

# Code Generation and Optimization

## Lecture 11

# Objectives

By the end of this lecture you should be able to:

- 1 Generate target code for a simple machine model.
- 2 Construct flow graphs.
- 3 Determine next-use information for variables.
- 4 Carry out simple optimizations on basic blocks.

# Outline

- 1 Code Generation
- 2 Flow Graphs
- 3 Optimizing Basic Blocks

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# Factors Affecting Code Generation

- The design, complexity, and optimality of a code generator depends on several factors:
  - 1 The intermediate representation.
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# Issues in Code Generation

## ① Instruction selection.

- For example, should we use an `inc` instruction or uniform addition?

## ② Register allocation.

- Which variables reside in registers.
- Which variable resides in which register.

## ③ Evaluation order.

- Finding the optimal order is **NP**-complete.

# Target Machine Model

We assume a target machine with the following specifications.

- Byte-addressable.
- $n$  general purpose registers:  $R0, R1, Rn - 1$ .
- Instruction set:
  - Loading:  $LD\ r, src$ ; loads the value in  $src$  into register  $r$ .
  - Storing:  $ST\ loc, r$ ; stores the value in register  $r$  into location  $loc$ .
  - Computing:  $OP\ dst, src1\ (, src2)?$ .
  - Jumping:  $BR\ label$ .
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# Target Machine Model: Addressing Modes

In instructions, a location can be any of the following.

- ① **A variable name**, standing for a memory location.
- ② **An indexed address**  $a(r)$ , where  $a$  is a variable name or an integer and  $r$  is a register. Here,  $a(r) = \text{contents}(a) + \text{contents}(r)$  or  $a(r) = a + \text{contents}(r)$ , respectively.
- ③ **An indirect address**  $*r$ , where  $r$  is a register. Here,  $*r = \text{contents}(\text{contents}(r))$ .
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# Instruction Costs

- Assume instruction cost depends solely on the addressing mode.
- Instructions with operands involving constants or variables need one extra word for each constant or variable.
- The cost is the number of memory references needed to fetch and execute the instruction.
- For instruction with only register operands, the cost is 1.

## Example

- $\text{cost}(\text{LD } R1, R2) = 1.$
- $\text{cost}(\text{LD } R1, \#100) = 2.$
- $\text{cost}(\text{ST } x, R1) = 3.$
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# Exercise 1

## Example

Generate target code for the three-address instruction  $b = a[i]$ .  
What is the cost of your code?

Code.

```
LD R1, i
LD R2, a(R1)
ST b, R2
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Cost.  $3 + 3 + 3 = 9$ .



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## Exercise 2

### Example

Generate target code for the three-address instruction  $*p = y$ . What is the cost of your code?

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# Outline

- 1 Code Generation
- 2 Flow Graphs
- 3 Optimizing Basic Blocks

# A Graphical Representation of Intermediate Code

- **Flow graphs** constitute a graphical representation of the intermediate code.
- By considering a flow graph, we may optimize generated code.
  - The flow graph need not be explicitly constructed.
- A flow graph shows how values are defined and used.
- Nodes of a flow graph correspond to **basic blocks** of the intermediate code.

# Basic Blocks

## Definition

The set of **leaders** of a segment of intermediate code is the smallest set satisfying the following.

- 1 The first instruction of the code segment is a leader.
- 2 An instruction which is the target of a (conditional or unconditional) jump is a leader.
- 3 An instruction which immediately follows a (conditional or unconditional) jump is a leader.

**Intuition:** Control flows to a leader not simply by following the textual sequence of instructions.

## Definition

A **basic block** of a segment of intermediate code is the sequence of instructions starting with a leader up to (i) but not including the next leader, or (ii) the end of the code segment.

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# Exercise

## Example

```
1) i = 1
2) j = 1
3) t1 = 10 * i
4) t2 = t1 + j
5) t3 = 8 * t2
6) t4 = t3 - 88
7) a[t4] = 0.0
8) j = j + 1
9) if j <= 10 goto (3)

