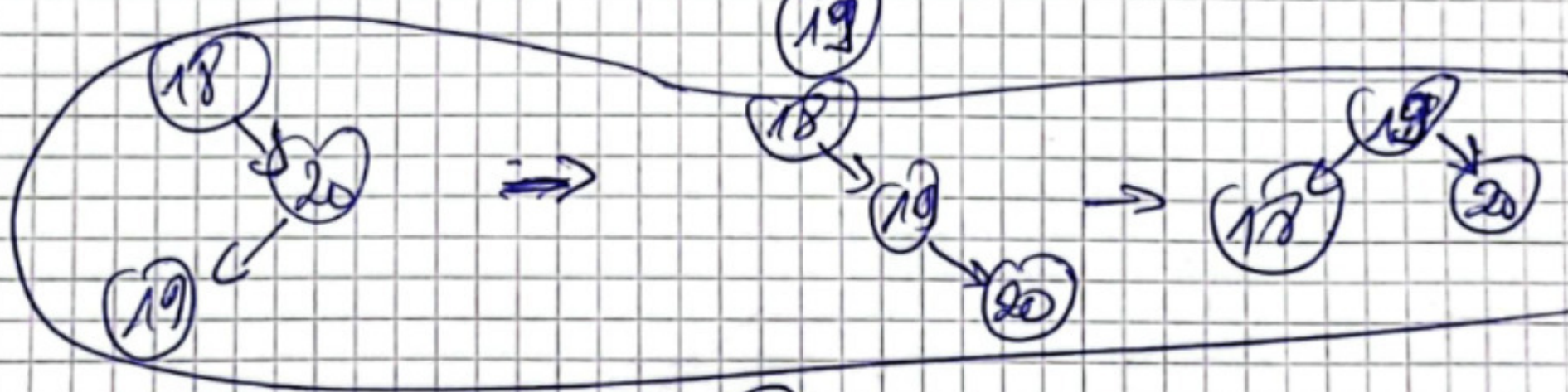
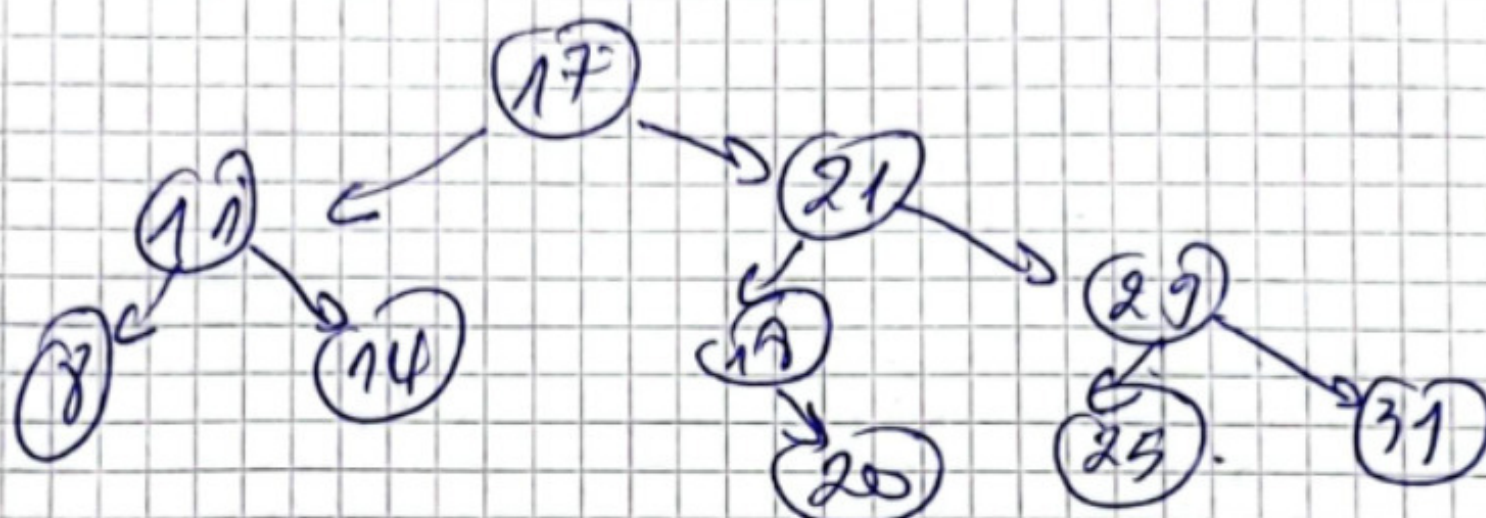


Inserting 20





Inserting 19.

