

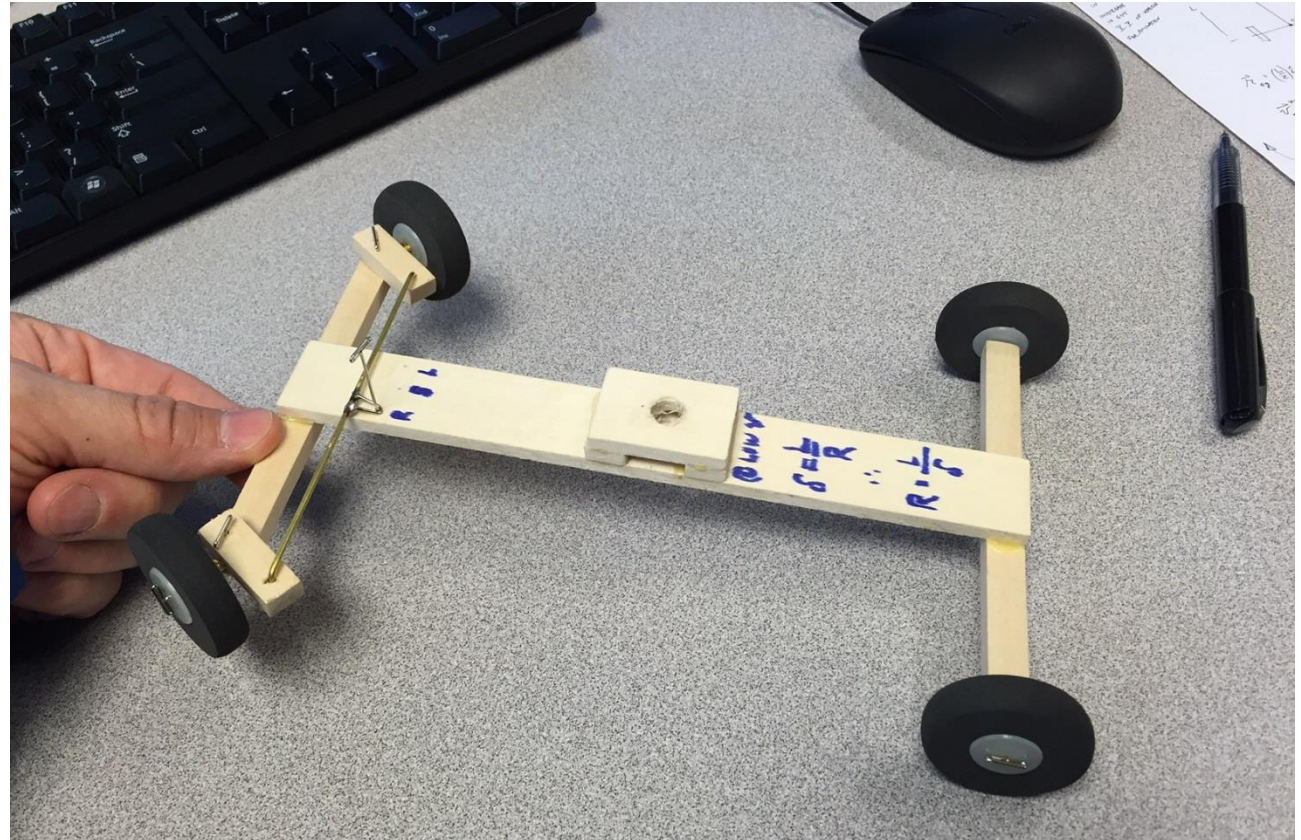
# Animating a Simple 2D Kinematic Steering Model