10) i = i + 1
11) if i <= 10 goto (2)
12) i = 1
13) t5 = i - 1
14) t6 = 88 * t5
15) a[t6] = 1.0
16) i = i + 1
17) if i <= 10 goto (13)
```

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**Basic Blocks:**  $\langle 1 \rangle$ ,  $\langle 2 \rangle$ ,  $\langle 3, 4, 5, 6, 7, 8, 9 \rangle$ ,  $\langle 10, 11 \rangle$ ,  $\langle 12 \rangle$ ,  
 $\langle 13, 14, 15, 16, 17 \rangle$ .

# The Flow Graph

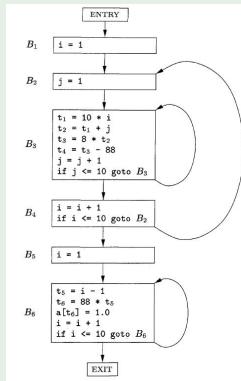
## Definition

The **flow graph** of a segment  $S$  of intermediate code is a graph  $F(S) = (\{\text{ENTRY}, \text{EXIT}\} \cup \mathcal{B}(S), E)$ , where

- ①  $\mathcal{B}(S)$  is the set of basic blocks of  $S$ , and
- ②  $(B_1, B_2) \in E$  if and only if
  - ① there is a (conditional or unconditional) jump from the last instruction of  $B_1$  to the leader of  $B_2$ ,
  - ② the leader of  $B_2$  immediately follows the last instruction of  $B_1$  which is not an unconditional jump,
  - ③  $B_1 = \text{ENTRY}$  and  $B_2$  is the block whose leader is the first instruction of  $S$ , or
  - ④  $B_2 = \text{EXIT}$  and  $B_1$  is a block that ends with a jump to an instruction outside  $S$  or is the block containing the last instruction of  $S$  (which is not an unconditional jump).

# Exercise

## Example



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# Next-Use

- To optimize register allocation, it is important to collect information about the use of values stored in registers.
- For example, if a value stored in a register will never be used following some instruction, then the register may be allocated to another value.

## Definition

Suppose that (i) instruction  $i$  assigns a value to variable  $x$ , (ii) instruction  $j$  uses  $x$  as an operand, and (iii) control can flow from statement  $i$  to statement  $j$  along a path that has no assignments to  $x$ . Then, we say that  $j$  uses the value of  $x$  computed at  $i$  and that  $x$  is alive at  $i$ .

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# Next-Use: Algorithm

- We would like to determine next-uses and liveness of variables within a basic block  $B$ .
- Assume the symbol table initially shows all non-temporary variables as alive.
- We start with the last instruction in  $B$  and scan backwards to the leader of  $B$ .
- For every instruction  $i : x = y \text{ op } z$ , do the following.
  - ① Attach to  $i$  the information in the symbol table about liveness and next-use of  $x$ ,  $y$ , and  $z$ .
  - ② In the symbol table, set  $x$  to “not live” and “no next use”.
  - ③ In the symbol table, set  $y$  and  $z$  to “live” and the next-uses of  $y$  and  $z$  to  $i$ .

# Exercise

## Example

Determine the liveness and next-use information for the instructions in the following basic block.

1.  $x = z + 1$
2.  $x = x * 4$
3.  $y = x + 1$
4.  $y = z * 3$
5.  $x = y + 2$
6. `if (x > 0) goto L`



# Exercise

## Example

Determine the liveness and next-use information for the instructions in the following basic block.

1.  $x = z + 1$   
 $x.liveness = 1; x.next - use = 2; z.liveness = 1; z.next - use = 4$
2.  $x = x * 4$   
 $x.liveness = 1; x.next - use = 3$
3.  $y = x + 1$   
 $y.liveness = 0; y.next - use = none; x.liveness = 0$
4.  $y = z * 3$   
 $y.liveness = 1; y.next - use = 5; z.liveness = 1$
5.  $x = y + 2$   
 $x.liveness = 1; y.liveness = 1$
6.  $if (x > 0) goto L$

# Optimization with the Next-Use Algorithm

- What is a simple modification to the Next-Use algorithm which admits some code optimization?
- Apply the new algorithm to the previous example.

# DAG Representation of a Basic Block

- Many optimization techniques for basic blocks assume a DAG representation of the block.

## DAG Representation

- There are nodes for initial values of variables in the block.
  - There are nodes for constants appearing in the block.
  - There is a node  $N(s)$  for each statement  $s$  in the block.  $N(s)$  is labelled by the operator applied in  $s$  and attached to it is a set of variables for which it is the last definition within the block.
  - Children of  $N(s)$  are nodes corresponding to statements which are the last definitions, before  $s$ , of operands used in  $s$ . The left-to-right ordering of children corresponds to the textual order of operands.
- The DAG representation allows us to carry out several block-optimizing transformations.

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  - 4 Children of  $N(s)$  are nodes corresponding to statements which are the last definitions, before  $s$ , of operands used in  $s$ . The left-to-right ordering of children corresponds to the textual order of operands.
- The DAG representation allows us to carry out several block-optimizing transformations.

# DAG Representation of a Basic Block

- Many optimization techniques for basic blocks assume a DAG representation of the block.

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# Detecting Common Sub-Expressions

## Rule

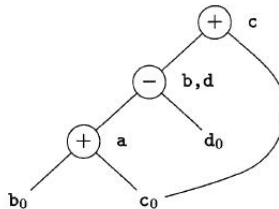
The DAG should never have two nodes with the same label and the same children.

- This is a sign of a common sub-expression.
- Instead of creating a new node, add a variable to the attached set.

# An Example

## Example

```
a = b + c  
b = a - d  
c = b + c  
d = a - d
```



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# Detecting Dead Code

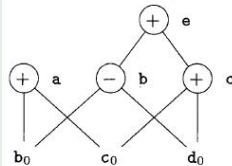
## Rule

A node with no parents and no live variables attached may be eliminated.

# An Example

## Example

```
a = b + c
b = b - d
c = c + d
e = b + c
```



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Supposing that  $e$  and  $c$  are not live, what is the result of applying the dead code rule?

# Using Algebraic Identities

## Rule

Whenever possible, use algebraic identities to simplify code:

- Constant folding: compute expressions involving only constants and replace them by their computed values.
- Use commutativity and associativity of operators wisely.
  - Use commutativity to discover equivalent common sub-expressions.
  - Use associativity to eliminate nodes.

# An Example

## Example

```
a = b + c
t = c + d
e = t + b
```