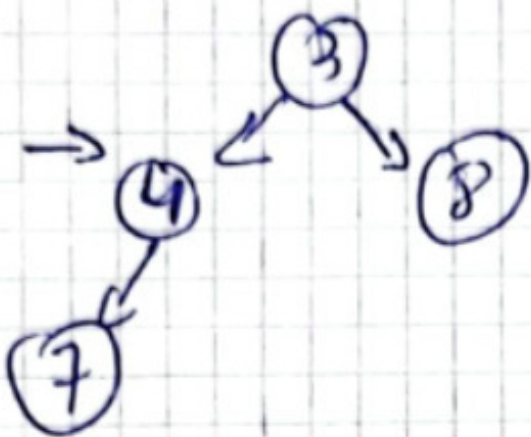
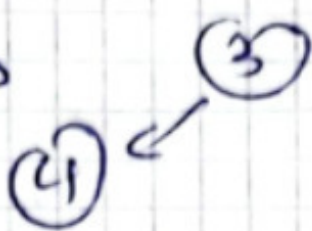


Exercise 2.

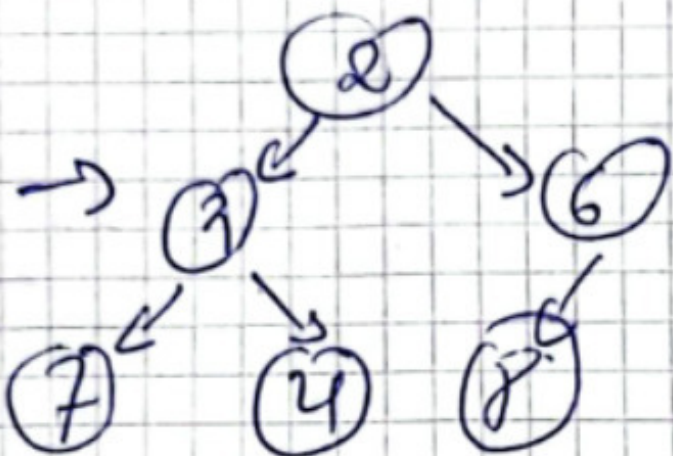
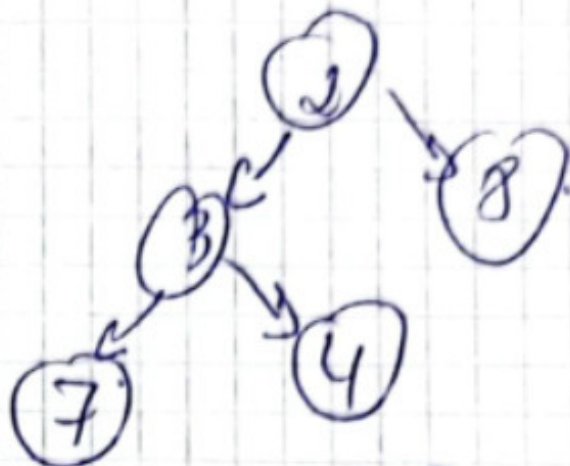
(a)