ME695B, Advanced Vehicle Dynamics  
Spring 2016

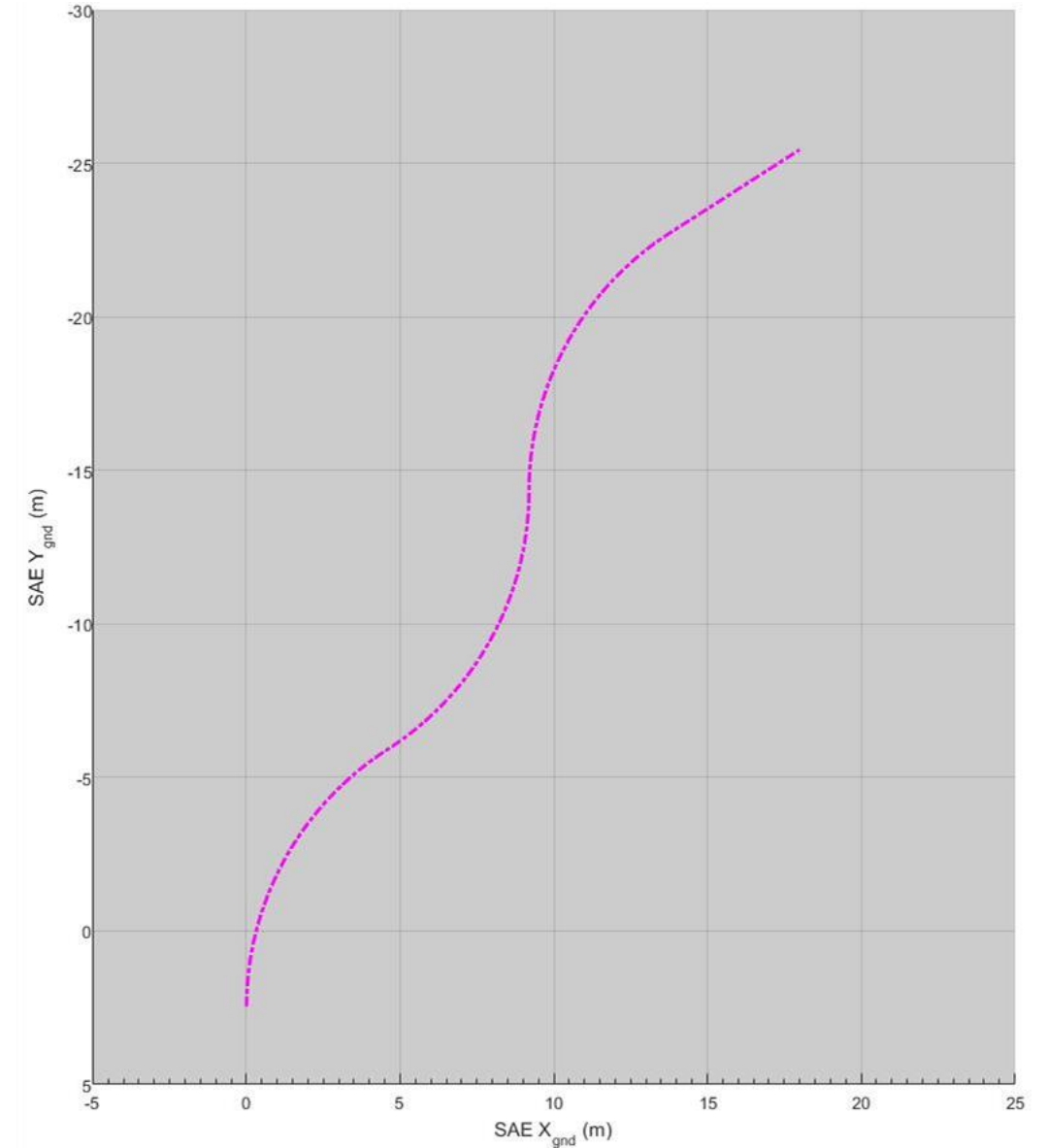
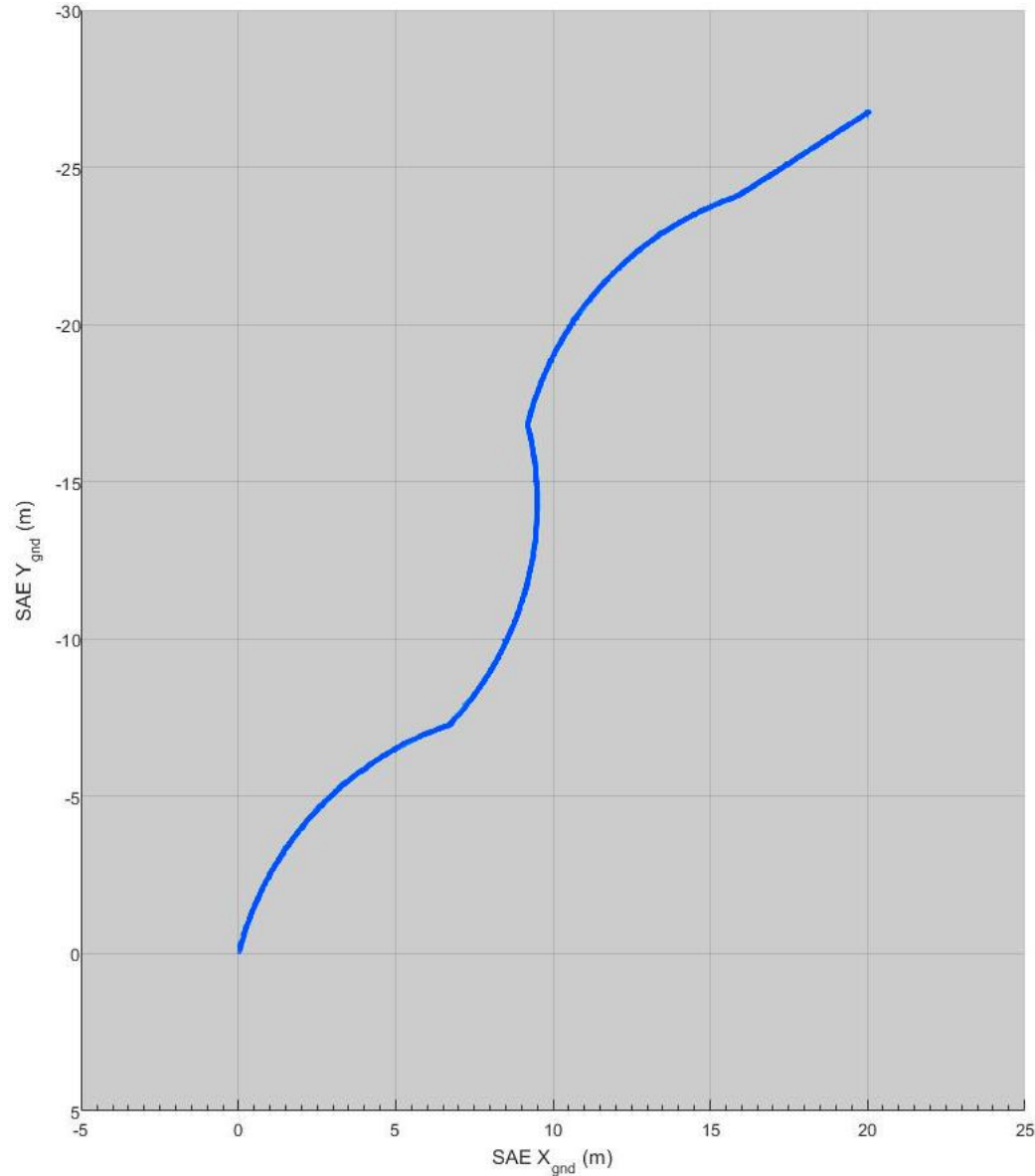
Marc Compere, Ph.D.  
Department of Mechanical Engineering  
Embry-Riddle Aeronautical University

