

Algorithm Task

Project Idea: 1 (Climbing Stair)

Team Number: 12

1- Climbing Stair

You are climbing a stair case. It takes n steps to reach to the top. Each time you can either climb 1 or 2 steps. Design an algorithm that calculate how many distinct ways can you climb to the top? Note: Given n will be a positive integer.

GitHub Link: [AhmedMetwaly12/algorithmtask \(github.com\)](https://github.com/AhmedMetwaly12/algorithmtask)

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Code Number 1:

```
int main()
{
    int n, f=1, s=1, tmp;
    scanf("%d", &n);

    for(int i=2; i<=n; i++) {
        // fib(n) = fib(n-1) + fib(n-2);
        tmp = f+s;
        f = s;
        s = tmp;
    }

    if(n < 1) s = 0; //this condition deals with negative numbers and zero

    printf("The distinct ways i can climb to the top is: %d\n", s);
}
```

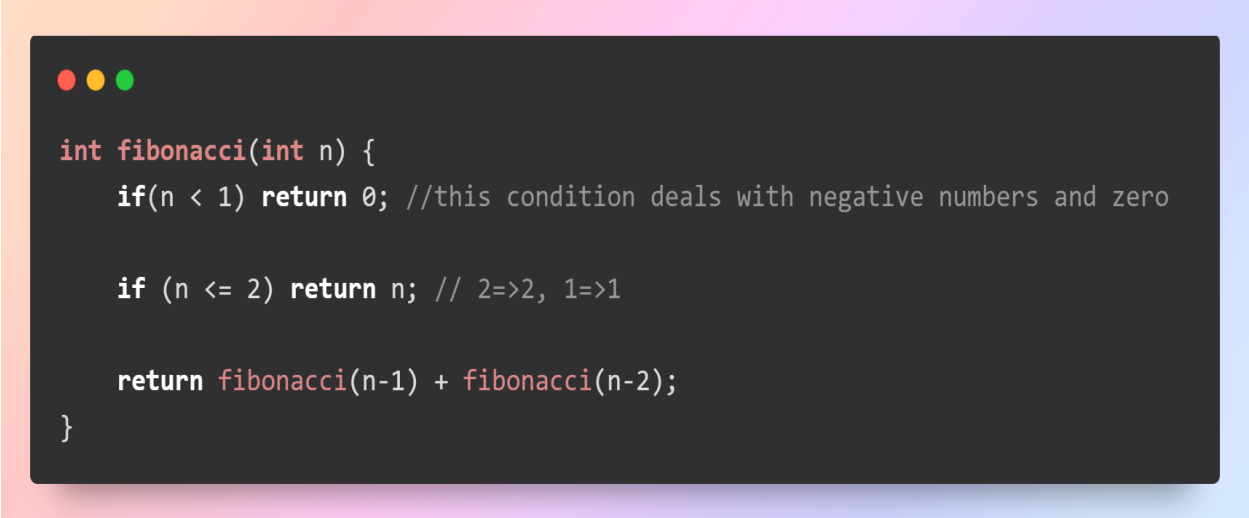
Pseudocode of Code Number 1

```
f := 1
s := 1
Read integer n from the user
for l := 2 to n do {
    tmp := f+s
    f := s
    s := tmp
}
If n < 1 then
    s := 0
print s
```

Analysis of Code Number 1

$$C(n) = \sum_{i=1}^n 1 = n-2 = O(n)$$

Code Number 2



```
int fibonacci(int n) {  
    if(n < 1) return 0; //this condition deals with negative numbers and zero  
  
    if (n <= 2) return n; // 2=>2, 1=>1  
  
    return fibonacci(n-1) + fibonacci(n-2);  
}
```

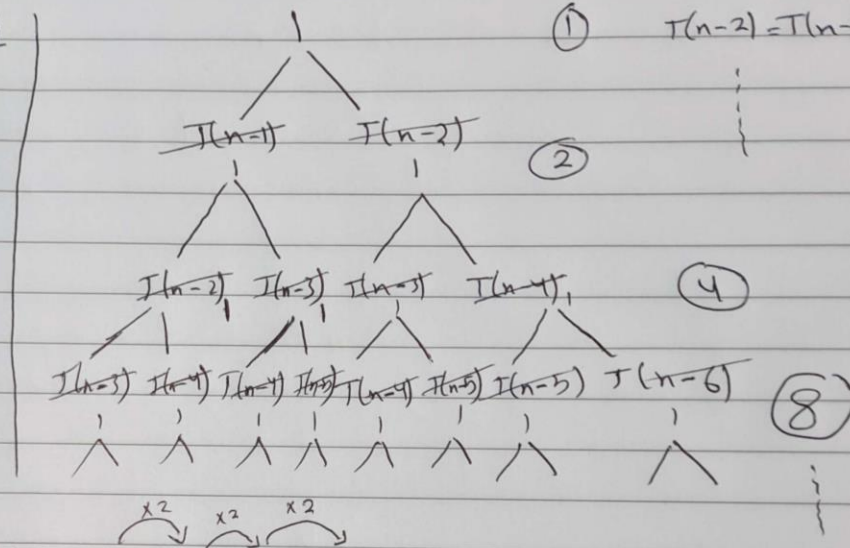
Pseudocode of Code Number 2

```
function fibonacci(n)  
    if n < 1 then  
        return 0  
    if n <= 2 then  
        return n  
    return fibonacci(n-1) + fibonacci(n-2)
```