3

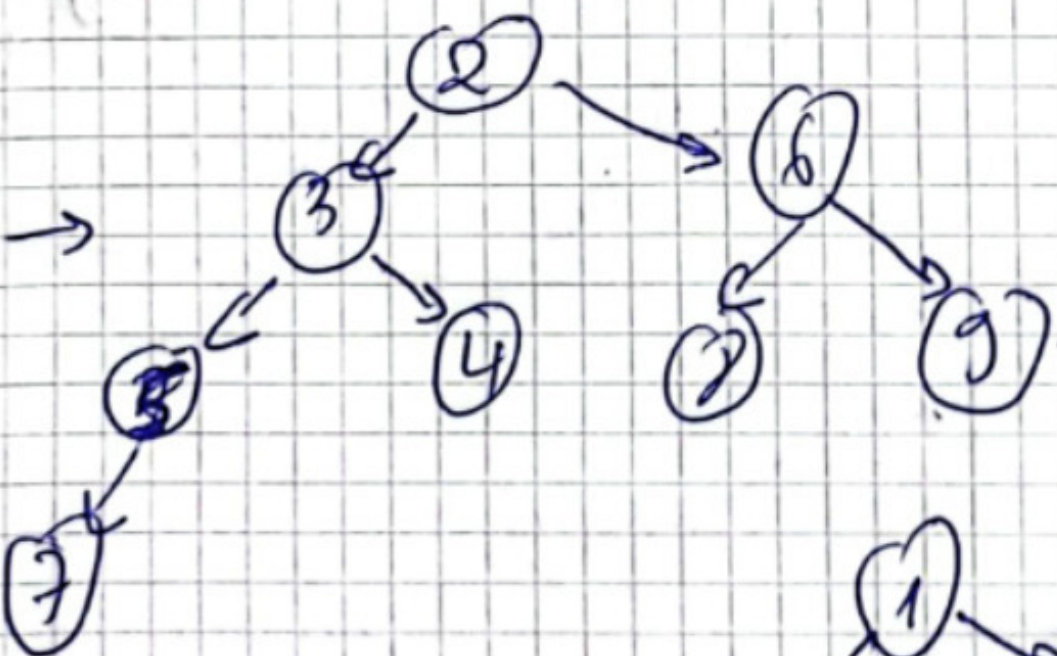
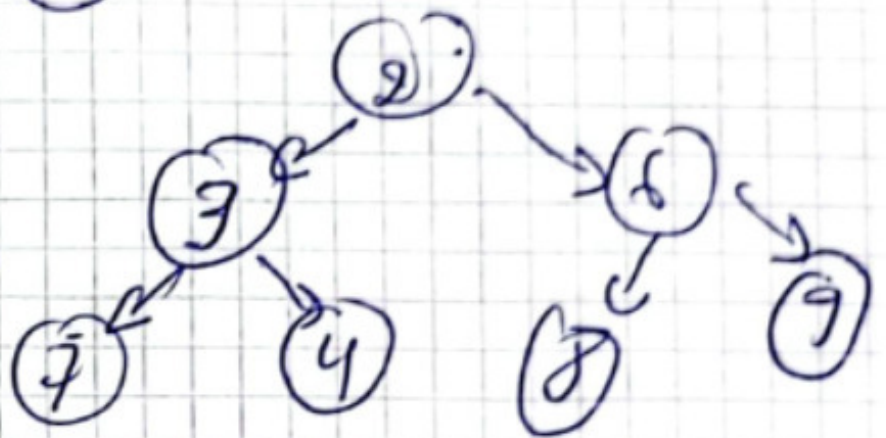
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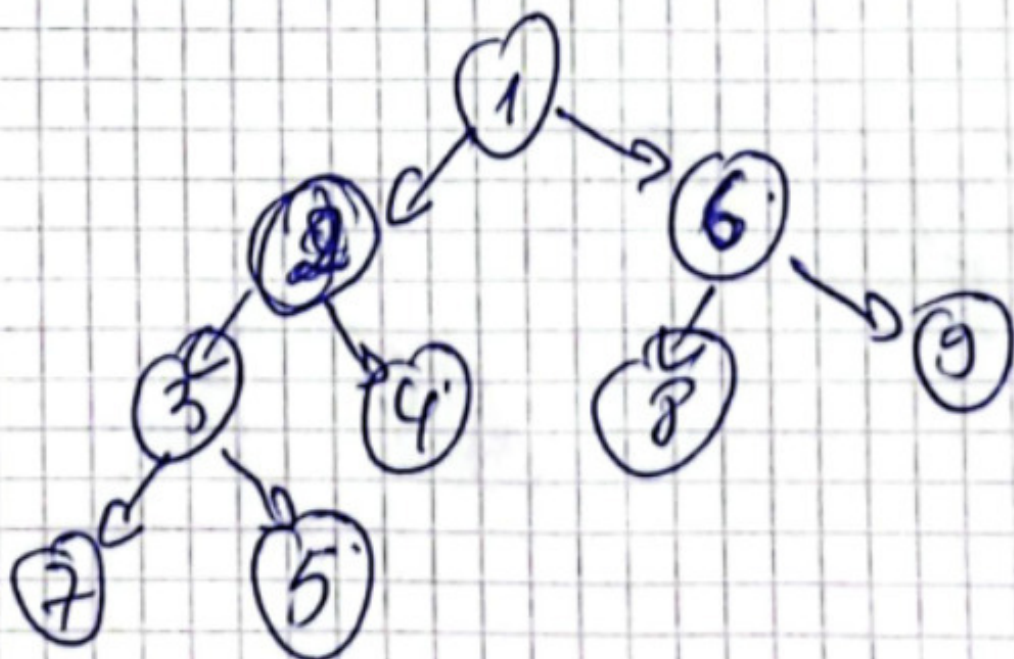
