German University in Cairo Department of Computer Science Assoc. Prof. Haythem O. Ismail

Knowledge Representation and Reasoning, Spring Term 2019 Assignment 4

Exercise 4-1

Using the FOPL system of natural deduction introduced in class, prove the following.

a)
$$\vdash (\neg \exists x P(x)) \Leftrightarrow \forall x (\neg P(x)).$$

b)
$$\vdash \exists x (P(x) \lor Q(x)) \Leftrightarrow (\exists x P(x) \lor \exists x Q(x))$$

c)
$$\vdash \forall x [P(a) \Rightarrow Q(x)] \Leftrightarrow [P(a) \Rightarrow \forall x [Q(x)]]$$

Exercise 4-2

Using the tableau method introduced in class, check whether

a)
$$\models \exists x (P(x) \lor Q(x)) \Leftrightarrow (\exists x P(x) \lor \exists x Q(x))$$

b)
$$\{\exists x P(x) \land \exists x Q(x)\} \models \exists x (P(x) \land Q(x))$$

| Exercise 4-3 | Submission | |
|--------------|--|----|
| | Due by 13:45. Tuesday February 26th 20 | 19 |

| Name: | $\mathbf{App} \ \# \mathbf{:}$ | |
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Part (b) of Exercise 4-1.