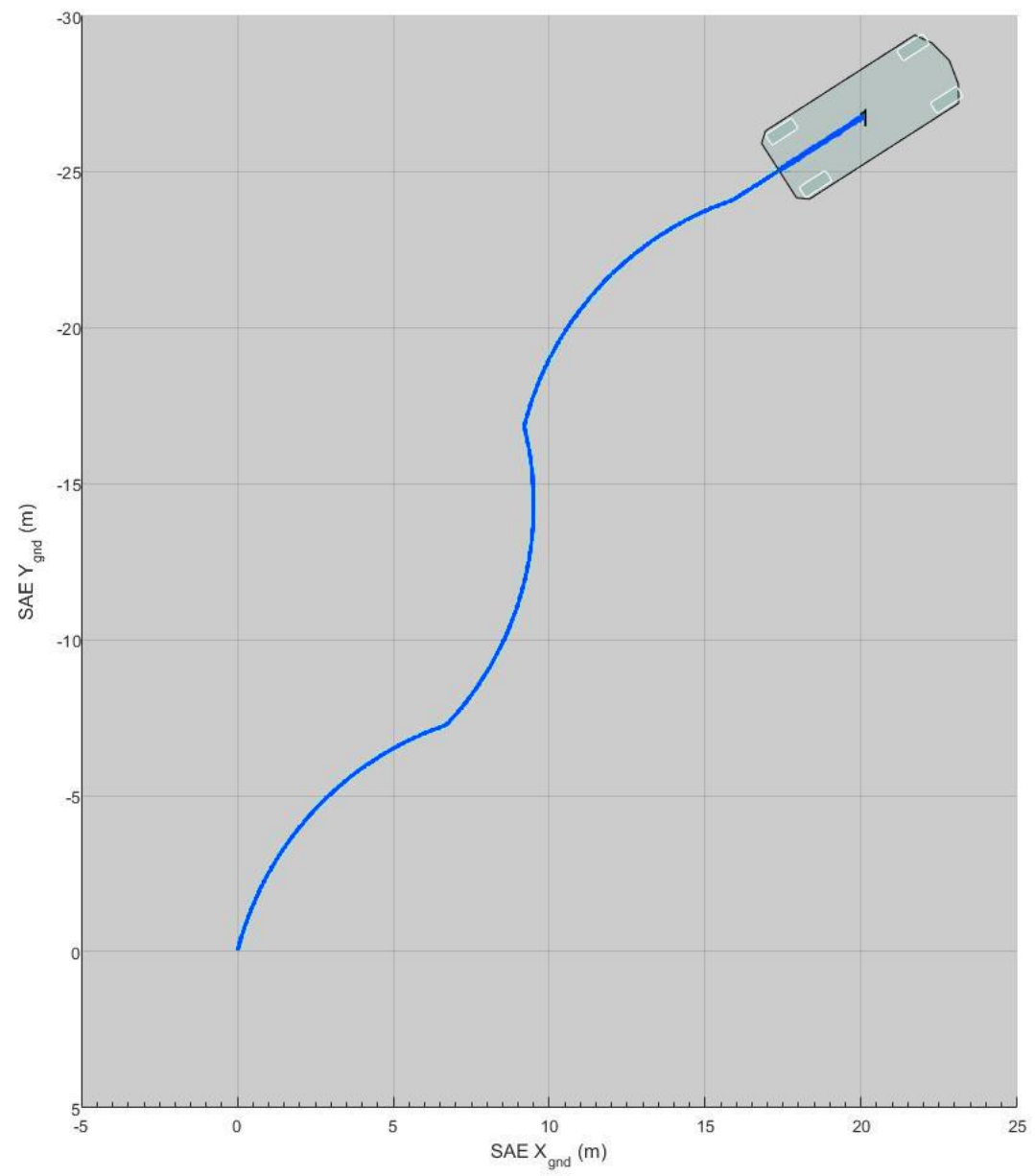
# Kinematic Steering Model – Rolling Without Slipping

