

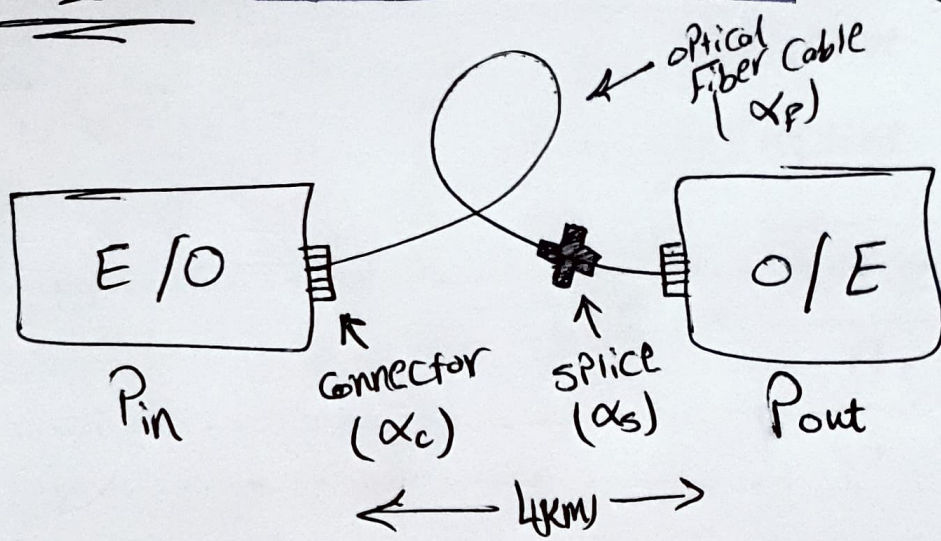


Sheet 01 (Laws Zatoona) & Answers

References
Mokhtar Sections

Electromagnetic
Waves 2

**No Excellence
Just Pass**



attenuation in optical Fiber Communication

$$\alpha_t |_{dB} = 10 \log \left(\frac{P_{in}}{P_{out}} \right) = P_{in} |_{dB} - P_{out} |_{dB}$$

α_f : optical Fiber attenuation Coefficient (dB/Km)

α_s : splice attenuation Coefficient (dB/^{splice}~~Km~~)

α_c : Connector attenuation Coefficient (dB/Connector)

n : no. of sections

$(n-1)$: no. of splices

α_{ICL} : input Coupling Loss

α_{OCL} : output Coupling Loss

$$n = \frac{\text{total Fiber Length}}{\text{real Length}}$$

$$\alpha_t |_{dB} = \alpha_f L + (n-1) \alpha_s + 2 \alpha_c + \alpha_{ICL} + \alpha_{OCL}$$

Waves SEC 2

Numerical aperture

$$N_A = \sqrt{n_1^2 - n_2^2}$$

$$N_A = n_1 \sqrt{2\Delta}$$

n_1 : refractive index of Core
 n_2 : refractive index of cladding

$$\Delta = \frac{n_1 - n_2}{n_1}$$

$$n = \frac{c}{v}$$

Δ : Fractional difference index

c : velocity of Light (3×10^8)
 v : velocity in the medium

$$\theta_{\max} = \sin^{-1}(N_A)$$

θ_{\max} : the acceptance angle

The normalized Frequency

$$V = \frac{\pi d}{\lambda} N_A$$

Core diameter

$$V = \frac{2\pi a}{\lambda} N_A$$

Core radius

note

For single mode optical Fiber (SM)

$$V = 2.405$$

The no. of modes (M)

$$M|_{SI} = \frac{V^2}{2}$$

$$M|_{GI} = \left(\frac{\alpha}{\alpha + 2} \right) M|_{SI}$$

$$M|_{GI} = \left(\frac{\alpha}{\alpha + 2} \right) a^2 k^2 n_1^2 \Delta$$

$$k = \frac{2\pi}{\lambda}$$

note

assume $(\alpha) = 2$
if not given

The Fractional Power wasted in Cladding

$$\frac{P_{\text{cladding}}}{P_{\text{Total}}} = \frac{4}{3\sqrt{M}}$$

Sheet (1)

WAVES

① $\alpha_F = 1.5 \text{ dB/Km}$ $P_{in} = 0.5 \text{ mW}$ $P_{out} = ??$

$L = 8 \text{ Km}$ max reel length = 2 Km

$\alpha_S = 0.1 \text{ dB/splice}$ $\alpha_{ICL} = 1 \text{ dB}$ $\alpha_{ocL} = 2 \text{ dB}$

$n = \frac{\text{total Fiber length}}{\text{reel length}} = \frac{8}{2} = 4$ must be integer