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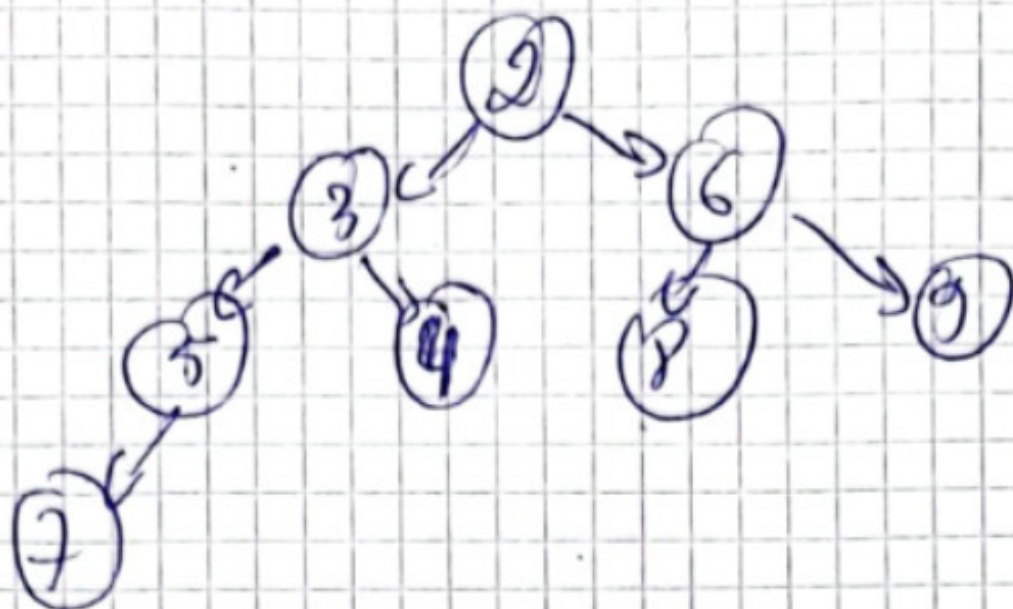
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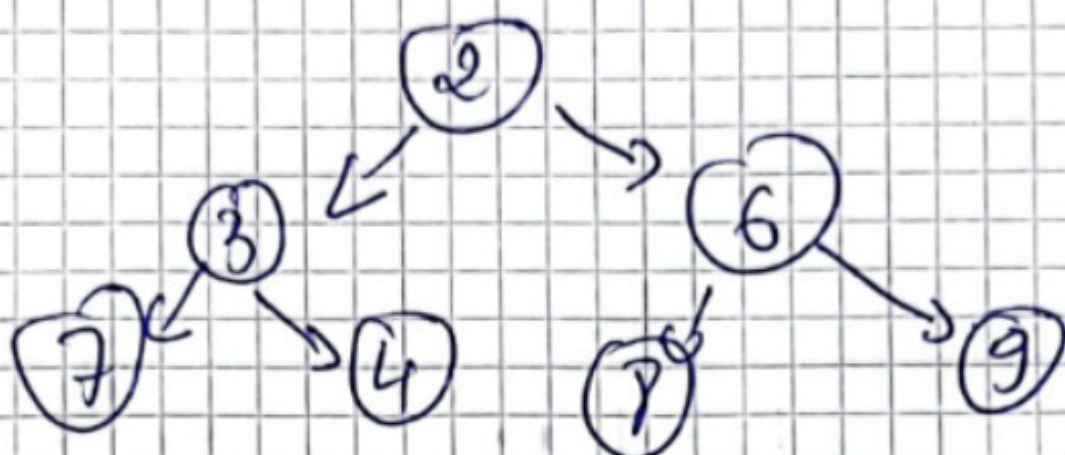
→