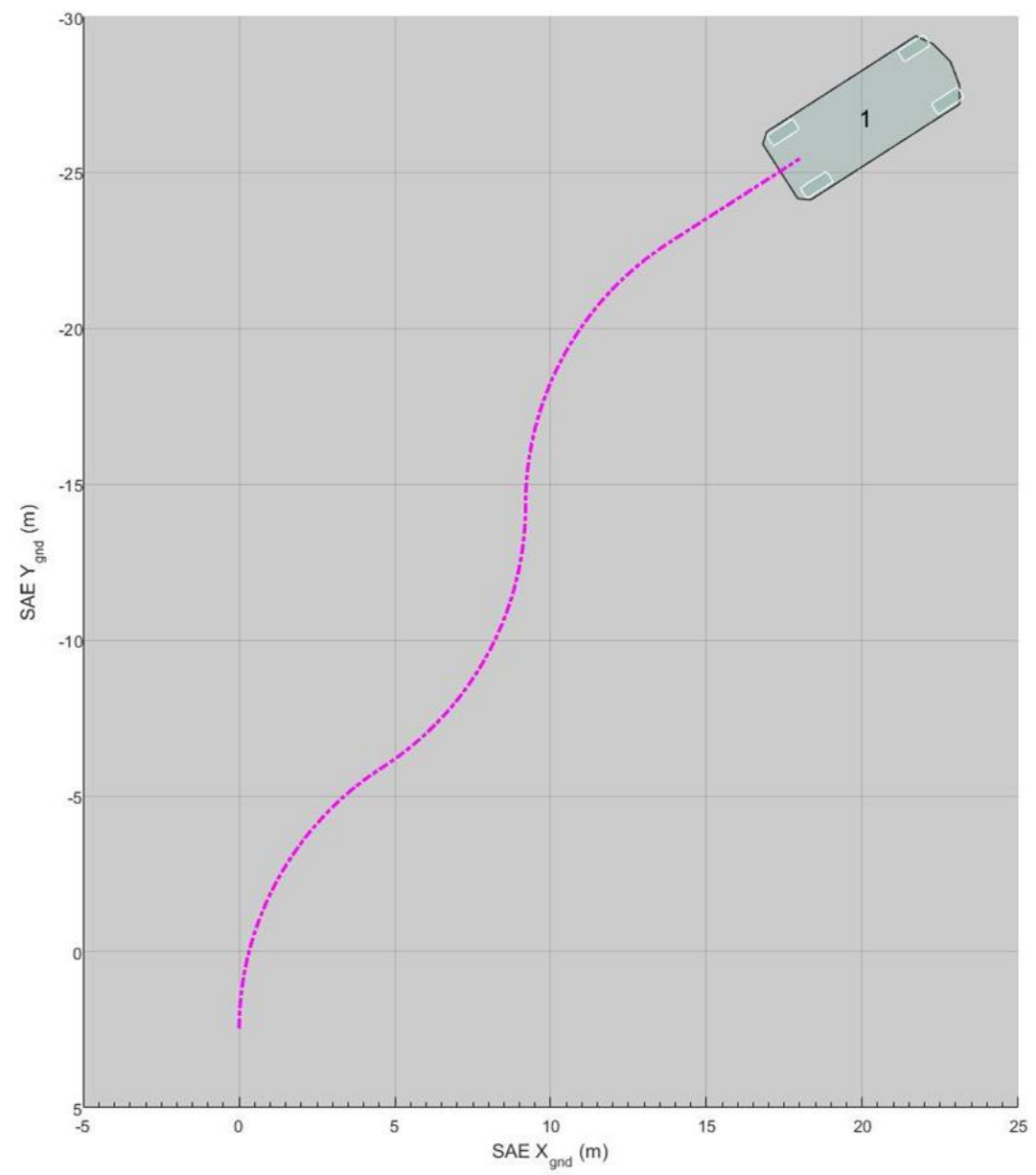
- Given this simple kinematic, low speed vehicle and
- Given a constant speed and steering input of:
  - RIGHT
  - LEFT
  - RIGHT
- Which trace do you think is correct?