Analysis of Code Number 2

$$T(n) = T(n-1) + T(n-2) + 1$$

height = (n)



$$T(n) = 1 + 2 + 4 + 8 + \dots \quad (\text{geometric})$$

$$a_1 = 1, \quad r = 2, \quad \text{height} = n$$

$$T(n) = a_1 \left(\frac{1 - r^{\text{height}}}{1 - r} \right) = 1 \left(\frac{1 - 2^n}{1 - 2} \right) = \boxed{O(2^n)}$$

Test Run of Codes

Code 1

```
#include <stdio.h>
#include <stdlib.h>
```

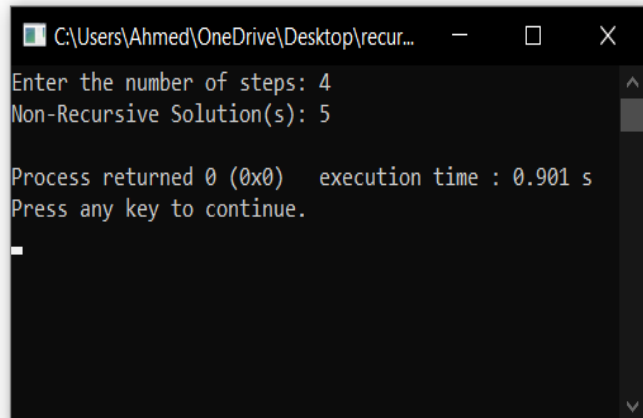
```
int main()
```

```
{
```

```
    int n, f=1, s=1, tmp;
    printf("Enter the number of steps: ");
    scanf("%d", &n);
```

```
    for(int i=2; i<=n; i++) {
        // fib(n) = fib(n-1) + fib(n-2);
        tmp = f+s;
        f = s;
        s = tmp;
    }
```

```
    if(n < 1) s = 0; //this condition deals with negative numbers and zero
    printf("Non-Recursive Solution(s): %d\n", s);
}
```



```
C:\Users\Ahmed\OneDrive\Desktop\recur...
Enter the number of steps: 4
Non-Recursive Solution(s): 5

Process returned 0 (0x0)   execution time : 0.901 s
Press any key to continue.
```

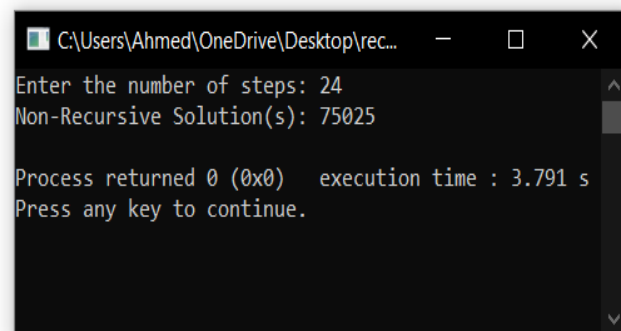
```
#include <stdio.h>
#include <stdlib.h>
```

```
int main(){
```

```
    int n, f=1, s=1, tmp;
    printf("Enter the number of steps: ");
    scanf("%d", &n);
```

```
    for(int i=2; i<=n; i++) {
        // fib(n) = fib(n-1) + fib(n-2);
        tmp = f+s;
        f = s;
        s = tmp;
    }
```

```
    if(n < 1) s = 0; //this condition deals with negative numbers and zero
    printf("Non-Recursive Solution(s): %d\n", s);
}
```



```
C:\Users\Ahmed\OneDrive\Desktop\rec...
Enter the number of steps: 24
Non-Recursive Solution(s): 75025

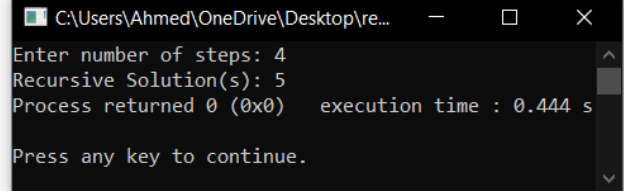
Process returned 0 (0x0)   execution time : 3.791 s
Press any key to continue.
```

Code 2

```
#include <stdio.h>
#include <stdlib.h>
```

```
int fibonacci(int n) {
    if(n < 1) return 0;
    if (n <= 2) return n; // 2=>2, 1=>1
    return fibonacci(n-1) + fibonacci(n-2);
}
```

```
int main()
{
    int n;
    printf("Enter number of steps: ");
    scanf("%d", &n);
    printf("Recursive Solution(s): %d", fibonacci(n));
}
```

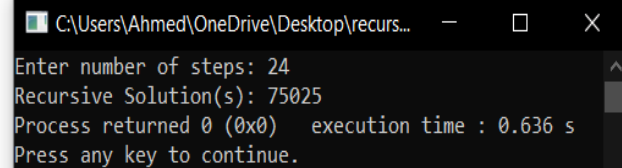


C:\Users\Ahmed\OneDrive\Desktop\re...
Enter number of steps: 4
Recursive Solution(s): 5
Process returned 0 (0x0) execution time : 0.444 s
Press any key to continue.

```
#include <stdio.h>
#include <stdlib.h>
```

```
int fibonacci(int n) {
    if(n < 1) return 0;
    if (n <= 2) return n; // 2=>2, 1=>1
    return fibonacci(n-1) + fibonacci(n-2);
}
```

```
int main()
{
    int n;
    printf("Enter number of steps: ");
    scanf("%d", &n);
    printf("Recursive Solution(s): %d", fibonacci(n));
}
```



C:\Users\Ahmed\OneDrive\Desktop\recurs...
Enter number of steps: 24
Recursive Solution(s): 75025
Process returned 0 (0x0) execution time : 0.636 s
Press any key to continue.

Comparison

Code No	Best Case	Worst Case
1	$\Omega(1)$	$O(n)$
2	$\Omega(1)$	$O(2^n)$

Therefore: Code number 1 is better, more time efficient.