(b)



(c)



(d) in the obtained tree in question (c):

- The minimum: ~~2~~ 2

- The maximum: 4

* for a min heap of height h :

- The minimum: h

- The maximum: $2h$

(f) The minimum of comparison : h

The maximum : $2h$

(e) 1) $O(\log N)$

2) $O(N \log N)$

3) $O(N)$

4) $O(\log N)$

Exo 3:

q/

Key Value	Home slot	Prob Sequence
43	1	
23	2	
1	5	
0	3	
15	1	2, 3, 4
31	0	
4	0	1, 2, 3, 4, 5, 6
7	8	
11	9	
3	9	no

Slot	0	1	2	3	4	5	6	7	8	9	10
content	31	43	23	0	15	1	4		7	11	3

b).

Key Value	Home Slot	Prob Sequence
43	1	
23	2	
1	5	
0	3	
15	1	2, 4
31	0	
4	0	1, 3, 6
7	8	
11	9	
3	9	no

Slot	0	1	2	3	4	5	6	7	8	9	10
Content	31	43	23	0	15	1	4		7	11	3

c)

Key Value	Home Slot	Prob Sequence
43	1	
23	2	
1	5	
0	3	
15	1	8
31	0	
4	0	4
7	8	4, 0, 7
11	9	
3	9	1, 4, 7, 10

Slot	0	1	2	3	4	5	6	7	8	9	10
Content	31	43	23	0	4	1		7	15	11	3

exercice 4:

1) structures :

```
class Book{
    friend ostream& operator<<(ostream&,const Book&);
private:
    string bookName;
    string authorName;
    Book* nextBook;
public:
    Book(string bookN,string authorN):bookName(bookN),authorName(authorN),nextBook(nullptr){};
    ~Book();
    string getbookName()const;
    string getauthorName()const;
    Book* getNextBook();
    void setbookName(string bookN);
    void setauthorName(string authorN);
    void setNextBook(Book* p);
};

class Category{
    friend ostream& operator<<(ostream& out,const Category& a);
private:
    string CategoryName;
    int NumOfBooks;
    Category* nextCategory;
    Book* books;           //pointer to the root of the linked list of books
public:
    Category(string cn):CategoryName(cn),NumOfBooks(0),nextCategory(nullptr),books(nullptr){};
    ~Category();
    Category* getNextCategory()const;
    string getCategoryName()const;
    void setNextCategory(Category* a);
    int getNumberOfBooks()const;
    void addBook(string bn,string an);
    void displayBooks();
};

class Library{
private:
    int NumberOfCat;
    Category* Categories;   // pointer to the root of the linked list of categories
public:
    Library():Categories(nullptr){};
    ~Library(){};
}

2)void addCategory(string CategoryName,int NumOfBooks=0){
    if(Categories==nullptr) Categories=new Category(CategoryName);
    else{
        Category* p=Categories;
        while (p->getNextCategory()!=nullptr){p=p->getNextCategory();}
        p->setNextCategory(new Category(CategoryName));
    }
};
```



```

3)
void addBookAtBegin(string CategoryName,string bookName,string authorName){
    Category* p=Categories;
    while(p!=nullptr && p->getCategoryName()!=CategoryName){p=p->getNextCategory();}
    if(p==nullptr){
        //if the category doesnt exist, create it
        this->addCategory(CategoryName);
        addBookAtBegin(CategoryName,bookName,authorName);
    }else{
        p->setNumberOfBooks(p->getNumberOfBooks()+1);
        Book* p1=p->getBooks();
        p->setBooks(new Book(bookName,authorName));
        (p->getBooks())->setNextBook(p1);
    }
};

4)
void displayBooksInCategory(string CategoryName){
    Category* p=Categories;
    while(p!=nullptr && p->getCategoryName()!=CategoryName){p=p->getNextCategory();}
    if(p==nullptr){
        cout << "This category does not exist(" << CategoryName << ")" << endl;
    }else{
        cout << "The books of category'" << CategoryName << " : " << endl;
        // p->displayBooks();
        Book* pp=p->getBooks();
        while (pp!=nullptr){
            cout << "----->Book name : " << pp->getbookName() << endl;
            cout << "\tAuthor name : " << pp->getauthorName() << endl;
            pp=pp->getNextBook();
        }
    }
};

5)
int Total(){
    int total=0;
    Category* p=Categories;
    while(p!=nullptr){
        total+=p->getNumberOfBooks();
        p=p->getNextCategory();
    }
    return total;
};

6)
void deleteCategory(string cn){
    if(Categories->getCategoryName()==cn){
        Category* p=Categories;
        Categories=p->getNextCategory();
        delete p;
    }else{
        Category* p=Categories;
        while(p!=nullptr && p->getCategoryName()!=cn){p=p->getNextCategory();}
        if(p!=nullptr){
            Category* k=Categories;
            while((k->getNextCategory())->getCategoryName()!=cn){
                k=k->getNextCategory();
            }
            k->setNextCategory(p->getNextCategory());
            delete p;
        }
    }
};

```


with the destructors :

```
~Category(){
    Book* a[NumOfBooks];
    int i=0;
    Book* p=books;
    while (p!=nullptr){
        a[i++]=p;
        p=p->getNextBook();
    }
    books=nullptr;
    for(int j=0;j<NumOfBooks;j++){
        delete a[j];
    }
};

~Book(){
    delete nextBook;
};
```