



# Semantic Analysis I

Tutorial (9)

# CFGs are not enough!

- The parse tree generated by the syntax analyzer is of minimal use to the task of semantic analysis.
- **Solution?** Augment the CFG with semantic rules.
- Example:

$$E \rightarrow E_1 + T \quad \{E.val = E_1.val + T.val\}$$

$$E \rightarrow T \quad \{E.val = T.val\}$$

$$T \rightarrow T_1 * F \quad \{T.val = T_1.val * F.val\}$$

$$T \rightarrow F \quad \{T.val = F.val\}$$

$$F \rightarrow digit \quad \{F.val = digit.lexval\}$$

# Syntax Directed Definitions (SDDs)



- **Syntax Directed Definitions:**
  - Symbols of the grammar have associated attributes.
  - Attributes carry information about the meaning of the program and how to translate it.
  - Computed by semantic rules.
  - Better suited for specification.

## Exercise 9-1

$$E \rightarrow E_1 + T \quad \{E.val = E_1.val + T.val\}$$

$$E \rightarrow T \quad \{E.val = T.val\}$$

$$T \rightarrow T_1 * F \quad \{T.val = T_1.val * F.val\}$$

$$T \rightarrow F \quad \{T.val = F.val\}$$

$$F \rightarrow digit \quad \{F.val = digit.lexval\}$$

Input: 3+4\*5

- Here all attributes are **synthesized**.
- An attribute is **synthesized** if its value is determined from **other attributes of itself or the attributes of its direct children**.
- A **post-order traversal** will be appropriate to compute all attributes.

# Synthesized attributes and Inherited attributes

- Sometimes, synthesized attributes are not sufficient.
- Typical Example: Left Recursion Elimination

$$\begin{aligned}T &\rightarrow FT' && \{T.val = T'.val \\ &&& T'.inh = F.val\} \\ T' &\rightarrow *FT'_1 && \{T'.val = T'_1.val \\ &&& T'_1.inh = T'.inh * F.val\} \\ T' &\rightarrow \varepsilon && \{T'.val = T'.inh\} \\ F &\rightarrow digit && \{F.val = digit.lexval\}\end{aligned}$$

- An attribute is **inherited** if its value is **determined by its parent or sibling attributes**.

# Order of Evaluation



- How to determine the order of evaluation of the attributes if the SDD contains inherited attributes?
  - a. Construct the dependency graph.
  - b. If the dependency graph is a DAG, an evaluation is valid. An order can be constructed by **topological sorting**.

Procedure: Use a queue

1. Enqueue a node  $n$  with zero in-degree.
2. Remove  $n$  from the graph together with all emanating arcs.
3. Repeat 1,2 until the graph becomes empty.
4. Start dequeuing from the queue. Evaluate a node when it is dequeued.

## Exercise 9-2



Extend the below SDD to match the grammar in Exercise 9-1.

$$\begin{aligned}T &\rightarrow FT' && \{T.val = T'.val \\& && T'.inh = F.val\} \\T' &\rightarrow *FT'_1 && \{T'.val = T'_1.val \\& && T'_1.inh = T'.inh * F.val\} \\T' &\rightarrow \epsilon && \{T'.val = T'.inh\} \\F &\rightarrow digit && \{F.val = digit.lexval\}\end{aligned}$$

# Some Special SDDs

- An SDD is **S-attributed** if all attributes are synthesized.
- An SDD is **L-attributed** if  $\forall B \rightarrow \alpha A \beta$ :
  - a. Every **inherited attribute of A** depends on **inherited attributes of B** and **any attributes of symbols in  $\alpha$** .
  - b. Every **synthesized attribute of B** depends on  **$\alpha A \beta$**  or **inherited attributes of B**.
- **Exercise 9-4:** Suppose we have a production  $A \rightarrow BCD$ . Determine whether the following rules are consistent with the definition of S-attributed SDDs or L-attributed SDDs or neither.
  - a.  $A.s = B.i + C.s$
  - b.  $A.s = B.i + C.s$        $D.i = A.i + B.s$
  - c.  $A.s = B.s + D.s$
  - d.  $A.s = D.i$        $B.i = A.s + C.s$        $C.i = B.s$        $D.i = B.i + C.i$



# Syntax Directed Translations (SDTs)



- Syntax Directed Translations:
  - Pieces of code associated at various positions in the RHS of a production rule.
  - The pieces of code generate the translation.
  - Better suited for implementation.

# From SDDs to SDTs

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- Given an L-attributed SDD:
  - a. Insert the action that computes an inherited attribute immediately before its corresponding grammar symbol on the RHS.
  - b. Insert the action that computes a synthesized attribute at the end of the rule.
- Exercise 9-6: Apply this to the SDD in 9-2.

# Writing SDDs



- **Exercise 9-5:** Write an SDD that converts binary numbers with decimal points to decimal numbers (base 10).