$\alpha_t |_{\text{dB}} = \alpha_F L + (n-1)\alpha_S + 2\alpha_c + \alpha_{ICL} + \alpha_{ocL}$

$\alpha_t |_{\text{dB}} = (1.5 \times 8) + (3 \times 0.1) + 1 + 2 = 15.3 \text{ dB}$

$\alpha_t |_{\text{dB}} = P_{in} |_{\text{dB}} - P_{out} |_{\text{dB}} \Rightarrow P_{out} |_{\text{dB}} = P_{in} |_{\text{dB}} - \alpha_t$

$P_{out} |_{\text{dB}} = 10 \log(0.5) - 15.3 = -18.3 \text{ dB}$

$P_{out} = 10^{-1.83} = \boxed{0.0148 \text{ mW}}$

② $L = 3.5 \text{ Km}$ max reel length = 3 Km $\alpha_S = 0.2$
 $\alpha_{ICL} = 1 \text{ dB}$ $\alpha_{ocL} = 0.8 \text{ dB}$ $P_{out} = 0.45 P_{in}$

$\alpha_t = 10 \log \left(\frac{P_{in}}{P_{out}} \right) = 10 \log \left(\frac{P_{in}}{0.45 P_{in}} \right) = 3.47 \text{ dB}$

$n = \frac{\text{total Fiber length}}{\text{reel length}} = \frac{3.5}{3} = 2$

$\alpha_t = \alpha_F L + (n-1)\alpha_S + 2\alpha_c + \alpha_{ICL} + \alpha_{ocL}$

$$3.47 = 3.5 \alpha_F + (1 \times 0.2) + 1 + 0.8$$

$$\alpha_F = \frac{(3.47 - 0.2 - 1 - 0.8)}{3.5} = \boxed{0.42 \text{ dB/Km}}$$

③ $\alpha_F = 0.5 \text{ dB/Km}$ $P_{in} = 1 \text{ mW}$ $P_{out} = 0.1 \text{ mW}$

$L = ??$ $\alpha_s, \alpha_c, \alpha_{ICL}, \alpha_{ocL} \Rightarrow \text{ignored}$

$$\alpha_t = 10 \log \left(\frac{P_{in}}{P_{out}} \right) = 10 \log \left(\frac{1}{0.1} \right) = 10 \text{ dB}$$

$$\alpha_t = \alpha_F L \Rightarrow L = \frac{\alpha_t}{\alpha_F} = \frac{10}{0.5} = \boxed{20 \text{ Km}}$$

④ $L = 12 \text{ Km}$ $\alpha_F = 1.5 \text{ dB/Km}$ $P_{in} = ??$ $P_{out} = 0.3 \mu\text{W}$

max reel length = 3 Km $\alpha_s = 0.1$

the coupling losses are (2 dB) at each transmit and receive end. $\Rightarrow \alpha_{ICL} = 2 \text{ dB}$, $\alpha_{ocL} = 2 \text{ dB}$

$$n = \frac{12}{3} = 4$$

$$\alpha_t = \alpha_F L + (n-1)\alpha_s + 2\alpha_c + \alpha_{ICL} + \alpha_{ocL}$$

$$\alpha_t = (1.5 \times 12) + (3 \times 0.1) + 2 + 2 = 22.3 \text{ dB}$$

$$\alpha_t|_{\text{dB}} = P_{in}|_{\text{dB}} - P_{out}|_{\text{dB}} \Rightarrow P_{in}|_{\text{dB}} = P_{out}|_{\text{dB}} + \alpha_t|_{\text{dB}}$$

$$P_{in}|_{\text{dB}} = 10 \log(0.3) + 22.3 = 17.071 \text{ dB}$$

$$P_{in} = 10^{1.7071} = \boxed{51 \mu\text{W}}$$

⑤ 50/125 step index $n_1 = 1.48$ $n_2 = 1.465$
 Core diameter (μm) cladding diameter (μm) $\lambda = 1320 \text{ nm}$

$$NA = \sqrt{n_1^2 - n_2^2} = \sqrt{(1.48)^2 - (1.465)^2} = \boxed{0.21}$$

$$\theta_{\max} = \sin^{-1}(NA) = \sin^{-1}(0.21) = \boxed{12.13^\circ}$$

$$V = \frac{\pi d}{\lambda} NA = \frac{\pi \times 50 \times 10^{-6}}{1320 \times 10^{-9}} \times 0.21 = 25$$

$$M|_{SI} = \frac{V^2}{2} = \frac{(25)^2}{2} = \boxed{312.5}$$

$$\frac{P_{\text{cladding}}}{P_{\text{total}}} = \frac{4}{3\sqrt{M}} = \frac{4}{3\sqrt{312.5}} = \boxed{7.5\%}$$