# Which trace do you think is correct, and why?







Answer:

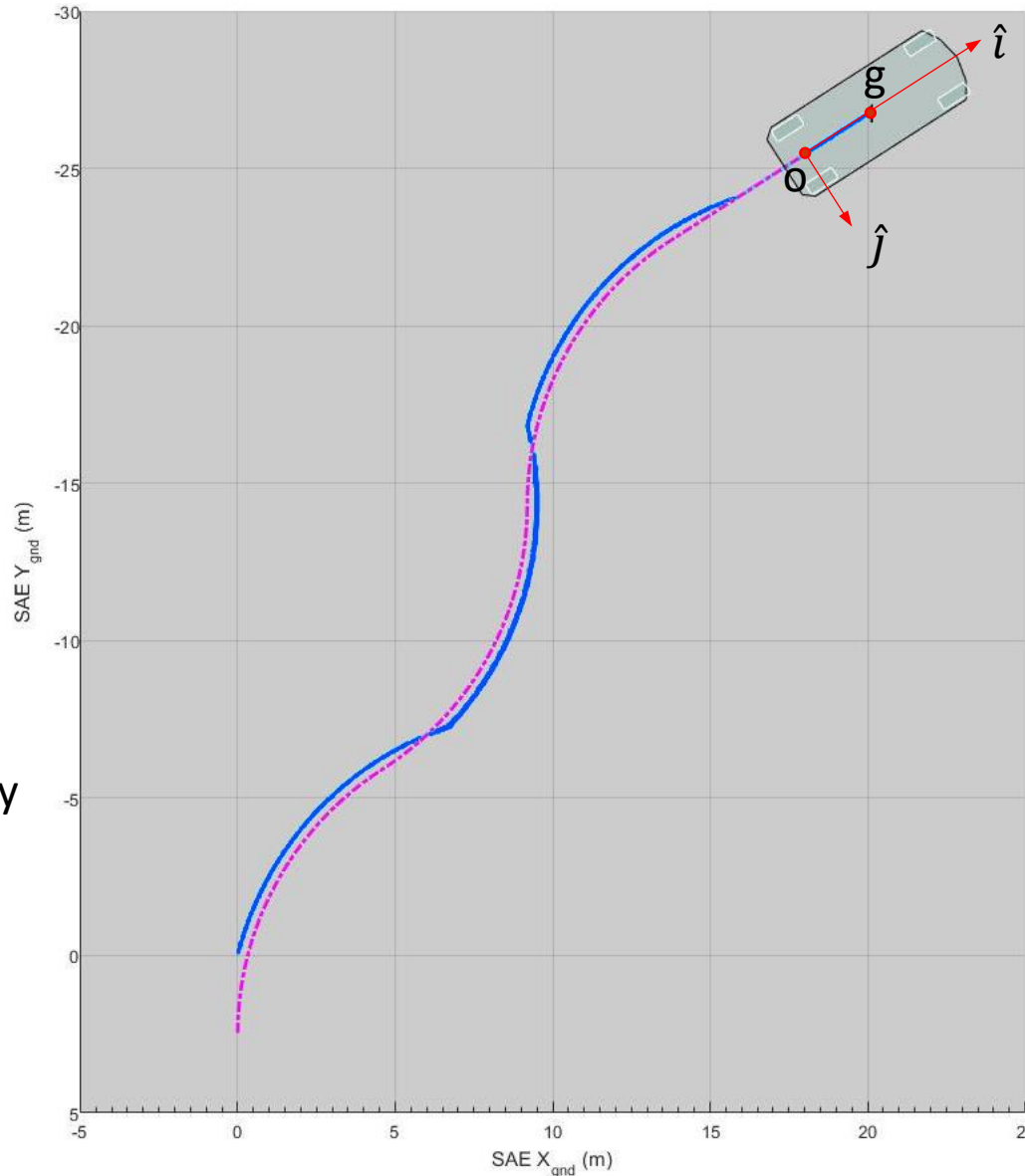
**BOTH** traces are correct.

The trace connected by smooth, continuous segments is the position trace from the rear axle's center at point 'o':

$$v_o^{xy} = \begin{bmatrix} v_x \hat{i} \\ 0 \hat{j} \end{bmatrix}$$

The trace with discontinuously connected segments is the trace from the vehicle's geometric center, 'g'.

$$v_g^{xy} = v_o^{xy} + \vec{\omega} \times \vec{r}_{og}$$



Using the coordinate transformation matrix,  $T$ , transform the velocity of point 'g' in the body-fixed  $xy$  frame to the inertial, or terrain-fixed  $XY$  frame with:

$$v_g^{XY} = \begin{bmatrix} \cos(\psi) & -\sin(\psi) \\ \sin(\psi) & \cos(\psi) \end{bmatrix} \cdot v_g^{xy}$$

