

Knowledge Representation and Reasoning, Spring Term 2019  
Assignment 3

**Exercise 3-1**

What requirements would you have to impose on an FOPL (in particular, on  $\mathcal{F}$  and  $\mathcal{I}_{\mathcal{F}}$ ) so that you can replace the notion of a variable assignment by that of a substitution in the definition of FOPL semantics?

**Exercise 3-2**

- a) Give a recursive definition of a function, *Free*, that returns the set of variables occurring free in a given FOPL WFF.
- b) Give a recursive definition of a function, *Bound*, that returns the set of variables occurring bound in a given FOPL WFF.
- c) Given an example of an FOPL formula  $\phi$  such that  $Free(\phi) \cap Bound(\phi) \neq \{\}$ .

**Exercise 3-3**

In the extended light-switch world introduced in class, determine the truth value of the following WFFs. You should justify your answer by working your way carefully through the definition of the interpretation function.

- a)  $\forall x[(\text{Bulb}(x) \wedge \text{Off}(x)) \Rightarrow \exists y[\text{Switch}(y) \wedge \text{Up}(y)]]$
- b)  $\forall x, y[(\text{Switch}(x) \wedge \text{Switch}(y) \wedge \text{Down}(x) \wedge \text{Down}(y)) \Rightarrow \forall z_1[\text{Bulb}(z_1) \Rightarrow \text{Off}(z_1)]]$

Note: Where  $Q$  is a quantifier,  $Qx, y(\phi)$  is a short-hand for  $Qx(Qy(\phi))$ .

**Exercise 3-4      Submission**  
**Due by 13:45, Tuesday February 19th**

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**Name:**

**App #:**

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Part (b) of Exercise 3-3.