For single mode Fiber $\Rightarrow V = 2.405$

$$d = \frac{V \lambda}{\pi NA} = \frac{2.405 \times 1320 \times 10^{-9}}{\pi \times 0.21} = \boxed{4.812 \mu m}$$

⑥ $a = 25 \mu m$ $n_1 = 1.48$ $\Delta = 0.01$ $\lambda = 0.84 \mu m$

$$NA = n_1 \sqrt{2\Delta} = 1.48 \sqrt{2 \times 0.01} = \boxed{0.21}$$

$$V = \frac{2\pi a}{\lambda} NA = \frac{2\pi \times 25 \times 10^{-6}}{0.84 \times 10^{-6}} \times 0.21 = \boxed{39.27}$$

$$M|_{SI} = \frac{V^2}{2} = \frac{(39.27)^2}{2} = \boxed{771}$$

$$\frac{P_{\text{cladding}}}{P_{\text{total}}} = \frac{4}{3\sqrt{M}} = \frac{4}{3\sqrt{771}} = \boxed{4.8\%}$$

⑦ single mode $\Rightarrow V = 2.405$ $d = 10 \mu\text{m}$

$\lambda = 1.3 \mu\text{m}$ $n_1 = 1.55$

$$V = \frac{\pi d}{\lambda} NA \Rightarrow NA = \frac{V \lambda}{\pi d}$$

$$NA = \frac{2.405 \times 1.3 \times 10^{-6}}{\pi \times 10 \times 10^{-6}} = \boxed{0.0995}$$

$$NA = \sqrt{n_1^2 - n_2^2} \Rightarrow (NA)^2 = n_1^2 - n_2^2$$

$$n_2 = \sqrt{n_1^2 - NA^2} = \sqrt{(1.55)^2 - (0.0995)^2} = \boxed{1.5468}$$

$$\Delta = \frac{n_1 - n_2}{n_1} = \frac{1.55 - 1.5468}{1.55} = \boxed{0.206\%}$$

$$\theta_{\max} = \sin^{-1}(NA) = \sin^{-1}(0.0995) = \boxed{5.712^\circ}$$

⑧ $n_1 = 1.55$ $n_2 = 1.51$ $d = 50 \mu\text{m}$ $\lambda = 0.8 \mu\text{m}$

$$NA = \sqrt{n_1^2 - n_2^2} = \sqrt{(1.55)^2 - (1.51)^2} = \boxed{0.35}$$

$$\theta_{\max} = \sin^{-1}(NA) = \sin^{-1}(0.35) = \boxed{20.487^\circ}$$

$$V = \frac{\pi d}{\lambda} NA = \frac{\pi \times 50 \times 10^{-6}}{0.8 \times 10^{-6}} \times 0.35 = \boxed{68.72}$$

$$M|_{SI} = \frac{V^2}{2} = \frac{(68.72)^2}{2} = \boxed{2361}$$

note
assume $\alpha = 2$
if not given

$$M|_{GI} = \left(\frac{\alpha}{\alpha + 2} \right) M|_{SI} = \left(\frac{2}{2 + 2} \right) \times 2361 = \boxed{1180}$$

9 $\alpha = 1300 \text{ nm}$ Graded Index ($\alpha = 1$)

$$n_1 = 1.48 \quad n_2 = 1.46 \quad d = 50 \mu\text{m}$$

$$NA = \sqrt{n_1^2 - n_2^2} = \sqrt{(1.48)^2 - (1.46)^2} = 0.24$$

$$V = \frac{\pi d}{\lambda} NA = \frac{\pi \times 50 \times 10^{-6}}{1300 \times 10^{-9}} \times 0.24 = 29$$

Step Index (SI)

$$M|_{SI} = \frac{V^2}{2} = \frac{(29)^2}{2} = \boxed{420}$$

$$\frac{P_{\text{cladding}}}{P_{\text{Total}}} = \frac{4}{3\sqrt{M}} = \frac{4}{3\sqrt{420}} = \boxed{6.5\%}$$

Graded Index (GI) ($\alpha = 1$)

$$M|_{GI} = \left(\frac{\alpha}{\alpha+2}\right) M|_{SI} = \left(\frac{1}{1+2}\right) \times 420 = \boxed{140}$$

$$\frac{P_{\text{cladding}}}{P_{\text{Total}}} = \frac{4}{3\sqrt{M}} = \frac{4}{3\sqrt{140}} = \boxed{11.3\%}$$