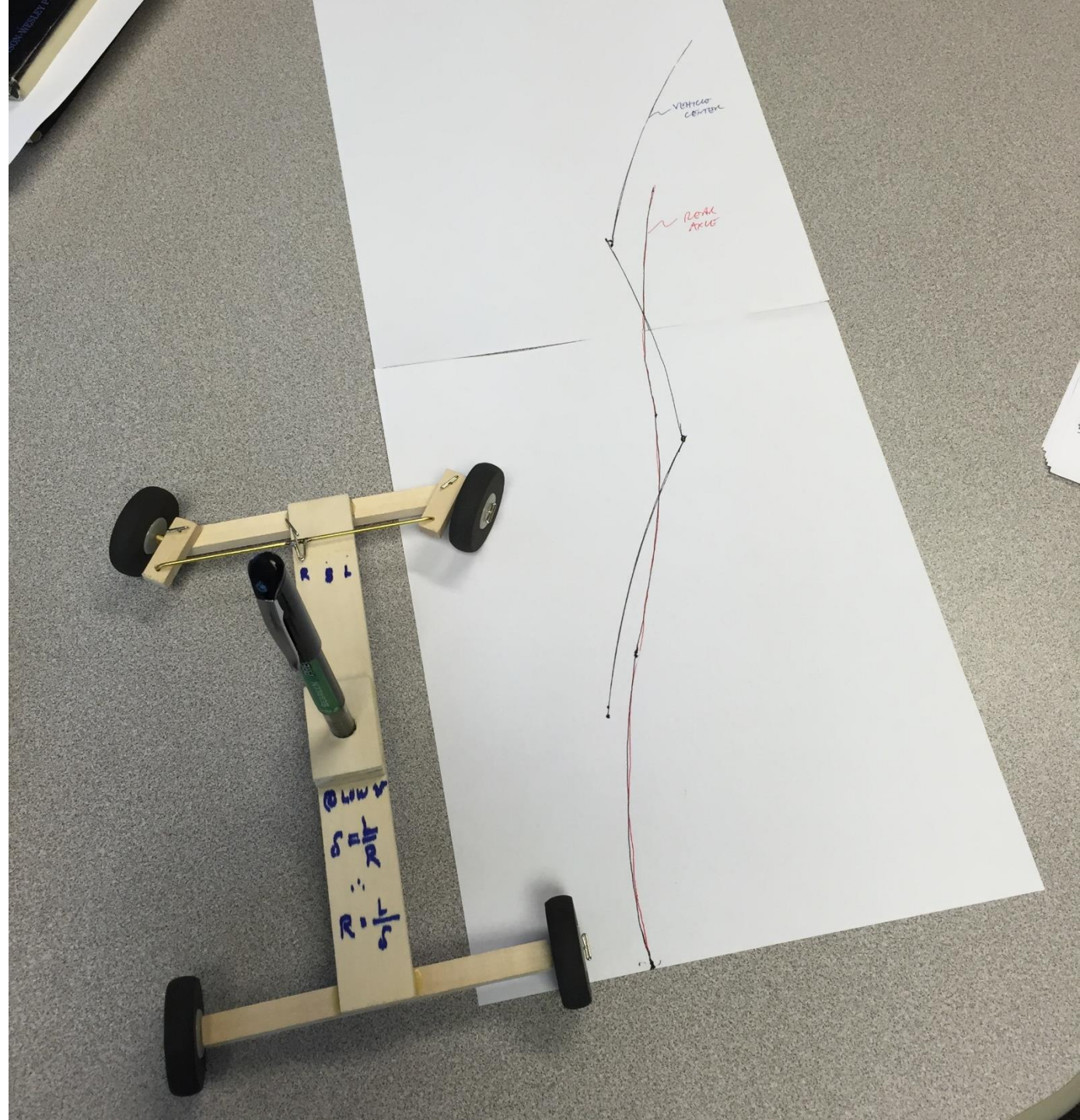
Then integrate the terrain-frame velocities to achieve position in  $XY$  as a function of body-fixed steering input, delta:

$$\begin{bmatrix} X_g \\ Y_g \end{bmatrix} = \int v_g^{XY} dt \quad \psi = \int \dot{\psi} dt$$

$$\dot{\psi} = \left( \frac{v_x}{L} \right) \delta_{steer}$$



- Dragging the pen while moving the car shows the smooth rear axle trace and the vehicle center trace.
- The smooth trace is from the center of the rear axle, at 'o'
- The discontinuous trace is from the pen's trace at the center of the vehicle, at 'g'

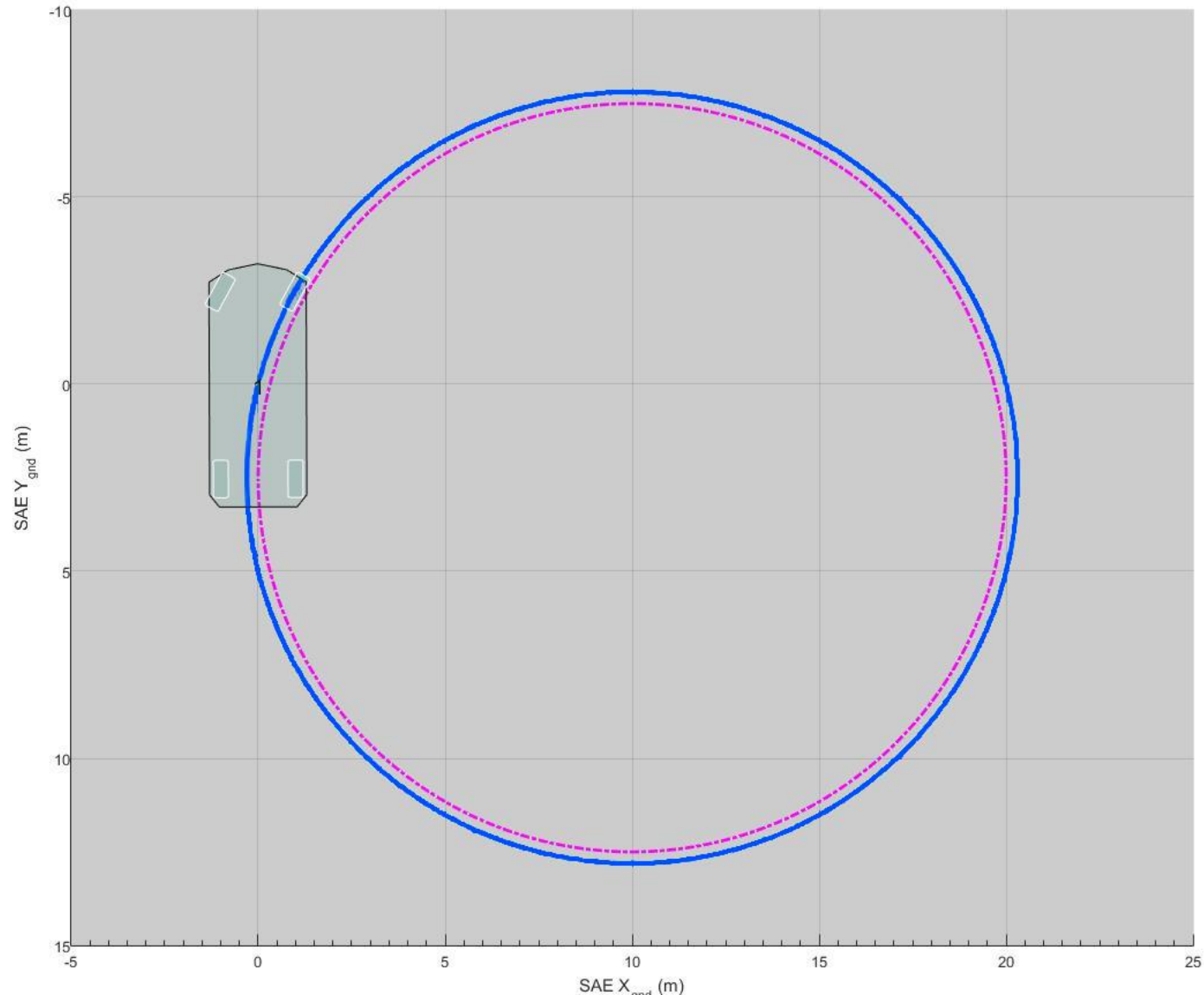


# Constant Radius Turning Scenarios



# Turning with Constant Radius.

Where is the circle centered?



# Tangential Entry and Exit

